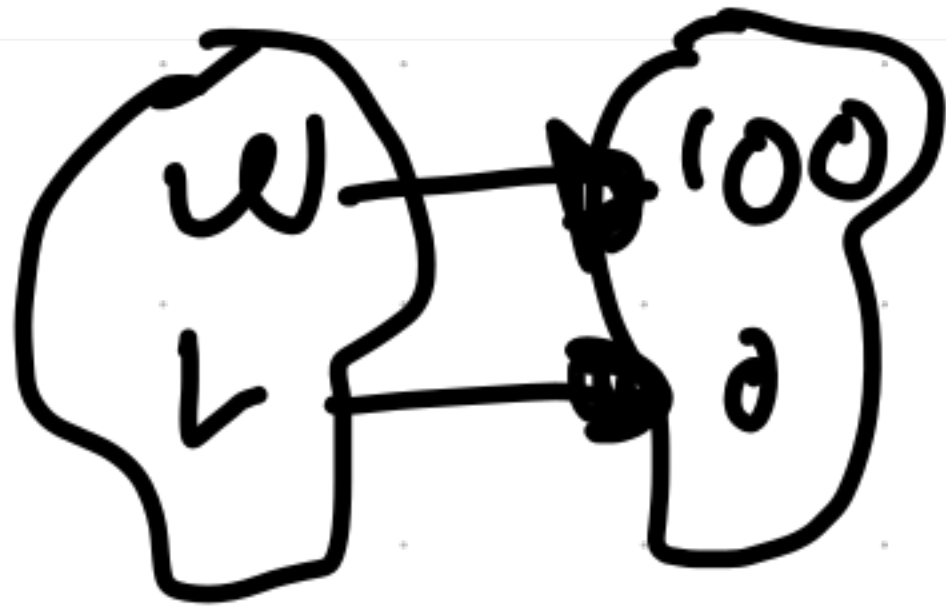


$$E[X] = \sum_{x_i \in X} P(x_i) x_i$$

$X$  is a r.v.

