

--- --- --- $\int^{\infty} \text{ognewt}$

Solve the following

$$4+6+8 \div 2 - 5$$

$$> 4+6+8/2-5$$

[1] 9



$$2^2 + \sqrt{-1-3) + \sqrt{45}}$$

$$> 2^2 + \text{abs}(-3) + \sqrt{45}$$

[1] 13.7082

$$5^3 + 7 \times 5 \times 8 + 96/5$$

$$> 5^3 + 7 \times 5 \times 8 + 96/5$$

[1] 414.2

$$\sqrt{4^2 + 5 \times 3 + 7/6}$$

$$> \sqrt{4^2 + 5 \times 3 + 7/6}$$

[1] 5.671567

round off

$$46 \div 7 + 9 \times 8$$

$$, round (46 \div 7 + 9 \times 8)$$

$$[1] 79$$

$$(2, 3, 5, 7) * 2 > C(2, 3, 5, 7) + C(2, 3)$$

$$[1] 461014 [1] 4191021$$

$$(2, 3, 5, 7) * C(2, 3, 6, 2) > C(1, 6, 2, 3) + C(-2, -3)$$

$$[1] 493014 [1] -2 - 18 - 8 - 3$$

$$C(2, 3, 5, 7)^{12} > C(4, 6, 8, 9, 4, 5)^{12} + C(1, 2,$$

$$[1] 492549 [1] 436512 9165$$

$$(16, 2, 3, 5) / C(4, 5)$$

$$[1] 1.50 0.40 1.75 1.00$$

$$x = 20 > y = 30 > z = 2$$

$$x^2 + y^3 + z$$

$$[1] 27402$$

$$\sqrt{x^2 + y}$$

$$[1] 2073644$$

$$x^2 + y^2$$

$$[1] 1300$$

(1)

Q4
>> x <- matrix (nrow = 4, ncol = 2, data = c(1, 2, 3, 4, 5, 6, 7, 8))

> x
[1,] [2,]
[1,]

[2,] 1 5
[3,] 2 6
[4,] 3 7
[5,] 4 8

Q5. Find $x+y$ & $2x+3y$ where $x = \begin{pmatrix} 4 & -2 & 6 \\ 7 & 0 & 7 \\ 9 & -5 & 3 \end{pmatrix}$

$y = \begin{pmatrix} 10 & -5 & 2 \\ 12 & -4 & 9 \\ 15 & 6 & 5 \end{pmatrix}$

> x <- matrix (nrow = 3, ncol = 3, data = c(4, 7, 9, -2, 0, -5, 6, 7, 3))

> x
[1,] [2,] [3,]

[1,] 4 -2 6

[2,] 7 0 7

[3,] 9 -5 3

> y <- matrix (nrow = 3, ncol = 3, data = c(10, 12, 15, -5, -4, -6, 9, 5))

> y
[1,] [2,] [3,]

[1,] 10 -5 2

[2,] 12 -4 9

[3,] 15 6 5

```
> x+y [1,] 19 -9 13
  [2,] 19 -4 16
  [3,] 21 -11 8
```

```
> z = x + 3 * y [1,] [2,] [3,]
  [1,] 38 -19 33
  [2,] 50 -12 41
  [3,] 63 -28 21
```

Marks of statistics of CS Batch A

$x = ((59, 20, 35, 24, 16, 56, 55, 45, 41, 27, 22, 47, 58,$
 $50, 32, 36, 29, 33, 39))$

> x = data

> breakpoints = seq(20, 60, 25)

> a = cut(x, breakpoints, right = FALSE)

> b = table(a)

> c = transform(b)

> c

		freq
1	[20, 25)	3
2	[25, 30)	2
3	[30, 35)	1
4	[35, 40)	4
5	[40, 45)	1
6	[45, 50)	3
7	[50, 55)	2
8	[55, 60)	4

(g)

Tactical 2
Probability distribution.

Check whether the following are p.m.f or not.

x	$P(x)$
0	0.1
1	0.2
2	0.5
3	0.4
4	0.3
5	0.5

If the given data is p.m.d then $\sum P(x) = 1$

$$\begin{aligned} \therefore P(0) + P(1) + P(2) + P(3) + P(4) + P(5) &= P(x) \\ &= 0.1 + 0.2 + 0.5 + 0.4 + 0.3 + 0.5 \\ &= 1.0 \end{aligned}$$

$\therefore P(x) \geq 0$ & it can't be a probability mass function

x	P(x)
1	0.2
2	0.2
3	0.3
4	0.2
5	0.2

The condition for P.M.D is $\sum P(x) = 1$ so,

$$\sum P(x) = P(1) + P(2) + P(3) + P(4) + P(5)$$

$$= 0.2 + 0.2 + 0.3 + 0.2 + 0.2$$

$$= 1.1$$

\therefore The given data is not a P.M.D because the $P(x) \neq 1$

x	P(x)
10	0.2
20	0.2
30	0.35
40	0.15
50	0.1

The condition for P.M.D is

$$1) P(x) \geq 0 \quad \text{for all values}$$

$$2) \sum P(x) = 1$$

$$\sum P(x) = P(10) + P(20) + P(30) + P(40) + P(50)$$

$$= 0.2 + 0.2 + 0.35 + 0.15 + 0.1$$

$$= 1$$

\therefore The given data is P.M.D

Code:

```
> prob = ((0.2, 0.2, 0.35, 0.15, 0.1))
```

```
> sum(prob)
```

```
(1) 1
```

