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## Assignment 2: Question 15 (b)

Abhay Shankar K: cs21btech11001

## **Question:**

Find the length of the perpendicular from the origin to the plane

$$\mathbf{r} \cdot (3i - 4j - 12k) + 39 = 0 \tag{1}$$

## **Solution:**

Clearly, the length of the perpendicular from a plane passing through some point is the distance of that point from the plane. The normal form of a plane is an equation of the form:

$$\mathbf{n}^{\mathsf{T}}\mathbf{x} = c \tag{2}$$

Where:

$$\mathbf{n} = \begin{pmatrix} p \\ q \\ r \end{pmatrix}, \mathbf{x} = \begin{pmatrix} x \\ y \\ z \end{pmatrix} \tag{3}$$

We can represent the given plane (equation (1)) using normal form (equation (2)) thus:

$$\begin{pmatrix} 3 \\ -4 \\ -12 \end{pmatrix}^{\top} \mathbf{x} = -39 \tag{4}$$

The formula for the distance of a point from a plane is :

$$Distance = \frac{\left|\mathbf{n}^{\top}\mathbf{x} - D\right|}{\|\mathbf{n}\|}$$
 (5)

The input parameters are:

$$\mathbf{n} = \begin{pmatrix} 3 \\ -4 \\ -12 \end{pmatrix}, \mathbf{x} = \begin{pmatrix} 0 \\ 0 \\ 0 \end{pmatrix}, c = -39 \tag{6}$$

Substituting (6) in (5),

$$Distance = \frac{\left| \begin{pmatrix} 3 \\ -4 \\ -12 \end{pmatrix}^{\top} \begin{pmatrix} 0 \\ 0 \\ 0 \end{pmatrix} + 39 \right|}{\left\| \begin{pmatrix} 3 \\ -4 \\ -12 \end{pmatrix} \right\|}$$
(7)

$$= \frac{39}{13}$$
 (8)  
= 3 (9)

 $\therefore$  The length of the perpendicular from the origin to the plane (equation (1)) is  $\underline{3}$  units.

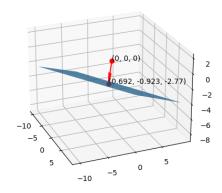


Fig. 1. Graph of the given plane