HEI Scheduling constraints problems

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Notations

- G denotes the set of all group g; T denotes the set of all teacher, C denotes the set of all course.
- All element of the set of all awarded courses AC will be indexed. In other words :

$$ac_i \in AC, i \in \mathbb{N}$$

- Let t_{ac_i} and c_{ac_i} be the corresponding teacher and the corresponding course resp. to ac_i .
- Let $SCT_{t,c} \subset AC$ be the set of all awarded course which has same teacher and course (Same Course and Teacher):

$$\forall i, j \in \mathbb{N} : (ac_i, ac_j \in SCT_{t,c}) \iff (t_{ac_i} = t_{ac_j} = t) \text{ and } (c_{ac_i} = c_{ac_j} = c)$$

• Let $STDC_t \subset AC$ be the set of all awarded course which has same teacher but different course (Same Teacher but Different Course):

$$\forall i, j \in \mathbb{N} : (ac_i, ac_j \in STDC_t) \iff (t_{ac_i} = t_{ac_j} = t) \text{ and } (c_{ac_i} \neq c_{ac_j})$$

• Let $p_{d,SCT_{t,c}} \in \{-1, 1\}$, be a an indicator constant.

$$p_{d,SCT_{t,c}} = \begin{cases} 1, & \text{if all } ac_i \text{ related to } SCT_{t,c} \text{ are presentials at a given day } d \\ -1, & \text{otherwise} \end{cases}$$

• Let $AC_g \subset AC$, the set of all awarded course related to a group g.

About the Constraints

Constraint 1 A teacher can't teach two or more different groups at the same time for a same course if it is face-to-face session but can if it is a video conference session.

 $\forall s \in S, \ \forall \ d \in D, \ \forall \ t \in T, \ \forall \ c \in C:$

$$2p_{d,SCT_{t,c}} \cdot \left(\sum_{r \in R} \left(\sum_{ac_i \in SCT_{t,c}} o_{ac_i,d,r,s}\right)\right) \le 3p_{SCT_{t,c}} - 1 \tag{1}$$

<u>Otherwise</u>: if $p_{d,SCT_{t,c}}$ is the binary variable such as:

$$p_{d,SCT_{t,c}} = \begin{cases} 1, & \text{if all awarded course related to } SCT_{t,c} \text{ are presential} \\ 0, & \text{otherwise} \end{cases}$$

which marks whether all awarded courses related to $SCT_{t,c}$ are presentials or not.

Let $M \in \mathbb{N}^*$ be a majoration constant.

Therefore:

$$\sum_{r \in R} \left(\sum_{ac_i \in SCT_{t,c}} o_{ac_i,d,r,s} \right) \le 1 + M(1 - p_{SCT_{t,c}}) \tag{2}$$

Constraint 2 A teacher cannot simultaneously teach two or more different courses.

 $\forall s \in S, \ \forall \ d \in D, \forall \ t \in T:$

$$\sum_{r \in R} \left(\sum_{ac_i \in STDC_t} o_{ac_i, d, r, s} \right) \le 1 \tag{3}$$

Constraint 3 A group cannot simultaneously have two or more different course sessions.

 $\forall g \in G, \ \forall s \in S, \ \forall d \in D$:

$$\sum_{r \in R} \left(\sum_{ac_i \in AC_g} o_{ac_i, d, r, s} \right) \le 1 \tag{4}$$

Constraint 4 A group should have 2 hours of break per day.

 $\forall g \in G, \ \forall \ d \in D$:

$$\sum_{ac_i \in AC_g} \left(\sum_{r \in R} \sum_{s \in S} o_{ac_i, d, r, s} \right) \le 3 \tag{5}$$

Constraint 5 Only one session per course in a day.

 $\forall ac_i \in AC, i \in I, \forall d \in D:$

$$\left(\sum_{r \in R} \sum_{s \in S} o_{ac_i, d, r, s}\right) \le 1 \tag{6}$$

Constraint 6 Give one day without the same course after a session of this course.

 $\forall d \in D, \ \forall ac_i \in AC, \ i \in I :$

$$\left(\sum_{r \in R} \sum_{s \in S} o_{ac_i, d+1_d, r, s}\right) + \left(\sum_{r \in R} \sum_{s \in S} o_{ac_i, d, r, s}\right) \le 1 \tag{7}$$

where 1_d is the unit of day.

Constraint 7 Suitable room for every course session.

- Let g_{ac_i} be the corresponding group to a ac_i .
- Let $s_{g_{ac_i}}$ be the group size of a group g_{ac_i} .
- Let rc_r be the room capacity of a room r.

 $\forall ac_i \in AC, i \in I, \forall r \in R, \forall s \in S, \forall d \in D$

$$o_{ac_i,d,r,s}rc_r \ge s_{g_{ac_i}} \tag{8}$$

Constraint 8 Finish the total hour of every course.

Let $D(ac_i, d_q)$ be the total duration of a ac_i within a time interval $[d_0, d_q] \subset D$, $d_0 \leq d_q$.

 $\forall ac_i \in AC, i \in I$:

$$\sum_{d=d_0}^{d_q} \sum_{r \in R} \sum_{s \in S} o_{ac_i, d, r, s} = D(ac_i, d_q)$$
(9)