

Electric Flux Φ (C)

- Total Q enclosed

$$Q = \Phi$$

Electric Flux Density D (C/m²)

$$D = \frac{\Phi}{A} \text{ C/m}^2$$

 $D = \epsilon_0 \vec{E}$ (in free space)

- Flow of electric field through surface

$$\text{cyl: } Q = \frac{Q}{2\pi a^2} \hat{r} \text{ C/m}^2$$

$$\text{scrub: } D = \frac{Q}{4\pi r^2} \hat{r} \text{ C/m}^2$$

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Assignment 3: Problem 2

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(1 point)

Let C denote the parametric curve detailed below:

$$\mathbf{r}(t) = \left(\sqrt{\frac{\pi}{t}} \cos(t), \sqrt{\frac{\pi}{t}} \sin(t), \frac{1}{\sqrt{x^2 + y^2}} \right), \pi \leq t \leq 64\pi.$$

Given $\mathbf{E} = \langle 4z^2e^z, 2e^z, 2ye^z - 8ze^z \rangle$, evaluate the following line integral.

$$\int_C -\mathbf{E} \cdot d\mathbf{L} =$$

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Assignment 3: Problem 3

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(1 point)

Consider the vector-valued function below, in which A , B , and C are constants:

$$\mathbf{E}(x, y, z) = \langle y^2z, Ax^2z + Bz^7 \cos(yz^7), xy^2 + 14z^C y \cos(yz^7) \rangle.$$

Given that \mathbf{E} is a true electric field, find the constants in its definition.ANSWER: $A =$, $B =$, $C =$

Note: You can earn partial credit on this problem.

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Assignment 3: Problem 4

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(1 point)

Let C denote the curve of intersection between $x = -3z^2$ and $y = -3z^2$, starting from $A(0, 0, 0)$ and ending at $B(24, 12, 2)$. Given $\mathbf{G} = \langle 5 \sin(x), 1 \cos(y), 9xz \rangle$, evaluate the following line integral.

$$\int_C -\mathbf{G} \cdot d\mathbf{L} =$$

$$\int_C \mathbf{F} \cdot d\mathbf{r} = \int_a^b \mathbf{F}(\mathbf{r}(t)) \cdot \mathbf{r}'(t) dt$$

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You have attempted this problem 0 times.

You have unlimited attempts remaining.

Assignment 3: Problem 5

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(1 point)

Suppose $\mathbf{F}(x, y) = x^2\mathbf{i} + y^2\mathbf{j}$ and C is the line segment from point $P = (1, 4)$ to $Q = (-3, -1)$.(a) Find a vector parametric equation $\mathbf{r}(t)$ for the line segment C so that points P and Q correspond to $t = 0$ and $t = 1$, respectively.

$$\mathbf{r}(t) =$$

(b) Using the parametrization in part (a), the line integral of \mathbf{F} along C is

$$\int_C \mathbf{F} \cdot d\mathbf{r} = \int_a^b \mathbf{F}(\mathbf{r}(t)) \cdot \mathbf{r}'(t) dt = \int_a^b$$

with limits of integration $a =$ and $b =$

(c) Evaluate the line integral in part (b).

$$\nabla f = \mathbf{F}$$

$$\frac{\partial V}{\partial x} = -4xz^2 \rightarrow \int -4xz^2 dx = -4z^2x + C(y, z)$$

$$\frac{\partial V}{\partial y} = 2e^y \rightarrow \int 2e^y dy = 2e^y + C(x, z)$$

$$\frac{\partial V}{\partial z} = 2ye^z - 8ze^z \rightarrow \int 2ye^z - 8ze^z dz = 2ye^z - 4z^2e^z + C(x, y)$$