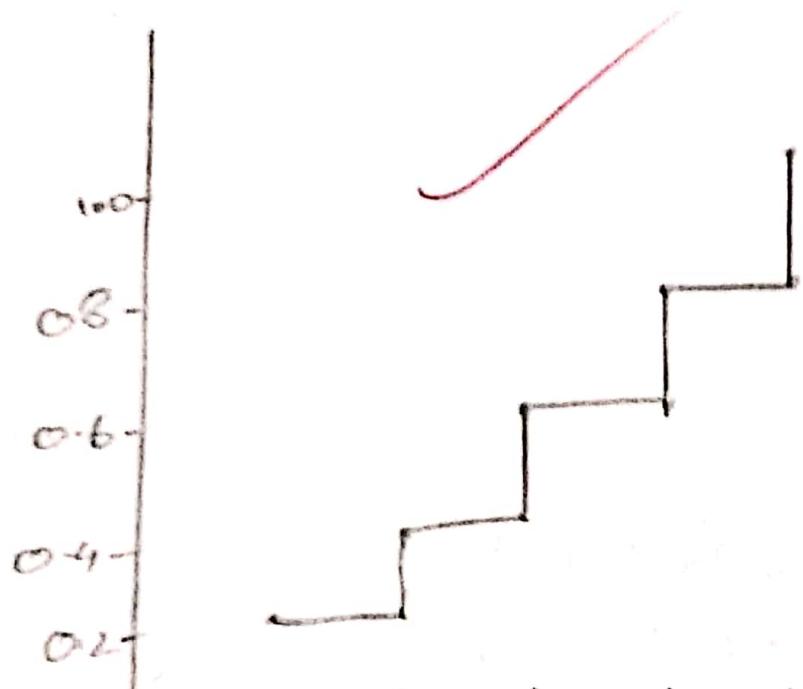
Q. 8.

a. Find the C.D.F. for the following Rand. and sketch the graph.

$$x \quad 10 \quad 20 \quad 30 \quad 40 \quad 50$$

$$P(x) \quad 0.2 \quad 0.2 \quad 0.35 \quad 0.15 \quad 0.1$$

$$\begin{aligned}F(x) &= 0 & x < 10 \\& 0.2 & 10 \leq x < 20 \\& 0.4 & 20 \leq x < 30 \\& 0.75 & 30 \leq x < 40 \\& 0.90 & 40 \leq x < 50 \\& 1.0 & x \geq 50\end{aligned}$$



x	1	2	3	4	5	6
$p(x)$	0.15	0.25	0.1	0.05	0.1	0.1
$p(x) = 0$	0.15	0.40	0.50	0.90	0.90	1.00
	$0 < x \leq 1$	$1 < x \leq 2$	$2 < x \leq 3$	$3 < x \leq 4$	$4 < x \leq 5$	$5 < x \leq 6$
						$x > 6$

$$\begin{aligned} & \text{Prob} = 0.15, 0.25, 0.1, 0.2, 0.02, 0.1 \\ & \text{Prob} = 0.15, 0.25, 0.1, 0.2, 0.02, 0.1 \end{aligned}$$

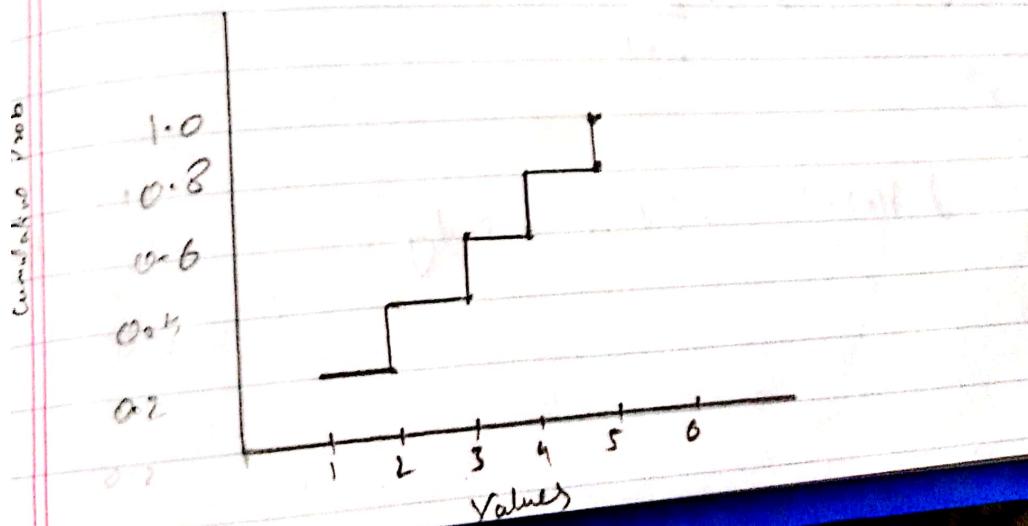
四

\rightarrow (umsum (prob))

[3] 0.15, 0.40, 0.50, 0.10, 0.40, 1.00
≈ 0.15 + 0.40 + 0.50 + 0.10 + 0.40 + 1.00

$\triangleright x = (1, 2, 3, 4, 5, 6)$

```
> plot(x, statfun(census(Prob)), "s", xlab = "Value", ylab = "Cumulative probability", main = "(DF) Graph", title = "boxcar")
```



Q. 8.

3. Check that whether the following is P.d.f or not

$$1) f(x) = 3 - 2x ; 0 \leq x \leq 1$$

$$2) f(x) = 3x^2 ; 0 < x < 1$$

$$1) f(x) = 3 - 2x$$

$$f'(x)$$

$$\int' (3 - 2x) dx$$

$$\int' 3 dx = \int' 2x dx$$

$$[3x - x^2]_0^1 = 2$$

\therefore The $f'(x) = 1$. It is not a P.d.f

$$2) f(x) = 3x^2 ; 0 < x < 1$$

$$f'(x)$$

$$\int' 3x^2$$

$$3 \int' x^2$$

$$[3x^3/3]_0^1 = \dots + x^n = \frac{x^{n+1}}{n+1}$$

$$= x^3$$

\therefore The $f'(x) = 1$ \therefore It is a P.d.f.

