

EECE 238 Exam II Regular

Name: Solutions

Problem 1 25/25

Problem 2 25/25

Problem 3 30/30

Problem 4 20/20

Total: 100/100

Good Luck!

Problem 1 (25 points total) Counter with Parallel Load

The digital logic circuit below represents a 4-Bit Binary Counter with Parallel Load.

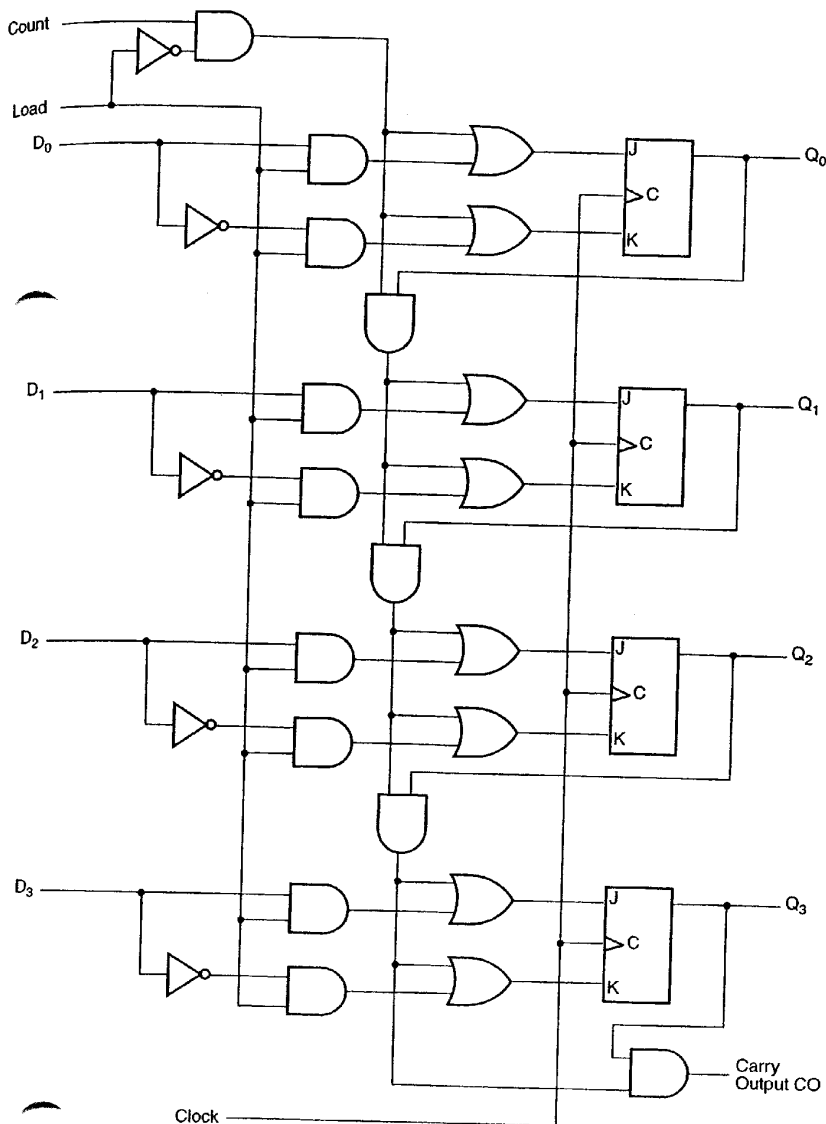
Assume that originally, all the ~~0~~ Flip-Flops store 0: ~~0000~~ ~~0000~~ ~~0000~~ ~~0000~~.

1(a) (5 points) Indicate how to make the counter count. How should you connect the inputs?

The following steps are used to make the counter count from 2 to 5. *For full-credit in parts 1(b) and 1(c), you must show the clock input, all the affected inputs (possible inputs are: D_0, D_1, D_2, D_3 , Load, and Count), and all the outputs: Q_0, Q_1, Q_2, Q_3 .*

1(b) (5 points) Indicate how to load 2 into the counter.

1(c) (15 points) Show how to make the counter count to 5, and then stop.



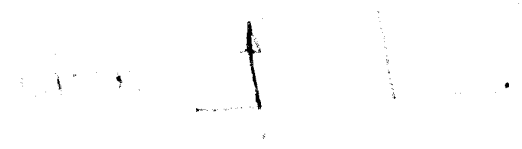
100) For counting

$$\text{Count} = 1$$

$$\text{Lead} = 0$$

and the other input is connected to the clock.

