

CS112: Data Structures

Lecture 03

Stacks and Queues

Review: Generic Lists

- **Problem:** suppose you want to have a list of Strings and a list of ints and ...
- **Class declarations and methods are almost identical**
- **Solution in java 1.5: “generics”**
 - **Class & method definitions parameterized by type**

Generic List

```
public class Node<E> {  
    private E data;  
    private Node<E> next;  
  
    public Node<E>(E dat, Node<E> nxt){  
        data = dat;  
        next = nxt;  
    }  
  
    public E getHead(Node<E> head){  
        E headData = head.data;  
        return headData;} ...
```

Type parameter, eg String

Declare an instance variable of type E, e.g. String

Generic List

In some method:

```
Node<String> n1 = new Node<String>;
```

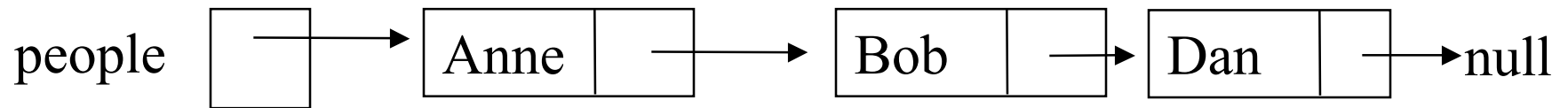
...

```
String name = n1.getHead( );
```

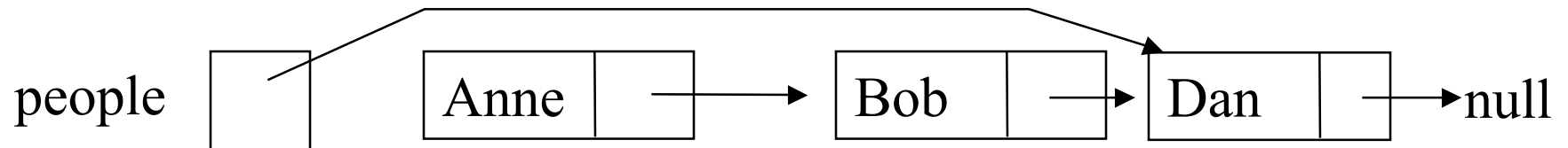
Actual argument corresponding to type parameter E

