

Homework 4, Due Date (Thursday, Feb 21st, 2013, In Class)

Problem 4.25

For the common-source circuit in Figure P4.24, the bias voltages are changed to $V^+ = 3\text{ V}$ and $V^- = -3\text{ V}$. The PMOS transistor parameters are: $V_{TP} = -0.5\text{ V}$, $K_p = 0.8\text{ mA/V}^2$, and $\lambda = 0$. The load resistor is $R_L = 2\text{ k}\Omega$. (a) Design the circuit such that $I_{DQ} = 0.25\text{ mA}$ and $V_{SDQ} = 1.5\text{ V}$. (b) Determine the small-signal voltage gain $A_v = v_o/v_i$.

$$0.25\text{ mA} = 0.8\text{ mA/V}^2 (|V_{GS}| - |-0.5\text{ V}|)^2$$

$$0.25\text{ mA} = 0.8\text{ mA} ((0 - (-3 - 0.25\text{ mA}(R_S))) - |-0.5|)^2$$

$$R_S = 7.764\text{ k}\Omega$$

$$V_{RS} = 0.25\text{ mA}(7.764\text{ k}) \Rightarrow V_{RS} = 1.941\text{ V}$$

$$V_S = 3 - 1.941\text{ V} \Rightarrow V_S = 1.059\text{ V}$$

$$V_D = 6 - 1.941 - 1.5$$

$$V_D = 2.56\text{ V}$$

$$R_D = \frac{2.56\text{ V}}{0.25\text{ mA}} = 10.24\text{ k}\Omega = R_D$$

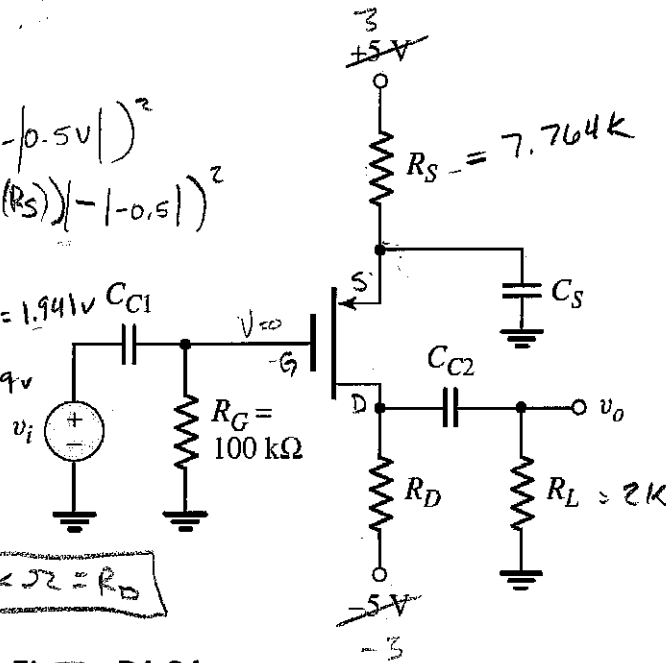
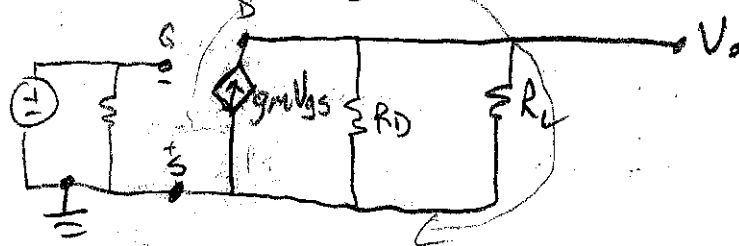