$$X: \Omega \rightarrow \mathbb{R} = .6 \cdot 100 + .4 \cdot 0 = 60$$



$$P(W) = .6$$

$$X_i = 100$$

$$P(L) = .4$$

$$X_i = 0$$

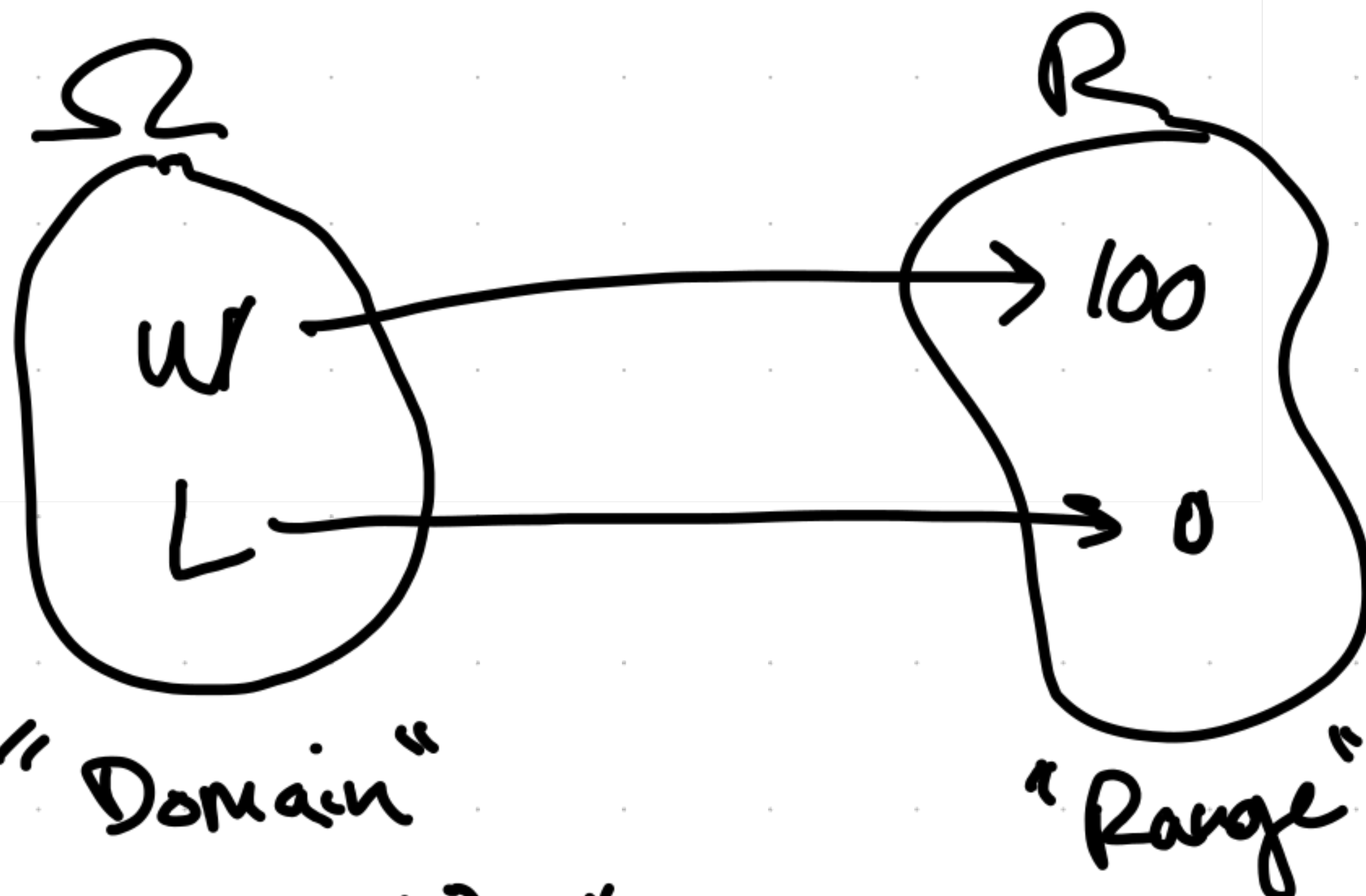
r.v.  $X$  is a function

$$X: \Omega \rightarrow \mathbb{R}$$

$$X := L \in \Omega$$