Circular Lists

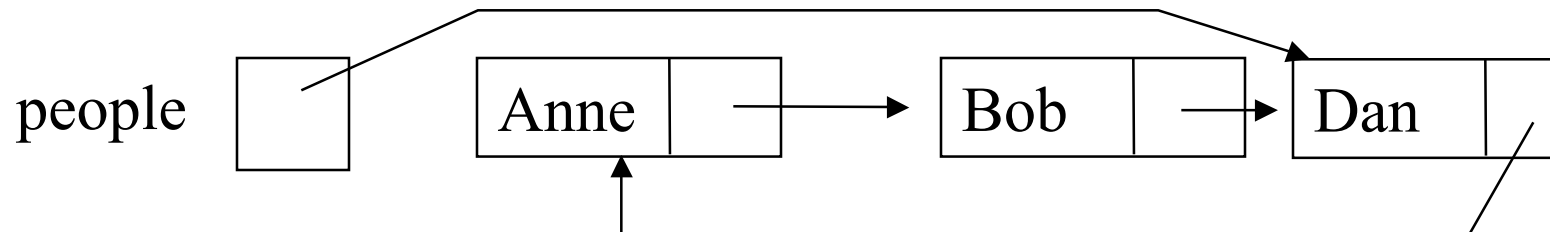
- **Problem: Cost to Access Tail**



- **Solution: point to tail, not head**

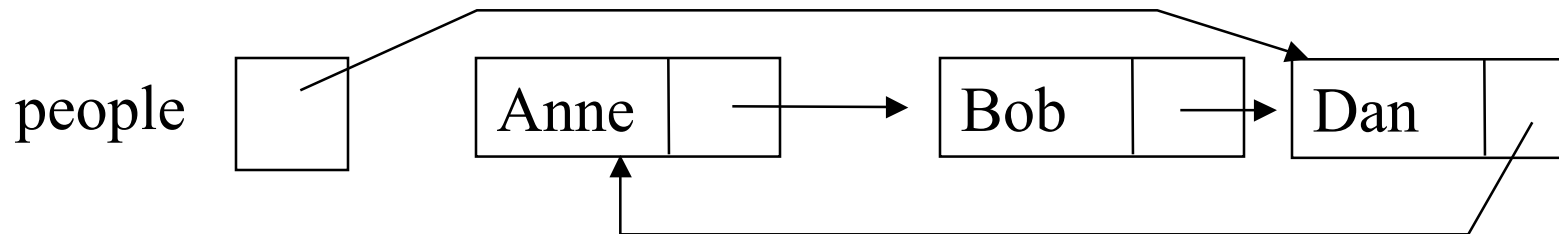


- **Problem: access to head. Solution:**



Circular List

- **First node is people.next**
- **Variable place points at last node when `place == people`**



Insert at Head

```
if(people == null){  
    people = new Node(newName, null);  
    people.next = people;  
} else {  
    Node newNode= new Node(newName,  
                             people.next);  
    people.next = newNode;  
}
```

Delete Head

- For circular lists

```
if (people == null){  
} else if (people == people.next){  
    people = null;  
} else {  
    people.next = people.next.next;  
}
```


Other CLL Methods

- **See resources => Java examples => fancy lists**

DLL Methods

- **See resources \Rightarrow Java examples \Rightarrow fancy lists**

Dummy Headers

- **Problem:** delete head is different that delete elsewhere in list
 - Change pointer to list as a whole vs change the next field of some node
- **Solution:** Keep an extra “dummy” node at the head of the list

Iterators

- **Abstract data type: a container**
 - **E.g. array or linked list**
 - **Can do mostly the same things with them, main difference is cost**
 - **Problem: one of the things I want to do is go through the data items one by one**

Processing Data Items

- **Normal way to handle same-process-different-structure problem is with a method that is defined appropriately for each class**
 - Same name and abstract behavior
 - Different code
- **But what would be the interface?**
 - What changes from call to call? Pieces of program 😞

Solution

- **Instead of a method to do whole loop, have methods you can use to build the loop**
 - **hasNext**
 - **getNext**
- **State: an object**
 - **Represents a particular instance of iteration**
 - **Initialized by new**

Abstract List Traversal

- **while (list.hasNext()) {
 print(list.getNext().data);
}**
- **list could be an Array:**
 hasNext() { return (i != list.length) }
 getNext() { i++; return list[i]; }

Abstract List Traversal

- **while (list.hasNext()) {
 print(list.getNext().data);
}**
- **list could be a LinkedList:**
 hasNext() { return (curr != null) }
 getNext() { curr = curr.next;
 return curr; }

