

$$T(^{\circ}C) = \frac{5}{9}(T(^{\circ}F) - 32)$$

$$T(K) = T(^{\circ}C) + 273.15$$

$$\Delta L = \alpha L_0 \Delta T$$

$$\Delta V = \beta V_0 \Delta T$$

$$Q = mc\Delta T = nC\Delta T$$

$$Q_{F/V} = \pm mL_{F/V}$$

$$H = \frac{dQ}{dt} = k \frac{A}{L} (T_H - T_C)$$

$$pV = nRT$$

$$K_{tr} = \frac{3}{2} nRT$$

$$C_V = \frac{3}{2} R \quad \text{ideal monatomic gas}$$

$$C_V = \frac{5}{2} R \quad \text{ideal diatomic gas w/o vibration}$$

$$W = \int_{V_1}^{V_2} p dV$$

$$\Delta U = Q - W$$

$$e = \frac{W}{Q_H} = 1 - \left| \frac{Q_C}{Q_H} \right|$$

$$e_{Carnot} = 1 - \left| \frac{T_C}{T_H} \right|$$

$$\Delta S = \int_1^2 \frac{dQ}{T}$$

$$S = k \ln w$$

$$R = 8.314 J/mol \cdot K$$

$$N_A = 6.02 \times 10^{23} \text{ molecules/mole}$$

$$1 \text{ atm} = 101\,325 \text{ N/m}^2$$

$$1/4\pi\epsilon_0 = 8.99 \times 10^9 \text{ Nm}^2/\text{C}^2$$

$$e = -1.602 \times 10^{-19} \text{ C}$$

$$\vec{F}_E = q\vec{E} = \frac{1}{4\pi\epsilon_0} \frac{qQ}{r^2} \hat{r}$$

$$\Phi_E = \oint \vec{E} \cdot d\vec{A} = \frac{q_{enc}}{\epsilon_0}$$

$$V_b - V_a = - \int_a^b \vec{E} \cdot d\vec{l}$$

$$\Delta U = q\Delta V$$

$$\vec{E} = - \left( \hat{i} \frac{\partial V}{\partial x} + \hat{j} \frac{\partial V}{\partial y} + \hat{k} \frac{\partial V}{\partial z} \right)$$

$$Q = CV$$

$$\frac{1}{C_{eq}} = \frac{1}{C_1} + \frac{1}{C_2} + \frac{1}{C_3} + \dots \quad \text{series}$$

$$C_{eq} = C_1 + C_2 + C_3 + \dots \quad \text{parallel}$$

$$U = \frac{1}{2} CV^2$$

$$u_E = \frac{1}{2} \epsilon_0 E^2$$

$$E = \frac{E_0}{K}$$

$$I = \frac{dq}{dt}$$

$$\vec{J} = nq\vec{v}_d$$

$$\rho = \frac{E}{J}$$

$$V = IR$$

$$P = VI$$

$$R_{eq} = R_1 + R_2 + R_3 + \dots \quad \text{series}$$

$$\frac{1}{R_{eq}} = \frac{1}{R_1} + \frac{1}{R_2} + \frac{1}{R_3} + \dots \quad \text{parallel}$$

$$q = C\mathcal{E} \left( 1 - e^{-t/RC} \right) \quad \text{charging}$$

$$q = Q_0 e^{-t/RC} \quad \text{discharging}$$

$$\vec{F} = q\vec{v} \times \vec{B}$$

$$\Phi_B = \int \vec{B} \cdot d\vec{A}$$

$$d\vec{F} = Id\vec{l} \times \vec{B}$$

$$\vec{\tau} = \vec{\mu} \times \vec{B}, \quad \vec{\mu} = NI\vec{A}$$

$$U = -\vec{\mu} \cdot \vec{B}$$

$$\vec{B} = \frac{\mu_0}{4\pi} \frac{q\vec{v} \times \hat{r}}{r^2}$$

$$d\vec{B} = \frac{\mu_0}{4\pi} \frac{Id\vec{l} \times \hat{r}}{r^2}$$

$$\oint \vec{B} \cdot d\vec{l} = \mu_0 (i_C + i_D)$$

$$\oint \vec{E} \cdot d\vec{l} = \mathcal{E} = - \frac{d\Phi_B}{dt}$$

$$i_D = \varepsilon \frac{d\Phi_E}{dt}$$

$$\mathcal{E}_2 = -M \frac{di_1}{dt} \text{ and } \mathcal{E}_1 = -M \frac{di_2}{dt}$$

$$M = \frac{N_2 \Phi_{B2}}{i_1} = \frac{N_1 \Phi_{B1}}{i_2}$$

$$\mathcal{E} = -L \frac{di}{dt},$$

$$L = \frac{N\Phi_B}{i}$$

$$U = \frac{1}{2} LI^2, \quad u_E = \frac{1}{2\mu_0} B^2,$$

$$\frac{di}{dt} = \frac{\mathcal{E}}{L} e^{-Rt/L}$$

$$\omega = \frac{1}{\sqrt{LC}}$$

$$I_{RMS} = \frac{1}{\sqrt{2}} I \quad \text{for } i = I \cos(\omega t)$$

$$V_{RMS} = \frac{1}{\sqrt{2}} V \quad \text{for } v = V \cos(\omega t)$$

$$V_R = IR$$

$$V_L = IX_L, \quad \text{where } X_L = \omega L$$

$$V_C = IX_C, \quad \text{where } X_C = \frac{1}{\omega C}$$

$$V = IZ, \quad \text{where } Z = \sqrt{R^2 + (X_L - X_C)^2}$$

$$P_{\text{Avg}} = \frac{1}{2} VI \cos \varphi, \quad \tan \varphi = \frac{X_L - X_C}{R}$$