7) $\text{dbinom}(10, 100, 0.1)$

[1] 0.1318653

8) $\text{dbinom}(4, 12, 0.2)$

[1] 0.1328756

9) $\text{dbinom}(4, 12, 0.2)$

[1] 0.0274445

10) $1 - \text{dbinom}(5, 12, 0.2)$

[1] 0.01940528

11) $\text{dbinom}(0:5, 5, 0.1)$

0 - 0.59049

1 - 0.32805

2 - 0.07290

3 - 0.00810

4 - 0.00045

5 - 0.00001

12) $\text{dbinom}(5, 12, 0.25)$

[1] 0.1032414

13) $\text{dbinom}(5, 12, 0.25)$

[1] 1 - $\text{dbinom}(7, 12, 0.25)$

[1] 0.00278151

14) $\text{dbinom}(6, 12, 0.25)$

[1] 0.04014995

61
80

Topic 3

Binomial distribution

$$\text{if } P(X=x) = \text{Binom}(X, n, p)$$

$$\text{if } P(X \leq x) = \text{Binom}(X, n, p)$$

$$\text{if } P(X > x) = 1 - \text{Binom}(X, n, p)$$

If θ is unknown

$$\theta_1 = P(X \leq x), \text{ Binom}(P, n, \theta)$$

- 1) Find the probability of exactly 10 success in hundred trials
 $p=0.1$
- 2) Suppose there are 12 mcq, each question has 3 options out of which 1 is correct. Find the probability of having exactly 4 correct answers.
 - i) Atmost 4 correct answers.
 - ii) More than 5 correct answers.
- 3) Find the complete distribution when $n=5$ and $p=0.1$
- 4) $n=12$, $p=0.25$, find the following probabilities
 - i) $P(X=5)$
 - ii) $P(X \geq 9)$
 - iii) $P(X \leq 5)$
 - iv) $P(5 < X < 9)$

$\rightarrow \text{dbinom}(U, 10, 0.15)$

[1] 0.1968944

$\rightarrow \text{Pbinom}(3, 20, 0.15)$

[1] 0.3522748

$\text{qbinom}(0.88, 30, 0.2)$

[1] 9

> n = 10

> p = 0.3

> x = 0:n

> prob = dbinom(x, n, p)

> cumprob = pbinom(x, n, p)

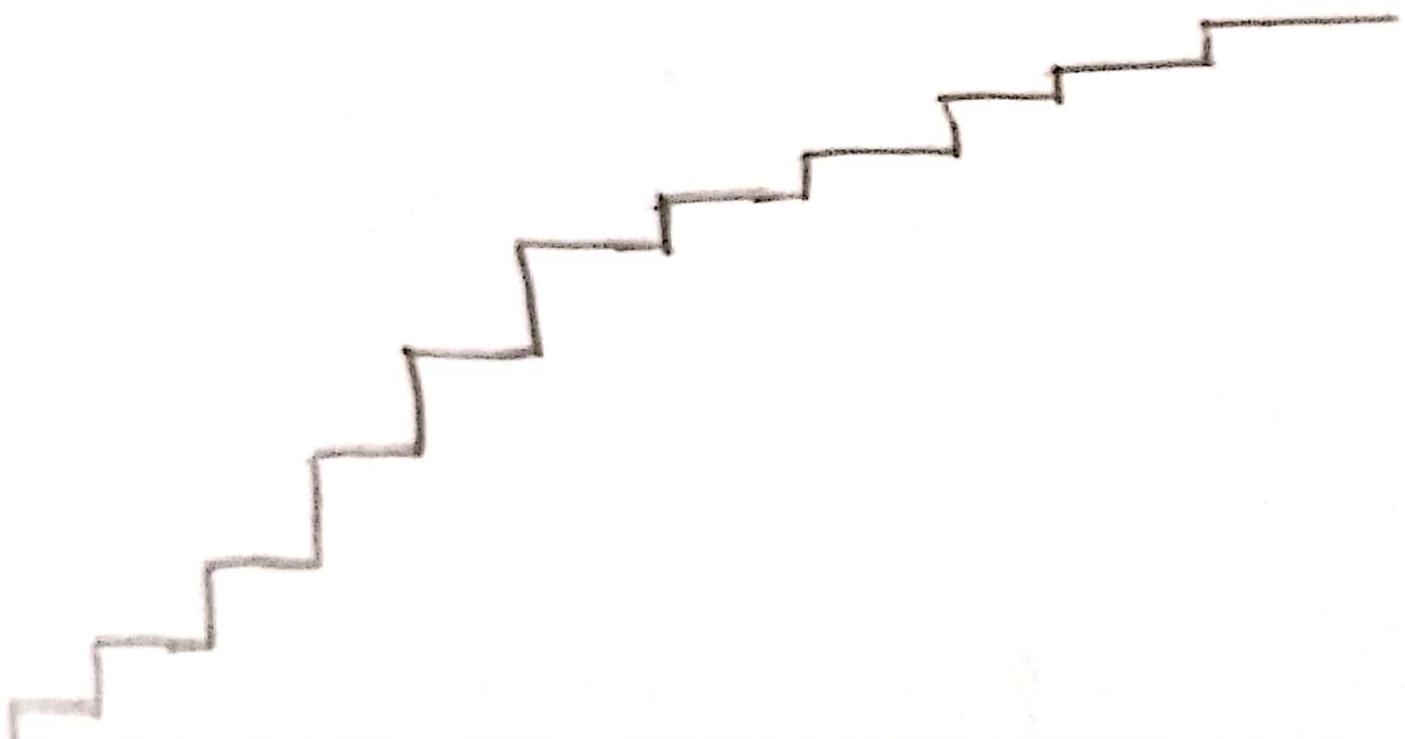
> d = data-frame ("xValues": x, "Probability": prob)