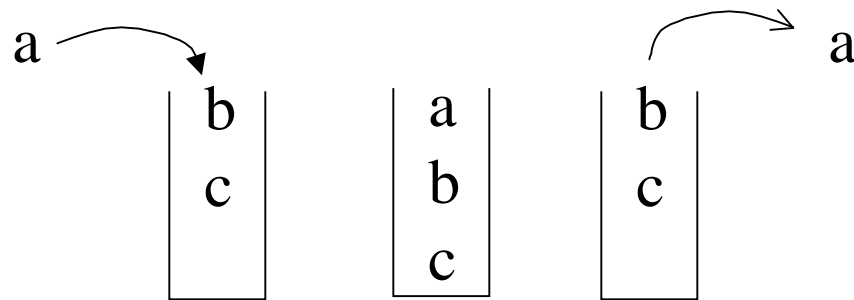
Iterators

- **See `StringList.java` and `StringListIterator.java`**

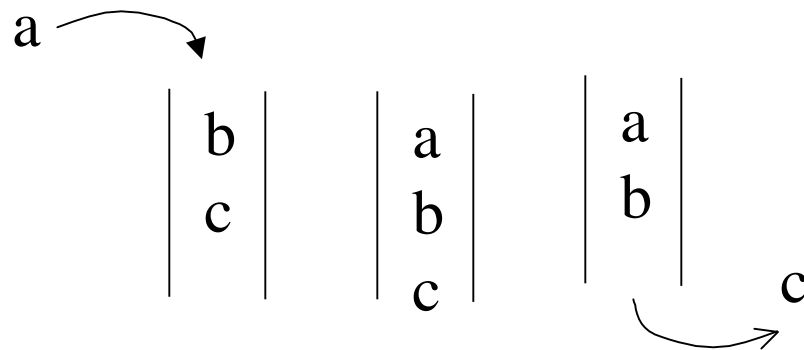
Stacks & Queues

Stacks & Queues

- **Last in first out: Stack**



- **First in first out: Queue**



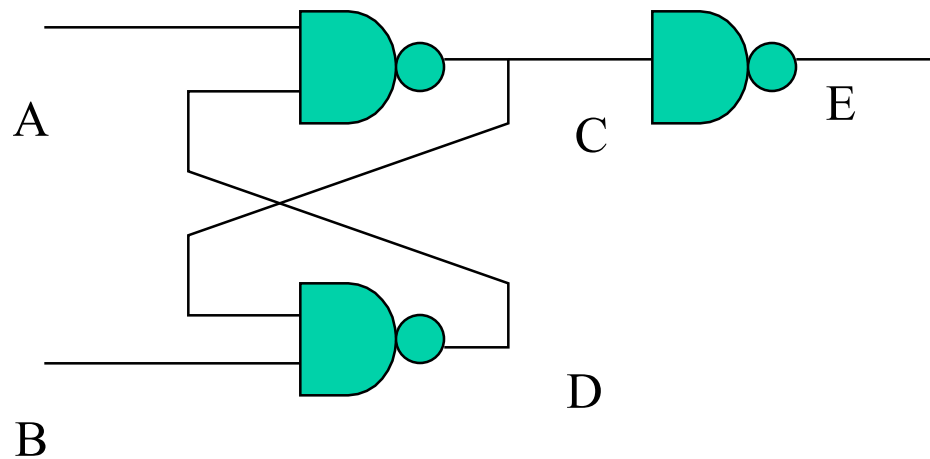
Operations

- **Queue**
 - enqueue, dequeue
 - isEmpty, size
 - clear, remove, removeAll
 - first, next (Enumerator would be better.)
- **Stack**
 - same but enqueue, dequeue called push, pop

Uses of Queues

- **Printer queue**
- **Simulation of real world queues**
 - **Queue in simulator models line of students.**
- **More generally, waiting lists when processing one item creates two more items to process**
 - **E.g. simulator**
 - **E.g. family tree**

Circuit Simulator



Initial state:

A,B,E = 0

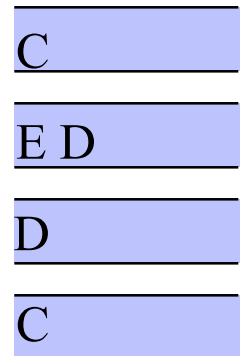
C,D = 1

Change at A => change at C

Change at C => changes at E, D

Change at E => no effect

Change at D => change at C



Invocation Record

- **Each procedure / method call needs to record values of**
 - **Parameters**
 - **Local variables**
 - **Other things**
- **When a procedure starts, space allocated for “invocation record” to store these things.**
- **Invocation record is kept until invocation exits**
- **Behavior is LIFO**

Stack of Invocation Records

Proc foo(int a)

... int b, c;

... fie(b);

... fie(c);