Figure P4.24



$$g_m = 2\sqrt{K_p I_{DQ}}$$

$$g_m = 2\sqrt{0.8\text{ mA}(0.25\text{ mA})} \Rightarrow g_m = 894.427\mu\text{ S}$$

$$A_v = \frac{v_o}{v_{in}} \Rightarrow$$

$$v_o = -g_m v_{gs} (R_D // R_L)$$

$$v_{gs} = v_g - v_s \Rightarrow v_g = v_{gs} + v_s = v_i$$

$$A_v = \frac{-g_m v_{gs} (R_D // R_L)}{v_{gs}} \Rightarrow A_v = -g_m (R_D // R_L) = -894.427\mu\text{ S} \left(\frac{1}{7.764\text{ k}} + \frac{1}{2\text{ k}} \right)$$

$$A_v = -1.422$$

Problem 4.31

The open-circuit ($R_L = \infty$) voltage gain of the ac equivalent source-follower circuit shown in Figure P4.31 is $A_v = 0.98$. When R_L is set to $1\text{ k}\Omega$, the voltage gain is reduced to $A_v = 0.49$. What are the values of g_m and r_o ?

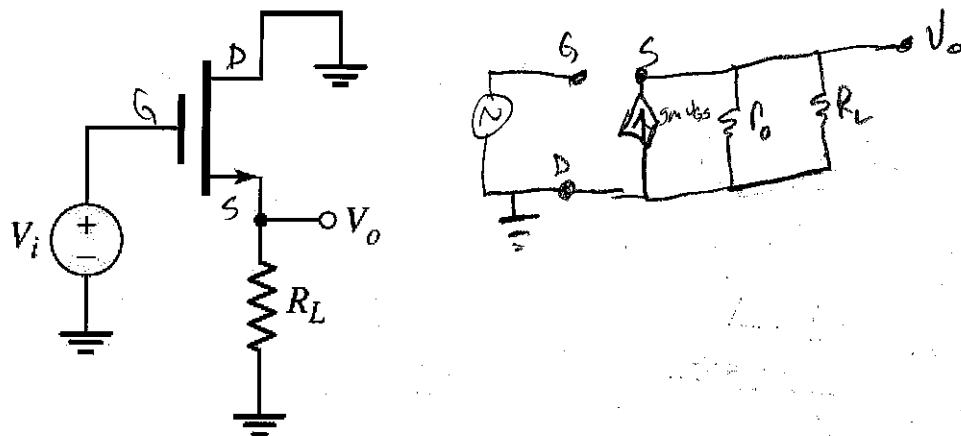


Figure P4.31

$$A_v = 0.98, R_L = \infty$$

$$0.98 = \frac{g_m(r_o)}{1 + g_m(r_o)}$$

$$0.98 + 0.98 g_m(r_o) = g_m(r_o)$$

$$0.98 = 0.02 g_m(r_o)$$

$$g_m(r_o) = 49$$

$$g_m = \frac{49}{r_o}$$

$$A_v = 0.49, R_L = 1\text{ k}\Omega$$

$$0.49 = \frac{g_m(r_o // 1\text{ k})}{1 + g_m(r_o // 1\text{ k})}$$

$$0.49 + 0.49 g_m(r_o // 1\text{ k}) = g_m(r_o // 1\text{ k})$$

$$0.49 = 0.51 g_m(r_o // 1\text{ k})$$

$$0.49 = 0.51 \left(\frac{49}{r_o} \right) \left(\frac{1}{\frac{1}{r_o} + \frac{1}{1\text{ k}}} \right)$$

$$\frac{0.49 r_o}{(0.51)(49)} = \frac{1}{\frac{1}{r_o} + \frac{1}{1\text{ k}}} \Rightarrow r_o \left(\frac{1}{r_o} + \frac{1}{1\text{ k}} \right) = \frac{0.51(49)}{0.49}$$

$$1 + \frac{r_o}{1\text{ k}} = 51 \Rightarrow \frac{r_o}{1\text{ k}} = 50 \Rightarrow r_o = 50\text{ k}\Omega$$