> print(d)

xValues	Probability
0	0.0282
1	0.1210
2	0.2100 0.2334
3	0.2334 0.2668
4	0.2668 0.1001
5	0.2001 0.1029
6	0.1029 0.0367
7	0.0367 0.0090
8	0.0090 0.0013
9	0.0014 0.0001
10	0.0000

0 2 4 6 8

(, lmp3obj, "S")



Normal Distribution
Practical 2)

$$\begin{aligned} i) P(x = x) &= \text{dnorm}(x, \mu, \sigma) \\ ii) P(x \leq x) &= \text{pnorm}(x, \mu, \sigma) \\ iii) P(x > x) &= 1 - \text{pnorm}(x, \mu, \sigma) \end{aligned}$$

i) To generate random numbers from a normal distribution (random numbers) the R code is $\text{rnorm}(n, \mu, \sigma)$

A random variable x follows normal distribution with $\mu = 12$ & $\sigma = 3$. Find i) $P(x < 13)$ ii) $P(10 < x < 13)$
iii) $P(x > 14)$ iv) Generate observation (random number)

$$> p1 = \text{pnorm}(13, 12, 3)$$

> p1

[1] 0.8413447

$$> (at ("P(x \leq 13) = ", p1))$$

$$p(1 < x < 13) = 0.8413447$$

$$> p2 = \text{pnorm}(13, 12, 3) - \text{pnorm}(10, 12, 3)$$

> p2

[1] 0.3980661

$$> (at ("P(10 < x < 13) = ", p2))$$

$$p(10 < x < 13) = 0.3980661$$

$$> p3 = 1 - \text{pnorm}(14, 12, 3)$$

> p3

[1] 0.2524925

> qnorm($P(x \leq 14)$, 10, 2)

$$P(x \leq 14) = 0.1824925$$

> ?
[1] 0.1824925

> pnorm

[1] 0.1824925 16.54850 11.280518
12.222460

6.619474 10

2. X follows normal distribution with $\mu=10$, $\sigma=2$. Find
i) $P(x \leq 7)$ ii) $P(5 < x < 12)$ iii) $P(x > 12)$ iv) Generate
observation v) find k such that $P(x \leq k) = 0.4$.

> a1 = rnorm(7, 10, 2)

> a1

[1] 0.0668072

> a2 = rnorm(5, 10, 2) - rnorm(12, 10, 2)

> a2

[1] -0.8351351

> a3 = 1 - pnorm(12, 10, 2)

> a3

[1] 0.1586553

> a4 = rnorm(10, 10, 2)

> a4

[1] 11.608931 9.920417 12.637751 8.093254

8.221380 9.143726 9.366824 11.7071

9.537584 10.715006

> a5 = qnorm(0.4, 10, 2)