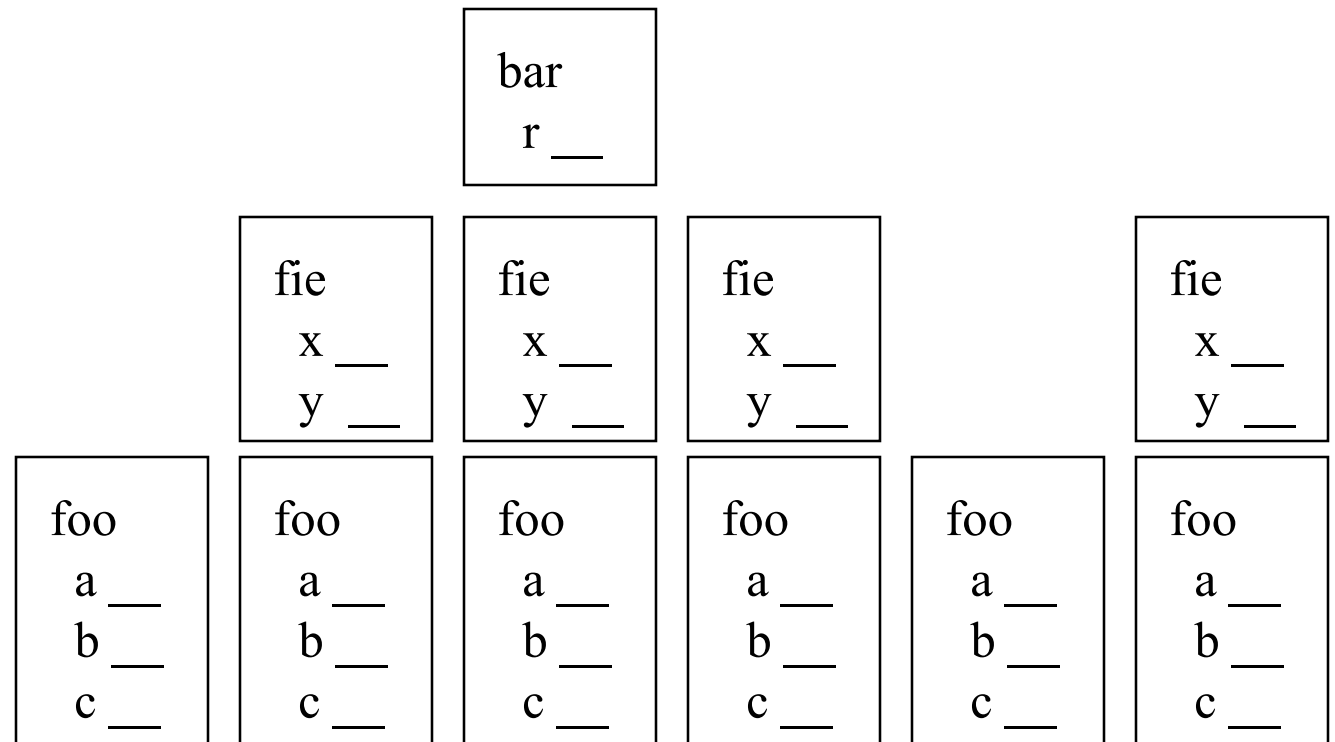
Proc fie(int x)

...int y;

...bar(y);

Proc bar(int r)

...

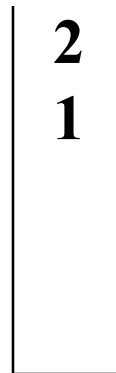


Uses of stacks

- **Postfix (RPN) calculator**
 - **Permits any expression to be evaluated**
 - **Does not require parentheses**

$((1 + 2) * (3 + 4)) / 7$

1 2 + 3 4 + * 7 /

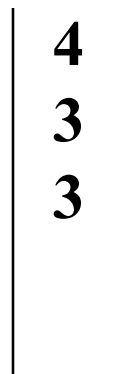


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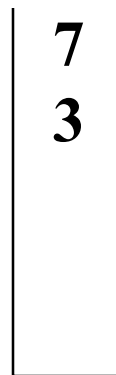


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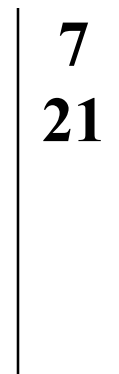
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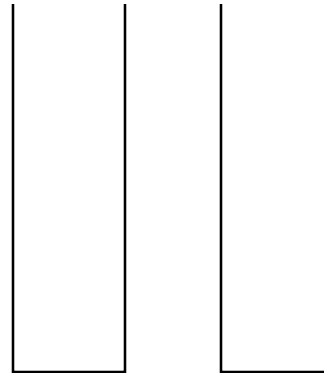