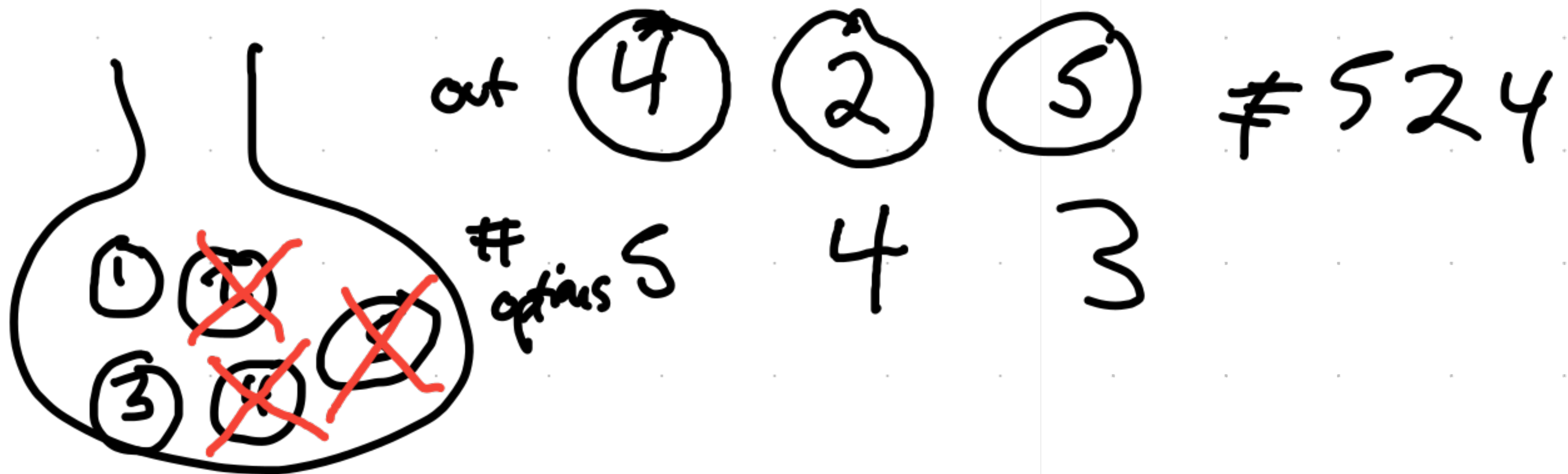
or

$$X := W \in \Omega$$



$$P(W) = .6 \quad P(L) = .4$$

# Permutations



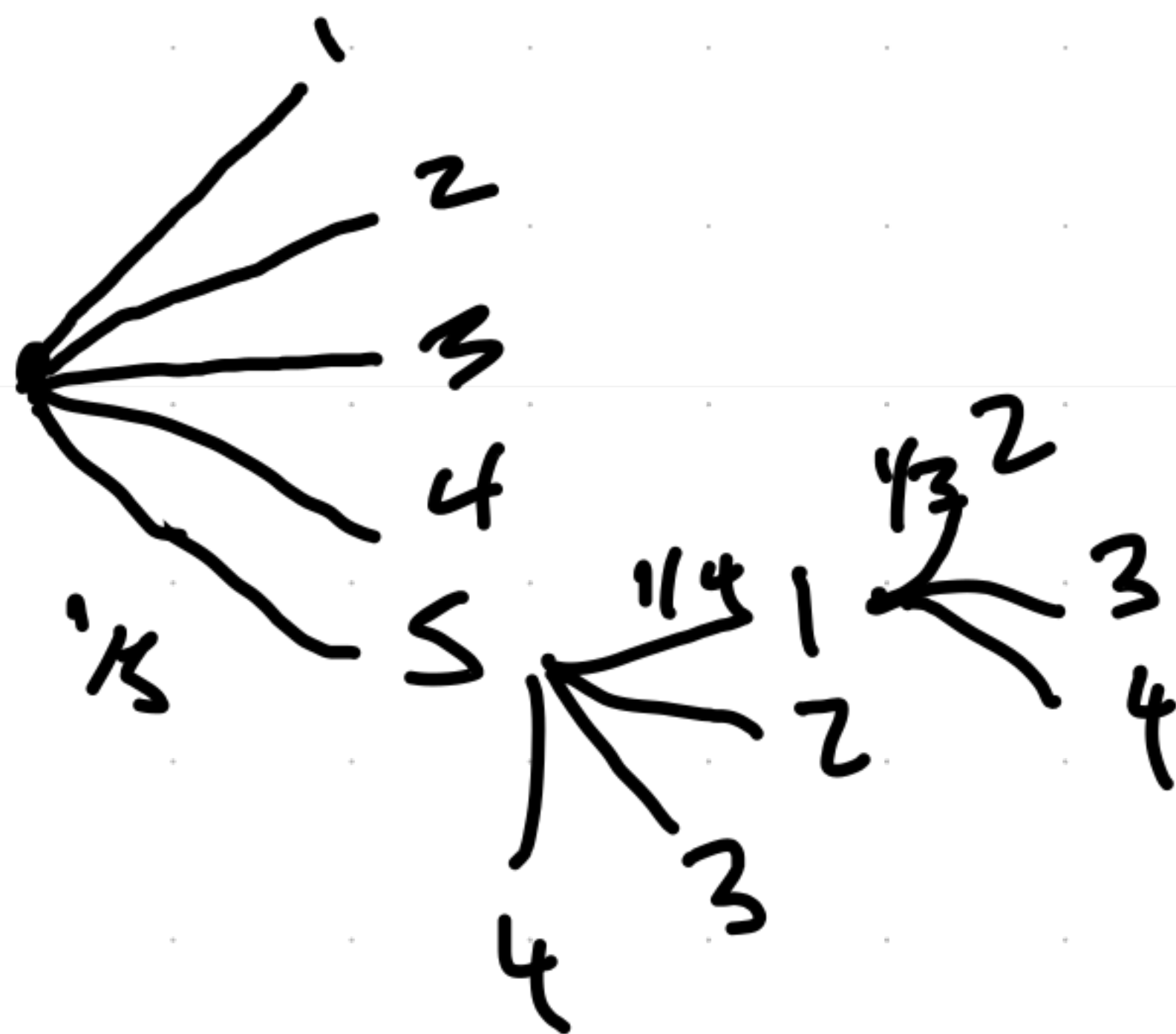
How many possible ways are there to draw 3 items from 5?  
 $5 \cdot 4 \cdot 3$