$$A_v = \frac{V_o}{V_i} \Rightarrow$$

$$V_o = g_m v_{gs} (r_o // R_L)$$

$$V_{gs} = V_g - V_s \Rightarrow V_g = V_{gs} + V_s$$

$$V_{in} = V_g = V_{gs} + V_s \quad V_s = V_o$$

$$V_{in} = V_{gs} + g_m v_{gs} (r_o // R_L)$$

$$= v_{gs} (1 + g_m (r_o // R_L))$$

$$A_v = \frac{g_m (r_o // R_L)}{1 + g_m (r_o // R_L)}$$

$$g_m = \frac{49}{r_o} \Rightarrow g_m = \frac{49}{50\text{ k}}$$

$$g_m = 0.98\text{ mA/V}$$

Problem 4.37

Consider the source follower circuit in Figure P4.37 with transistor parameters $V_{TN} = 0.8 \text{ V}$, $k_n' = 100 \mu\text{A/V}^2$, $W/L = 20$, and $\lambda = 0.02 \text{ V}^{-1}$. (a) Let $I_Q = 5 \text{ mA}$.

(i) Determine the small-signal voltage gain. (ii) Find the output resistance R_o .

(b) Repeat part (a) for $I_Q = 2 \text{ mA}$.

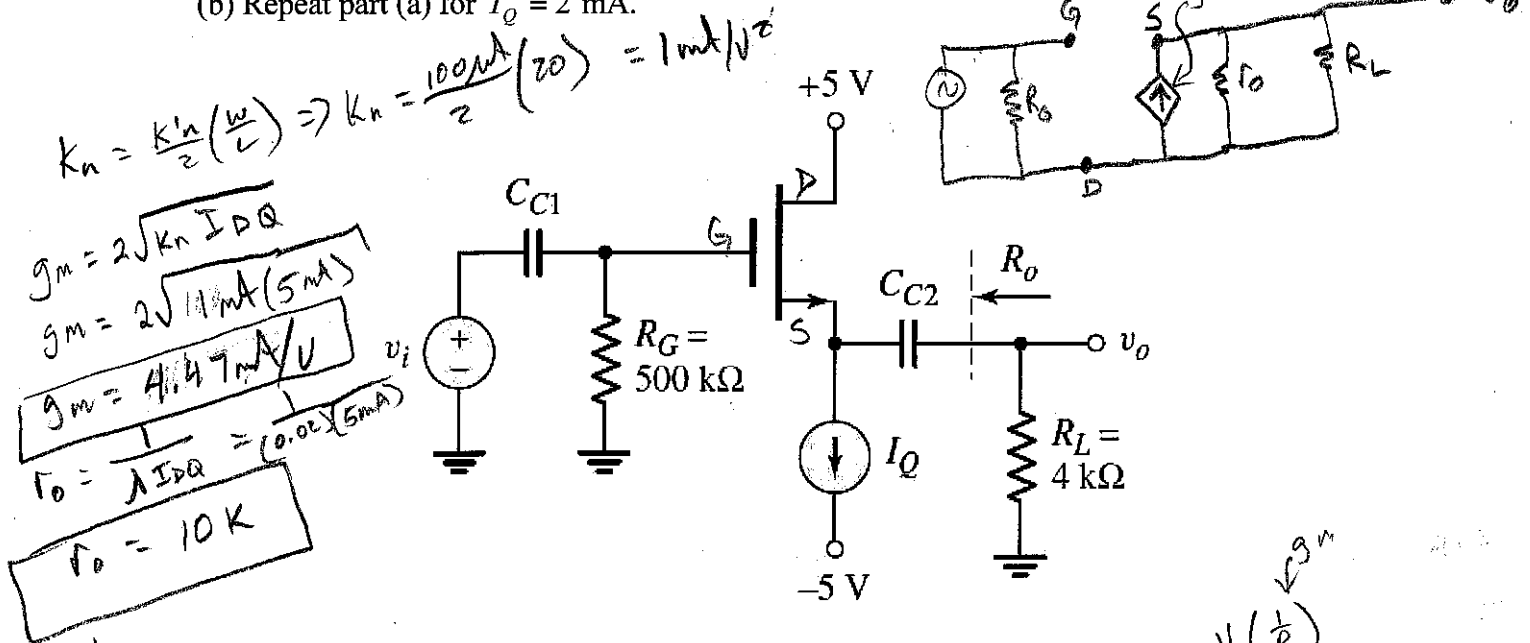


Figure P4.37

$$A_v = \frac{v_o}{v_{in}}$$

$$V_{GS} = V_G - V_S \Rightarrow V_{in} = V_{GS} + V_S$$

$$V_{in} = V_{GS} + V_o$$

$$V_o = g_m V_{GS} (r_o \parallel R_L)$$

$$A_v = \frac{g_m V_{GS} (r_o \parallel R_L)}{V_{GS} + (g_m V_{GS} (r_o \parallel R_L))}$$

$$A_v = \frac{g_m (r_o \parallel R_L)}{1 + g_m (r_o \parallel R_L)}$$

$$A_v = \frac{4.47 \text{ mA/V} \left(\frac{1}{\frac{1}{10 \text{ k}} + \frac{1}{4 \text{ k}}} \right)}{1 + 4.47 \text{ mA/V} \left(\frac{1}{\frac{1}{10 \text{ k}} + \frac{1}{4 \text{ k}}} \right)}$$