106)



$$D_1 = 1$$

$$Q_1 = 1$$

$$D_1 = 1$$

only a clock change

$$D_2 = 0$$

$$Q_2 = 0$$

$$D_3 = 1$$

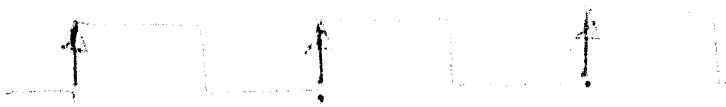
$$Q_3 = 1$$

Lead

After counting, lead
you have to zero



100) Some of the ...



... after the third ...



... and ...

Problem 2 (25 points total) Synchronous Counter Design.

Design a binary counter that counts through the 3-bit binary numbers: 000, 001, 010, 100, and then repeat from 000. For your design, assume that there is a reset signal that will force counting to start at 000. Assume that the states codes are assigned unsigned integer representations.

2 (a) (5 points) Draw the state transition diagram.

2 (b) (10 points) Derive the state table for implementing the counter using S-R Flip-Flops.

2 (c) (5 points) Use K-maps to minimize the inputs to the S-R Flip-Flops.

2 (d) (5 points) Indicate the final circuit.

2(a)



2(a) → 2(b)

Present State	Next State	S ₂	R ₂	S ₁	R ₁	S ₀	R ₀
000	001	0	0	0	0	1	0
001	010	0	0	1	0	0	0
010	100	0	0	0	1	0	0
011	xxx	xx	xx	xx	xx	xx	xx
100	000	0	0	0	0	0	0
101	xxx	xx	xx	xx	xx	xx	xx
110	xxx	xx	xx	xx	xx	xx	xx
111	xxx	xx	xx	xx	xx	xx	xx

2(b)

Present State	Next State	S ₂	R ₂	S ₁	R ₁	S ₀	R ₀
000	001	0	0	0	0	1	0
001	010	0	0	1	0	0	0
010	100	0	0	0	1	0	0
011	xxx	xx	xx	xx	xx	xx	xx
100	000	0	0	0	0	0	0
101	xxx	xx	xx	xx	xx	xx	xx
110	xxx	xx	xx	xx	xx	xx	xx
111	xxx	xx	xx	xx	xx	xx	xx

200)

