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Wisdom & Virtue

MIRPUR UNIVERSITY OF SCIENCE AND TECHNOLOGY (MUST), MIRPUR  
DEPARTMENT OF SOFTWARE ENGINEERING

# Formal Methods in Software Engineering

Lecture [9]: Deterministic Finite Automata

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## ***Topics discussed in Today's Lectures***

- Deterministic Finite Automata
- DFA with Transition Table
- How a DFA Processes Strings

# Deterministic Finite Automata

**Definition:** A deterministic finite automaton (DFA) consists of

1. a finite set of *states* (often denoted  $Q$ )
2. a finite set  $\Sigma$  of *symbols* (alphabet)
3. a *transition function* that takes as argument a state and a symbol and returns a state (often denoted  $\delta$ )
4. a *start state* often denoted  $q_0$
5. a set of *final* or *accepting* states (often denoted  $F$ )

We have  $q_0 \in Q$  and  $F \subseteq Q$



# Deterministic Finite Automata

So a DFA is mathematically represented as a 5-uple

$$(Q, \Sigma, \delta, q_0, F)$$

The transition function  $\delta$  is a function in

$$Q \times \Sigma \rightarrow Q$$

$Q \times \Sigma$  is the set of 2-tuples  $(q, a)$  with  $q \in Q$  and  $a \in \Sigma$



# DFA with Transition Table

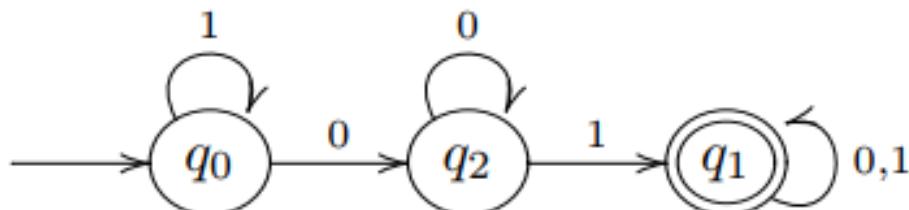
How to present a DFA? With a *transition table*

	0	1
$\rightarrow q_0$	$q_2$	$q_0$
$*q_1$	$q_1$	$q_1$
$q_2$	$q_2$	$q_1$

The  $\rightarrow$  indicates the *start state*: here  $q_0$

The \* indicates the final state(s) (here only one final state  $q_1$ )

This defines the following *transition diagram*



# Deterministic Finite Automata

For this example

$$Q = \{q_0, q_1, q_2\}$$

start state  $q_0$

$$F = \{q_1\}$$

$$\Sigma = \{0, 1\}$$

$\delta$  is a *function* from  $Q \times \Sigma$  to  $Q$

$$\delta : Q \times \Sigma \rightarrow Q$$

$$\delta(q_0, 1) = q_0$$

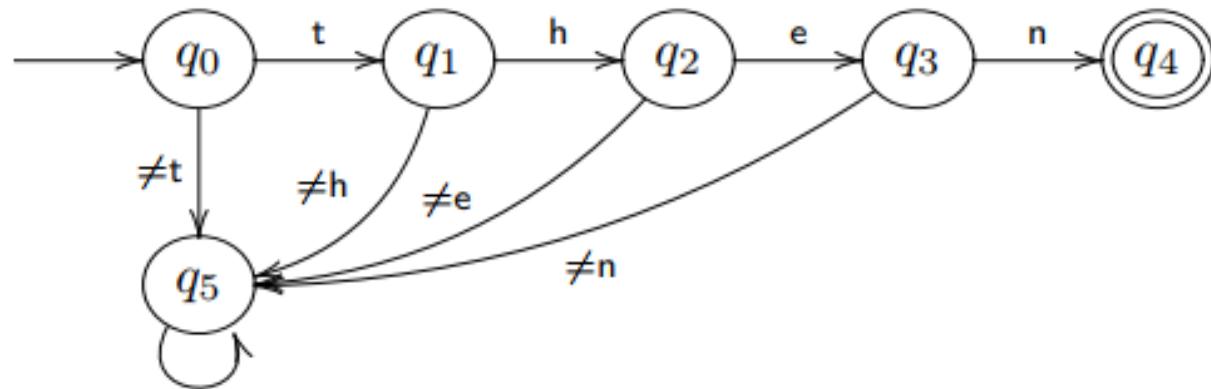
$$\delta(q_0, 0) = q_2$$



# DFA Example: password

When does the automaton accept a word??

