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**Midterm Exam II, Fall 2008**  
Signals and Systems  
University of New Mexico  
Instructor: Balu Santhanam  
Date Assigned: 11/25/2008  
Duration: 2:00 - 3:15 PM

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**Instructions**

1. Write clearly and legibly
  2. Provide steps to obtain partial credit
  3. You are allowed to bring 2 sheets of Fourier transform formulas.
  4. It is assumed that you are aware of the UNM academic honesty policy.  
Needless to say copying will be dealt with seriously.
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## Problem # 1.0

A discrete-time LTI system is characterized by the following input-output difference equation:

$$y[n] = ay[n-1] + x[n-1] - ax[n], \quad a \in \mathbf{R}, \quad 0 < a < 1.$$

For the system described here:

1. Calculate the frequency response  $H(e^{j\Omega})$  of this system by taking the DTFT of both sides of the difference equation.
2. Plot the magnitude and phase response of this system versus the digital frequency variable  $\Omega \in [-\pi, \pi]$
3. Calculate the impulse response  $h[n]$  of this system by computing the inverse DTFT of  $H(e^{j\Omega})$ .
4. Is this system BIBO stable? is it causal? justify your answer properly.

## Problem # 2.0

Compute the spectrum of the following signals using Fourier transform tables:

1.  $x(t) = \frac{1}{1+t^2}, \quad t \in \mathbf{R}$

2.  $x(t) = \frac{1}{\pi t}, \quad t \in \mathbf{R}$

3.  $x(t) = \exp(-|\tau|) \cos \omega_o t$

In each case, specify the properties that you are using to calculate spectrum.

### Problem # 3.0

A unit amplitude, 50% duty-cycle, rectangular pulse train  $x(t)$  is the input to lowpass R-C filter with output  $y(t)$ . For this system:

1. What are Fourier series coefficients of the output signal  $y(t)$ .
2. Compute the spectrum  $Y(j\omega)$  of the output signal  $y(t)$ .
3. How would the results change, if the input was a unit amplitude triangular pulse train with the same duty-cycle?