

## #8 Circular Motion Pre-class

Due: 11:00am on Monday, September 10, 2012

**Note:** *You will receive no credit for late submissions.* To learn more, read your instructor's [Grading Policy](#)

### Exercise 3.33

A Ferris wheel with radius  $14.0\text{ m}$  is turning about a horizontal axis through its center (the figure ). The linear speed of a passenger on the rim is constant and equal to  $6.99\text{ m/s}$  .



#### Part A

What is the magnitude of the passenger's acceleration as she passes through the lowest point in her circular motion?

ANSWER:

$$a = 3.49 \text{ m/s}^2$$

**Correct**

#### Part B

What is the direction of the passenger's acceleration as she passes through the lowest point in her circular motion?

ANSWER:

- ☒ towards the center
- ☐ outwards the center

**Correct**

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### Part C

What is the magnitude of the passenger's acceleration as she passes through the highest point in her circular motion?

ANSWER:

$$a = 3.49 \text{ m/s}^2$$

**Correct**

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### Part D

What is the direction of the passenger's acceleration as she passes through the highest point in her circular motion?

ANSWER:

- ☒ towards the center
- ☐ outwards the center

Correct

### Part E

How much time does it take the Ferris wheel to make one revolution?

ANSWER:

$$T = 12.6 \text{ s}$$

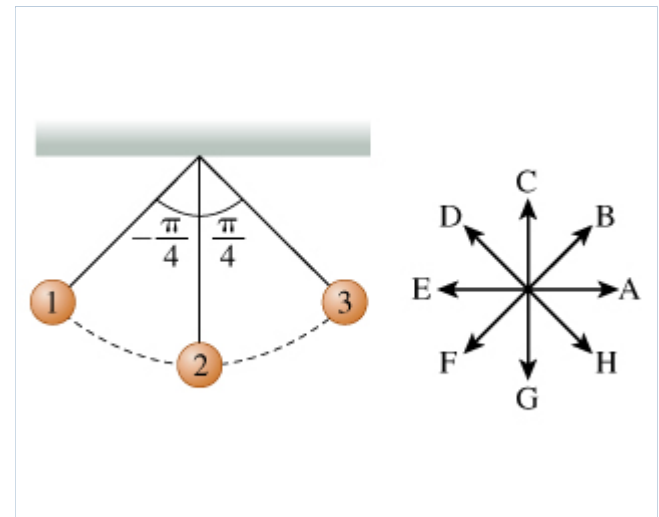
Correct

## Direction of Acceleration of Pendulum

### Learning Goal:

To understand that the direction of acceleration is in the direction of the *change* of the velocity, which is unrelated to the direction of the velocity.

The pendulum shown makes a full swing from  $-\pi/4$  to  $+\pi/4$ . Ignore friction and assume that the string is massless. The eight labeled arrows represent directions to be referred to when answering the following questions.



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**Part A**

Which of the following is a true statement about the acceleration of the pendulum bob,  $\vec{a}$ .

ANSWER:

- ☐  $\vec{a}$  is equal to the acceleration due to gravity.
- ☒  $\vec{a}$  is equal to the instantaneous rate of change in velocity.
- ☐  $\vec{a}$  is perpendicular to the bob's trajectory.
- ☐  $\vec{a}$  is tangent to the bob's trajectory.

**Correct**

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**Part B**

What is the direction of  $\vec{a}$  when the pendulum is at position 1?

**Enter the letter of the arrow parallel to  $\vec{a}$ .**

**Hint 1. Velocity at position 1**

What is the velocity of the bob when it is exactly at position 1?

ANSWER:

$$v_1 = 0 \text{ m/s}$$

**Hint 2. Velocity of bob after it has descended**

What is the velocity of the bob just after it has descended from position 1?

ANSWER:

- ☐ very small and having a direction best approximated by arrow D
- ☐ very small and having a direction best approximated by arrow A
- ☒ very small and having a direction best approximated by arrow H
- ☐ The velocity cannot be determined without more information.

ANSWER:

H

**Correct**

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**Part C**

What is the direction of  $\vec{a}$  at the moment the pendulum passes position 2?

**Enter the letter of the arrow that best approximates the direction of  $\vec{a}$ .**

**Hint 1. Instantaneous motion**

At position 2, the instantaneous motion of the pendulum can be approximated as uniform circular motion. What is the direction of acceleration for an object executing uniform circular motion?

ANSWER:

**Correct**

We know that for the object to be traveling in a circle, some component of its acceleration must be pointing radially inward.

**Part D**

What is the direction of  $\vec{a}$  when the pendulum reaches position 3?

**Give the letter of the arrow that best approximates the direction of  $\vec{a}$ .**

**Hint 1. Velocity just before position 3**

What is the velocity of the bob just before it reaches position 3?

ANSWER:

- ☒ very small and having a direction best approximated by arrow B
- ☐ very small and having a direction best approximated by arrow C
- ☐ very small and having a direction best approximated by arrow H
- ☐ The velocity cannot be determined without more information.

**Hint 2. Velocity of bob at position 3**

What is the velocity of the bob when it reaches position 3?

ANSWER:

ANSWER:

F

**Correct**

### Part E

As the pendulum *approaches* or *recedes from* which position(s) is the acceleration vector  $\vec{a}$  almost parallel to the velocity vector  $\vec{v}$ .

ANSWER:

- ☐ position 2 only
- ☐ positions 1 and 2
- ☐ positions 2 and 3
- ☒ positions 1 and 3

**Correct**

## Exercise 3.32

The radius of the earth's orbit around the sun (assumed to be circular) is  $1.50 \times 10^8$  km, and the earth travels around this orbit in 365 days.

### Part A

What is the magnitude of the orbital velocity of the earth in m/s?

ANSWER:

$$2.97 \times 10^4 \text{ m/s}$$

All attempts used; correct answer displayed

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### Part B

What is the radial acceleration of the earth toward the sun?

ANSWER:

$$5.91 \times 10^{-3} \text{ m/s}^2$$

Correct

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### Part C

What is the magnitude of the orbital velocity of the planet Mercury (orbit radius =  $5.79 \times 10^7 \text{ km}$ , orbital period = 88.0 days)?

ANSWER:

$$4.78 \times 10^4 \text{ m/s}$$

Correct

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### Part D



What is the radial acceleration of the Mercury?

ANSWER:

$$3.95 \times 10^{-2} \text{ m/s}^2$$

**Correct**

## Test Your Understanding 3.4: Circular Motion

An object moves around a horizontal circle at constant speed.

### Part A

If the radius of the circle is halved while the speed of the object is doubled, how does the acceleration of the object change?

ANSWER:

- ☐ it becomes 2 times as great
- ☒ it becomes 8 times as great
- ☐ it becomes 1/2 as great
- ☐ it remains the same
- ☐ it becomes 4 times as great

**Correct**

The acceleration of an object moving at a constant speed  $v$  in a horizontal circle of radius  $R$  is  $a_{\text{rad}} = v^2/R$ . If  $v$  increases by a factor of 2 and  $R$  becomes  $1/2$  as great, the acceleration increases by a factor of  $2^2 / (1/2) = 2^3 = 8$ .

## Score Summary:

Your score on this assignment is 89.5%.

You received 17.89 out of a possible total of 20 points.