It reads the word and accepts it if it stops in an accepting state



Only the word **then** is accepted

Here  $Q = \{q_0, q_1, q_2, q_3, q_4\}$

$\Sigma$  is the set of all characters

$F = \{q_4\}$

We have a “stop” or “dead” state  $q_5$ , *not* accepting

# How a DFA Processes Strings

Let us build an automaton that accepts the words that contain 01 as a subword

$$\Sigma = \{0, 1\}$$

$$L = \{x01y \mid x, y \in \Sigma^*\}$$

We use the following states

A: start

B: the most recent input was 1 (but not 01 yet)

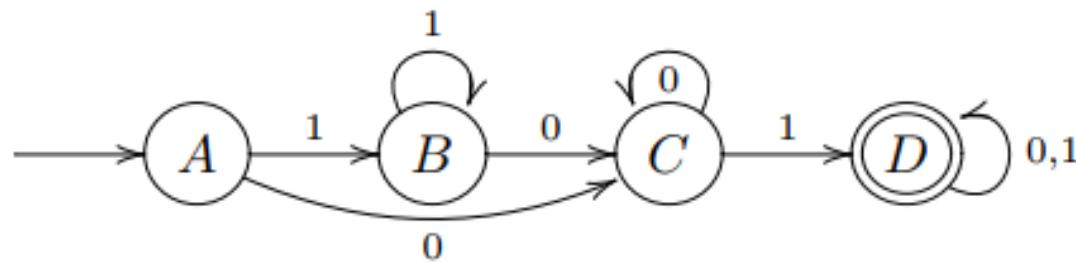
C: the most recent input was 0 (so if we get a 1 next we should go to the accepting state D)

D: we have encountered 01 (accepting state)



# How a DFA Processes Strings (Contd...)

We get the following automaton



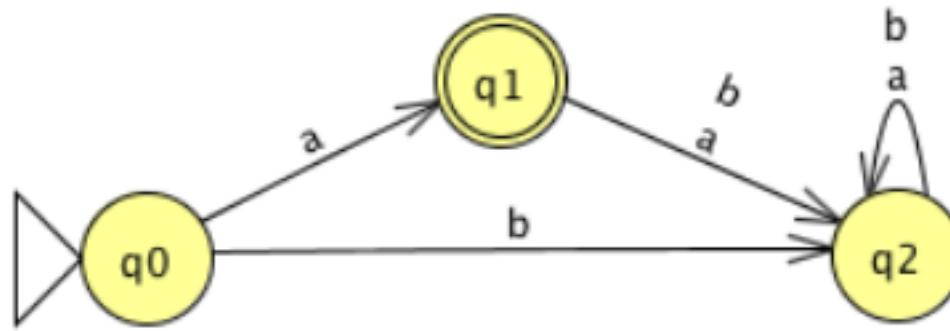
Transition table

	0	1
$\rightarrow A$	C	B
B	C	B
C	C	D
*D	D	D

$Q = \{A, B, C, D\}$ ,  $\Sigma = \{0, 1\}$ , start state A, final state(s) {D}



# DFA Example 2

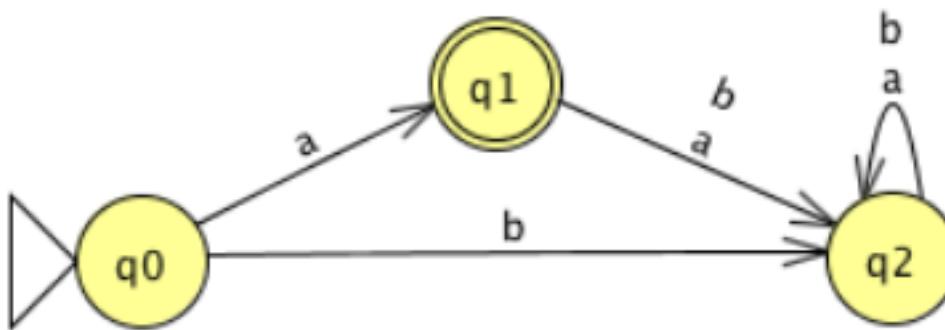


Formally, a DFA is described by a 5-tuple  $(Q, \Sigma, \delta, q_0, F)$  in which  
Q is a finite set of states,  
 $\Sigma$  is a finite set of input symbols also known as the **alphabet**,  
 $\delta$  is a state transition function ( $\delta : Q \times \Sigma \rightarrow Q$ ),  
 $q_0$  is the start state and  
F is a set of accept states.