> a5

[1] 9.493306

> $\text{sd} = \sqrt{v}$

> sd

[1] 3.331613

$\text{sd} = \text{sd}(\text{"SD": "sd"})$

$\text{sd} = 3.331613$

$$4. \quad \alpha \sim N(30, 100) \quad \sigma = 10$$

$$\text{i)} P(x \leq 40)$$

$$\text{ii)} P(x > 35)$$

$$\text{iii)} P(25 < x < 35)$$

iv) find k such that $P(x < k) = 0.6$

$$> R_1 = \text{pnorm}(40, 30, 10)$$

$$> R_1$$

$$[1] 0.891347$$

$$> p_2 = 1 - \text{pnorm}(35, 30, 10)$$

$$> p_2$$

$$[1] 0.3085375$$

$$> p_3 = \text{pnorm}(25, 30, 10) - \text{pnorm}(35, 30, 10)$$

$$> p_3$$

$$[1] -0.382949$$

$$?_4 = \text{pnorm}(0.6, 30, 10)$$

$$p_4$$

$$132.53347$$

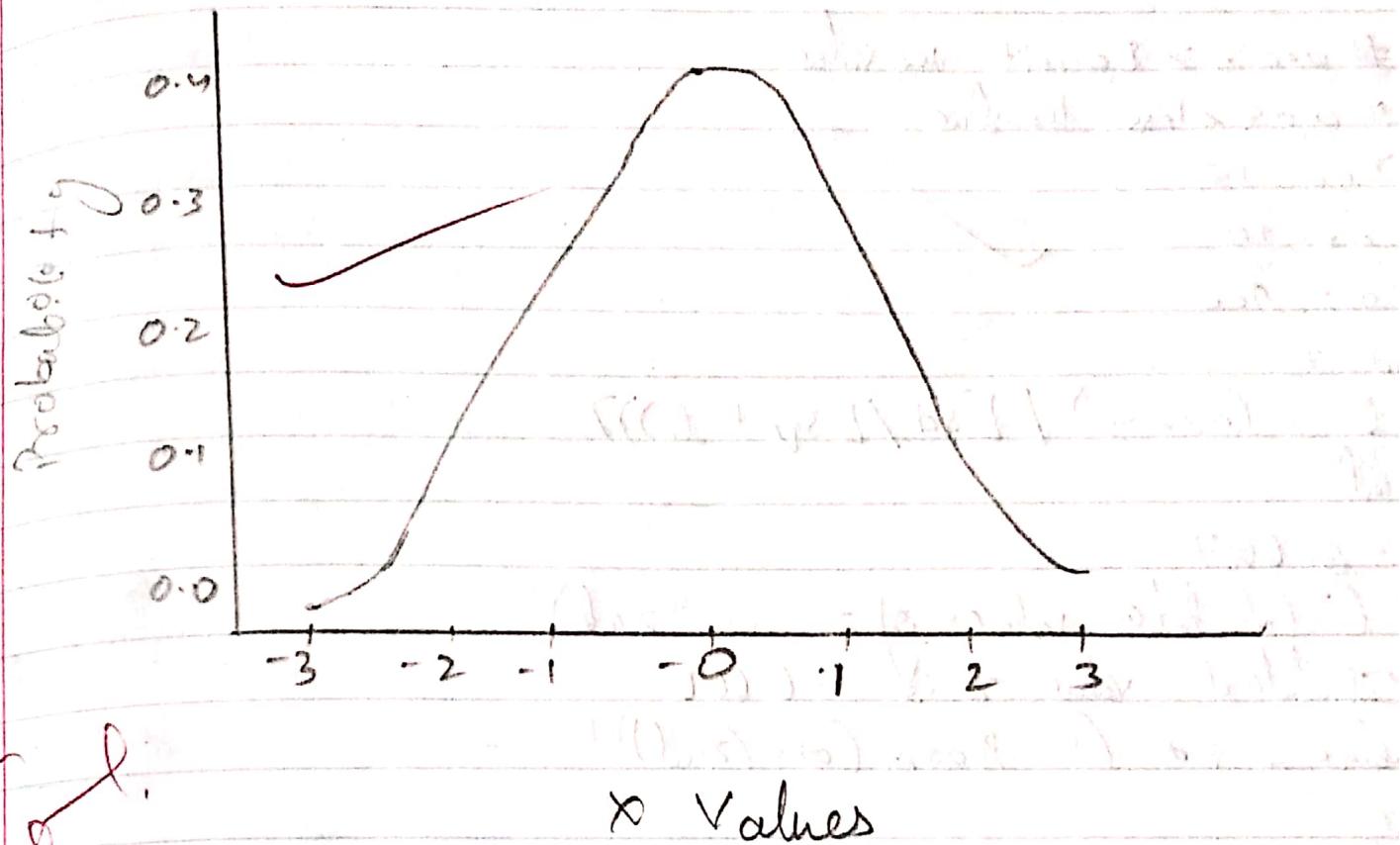
plot the standard normal graph

$\geq x = \text{seq}(-3, 3, by = 0.1)$

$\geq y = \text{dnorm}(x)$

$\geq \text{plot}(x, y, xlab = "x values", ylab = "probability", main = "standard normal graph")$

Standard Normal Graph



Q. 4

Bacterial S

Normal Eq. Z-test
 $H_0: \mu = 15$ $H_1: \mu \neq 15$

Test the hypothesis:
Random sample of size 400 is drawn and it is
fully calculated. The sample mean is 14 and $S.D.$ is 3.
The hypothesis at 5% level of significance at

$0.05 > 1$ accept the value

$0.05 <$ less the value.

> $m_0 = 15$

> $m_d = 14$

> $n = 400$

> $s_d = 3$

$$z_{cal} = (m_d - m_0) / [s_d / (\sqrt{n})]$$

> z_{cal}

[i] - 6.667

> Cal ("absolute values of z is = " z_{cal})

Calculated value z is = -6.666

$$\Rightarrow P\text{value} = 2 \times (1 - \text{Pr}(Z \geq |z_{cal}|))$$

> Pvalue

[i] 2.616796

The value is less than 0.05 we will reject the
Value of $H_0: \mu = 15$



Test the hypothesis $H_0: \mu = 10$ against $H_1: \mu < 10$
A random sample size $n = 400$ is drawn with sample mean $\bar{x} = 10.2$
 $s.d = 2.25$ Test the hypothesis H_0 . 50

$$n = 10$$

$$n = 400$$

$$\bar{x} = 10.2$$

$$s.d = 2.25$$

$$z_{cal} = (m - \mu) / [s.d / \sqrt{n}]$$

cal

$$z_{cal} = 1.7773$$

$$\text{p-value} = 2 * (1 - \text{norm}(\text{abs}(z_{cal})))$$

p-value

$$> 0.07544036$$

The value p-value is greater than 0.05. The value is accepted.

Test the hypothesis $H_0: p = p_0$ proportional of smokers in college is 0
is collected & calculated the sample of as 0.125 test the
at 5% level of significance

$$p = 0.125$$

$$p = 0.125$$

$$n = 400$$

$$Q = 1.9$$

$$z_{cal} = (p - p_0) / \sqrt{p_0(1 - p_0) / n}$$

$$z_{cal} (\text{calculated value of } z \text{ is}) = 2.75$$

$$\text{p-value} (\text{calculated value of } z \text{ is}) = -3.75$$

$$\text{p-value} = 2 * (1 - \text{norm}(\text{abs}(z_{cal})))$$

p-value

$$> 0.0001768346 \text{ (Reject)}$$

6) last year farmers lost 20% of their crop - A
of 60 fields are collected 80% is first hypothesis of 1.
Significance.