$$A_v = 0.927$$

$$V = IR \Rightarrow \frac{V}{R} = I = V \left(\frac{1}{R} \right)$$

$$R_o = \left(\frac{1}{g_m} \parallel r_o \right) \Rightarrow \frac{1}{g_m + \frac{1}{r_o}} = \frac{1}{4.47 \text{ mA/V} + \frac{1}{10 \text{ k}}}$$

$$R_o = 218.716 \Omega$$

b) $g_m = 2 \sqrt{1 \text{ mA} (2 \text{ mA})} \Rightarrow g_m = 2.828 \text{ mA/V}$
 $r_o = \frac{1}{(0.02)(2 \text{ mA})} \Rightarrow r_o = 25 \text{ k}\Omega$

$$A_v = \frac{2.828 \text{ mA/V} \left(\frac{1}{\frac{1}{25 \text{ k}} + \frac{1}{4 \text{ k}}} \right)}{1 + 2.828 \text{ mA/V} \left(\frac{1}{\frac{1}{25 \text{ k}} + \frac{1}{4 \text{ k}}} \right)}$$

$$A_v = 0.907$$

$$R_o = \frac{1}{g_m} \parallel r_o \Rightarrow R_o = \frac{1}{(2.828 \text{ mA/V}) \left(\frac{1}{25 \text{ k}} \right)} \Rightarrow R_o = 348.623 \Omega$$

Problem 4.49

Consider the PMOS common-gate circuit in Figure P4.49. The transistor parameters are: $V_{TP} = -1\text{V}$, $K_p = 0.5\text{ mA/V}^2$, and $\lambda = 0$. (a) Determine R_S and R_D such that $I_{DQ} = 0.75\text{ mA}$ and $V_{SDQ} = 6\text{ V}$. (b) Determine the input impedance R_i and the output impedance R_o . (c) Determine the load current i_o and the output voltage v_o , if $i_i = 5\sin\omega t\text{ }\mu\text{A}$.

