## Assignment 2: Question 15 (b)

Abhay Shankar K: cs21btech11001

April 10, 2022

## Question:

a plane is:

Find the length of the perpendicular from the origin to the plane

$$\vec{r} \cdot (3i - 4j - 12k) + 39 = 0 \tag{1}$$

**Solution:** Clearly, the length of the perpendicular from a plane passing through some point is the distance of that point from the plane.

The normal form of a plane is an equation of the form:

$$\vec{A}\vec{x} = D \tag{2}$$

Where:

- $\vec{A} = (a \ b \ c)$
- $\vec{x} = \begin{pmatrix} x \\ y \\ z \end{pmatrix}$ , called the point vector
- D is some scalar constant.

represent given can the (equation (1)) using normal form from equation (2) thus:

$$(3 \quad -4 \quad -12) \vec{x} = -39$$
 (3)

The formula for the distance of a point from

$$Distance = \begin{vmatrix} (a & b & c & D) \begin{pmatrix} x \\ y \\ z \\ 1 \end{vmatrix}$$
 (4)

Substituting input parameters into equation (4),

• 
$$(a \ b \ c) = \vec{A} = (3 \ -4 \ -12)$$

$$\bullet \ \begin{pmatrix} x \\ y \\ z \end{pmatrix} = \vec{x} = \begin{pmatrix} 0 \\ 0 \\ 0 \end{pmatrix}$$

• D = -39

$$Distance = \begin{vmatrix} (a & b & c & D) \begin{pmatrix} x \\ y \\ z \\ 1 \end{pmatrix} \\ = \begin{vmatrix} (3 & -4 & -12 & -39) \begin{pmatrix} 0 \\ 0 \\ 0 \\ 1 \end{pmatrix} \\ \hline \sqrt{3^2 + (-4)^2 + (-12)^2} \\ = \begin{vmatrix} -39 \\ \sqrt{169} \end{vmatrix} & (7) \\ = |-3| & (8) \\ = 3 & (9) \end{vmatrix}$$

... The length of the perpendicular from the origin to the plane  $\vec{r} \cdot (3i - 4j - 12k) + 39 = 0$  is 3 units.