

25/01/25

Day-3

Page No.
 Date

* Agenda

1. p-value & Significant value
2. Distribution
3. Central limit theorem
4. Bernomial Distribution
5. Binomial Distribution
6. Pareto's distribution
7. Log Normal distribution (power law)

* p-value & Significant
→ Derive the p-value

Q-1 The average weight of all residents in Bangalore City is 168 pounds with a standard deviation 3.9. we take a sample of 36 individuals and the mean is 169.5 pounds. CI: 95%.

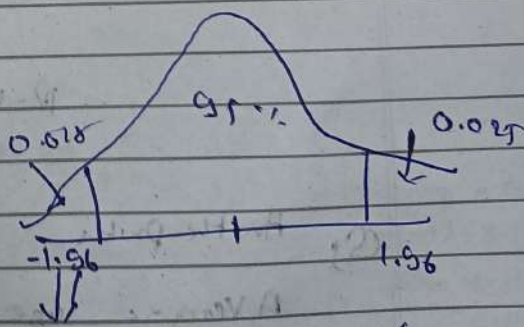
$$\mu = 168 \quad \sigma = 3.9 \quad n = 36$$

Ans:- $n = 36 \quad \alpha = 0.05 \quad Z\text{-test?}$

1. $H_0 = \mu = 168$
 $H_1 = \mu \neq 168$

2. $\alpha = 0.05$

3. decision boundary



$$1 - 0.025 = 0.975 \quad (\text{Check in } Z\text{-table})$$

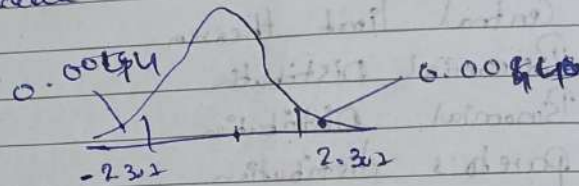
Z test

$$Z = \frac{\bar{x} - \mu}{\frac{\sigma}{\sqrt{n}}} = \frac{169.5 - 168}{\frac{3.9}{\sqrt{36}}} = \frac{1.5}{3.9/6} = \frac{1.5}{0.65} = 2.3077$$

= 2.3077

* Decision rule $\bar{x} = 2.302 > 1.96$ Reject the Null hypothesis

p-value



Now, we check 2 tails :- 0.9911
 $= 1 - 0.9911 = 0.0089$

p-value = $0.0089 + 0.0089$
 $= 0.0178$

p-value = $0.0089 + 0.0089$
 $= 0.0178$

p-value < 0.05

$0.0178 < 0.05$ // \rightarrow Reject the Null hypothesis

p-value $<$ Significant level

Reject Null hypothesis

p-value $>$ Significant level

Fail to Reject the Null hypothesis
 accept the null hypothesis

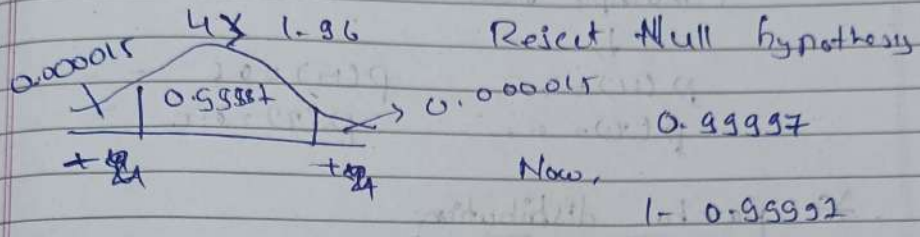
Q3 Another problem

Average age of a college 24 years with a standard deviation 1.5. Sample of 36 students mean is 25 years. $\alpha = 0.05$ (5%) do the age vary?

