n and m even

n

m

k even

n even   m odd

n

m

k even
$$k \leq \left(\frac{m-1}{2}\right) n$$

m odd

n odd   m even

n

m

$k - \frac{m}{2}$ even

$k > \frac{m}{2}$