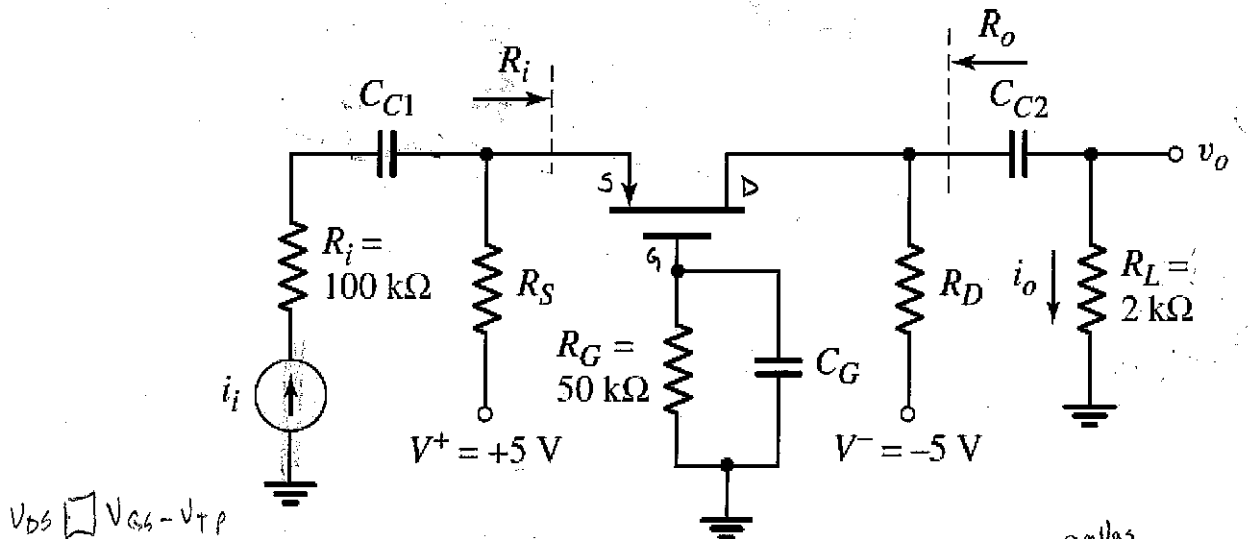


Figure P4.49

$$0.75\text{ mA} = 0.5\text{ mA/V}^2 (|V_{GS}| - |-1|)^2$$

$$V_{GS} = \sqrt{\frac{0.75\text{ mA}}{0.5\text{ mA/V}^2}} + 1 \Rightarrow V_{GS} = -2.225\text{ V}$$

$$V_{GS} = V_G - V_S \quad V_S = -V_{GS} = 2.225\text{ V}$$

$$R_S = \frac{5 - 2.225\text{ V}}{0.75\text{ mA}} \Rightarrow R_S = 3.7\text{ k}\Omega$$

$$V_{DS} = V_D - V_S$$

$$-6 + V_S = V_D = 2.225 - 6 = V_D = -3.775\text{ V}$$

$$R_D = \frac{-3.775 - (-5)}{0.75\text{ mA}} \Rightarrow R_D = 1.633\text{ k}\Omega$$

$$g_m = 2\sqrt{K_p I_{DQ}} = 2\sqrt{0.5\text{ mA/V}^2 (0.75\text{ mA})} \Rightarrow g_m = 1.225\text{ mS}$$

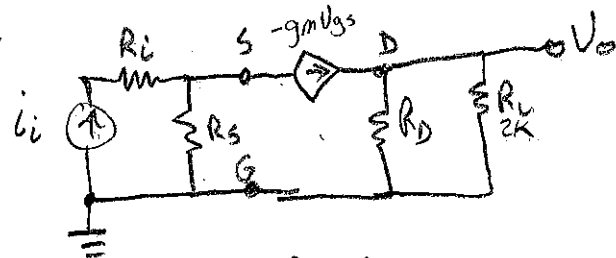
for open Gate circuits

$$R_i = \frac{1}{g_m} \Rightarrow R_i = 816.5\Omega$$

$$R_o = R_D \Rightarrow R_o = 1.633\text{ k}\Omega$$

Neamen, Microelectronics, 4th edition, 2010. © The McGraw-Hill Companies.

