

# Assignment 3 : Example 9

Abhay Shankar K : cs21btech11001

## Question:

Consider the frequency distribution table (given below), which gives the weights of 38 students in a class.

- (i) Find the probability that the weight of a student in a class lies in the interval 46 – 50.
- (ii) Give two events in this context, one having probability 0, and the other having probability 1.

TABLE I  
DISTRIBUTION OF WEIGHTS OF STUDENTS IN A CLASS

| Weight class | Number of students (frequency) |
|--------------|--------------------------------|
| 31 - 35      | 9                              |
| 36 - 40      | 5                              |
| 41 - 45      | 14                             |
| 46 - 50      | 3                              |
| 51 - 55      | 1                              |
| 56 - 60      | 2                              |
| 61 - 65      | 2                              |
| 66 - 70      | 1                              |
| 71 - 75      | 1                              |

## Solution:

- (i) Let us define a random variable X, which represents the weight class of a student. The range of X and the corresponding weight class is given in the table below.

TABLE II  
RANGE OF X MAPPED TO WEIGHT CLASSES FROM I

| Weight class | X |
|--------------|---|
| 31 - 35      | 1 |
| 36 - 40      | 2 |
| 41 - 45      | 3 |
| 46 - 50      | 4 |
| 51 - 55      | 5 |
| 56 - 60      | 6 |
| 61 - 65      | 7 |
| 66 - 70      | 8 |
| 71 - 75      | 9 |

Therefore,

$$P_X(1) = \frac{9}{38} = 0.237 \quad (1)$$

$$P_X(2) = \frac{5}{38} = 0.131 \quad (2)$$

$$P_X(3) = \frac{14}{38} = 0.368 \quad (3)$$

$$P_X(4) = \frac{3}{38} = 0.079 \quad (4)$$

$$P_X(5) = \frac{1}{38} = 0.026 \quad (5)$$

$$P_X(6) = \frac{2}{38} = 0.053 \quad (6)$$

$$P_X(7) = \frac{2}{38} = 0.053 \quad (7)$$

$$P_X(8) = \frac{1}{38} = 0.026 \quad (8)$$

$$P_X(9) = \frac{1}{38} = 0.026 \quad (9)$$

From (4), the probability that the weight of a student is in the weight class (46 – 50) is 0.079.

- (ii)
  - The probability that the weight of a student is greater than 75 is 0.
  - The probability that the weight of a student is in the interval [31, 75] is 1.

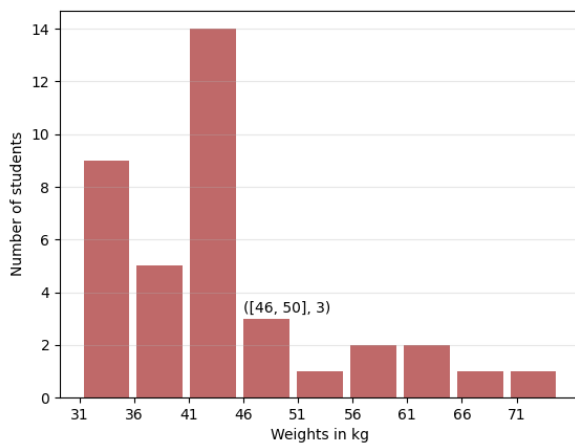


Fig. 1. Histogram of given data (produced using python)