

$$y_n(x,y)=na(x,y),y_{n-1}(x+p,y+q)$$