$$V_s = V_p \frac{N_s}{N_p}$$

## Calculus

### Derivatives:

$$\frac{d}{dx} x^n = nx^{n-1}$$

$$\frac{d}{dx} \sin ax = a \cos ax$$

$$\frac{d}{dx} \ln ax = \frac{1}{x}$$

$$\frac{d}{dx} \cos ax = -a \sin ax$$

$$\frac{d}{dx} e^{ax} = ae^{ax}$$

### Integrals:

$$\int x^n dx = \frac{x^{n+1}}{n+1} \quad (n \neq -1)$$

$$\int \sin ax dx = -\frac{1}{a} \cos ax$$

$$\int \frac{dx}{\sqrt{x^2 + a^2}} = \ln(x + \sqrt{x^2 + a^2})$$

$$\int \frac{x dx}{(x^2 + a^2)^{3/2}} = -\frac{1}{\sqrt{x^2 + a^2}}$$

$$\int \frac{dx}{x} = \ln x$$

$$\int \cos ax dx = \frac{1}{a} \sin ax$$

$$\int \frac{dx}{x^2 + a^2} = \frac{1}{a} \arctan \frac{x}{a}$$

$$\int e^{ax} dx = \frac{1}{a} e^{ax}$$

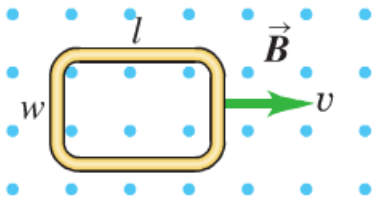
$$\int \frac{dx}{\sqrt{a^2 - x^2}} = \arcsin \frac{x}{a}$$

$$\int \frac{dx}{(x^2 + a^2)^{3/2}} = \frac{1}{a^2} \frac{x}{\sqrt{x^2 + a^2}}$$

## Physics 161-001 Spring 2012 Exam 4

Name: \_\_\_\_\_ Box# \_\_\_\_\_

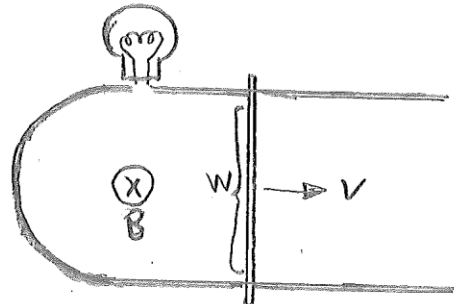
1) A flat rectangular coil of dimensions  $l = 4.0\text{m}$  and  $w = 2.0\text{m}$  is pulled with uniform speed  $v = 2.0\text{m/s}$  through a uniform magnetic field  $B = 2.0\text{T}$  with the plane of its area perpendicular to the magnetic field as shown. The coil has a resistance of  $10.0\ \Omega$ . What is the current induced in this coil?



- A) 1.6 A
- B) 3.2 A
- C) 8.0 A
- D) 0.0 A**
- E) 4.0 A

2) A copper bar pulled with speed  $v$  along parallel copper tracks separated by a distance  $w$  in a uniform  $B$  field, into the page. What is the direction of the emf induced?

- A) clockwise
- B) counterclockwise**
- C) it depends on the sign of the charge carriers
- D) there is no emf, because copper is not a magnetic metal like iron.



3) A rectangular coil is rotated at angular speed  $\omega$  in a uniform horizontal  $B$  field, as shown. What is the position of the coil when the emf around the loop is clockwise (from above) and largest? (That is, when would maximum current flow from b to a through the light bulb?)

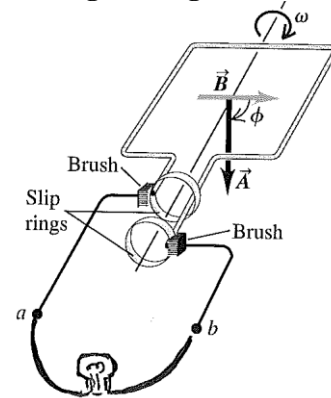
A) in the orientation shown

B)  $90^\circ$  clockwise (loop vertical)

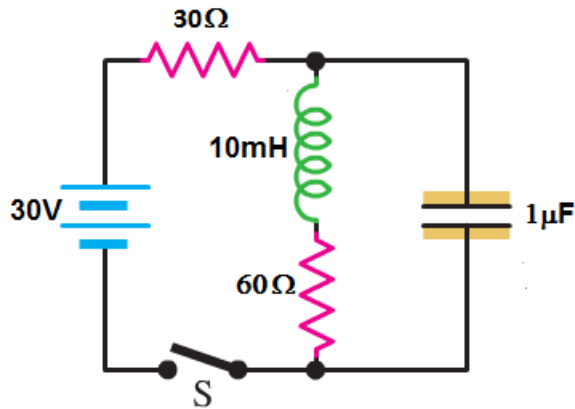
C)  $180^\circ$  flipped from what is shown

D)  $270^\circ$  clockwise from drawing

E) at an intermediate position



4) In the DC circuit shown, immediately after the switch is closed, what is the current through the capacitor?