Uses of stacks

- **Interpret infix-with-precedence**
 - **Each operator has a numeric precedence**
 $+ 10, * 20, > 5, < 5$
 - **Two stacks: operators, operands**
 - **scan expression:**
 - **operand: push**
 - **operator:**
 - **if operator stack empty or**
precedence of op in string > precedence of top of stack, push
 - **else: pop operator , pop operands, push result**
- **e.g. $1 + 2 * 3 > 4 * 5$**

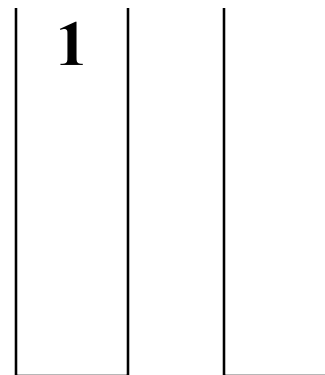
Uses of stacks

- operand: push
- operator:
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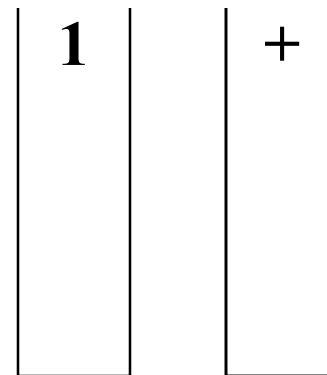
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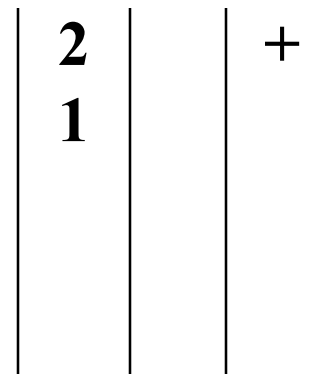
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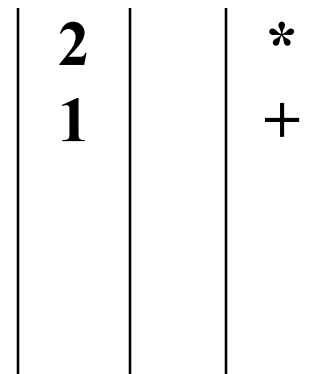
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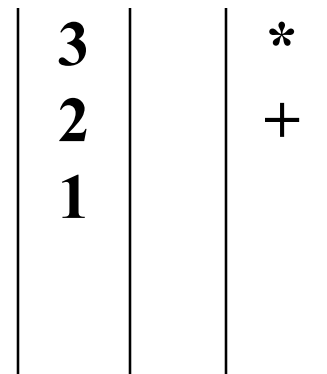
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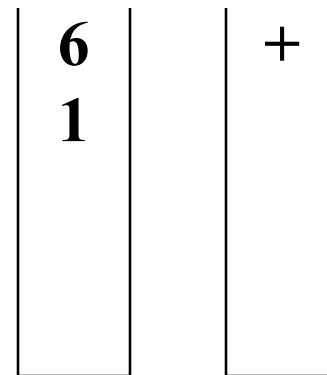