Sanjay Krishna: University of New Mexico



$$-g_m V_{gs} \left(\frac{R_D}{R_D + R_L} \right)$$

$$i_i = \frac{V_S - V_G}{R_S} + (-g_m V_{gs})$$

$$i_i = \frac{V_{SG}}{R_S} + g_m V_{SG}$$

$$i_i = V_{SG} \left(\frac{1}{R_S} + g_m \right)$$

$$V_{SG} = \frac{i_i}{\frac{1}{R_S} + g_m} = -V_{GS}$$

$$\text{Current Divider} \quad -g_m \left(\frac{-i_i}{\frac{1}{R_S} + g_m} \right) \left(\frac{R_D}{R_D + R_L} \right) = i_o$$

$$i_o = 1.225\text{ mS} \left(\frac{5\sin(\omega t)\text{ }\mu\text{A}}{\frac{1}{3.7\text{ k}\Omega} + 1.225\text{ mS}} \right) \left(\frac{1.633\text{ k}\Omega}{1.633\text{ k}\Omega + 2\text{ k}\Omega} \right)$$

$$i_o = 1.845\sin(\omega t)\text{ }\mu\text{A}$$

$$v_o = 1.845\sin(\omega t)(2\text{ k}\Omega) \Rightarrow v_o = 3.685\sin(\omega t)\text{ mV}$$

Problem 4.57

A source-follower circuit with a saturated load is shown in Figure P4.57. The transistor parameters are $V_{TND} = 1\text{ V}$, $K_{nD} = 1\text{ mA/V}^2$ for M_D , and $V_{TNL} = 1\text{ V}$, $K_{nL} = 0.1\text{ mA/V}^2$ for M_L . Assume $\lambda = 0$ for both transistors. Let $V_{DD} = 9\text{ V}$. (a) Determine V_{GG} such that the quiescent value of v_{DSL} is 4 V . (b) Show that the small-signal open-circuit ($R_L = \infty$) voltage gain about this Q -point is given by $A_v = 1/[1 + \sqrt{(K_{nL}/K_{nD})}]$. (c) Calculate the small-signal voltage gain for $R_L = 4\text{ k}\Omega$.

a)

$$V_{GS_D} = V_{GG} - V_{DSL}$$

$$V_{GS_L} = V_{DSL}$$

$$K_{nD}(V_{GS_D} - V_{TND})^2 = K_{nL}(V_{GS_L} - V_{TNL})^2$$

$$K_{nD}(V_{GG} - V_{DSL} - V_{TND})^2 = K_{nL}(V_{DSL} - V_{TNL})^2$$

$$1\text{ mA} \left(\frac{V_{GG} - 4 - 1}{V_{GS} - 5} \right)^2 = 0.1\text{ mA} (4 - 1)^2$$