$Q_2 \backslash Q_1$

0	0	0	1	0
1	0	1	1	1

$S_{10} = 0, S_{11} = 1$

$Q_2 \backslash Q_1$

0	1	1	0	0
1	1	1	1	1

$S_{10} = 1, S_{11} = 0$

$Q_2 \backslash Q_1$

0	0	1	1	0
1	0	1	1	1

$S_{10} = 0, S_{11} = 1$

$Q_2 \backslash Q_1$

0	1	1	1	0
1	1	1	1	1

$S_{10} = 1, S_{11} = 0$

$Q_2 \backslash Q_1$

0	0	1	1	0
1	0	1	1	1

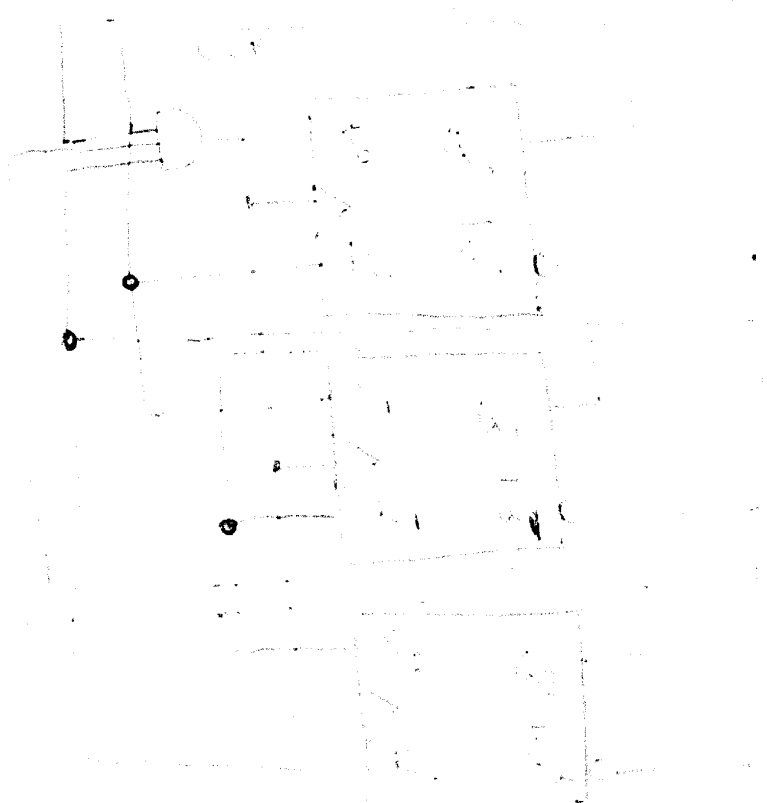
$S_{10} = 0, S_{11} = 1$

$Q_2 \backslash Q_1$

0	1	1	1	0
1	1	1	1	1

$S_{10} = 1, S_{11} = 0$

201)



closed

Problem 3 (20 points total) Sequential Circuit Design

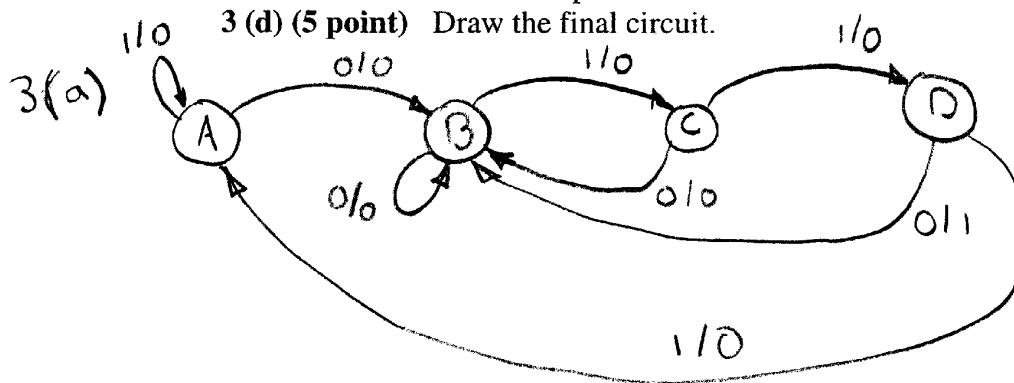
Design a digital circuit to recognize the occurrence of the input sequence 0110. The circuit will output a 1 when the previous inputs were 011 and the current input is 0. Note that since the output depends on the input (as well as the current state), you need a *Mealy* solution to this problem.

3 (a) (5 points) Derive the state transition diagram.

3 (b) (5 points) Derive the state table and Flip-Flop inputs for J-K Flip-Flops.

3 (c) (5 points) Use Karnaugh maps to minimize the equations for the Flip-Flop inputs, and the output.

3 (d) (5 point) Draw the final circuit.



A: no '0' yet
B: "0" received
C: "01" received
D: "011" received

3(b)

Present State	I=0		I=1		I=0		I=1		Out
	Next State	J, K	Next State	J, K	Next State	J, K	Next State	J, K	
A: 00	B: 01	0x	A: 00	1x	0x	0x	00	00	
B: 01	B: 01	0x	C: 11	x0	1x	x0	00	00	
C: 11	B: 01	x1	D: 10	x0	x0	x1	00	00	
D: 10	B: 01	x1	A: 00	1x	x1	0x	10	10	

$Q_1, Q_0 \rightarrow Q(t+1)$	J	K
00	0	x
01	1	x
11	x	1
10	x	0

3(c)