Null hyp

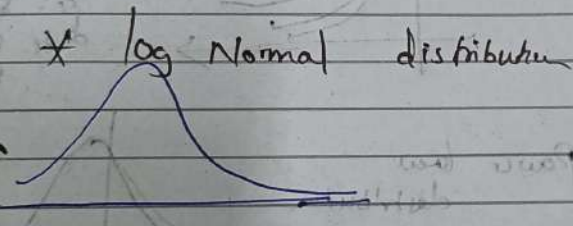
Another $H_0: \mu = 24$ $\sigma = 1.5$ $\bar{x} = 25$ $n = 36$ $\alpha = 0.05$
 $H_a: \mu \neq 24$

$$\frac{\bar{x} - \mu}{\sigma/\sqrt{n}} = \frac{25 - 24}{1.5} \times 6 = \frac{6}{1.5} = 4$$



$P\text{-value} = 0.000015 + 0.000015 = 0.00003$

$P\text{-value} \leq \text{Significance}$ $\left\{ \begin{array}{l} \text{Reject the Null} \\ \text{hypothesis} \end{array} \right\}$

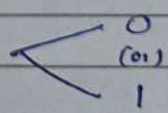


Ex: Wealth Distri

if y Random Variable it's belongs to log Normal distri
 if i apply $\log(y) \rightarrow$ Normal distribution

* Bernoulli's distribution:

2 Outcomes



$p = 0.5$

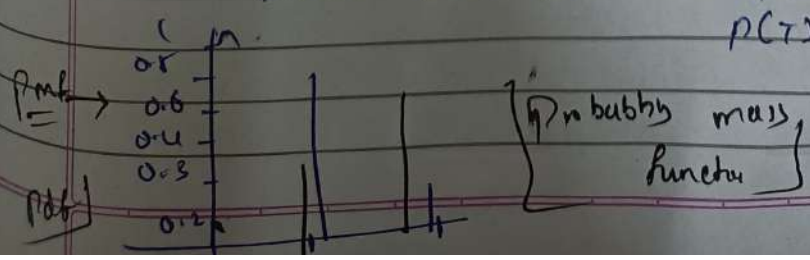
$q = 1 - p = 0.5$

Tossing a coin
 $P(H) = 0.5 \Rightarrow p$

Don't have fair coin $p(=1) = 0.3 \Rightarrow p$

$p(T) = q = 1 - 0.3 = 0.7$

$P(T) = 1 - p = 0.5 - 1 = 0.5$



* Binomial Distribution

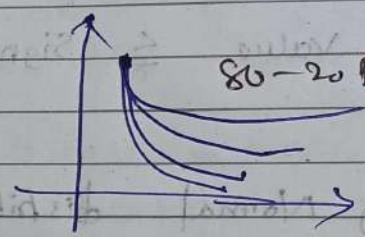
Every \rightarrow Binomial distribution
multiple trial

\downarrow
 $P(H) = 0.5$
 $P(T) = 0.5$

$P(H) = 0.6$
 $P(T) = 0.4$

* Pareto distribution

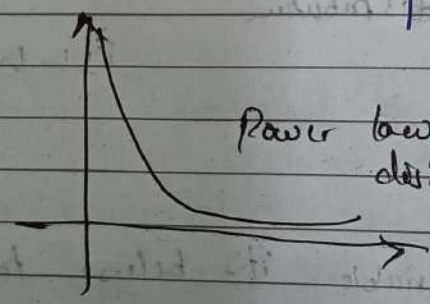
- Pareto distribution it is not a normal-gaussian distrib



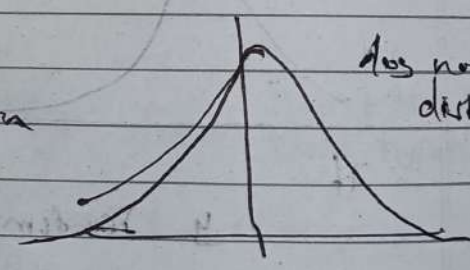
80-20 Rule

Eg: 80% web
20% Prof

Eg: 80% of people
20% of people
in a team



Power law
distribution



Normal
distribution