For example, the DFA whose state diagram is shown above is represented by the 5-tuple  
 $(\{q_0, q_1, q_2\}, \{a, b\}, \delta \text{ as given by state diagram above}, q_0, \{q_1\})$



# DFA Example 2 – Contd...



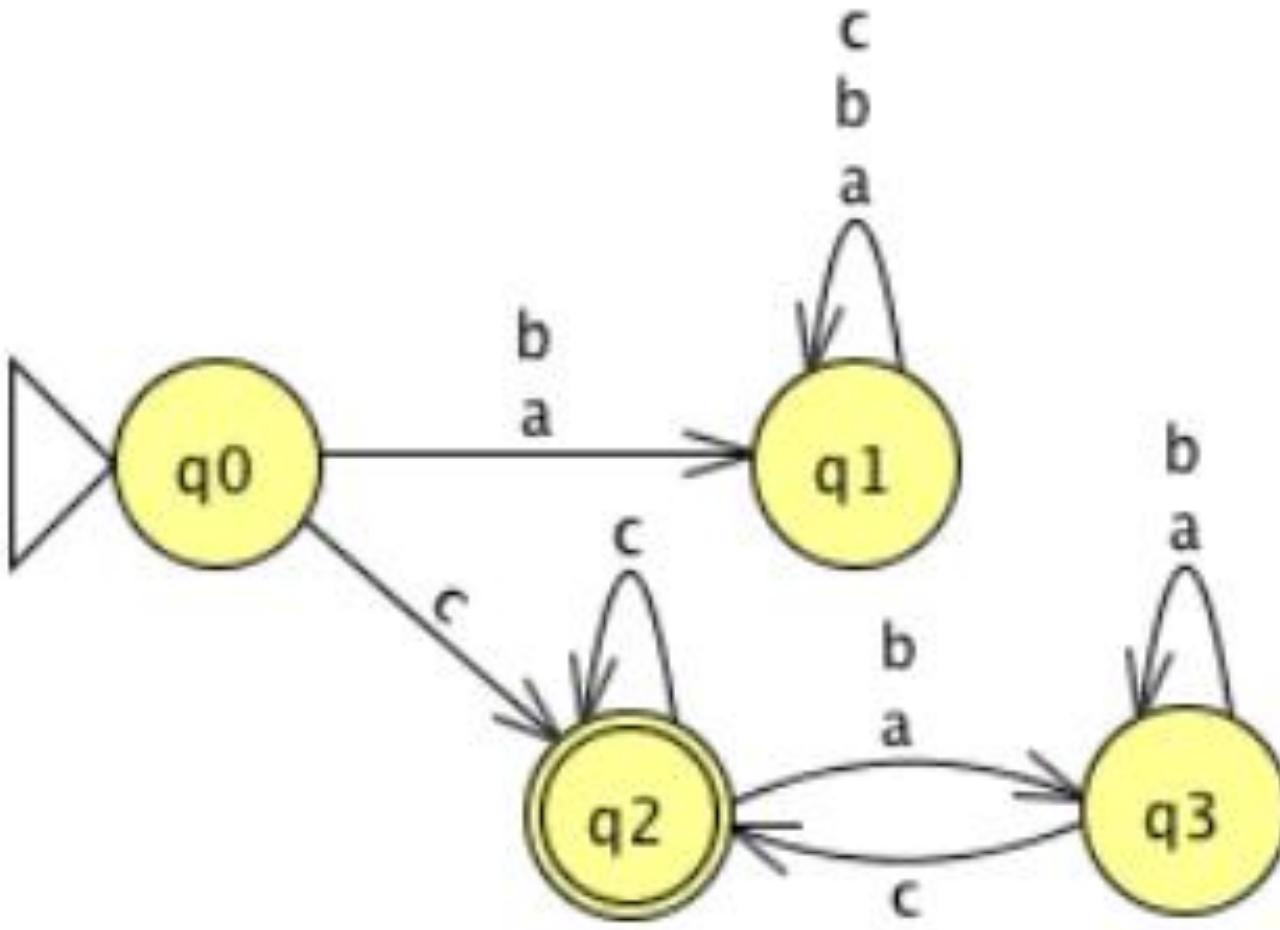
The transition function given by state diagram above is also described by the following table:

	a	b
q0	q1	q2
q1	q2	q2
q2	q2	q2

In the transition function of a DFA, every state has exactly one transition associated with each symbol of the alphabet. Because the DFA determines the unique next state for each next input symbol, this is a deterministic finite automaton.



# DFA Task - To be done by Students



# THANKS