

# University of New Mexico

Department of Electrical and Computer Engineering

ECE 321L-Electronics I (Fall 2012)

Homework Solutions #5

$$2.11 - N_D(\text{eff}) = 10^{18} - 10^{16} = 9.9 \times 10^{17} \text{ cm}^{-3} \Rightarrow n_o p_o = n_i^2$$

$$\Rightarrow 9.9 \times 10^{17} \times p_o = (1.062 \times 10^{10})^2 \Rightarrow \underline{p_o = 114 \text{ cm}^{-3}}$$

$$2.15 - a) \mathcal{E} = V/d = \frac{1 \text{ V}}{20 \times 10^{-4} \text{ cm}} = \underline{500 \text{ V/cm}}$$

$$b) n_o p_o = n_i^2; \quad n_i = B T^{3/2} \exp\left(\frac{-E_g}{2kT/q}\right)$$

$$n_i = 5.23 \times 10^{15} (280)^{3/2} \exp\left(\frac{-1.12}{2 \times 86.17 \text{ mV/K} \times 280}\right) = 2.04 \times 10^9 \text{ cm}^{-3}$$

$$n_o \times 10^{18} = (2.04 \times 10^9)^2 \Rightarrow \underline{n_o = 2.04 \times 10^9 \text{ cm}^{-3}}$$

$$c) J = \mu_n q \mathcal{E} n_o + \mu_p q \mathcal{E} p_o$$

$$= 1500 \times 1.6 \times 10^{-19} \times 500 \times 2.04 \times 10^9 + 500 \times 1.6 \times 10^{-19} \times 500 \times 10^{18}$$

$$\Rightarrow \underline{J = 40050 \text{ A/cm}^2}$$

$$d) J = 40050 \frac{\text{A}}{\text{cm}^2} \times (10^{-4} \text{ cm}/\mu)^2 \Rightarrow \underline{J = 400.5 \text{ mA}/\mu\text{m}^2}$$

$$2.16 - J \approx \mu_n q \mathcal{E} n_o = 1200 \times 1.602 \times 10^{-19} \times \mathcal{E} \times 10^{18} = 10 \text{ kA/cm}^2$$

$$\Rightarrow \underline{\mathcal{E} = 52 \text{ V/cm}}$$

$$b) \mathcal{E} = \frac{V}{d} \Rightarrow 52 \frac{\text{V}}{\text{cm}} = \frac{2 \text{ V}}{d} \Rightarrow \underline{d = 384 \text{ }\mu\text{m}}$$

$$2.17 - J = \sigma \mathcal{E} \Rightarrow 10 \text{ kA/cm}^2 = \sigma \times 52 \text{ V/cm} \Rightarrow \sigma = 192 \frac{1}{\Omega\text{cm}}$$

$$\rho = \frac{1}{\sigma} = 5.2 \times 10^{-3} \text{ }\Omega\text{cm}$$

$$2.22 - J = D_n q \frac{dn}{dx} + D_p q \frac{dp}{dx} ; \frac{D_n}{\mu_n} = \frac{D_p}{\mu_p} = \frac{KT}{q} = 25.9 \text{ mV}$$

$$\Rightarrow D_n = 1300 \times 25.9 \text{ mV} = 33.67 \text{ cm}^2/\text{s}$$

$$\Rightarrow D_p = 400 \times 25.9 \text{ mV} = 10.36 \text{ cm}^2/\text{s}$$

$$\Rightarrow J = 33.67 \times 1.602 \times 10^{-19} \times 10^{20} + 10.36 \times 1.62 \times 10^{-19} \times 10^{17} \Rightarrow \underline{J = 539.56 \text{ A/cm}^2}$$

$$2.25 - n_i = 5.23 \times 10^{15} * (345)^{3/2} \exp\left(\frac{-1.12}{2 \times 86.17 \text{ mV/K} \times 345}\right) = 2.21 \times 10^{11} \text{ cm}^{-3}$$

$$V_{bi} = \frac{KT}{q} \ln\left(\frac{N_A N_D}{n_i^2}\right) = 86.17 \text{ mV/K} * 345 \ln\left(\frac{10^{18} \times 10^{15}}{(2.21 \times 10^{11})^2}\right) \Rightarrow \underline{V_{bi} = 0.706 \text{ V}}$$

$$2.30 - I_D = I_S (e^{\frac{V_D}{V_{th}}} - 1) \approx I_S e^{\frac{V_D}{V_{th}}} \Rightarrow \frac{I_{D1}}{I_{D2}} = e^{\frac{V_{D1} - V_{D2}}{V_{th}}} = e^{\frac{\Delta V}{V_{th}}}$$

$$\Rightarrow \Delta V = V_{th} \cdot \ln\left(\frac{I_{D1}}{I_{D2}}\right) \Rightarrow \Delta V = 25.9 \text{ mV} \ln(100) \Rightarrow \underline{\Delta V = 0.119 \text{ V}}$$

$$2.31 - C_j = \frac{C_{j0}}{\sqrt{1 + \frac{V_R}{V_{bi}}}} \Rightarrow C_j = \frac{2 \text{ PF}}{\sqrt{1 + \frac{V_R}{0.65}}}$$

$$V_R = 1 \text{ V} \Rightarrow C_j = 1.255 \text{ PF}$$

$$V_R = 2 \text{ V} \Rightarrow C_j = 0.99 \text{ PF}$$

$$\underline{V_R = 3 \text{ V} \Rightarrow C_j = 0.844 \text{ PF}}$$