1000 ticket holders

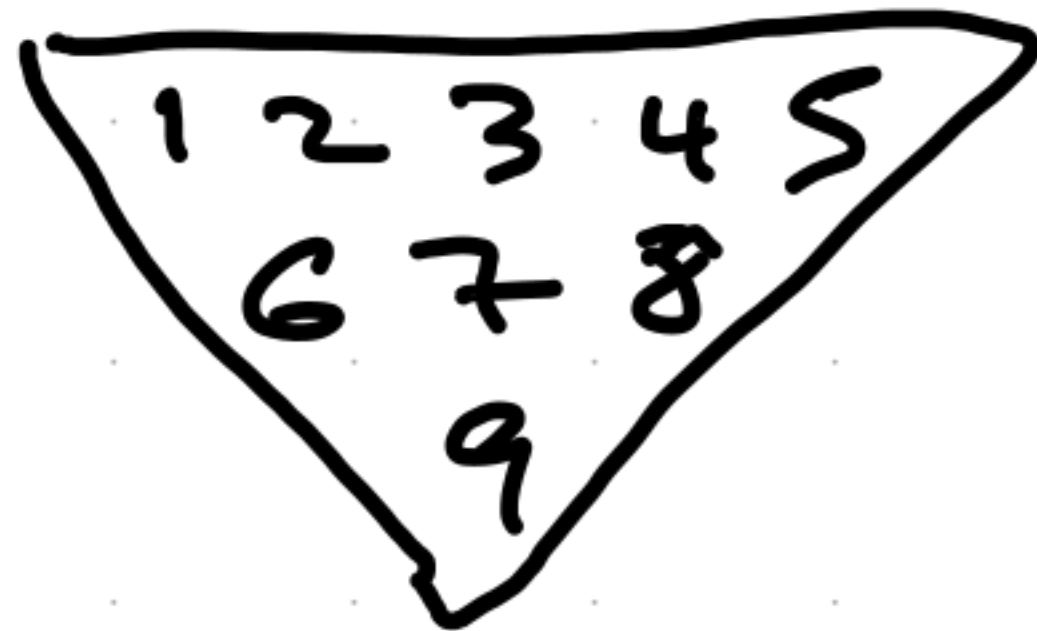
How many different #s  
can be formed?

$$5 \cdot 4 \cdot 3 = 60$$



$$\begin{array}{c} 123 \\ 234 \\ 512 \\ \vdots \end{array} \Bigg] 5 \cdot 4 \cdot 3$$

