

2. Gravitation

For the satellite to be in a circular orbit, we know:

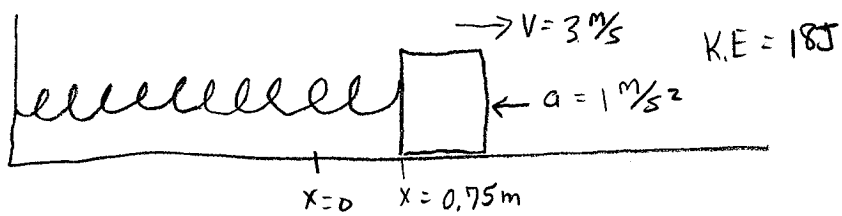
$$\Sigma F = G \frac{m_s m_E}{(R_E + h)^2} = m_s a_s = m_s \frac{V_s^2}{(R_E + h)}$$

$$\Rightarrow V_s = \sqrt{\frac{G m_E}{(R_E + h)}}$$

$$= \sqrt{\frac{6.67 \times 10^{-11} \frac{\text{m}^3}{\text{kg s}^2} \cdot 5.97 \times 10^{24} \text{ kg}}{(6.37 \times 10^6 \text{ m} + 3.00 \times 10^6 \text{ m})}}$$

$$V_s = 6.5 \times 10^3 \frac{\text{m}}{\text{s}}$$

1) Simple Harmonic Motion



$$|F| = kx = ma \Rightarrow \frac{k}{m} = \frac{a}{x}$$

$$K.E = 18 \text{ J} = \frac{1}{2} m v^2 \Rightarrow m = \frac{2 \cdot K.E}{v^2} = 4 \text{ kg}$$

$$\therefore k = \frac{ma}{x} = \frac{(4 \text{ kg})(1 \text{ m/s}^2)}{0.75 \text{ m}} = 5.33 \frac{\text{N}}{\text{m}}$$

$$U = \frac{1}{2} k x^2 = \frac{1}{2} (5.33 \frac{\text{N}}{\text{m}}) (0.75 \text{ m})^2 = 1.5 \text{ J}$$

$$\therefore E_{\text{tot}} = K.E + U = 18 \text{ J} + 1.5 \text{ J} = 19.5 \text{ J} = K.E_{\text{max}}$$

$$= \frac{1}{2} m v_{\text{max}}^2 \Rightarrow$$

$$v_{\text{max}} = \sqrt{\frac{2 K.E_{\text{max}}}{m}} = 3.12 \frac{\text{m}}{\text{s}}$$