> $p = 0.2$

> $p = 0.160$

> $n = 60$

> $\text{zcal} = (p - p_0) / \text{Estat}(p + 0.1)$

> zcal

> $[1] = 0.9682^4$

> $\text{Pvalue} = 2 \times (1 - \text{norm}(\text{abs}(\text{zcal})))$

Pvalue

> $[1] = 0.332916$

Test

Test the hypothesis $H_0: \mu = 12.5$ from the following sample
5% level of significance.

$x = [12.25, 11.97, 12.25, 12.08, 12.31, 12.28, 11.94, 11.8, 12.04]$

$n = \text{length}(x)$

n

[1] 10
 $m = \text{mean}(x)$

m

[1] 12.107

$\text{variance} = ((n-1) * \text{var}(x)) / n$

variance

[1] 0.01952

$s.d = \sqrt{\text{variance}}$

$s.d$

[1] 0.1397176

$t = (m_s - m_0) / (s.d / \sqrt{n})$

t

[1] -8.894909

$p\text{value} = 2 * (1 - \text{pnorm}(\text{abs}(t)))$

$p\text{value}$

[1] 0

∴ This value is less than 0.05 hence accepted

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Practical 6

- Q) Let the population mean (the mean spent per customer in restaurant) is 250. A sample of 100 customers selected from now is customer as 275 & S.D = 30. Test the hypothesis that the population mean is 250 at α = 5%.
- Significant.
- Q) In a random sample of 100 student it is found that 750 wear spectacles. Test the null hypothesis that the proportion of students who wear spectacles is 0.8 at 1% level of significance.
- $\rightarrow \bar{x} = 275$
- $S.D = 30$
- $n = 100$
- $Z_{cal} = (\bar{x} - \mu_0) / S.D / \sqrt{n}$
- Z_{cal} ("Calculated value of Z", "cal")
- [1] Calculated value of Z is = 8.333
- $P\text{Value} = 2 * (1 - \text{Norm}(Z_{cal}))$
- Practical
- [1] D
- The value is less than 0.05 we will reject $H_0: \mu = 250$

$$\frac{P=0.8}{P=1-P} \quad P = \frac{750}{1000} \\ P = 75\% \quad P = 1 - (P_0 - P_1) / \text{Sqrt}(P_0 \cdot P_1 \cdot n_1)$$

Actual ("calulation Value is 2.15;" , 2nd)
Actual Value of $z^1 = 2.15$

(1) calculated Value of Z: -3.95528
 $Z = 2\sigma (1 - P_{\text{norm}})$ (See Fig 11.11)

$$p_{\text{value}} = 2 \alpha (1 - P_{\text{norm}}(\text{abs}(z_{\text{red}})))$$

*Frank
Robert*

7-7-77628-32

11628.32

(1) The value is low and

The value is less 0.01 us

ان ۱۰۰ سو ام

A study of noise Level in 2 hrs.

3) Founding of more Level in 2 hosps
, hospital have same level

2 hospitals have same level of no. of
Hosp. n

Hos. A

84

61-2 5

~~7:9~~

7-9 ✓ 7

$$n = 84$$

$$n_2 = 3^4$$

$$m \times l = 61 \cdot 2$$

$$m_{12} = 59.4$$

$$sd1 = 7.9$$

$$d_2 = 7 : 5$$

$$d_2 = 7.5 \text{ cm} \approx m_{2,1} / \sin(\pi s d^{1.12}/m)$$

$$\rho_{\text{eff}} = (m_{11} - m_{22}) / \text{Sart} ((\text{Sc}^{\text{eff}})^2 + m)$$

26

71.16 2528

3116 CS20



$$\geq \text{value} = 2 * (1 - \text{Pnorm}(\text{abs}(z_{\text{cal}})))$$

value
10 value

(1) 0.745021

The value is greater than 0.1 we accept the value.

In a sample of 600 student is 400 used a blue ink. In a sample of 900 student is 450 use blue ink. Test the hypothesis that the proportion of students using blue ink in two colleges to be equal or not at 1% level of significance.

As $H_0: p_1 = p_2$ against $H_1: p_1 \neq p_2$

$$n_1 = 600$$

$$n_2 = 900$$

$$p_1 = 400/600$$

$$p_2 = 450/900$$

$$p = (n_1 * p_1 + n_2 * p_2) / (n_1 + n_2)$$

PP

(1) 0.4333

$$\geq z_{\text{cal}} = (p_1 - p^2) / \sqrt{p(1-p)(1/n_1 + 1/n_2)}$$

z_{cal}

(1) 6.381534

$$\geq \text{pvalue} = 2 * (1 - \text{Pnorm}(\text{abs}(z_{\text{cal}})))$$

pvalue

$$3.17532 e^{-10}$$

\therefore Pvalue is less than 0.01 the value is rejected

Practical 9

Topic : Small Sample test

The marks of 10 students are given 63, 63, 66, 67, 68, 69, 70, 70, 71, 72. Test the hypothesis that the sample comes from the population with average 66.