# of permutations

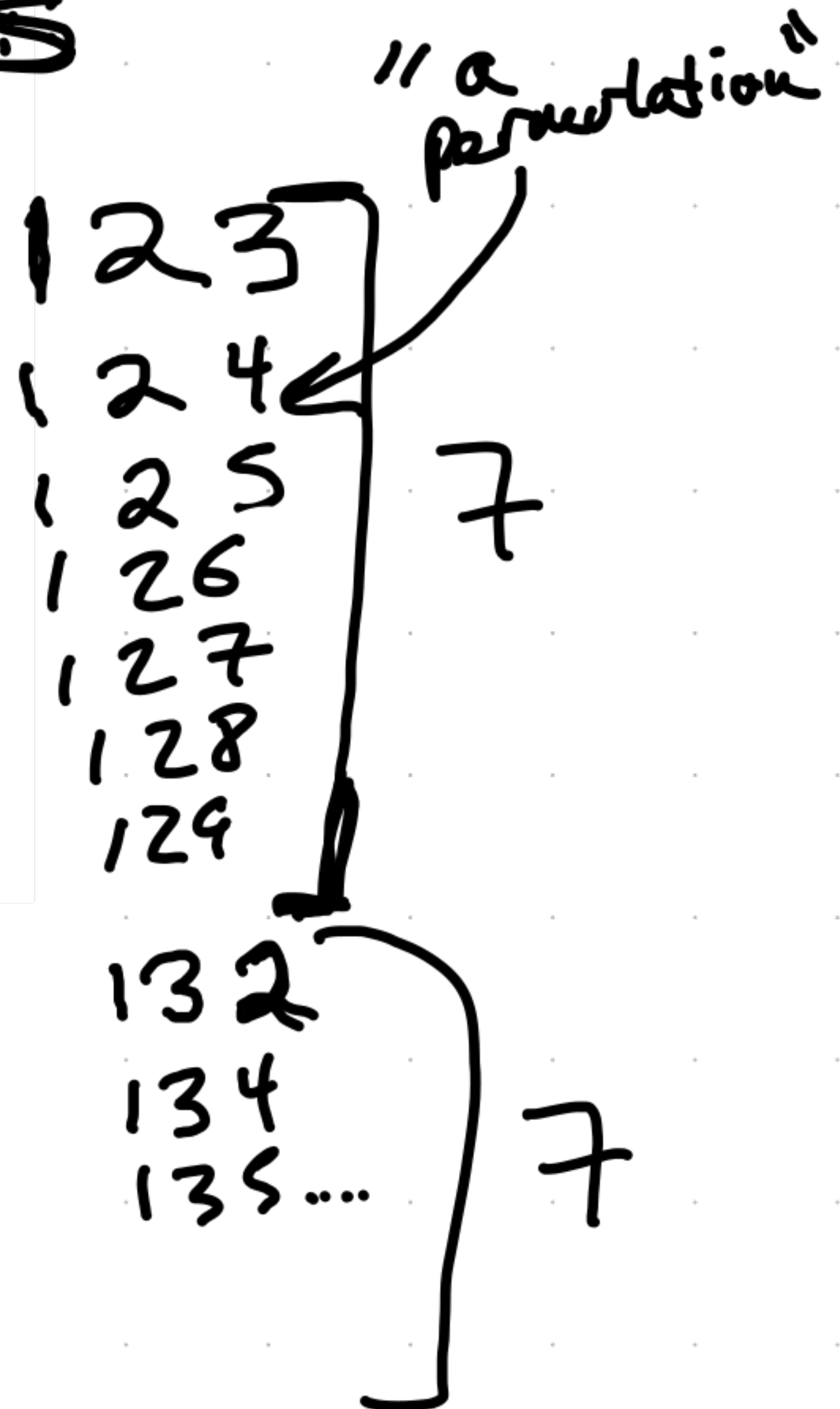


$9 \cdot 8 \cdot 7$

$1 \cdot 2 \cdot 3$



$9 \cdot 8 \cdot 7$



$n$  total of things (e.g. 9 pool balls)

↖ choose things (e.g. 3 pool balls)

$$n(n-1)(n-2)\dots(n-r)$$

9 things, choose 4 of them...