$$\nabla V = -4xz^2\mathbf{i} - 2e^y\mathbf{j} + C$$

$$V_x = -4xz^2\mathbf{i} + 2e^y\mathbf{j} + C = -\vec{E}_x$$

$$V_y = 2e^y = -\vec{E}_y$$

$$V_z = -8ze^z + 2e^y = -\vec{E}_z$$

$$\text{Endpoints: } \pi \leq t \leq 64\pi$$

$$t = \pi: x = -1, y = 0, z = -1$$

$$t = 64\pi: x = 1/8, y = 0, z = -8$$

$$\rightarrow \text{plug } x, y, z: \int_{t=\pi}^{64\pi} [-4(-1)^2(-1) + 0] - [-4(-8)^2(-8) + 0] = 288.61448622$$

$$\nabla f = \mathbf{F}$$

$$u = y^2z \rightarrow \int y^2z dz = \frac{1}{3}y^2z^3 + C(y, z)$$

$$u = Ax^2z + Bz^7 \cos(yz^7) \rightarrow \int Ax^2z dz = \frac{1}{2}Ax^2z^2 + Bz^8 \cos(yz^7) + C(x, z)$$

$$u = xy^2 + 14z^C y \cos(yz^7) \rightarrow \int xy^2 dz = \frac{1}{3}xy^3 + 14z^C y \cos(yz^7) + C(x, y)$$

$$u = xy^2 + 14z^C y \cos(yz^7)$$

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$$u = xy^2 + 14z^C y \cos(yz^7)$$

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with limits of integration $a =$ and $b =$

(c) Evaluate the line integral in part (b).

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Assignment 3: Problem 6

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(1 point) Determine whether each of the following vector fields \vec{F} is path independent (conservative) or not. If it is path independent, enter a potential function for it. If it is path dependent, enter NONE.

(a) If $\vec{F}(x, y) = (3x^2 - y^2, -2xy)$, then
 $f(x, y) =$

(b) If $\vec{F}(x, y) = \frac{4y}{x+6}\vec{i} + 4\ln(x+6)\vec{j}$, then
 $f(x, y) =$

(c) If $\vec{F}(x, y) = 5y \sin(xy)\vec{i} + 5x \sin(xy)\vec{j}$, then
 $f(x, y) =$

Note: You can earn partial credit on this problem.

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You have attempted this problem 0 times.

You have unlimited attempts remaining.

Path independent if:

$$\vec{F} = A\vec{i} + B\vec{j} + C\vec{k}$$

- For $u(x, y, z)$,

$$\vec{F} = \nabla u, \quad \frac{\partial u}{\partial x} = A, \quad \frac{\partial u}{\partial y} = B, \quad \frac{\partial u}{\partial z} = C$$

- Line integral: $\int_C \vec{F}(\vec{r}) \cdot d\vec{r} = \int A dx + B dy + C dz = u(P_1) - u(P_0)$
 along C
 from $P_0 \rightarrow P_1$

- For closed contour C : $\oint_C \vec{F}(\vec{r}) \cdot d\vec{r} = 0$

- Test for conservative fields:

$$\text{rot} \begin{bmatrix} \vec{i} & \vec{j} & \vec{k} \\ A & B & C \end{bmatrix}$$

- For conservative fields, $\frac{\partial F_1}{\partial y} = \frac{\partial F_2}{\partial x}$

①

$$\text{a) } \nabla F = f(x, y) = \left\langle \frac{\partial F}{\partial x}, \frac{\partial F}{\partial y} \right\rangle = \langle -2y, -2x \rangle$$

$\therefore \frac{\partial F}{\partial x} = \frac{\partial F}{\partial y} \therefore$ conservative ($\partial x = \partial y$)

Potential func. for vector field:

$$\frac{\partial F}{\partial x} = 3x^2 - y^2 \quad \frac{\partial F}{\partial y} = -2xy$$

$$\int \frac{\partial F}{\partial x} dx = x^3 - y^2 x + C(y)$$

Find $C(y)$:

$$\frac{\partial F}{\partial y} = -2yx + C'(y) = -2xy = \frac{\partial F}{\partial y}$$

$$\therefore C'(y) = 0 \quad C(y) = \int 0 dy = C$$

$$\therefore F = x^3 - y^2 x + C$$