$$\frac{0.1\text{ mA} (9\text{ V})}{1\text{ mA}} = (V_{GS} - 5)^2$$

$$V_{GG} = \sqrt{\frac{0.1\text{ mA} (9\text{ V})}{1\text{ mA}}} + 5$$

$$V_{GG} = 5.949\text{ V}$$

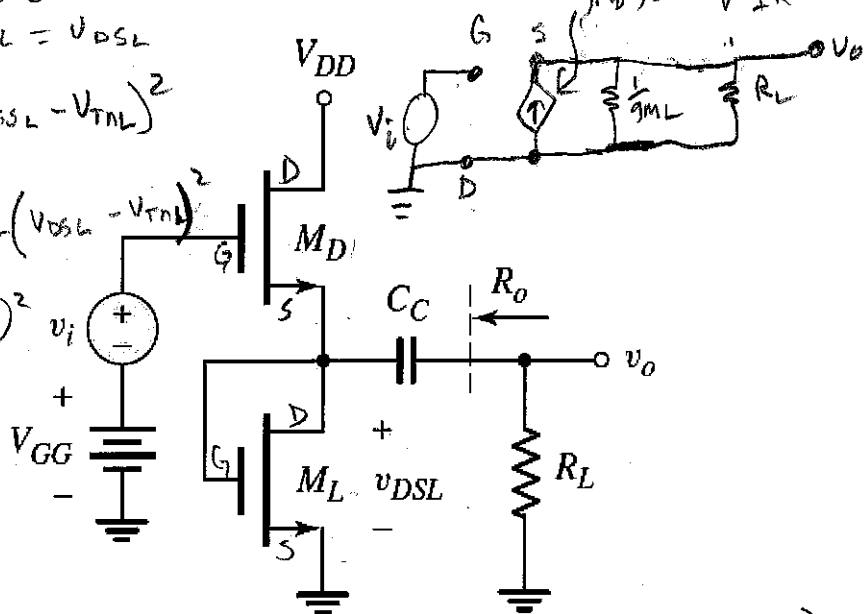


Figure P4.57

b)

$$A_v = \frac{v_o}{v_{in}}$$

$$v_o = g_{mD} v_{gs} \left(\frac{1}{g_{mL}} \right)$$

$$v_{gs} = v_g - v_s \Rightarrow v_s = v_o$$

$$v_i = v_g = v_{gs} + v_o$$

$$v_{in} = v_{gs} + (g_{mD} v_{gs} \left(\frac{1}{g_{mL}} \right))$$

$$v_{in} = v_{gs} \left(1 + \frac{g_{mD}}{g_{mL}} \right)$$

$$A_v = \frac{\left(\frac{g_{mD}}{g_{mL}} \right)}{1 + \left(\frac{g_{mD}}{g_{mL}} \right)}$$

$$g_{mD} = 2\sqrt{K_{nD} I_{DQ}}$$

$$g_{mL} = 2\sqrt{K_{nL} I_{DQ}}$$

$$\frac{g_{mD}}{g_{mL}} = \sqrt{\frac{K_{nD} I_{DQ}}{K_{nL} I_{DQ}}}$$

$$\frac{g_{mD}}{g_{mL}} = \sqrt{\frac{K_{nD}}{K_{nL}}}$$

$$A_v = \frac{\sqrt{\frac{K_{nD}}{K_{nL}}}}{1 + \sqrt{\frac{K_{nD}}{K_{nL}}}}$$

$$A_v = \frac{1}{\sqrt{\frac{K_{nD}}{K_{nL}}} + 1}$$

c)

$$v_o = g_{mD} v_{gs} \left(\frac{1}{g_{mL} \parallel R_L} \right)$$

$$v_{gs} = v_g - v_s$$

$$v_g = v_{gs} + v_s \quad v_s = v_o, \quad v_g = v_{in}$$

$$v_{in} = v_{gs} + v_o$$

$$A_v = \frac{v_o}{v_{in}} = \frac{g_{mD} \left(\frac{1}{g_{mL} \parallel R_L} \right)}{1 + g_{mD} \left(\frac{1}{g_{mL} \parallel R_L} \right)}$$

$$I_D = K_{nL}(V_{GS_L} - V_{TNL})^2 = K_{nL}(V_{DSL} - V_{TNL})^2$$

$$I_D = 0.1\text{ mA} (4 - 1)^2 \Rightarrow I_D = 0.9\text{ mA}$$

$$g_{mL} = 2\sqrt{0.1\text{ mA} (0.9\text{ mA})} \Rightarrow g_{mL} = 600\mu\text{A/V}$$

$$g_{mD} = 2\sqrt{1\text{ mA} (0.9\text{ mA})} \Rightarrow g_{mD} = 1.897\text{ mA/V}$$

$$A_v = \frac{1.897\text{ m} \left(\frac{1}{600\mu \parallel 4\text{ k}} \right)}{1 + 1.897\text{ m} \left(\frac{1}{600\mu \parallel 4\text{ k}} \right)} = \frac{2.232}{3.232}$$

$$A_v = 690.61\text{ m}$$