$$H_0: \mu = 66$$

$$H_a: \mu \neq 66$$

t-test (x)

one sample

data: x

$$\bar{x} = 68.319, df = 9, p\text{value} = 1.558e^{-13}$$

alternative hypothesis

True mean is not equal to 0

95 percent confidence interval

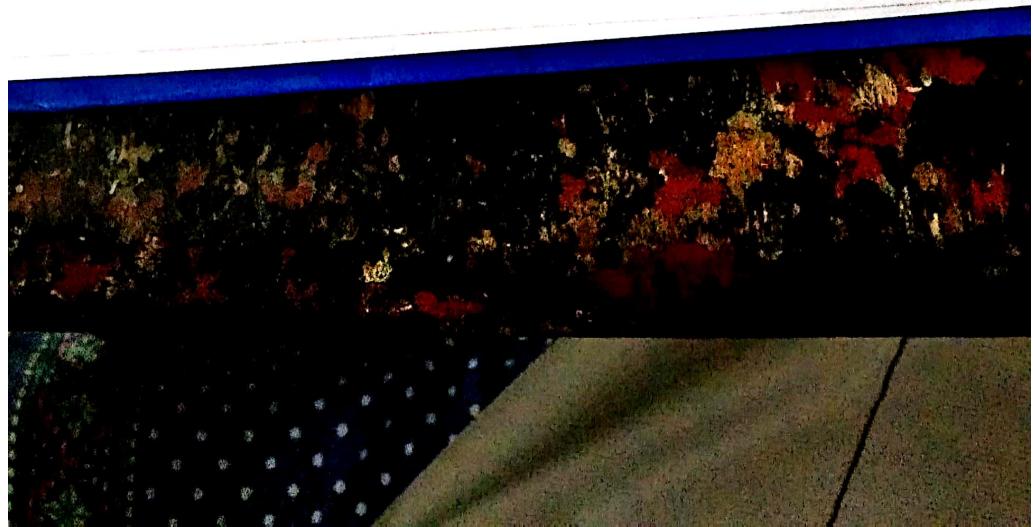
$$[65.65171, 70.14829]$$

sample estimates

mean of x

$$68.319$$

The p-value is less than 0.05 we reject the hypothesis of significance.



2. Two groups of student scored the following marks - Test hypothesis that there is no significant difference between the 2 groups.

GR1 = 18, 22, 21, 19, 20, 17, 23, 20, 22, 21

GR2 = 16, 20, 14, 21, 20, 18, 13, 15, 17, 21

H₀: There is no difference b/w the 2 groups

>x=c(18, 22, 21, 19, 20, 17, 23, 20, 22, 21)

>y=c(16, 20, 14, 21, 20, 18, 13, 15, 17, 21)

>t.test(x,y)

w Two sample t-test

Data: x and y

t = 2.2573 df = 16.376 p-value = 0.03798

alternative hypothesis:

True difference in means is not equal to 0.95

confidence interval:

0.1628205 - 5.0371795

Sample estimates:

mean of x mean of y

20.1 19.5

>p.value = 0.03798

>if(p.value > 0.05) cat("accept H₀") {

else {cat("reject H₀")}}

reject H₀.

The sales data of 36 shops before & after a special campaign are given below.

Before: 63, 18, 31, 48, 50, 42

After: 68, 29, 30, 55, 66, 45

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H₀: The hypothesis that the campaign is effective do not.

H₁: There is no significant difference of sales before & after campaign.

(Before)

(After)

H₀: (x_i, y_i) Paired = T, alternative = "greater"

paired t-test

df: 35

-2.7815, df = 5, Pvalue = 0.9806

reject the hypothesis

True difference in means is greater than 0.95 percent confidence

-6.035547 if

sample estimates

mean of the difference

-3.05

Pvalue is greater than 0.05, we accept the hypothesis at s of significance.



Two difference
Q9 - 83333

Value is greater than 0.05 we accept the null hypothesis.

2 medicine are applied to two group of period respectively

$$g_1: 10, 12, 13, 11, 14$$

$$g_2: 8, 9, 12, 14, 15, 10, 9$$

is there any significant difference.

Wilk's medians.

H0: There is no significant difference.

χ^2 (GDP)

χ^2 (GDP)

$t_{t, 10} + (x, y)$

Data: x, y

$$t = 0.80384, df = 9, 7594, p\text{ value} = 0.4406$$

alternative hypothesis: true difference in means is not 10.0

95 percent confidence interval

$$-0.9698553 \quad 4.2981886$$

sample estimates:

mean of x	mean of y
12.0000	10.3333

As p-value is greater than 0.05 we accept the H₀ at 5% level of significance.

Q1:

> real

[30]

> make = 2 & (Pnorm (abs (real)))

> value

[31]

As value is greater than 0.05 we accept null hypothesis of significance.

$H_0: \mu = 66$ against $H_1: \mu \neq 66$
 $\{70, 63, 61, 69, 74, 71, 72\}$
 $\text{std dev} = 4.16$

$\bar{x} = 68.99$
 $s = 6$ value: 5.522504

Alternative hypothesis: true mean is not equal to 66
 95% confidence interval
 $64.6649 \leq \mu \leq 71.6709$

Sample size
 n = 7

Since P-value is less than 0.05 we reject H_0 at 1%. Thus

$H_0: \mu = 66$ against $H_1: \mu \neq 66$
 $\bar{x} = 71.66$
 $\{76, 66, 66, 74, 78, 82, 87, 92, 93, 95, 97\}$

$\bar{x} = 80.1134$ ($n=11$)

Test to compare two variance

obs: 80.1134
 $\text{std dev} = 7$. num. df = 10

f: 0.7838
 value: 0.7737

alternative hypothesis: The ratio of var. value is off
 95% + Confidence interval
 7.75188
 0.199509

(18)

Searson's estimate
ratio of variance
 0.2880255

p-value is greater than 0.05 we accept the null hypothesis.