$Q_1, Q_0 \backslash I$	0	1
00	0	0
01	0	1
11	x	x
10	x	x

$J_1 = Q_0 I$

$Q_1, Q_0 \backslash I$	0	1
00	x	x
01	x	x
11	1	0
10	x	1

$K_1 = I + Q_0$

$Q_1, Q_0 \backslash I$	0	1
00	1	0
01	x	x
11	x	x
10	1	0

$J_0 = I$

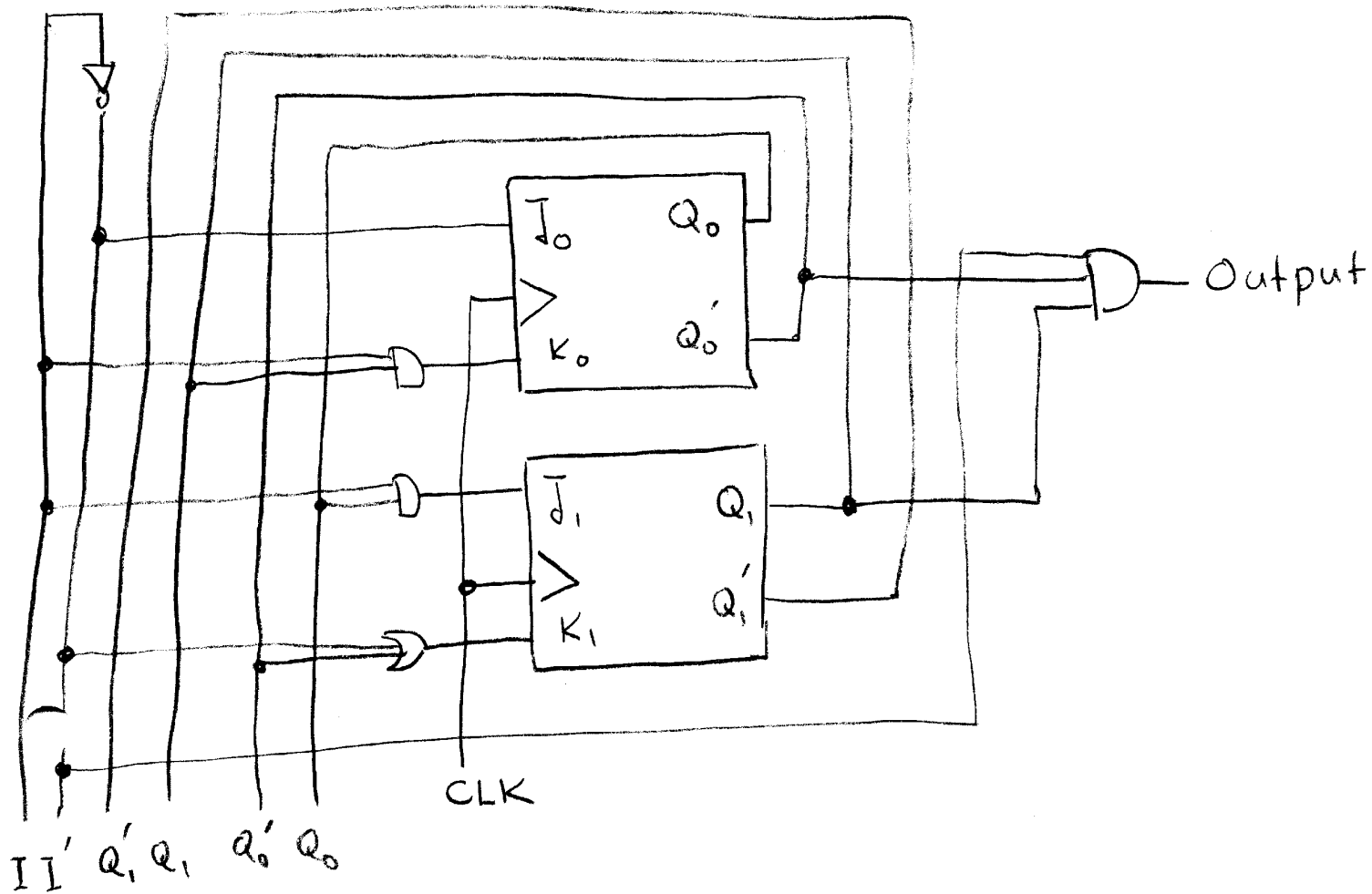
$Q_1, Q_0 \backslash I$	0	1
00	x	x
01	0	0
11	0	1
10	x	x

$K_0 = I Q_1$

$$\text{Output} = I' Q_1 Q_0'$$

3(d)

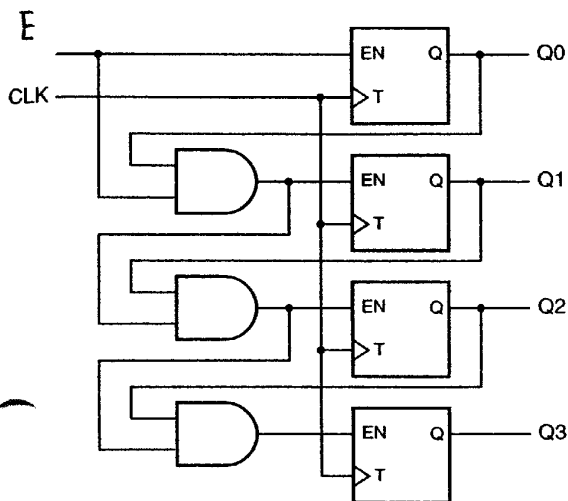
I



Problem 4 (20 points total) Sequential Circuit Analysis

Consider the sequential circuit given below. We would like to analyze the circuit and understand what it does.