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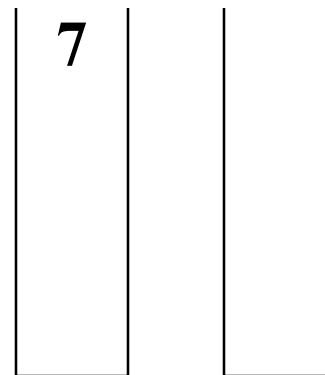
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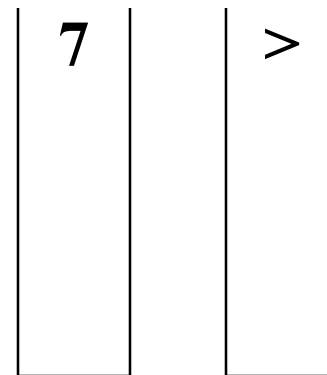
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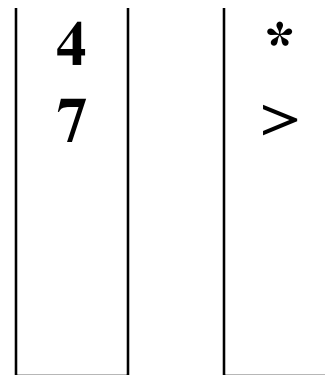
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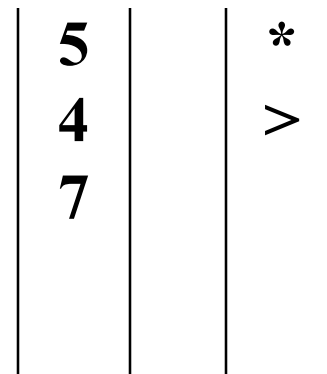
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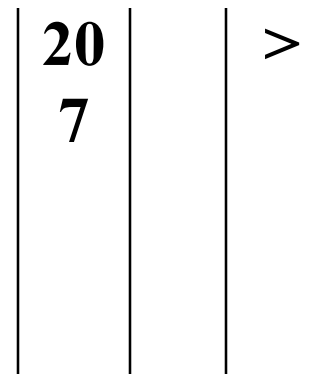
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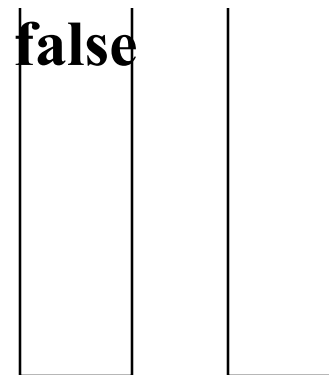
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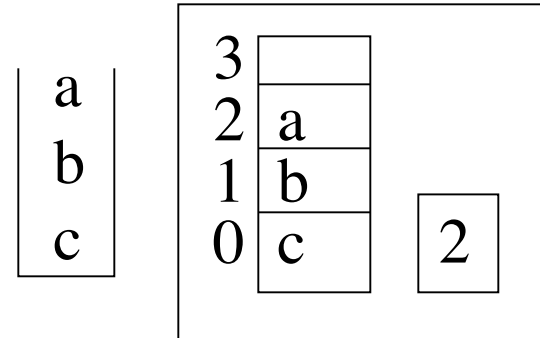
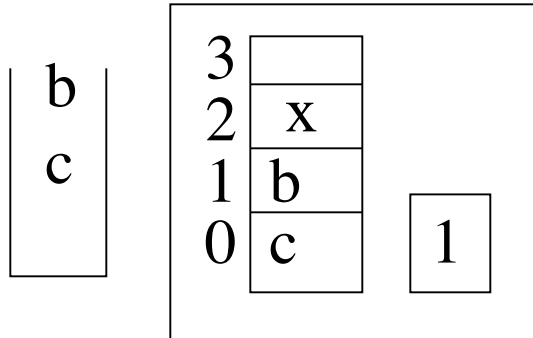
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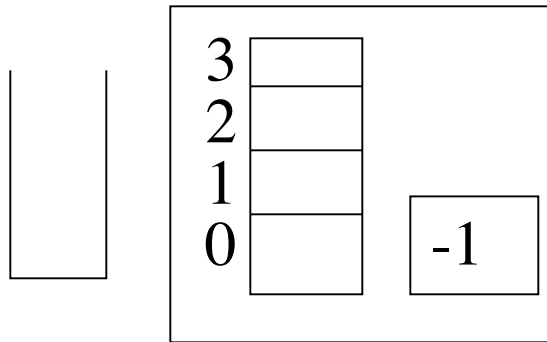
Implementing Stacks

- **Stacks can be implemented using**
 - **Arrays**
 - **Linked lists**
- **Arrays:**
 - **Array holds data, also need int “top of stack”**