Significance.

Q) $H_0: p_1 = p_2$ against $H_1: p_1 \neq p_2$

$$> n_1 = 200$$

$$> n_2 = 300$$

$$> p_1 = 0.48$$

$$> p_2 = 0.56 / 300$$

$$> p(p_1 + p_2) / (n_1 + n_2)$$

$$> P$$

$$[.] 0.2$$

$$> q = 1 - P$$

$$[.] 0.8$$

$$> z_{cal} = (p_1 - p_2) / \sqrt{p(1-p)(1/n_1 + 1/n_2)}$$

$$> z_{cal}$$

$$[.] 0.3613104$$

\therefore p-value is greater than 0.05 we accept the null hypothesis.

Significance.

(S)

$x = c(1.68, 3.35, 2.50, 6.23, 3.24)$
 $n = c(\text{length}(x); p_0 = 0.5)$
 $y > y$
 $[1] \text{ FALSE FALSE FALSE TRUE FALSE}$
 $s = \sum(x > y); s$
 $x > y$
 $[1] 1$
 $\rightarrow \text{binom.test}(s, n, p = 0.5, \text{alternative} = \text{"greater"})$

Exact binomial test

data: s & n
number of successes = 1, number of trials = s, p = 0.9688

Alternative hypothesis: true probability of success is not 0.595%. Confidence interval:

0.01020622 1.00000

Sample estimates

Probability of success

~~without ties~~

wilcoxon test
The scores of 8 student in reading before & after lesson are as follow. Test whether there is any difference in reading.

Student no:	1	2	3	4	5	6	7	8
Score before	10	15	16	12	09	07	11	12
Score after	13	16	15	13	09	10	13	10

> b <- c (10, 15, 16, 12, 09, 07, 11, 12);

> a <- c (13, 16, 15, 13, 09, 10, 13, 10);

> 0 <- b-a;

> wilcox.test (P, alternative = "greater");

data: P

V = 10.5, p-value = 0.8722
alternative hypothesis: true location is greater

warning message:

✓ wilcox.test.default (P, alternative = "gr")
cannot compute exact p-value with ties



using Wilcoxon's test.

The diameter of a ball bearing was measured by 6 methods on 400 different kinds of materials. The results were as follows:

Measurement	1	2	3	4	5	6
Method 1	0.265	0.268	0.266	0.269	0.269	0.264
Method 2	0.263	0.262	0.270	0.261	0.271	0.260

Wilcoxon's test (x, y , alternative = "greater")

Wilcoxon rank sum test

data: $x & y$

$n = 24$, p-value = 0.197 ✓

alternative hypothesis: true location shift is gr

✓

Practical 10

Use the following data to test whether the condition of home & condition of child are independent or not:

Child	cond	clean	dirty
Home	clean	70	50
	Fairly clean	80	20
	dirty	35	45

H0: Condition of Home & Child are independent

> x = c(70, 80, 35, 50, 20, 45)

> m = 3

> n = 2

> y = matrix(x, nrow = m, ncol = n)

> y

[1] [2]

[1,] 70 50

[2,] 80 20

[3,] 25 45

> Pv = chisq.test(y)

> Pv

Pearson's Chi-squared test

data: y

$$\chi^2 = 25.646$$

$$df = 2$$

$$p\text{-value} = 2.698 \times 10^{-6}$$

They are dependent

\therefore p-value is less than 0.05 we reject the hypothesis at 5 level of significance.

2. Test the hypothesis that varcine & disease are independent not.

Varcline		
Disease	Affected	No affected
Affected	70	46
Non-affected	35	37

H_0 : Disease & Varcline are independent.

$$> \chi = \chi(70, 35, 46, 37)$$

$$> m = 2$$

$$> n = 2$$

$> y = \text{matrix}(x, \text{ncol} = m, \text{nrow} = n)$

$\Rightarrow y$

$[,1] [,2]$

$[1,] 70 46$

$[2,] 35 37$

$$> PV = \text{chisq.test}(y)$$

$\Rightarrow PV$

Pearson's Chi-squared test with Yates continuity correction

$$\text{df} = 1$$

$$x_{\text{treat}} = 2.0272$$

$$df = 1$$

$$p\text{-value} = 0.1545$$

∴ p-value is more than 0.05 we don't reject hypothesis of 5% level of significance.

60

perform a ANOVA for two following data

Type

Observation

A

50, 52

B

53, 53, 53

C

60, 58, 57, 56

D

52, 54, 54, 55

H0: The mean's are equal for A, B, C, D.

> $x_1 = c(50, 52)$

> $x_2 = c(53, 53, 53)$

> $x_3 = c(60, 58, 57, 56)$

> $x_4 = c(52, 54, 54, 55)$

> d = stack(list(b1 = x1, b2 = x2, b3 = x3, b4 = x4))

> range(d)

[1] "values" "ind"

, one-way, fct (Value=ind, df=3, var=var=r)

one-way analysis of means

data: value and ind

f: 11.733 df: 3, chisq: 9.1

pvalue: 0.00183

10

Habit is less than 0.01 we reject the hypothesis
anova - one (treats and, standard)

summary (anova)

df	sum_sq	mean_sq	f_value	p > F
2	71.06	35.53	11.73	0.00183
9	18.17	2.02		

signif: 0.001 < 0.01
0.05 < 0.01

