

(2-1)

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ECE321
HW-3
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$$n_i = 1.67 \times 10^{10} \frac{\text{carriers}}{\text{cm}^3}$$

$$1.67 \times 10^{10} \frac{\text{carriers}}{\text{cm}^3} = B T^{3/2} e^{\frac{-E_g}{2(kT_q)}}$$

$$1.67 \times 10^{10} = (5.23 \times 10^{15}) (T^{3/2}) e^{\frac{-1.12 \text{ eV}}{2(86.174 \text{ eV})T}}$$

$$T = 340.31 \text{ K}$$

(2-2) What fraction of Si atoms is ionized at $T = 100^\circ\text{C}$

$$n_i(373 \text{ K}) = 5.23 \times 10^{15} (373^{3/2}) e^{\frac{-1.12 \text{ eV}}{2(86.174 \text{ eV})373}} = 1.02 \times 10^{12} \frac{\text{electrons}}{\text{cm}^3} = 373 \text{ K}$$

$$\frac{n_i(100^\circ\text{C})}{5 \times 10^{22} \frac{\text{atoms}}{\text{cm}^3}} = 2.04 \times 10^{-11} \frac{\text{electrons}}{\text{Si atom}}$$

(2-3) $\frac{n_i(T_1)}{n_i(T_2)} = 303$, $T_2 = 300 \text{ K}$

$$n_i(T_2) = 1.062 \times 10^{11} \frac{\text{electrons}}{\text{cm}^3}$$

$$n_i(T_1) = (303) (1.062 \times 10^{11} \frac{\text{electrons}}{\text{cm}^3})$$

$$n_i(T_1) = 3.218 \times 10^{13} \frac{\text{electrons}}{\text{cm}^3}$$

$$3.218 \times 10^{13} \frac{\text{electrons}}{\text{cm}^3} = (5.23 \times 10^{15}) (T_1^{3/2}) e^{\frac{-1.12 \text{ eV}}{2(86.174 \text{ eV})T_1}}$$

$$T_1 = 397 \text{ K}$$

(2-4) $n_i(250 \text{ K}) = 1.061 \times 10^8 \frac{\text{electrons}}{\text{cm}^3}$

$$n_i(300 \text{ K}) = 1.062 \times 10^{10} \text{ "}$$

$$n_i(350 \text{ K}) = 2.956 \times 10^{11} \text{ "}$$

$$n_i(400 \text{ K}) = 3.678 \times 10^{12} \text{ "}$$

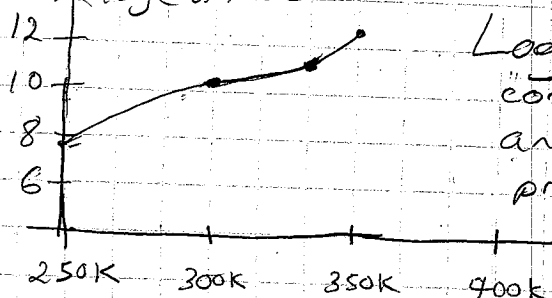
$$\log_{10}[n_i(250 \text{ K})] = 8.02 \text{ dB}$$

$$\log_{10}[n_i(300 \text{ K})] = 10.03 \text{ dB}$$

$$\log_{10}[n_i(350 \text{ K})] = 11.47 \text{ dB}$$

$$\log_{10}[n_i(400 \text{ K})] = 12.57 \text{ dB}$$

$\log(n_i) \text{ in dB}$



Log plot is preferred because it compresses changes at higher magnitudes and expands changes at lower magnitudes, providing better overall representation of response.

This plot is fairly linear over the range.

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(2-5) $T = 100^\circ\text{C} = 373\text{K}$

$$n_i(373\text{K}) = 1.02 \times 10^{12} \frac{\text{electrons}}{\text{cm}^3}$$

$$\frac{n_i(373\text{K})}{5} = 2.044 \times 10^{11} \frac{\text{electrons}}{\text{cm}^3}$$

$$2.044 \times 10^{11} \frac{\text{electrons}}{\text{cm}^3} = (5.23 \times 10^{15}) (T^{3/2}) \left(e^{\frac{-1.12\text{eV}}{2(86.17\text{eV})T}} \right)$$

$$T_{(n_i\text{-reduced})} = \boxed{343.7\text{K}} = \boxed{70.7^\circ\text{C}}$$

(2-6)

$$N_A = 10^{17} \text{cm}^{-3} \text{ at } 300\text{K}$$

$$n_o = \frac{n_i^2}{N_A} = \frac{(1.062 \times 10^{10} \text{cm}^{-3})^2}{10^{17} \text{cm}^{-3}} = \boxed{1.128 \times 10^3 \frac{\text{electrons}}{\text{cm}^3}}$$

(2-7)

$$\frac{Si(\text{atoms})}{N_x(\text{atoms})} = \frac{10,000}{1} \Rightarrow \frac{5 \times 10^{22} (\frac{\text{atoms}}{\text{cm}^3})}{N_D} = 10,000$$

$$N_D = \frac{5 \times 10^{22} \frac{\text{atoms}}{\text{cm}^3}}{10,000} = 5 \times 10^{18} \frac{\text{electrons}}{\text{cm}^3}$$

$$p_o = \frac{n_i^2}{N_D} = \frac{(1.062 \times 10^{10} \frac{\text{carriers}}{\text{cm}^3})^2}{5 \times 10^{18} \frac{\text{electrons}}{\text{cm}^3}} = \boxed{22.56 \frac{\text{holes}}{\text{cm}^3}}$$

(2-8) $T = 358\text{K}, N_A = 6 \times 10^{18}$

$$n_o = \frac{[n_i(358\text{K})]^2}{N_A} = \boxed{3.573 \times 10^4 \frac{\text{electrons}}{\text{cm}^3}}$$

(2-9)

electron concentration in Si at 300K = $5 \times 10^4 \text{cm}^{-3}$

n_i at 300K = $1.5 \times 10^{10} \text{cm}^{-3}$

$$\text{hole concentration} = \frac{(1.5 \times 10^{10} \text{cm}^{-3})^2}{5 \times 10^4 \text{cm}^{-3}} = \boxed{4.5 \times 10^{15} \frac{\text{holes}}{\text{cm}^3}}$$

(p-type)

(2-10) $n_o = 4.5 \times 10^4, N_A = 10^{18}$

$$n_i = \sqrt{n_o N_A} = 2.12 \times 10^{11} = (5.23 \times 10^{15}) (T^{3/2}) \left(e^{\frac{-1.12\text{eV}}{2(86.17\text{eV})T}} \right) \Rightarrow T = \boxed{344\text{K}}$$