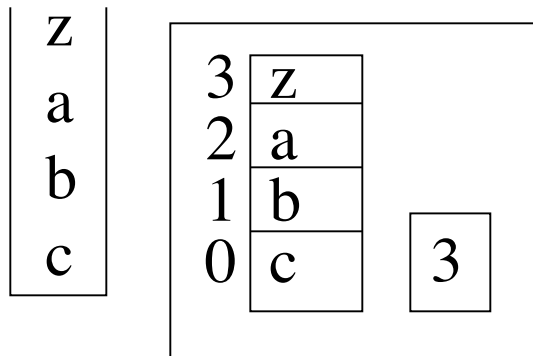


Implementing Stacks

- **Empty stack: $\text{top} == -1$**

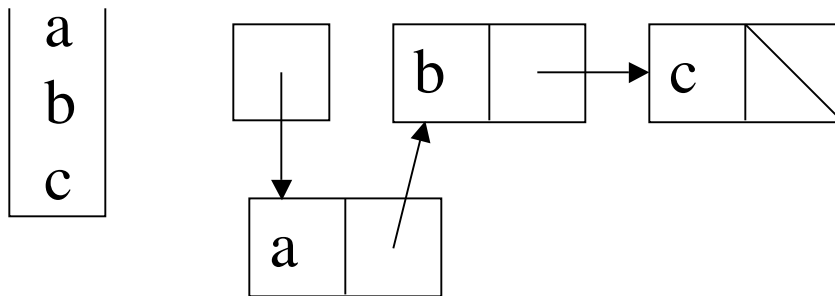
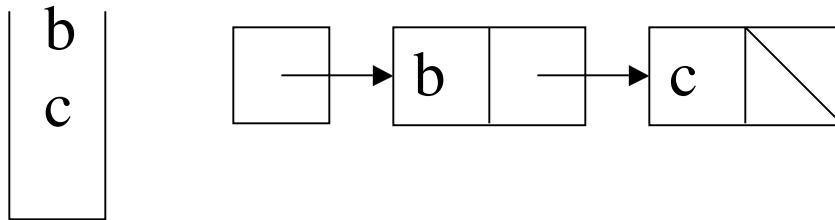


- **Full stack: $\text{top} == \text{array size} - 1$**



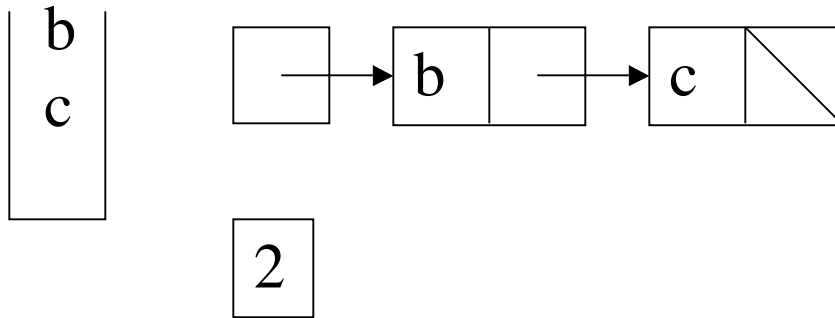
Stacks as linked lists

- **Linked lists are easy to manipulate at head -> natural representation for stacks**