$$n(n-1)(n-2)(n-3)$$

$$9 \cdot 8 \cdot 7 \cdot 6$$

$$\nwarrow \begin{matrix} (n-r+1) \\ 9-4+1=6 \end{matrix}$$

$$5! = 5 \cdot 4 \cdot 3 \cdot 2 \cdot 1$$

5 items, choose 3, order matters

$$5 \cdot 4 \cdot 3 \text{ } \text{⬡}$$

$$5! = 5 \cdot 4 \cdot 3 \cdot 2 \cdot 1$$

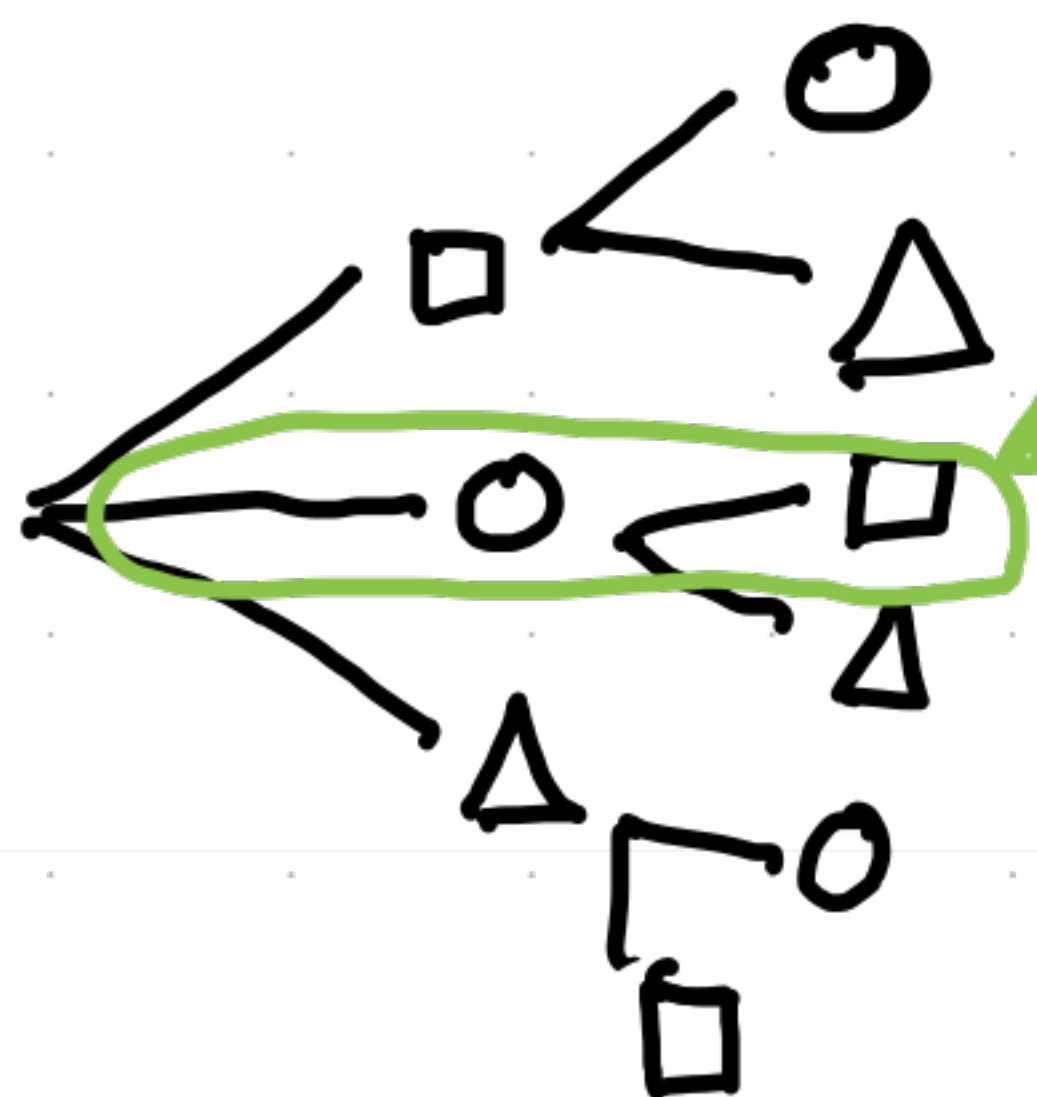
$$\boxed{5P_3} = \frac{5!}{2!} = \frac{5 \cdot 4 \cdot 3 \cdot 2 \cdot 1}{2 \cdot 1} = 5 \cdot 4 \cdot 3$$

$${}_nP_r = \frac{n!}{(n-r)!}$$

$${}_9P_2 = \frac{9!}{(9-2)!} = \frac{9!}{7!} = 9 \cdot 8$$







6  
 □○  
 □△

○□  
 ○△  
 △○  
 △□

$$3 \cdot 2 = 6$$

$${}_nP_r = \begin{matrix} n=3 \\ r=2 \end{matrix}$$

$$= \frac{n!}{(n-r)!}$$

$$= \frac{3!}{1!} = \frac{3 \cdot 2 \cdot 1}{1}$$