- 4 (a) (5 points) Derive the T flip-flop input equations.
 4 (b) (5 points) Derive the next-state table based on 3(a).
 4 (c) (5 points) Derive the state-diagram based on the next-state table.
 4 (d) (5 points) What does this circuit do?



$$4(a) \quad Q_{0,EN} = E$$

$$Q_{1,EN} = EQ_0$$

$$Q_{2,EN} = EQ_0Q_1$$

$$Q_{3,EN} = EQ_0Q_1Q_2$$

Next state ← table for E=1

4(b) Present state

$Q_3Q_2Q_1Q_0$	$Q_{3,EN}$	$Q_{2,EN}$	$Q_{1,EN}$	$Q_{0,EN}$	Q_3^+	Q_2^+	Q_1^+	Q_0^+
0000	0	0	0	1	0	0	0	1
0001	0	0	1	1	0	0	1	0
0010	0	0	0	1	0	0	1	1
0011	0	0	1	1	0	1	0	0
0100	0	0	0	1	0	1	0	1
0101	0	0	1	1	0	1	1	0
0110	0	0	0	1	0	1	1	1
0111	1	1	1	1	1	0	0	0
1000	0	0	0	1	1	0	0	1
1001	0	0	1	1	1	0	1	0
1010	0	0	0	1	1	0	1	1
1011	0	1	1	1	1	1	0	0
1100	0	0	0	1	1	1	0	1
1101	0	0	1	1	1	1	1	0
1110	0	0	0	1	1	1	1	1
1111	1	1	1	1	0	0	0	0

440

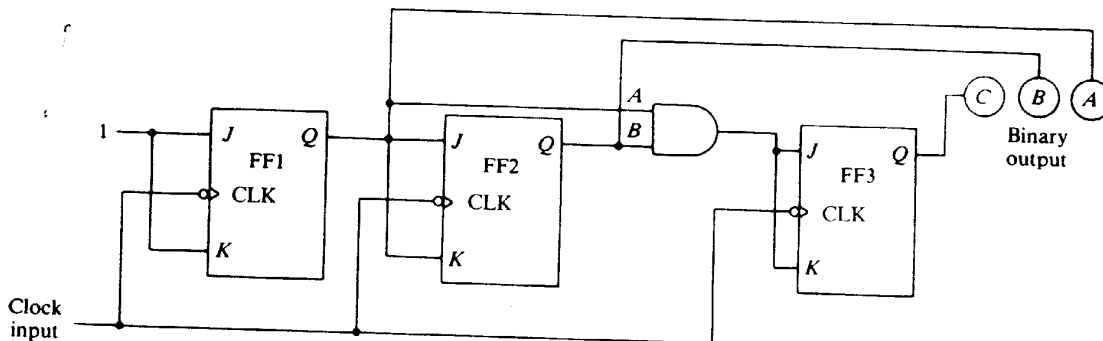


44d) When I write the circuit counts
from C to 15 and then back from 15 to C.

Problem 3 (30 points total) Sequential Circuit Analysis

Consider the sequential circuit given below. We would like to analyze the circuit and understand what it does.

- 3(a) (5 points) Derive the J-K flip-flop input equations.
- 3(b) (15 points) Derive the next-state table based on 3(a).
- 3(c) (5 points) Derive the state-diagram based on the next-state table.
- 3(d) (5 points) What does this circuit do?



Problem 4 (20 points total) *Sequential Circuit Analysis*

Consider the sequential circuit given below. We would like to analyze the circuit and understand what it does.

- 4 (a) (5 points) Derive the T flip-flop input equations.
- 4 (b) (5 points) Derive the next-state table based on (a).
- 4 (c) (5 points) Derive the state-diagram based on the next-state table.
- 4 (d) (5 points) What does this circuit do?