A) 0

B)  $1/3$  A

C) 1 A

D) 106 A

E)  $30 \times 106$  A

F) cannot determine

5) In the same circuit, what is the rate of change of the current through the inductor immediately after the switch is closed?

A) 0 A/s

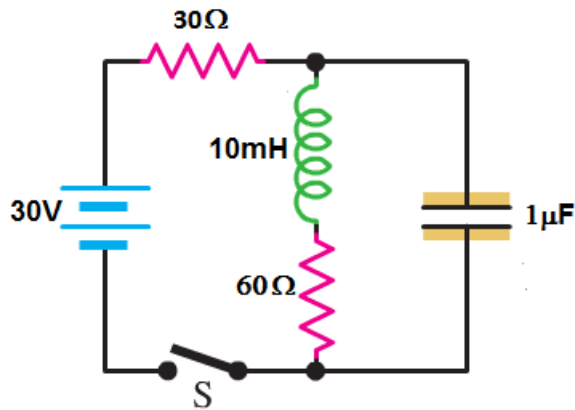
B)  $3 \times 10^3$  A/s

C) cannot determine

D)  $3 \times 10^4$  A/s

E) 1 A/s

6) A long time later (after the circuit has reached a steady state), the switch is opened. What happens in this circuit?



- A) all currents stop immediately
- B) the current through the inductor decays gradually and monotonically
- C) the current through the inductor oscillates without decay
- D) the current through the inductor oscillates and gradually decays**

7) In the previous problem, assuming that the damping factor is small enough to ignore, what is the approximate angular frequency of the subsequent oscillation, if any?

- A) there is no oscillation
- B)  $10^{-8}$  rad/s
- C) 6 krad/s
- D)  $60 \times 10^6$  rad/s
- E)  $10^4$  rad/s**

8) You are given a solenoid of length 1m and cross-sectional area of  $0.01\text{m}^2$ . If you double the current through the solenoid, what happens to the self inductance of the solenoid?

- A) Nothing.**
- B) It goes up by a factor of 2.
- C) It goes up by a factor of 4.
- D) It goes down by a factor of 2.
- E) It goes down by a factor of 4.

9) In an LC circuit, with  $L = 10\text{H}$  and  $C = 1\text{mF}$ , the capacitor has an initial total energy stored in its electric field of  $1\text{mJ}$ , and the inductor initially has no current through it.  $157\text{ms}$  later, what is the total energy stored in the inductor?

- A)  $0\text{J}$
- B)  $1\text{mJ}$
- C)  $-1\text{mJ}$
- D)  $0.5\text{mJ}$
- E)  $-0.25\text{mJ}$

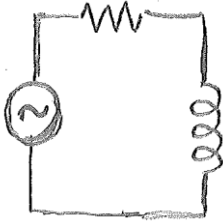
10) A capacitor is charging in a simple RC circuit with a dc battery. Which one of the following statements about this capacitor is accurate?

- A) There is a magnetic field between the capacitor plates because charge travels between the plates by jumping from one plate to the other.
- B) There is a magnetic field between the capacitor plates, even though no charge travels between them, because the magnetic flux between the plates is changing.
- C) There is no magnetic field between the capacitor plates because no charge travels between the plates.
- D) The magnetic field between the capacitor plates is increasing with time because the charge on the plates is increasing.
- E) There is a magnetic field between the capacitor plates, even though no charge travels between them, because the electric flux between the plates is changing.

11) For a long ideal solenoid having a circular cross-section, the magnetic field strength within the solenoid is given by the equation  $B(t) = 2.0t\text{ T}$ , where  $t$  is time in seconds. If the induced electric field outside the solenoid is  $3.0\text{ V/m}$  at a distance of  $3.0\text{ m}$  from the axis of the solenoid, find the radius of the solenoid.

- A)  $2.2\text{m}$
- B)  $3.0\text{m}$
- C)  $3.6\text{m}$
- D)  $4.0\text{m}$
- E)  $1.0\text{m}$

12) In the AC circuit shown, the amplitude of the voltage across the inductor is 8 V; the amplitude of the voltage across the resistor is 6 V. What is the amplitude of the voltage provided by the source?



- A) Cannot determine without R and L.
- B) 2 V
- C) 6 V
- D) 8 V
- E) 10 V

13) A magnet is perpendicular to a loop of copper wire with its N pole in the center. The magnet is pulled down, away from the loop. What is the direction of the induced EMF in the loop, as seen from above?

- A) There is no induced EMF, since the wire is not moving and  $F=qv \times B$ .
- B) clockwise
- C) counterclockwise