Stacks as linked lists

- Only operation that is not fast is size
- So also have an int

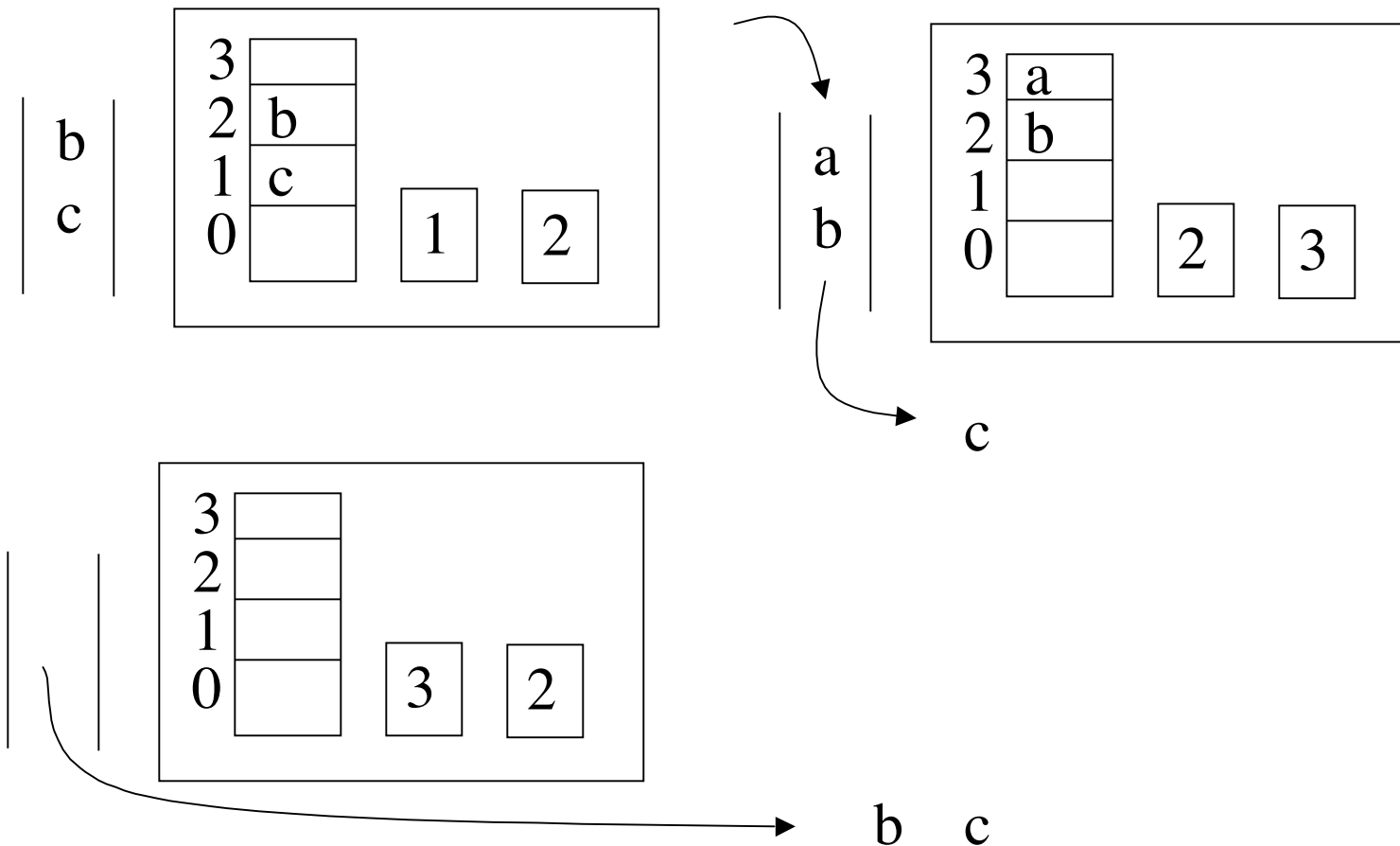


Implementing Queues

- **Queues need to be accessed at both ends, so implementations are a bit messier**
 - **Arrays: need two ints to keep track of both front and back**
 - **linked lists: use circular lists or have two pointers**

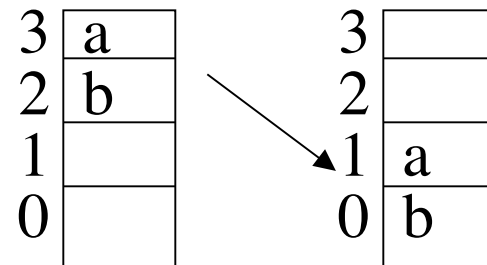
Queues as arrays

- Keep track of both front & rear

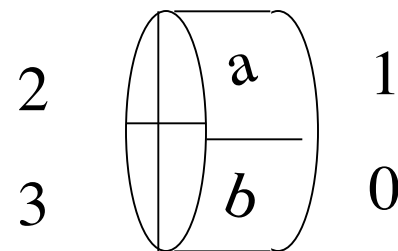


Queues as arrays

- **Problem: how to reuse space emptied by dequeue?**
 - **Could move data down**



- **Treat array as circular**
 $\text{front} = (\text{front} + 1) \% \text{size}$



Queues as linked lists

- **Problem:** Need to access both ends
- **Solution:** Linked list with head/tail pointer
- **Which end of the list should be the front of the queue?**
 - enqueue is $O(1)$ time whether at head or tail
 - dequeue is $O(1)$ at head but $O(n)$ at tail
(Why? Need pointer to second to last.)
 - so more efficient when front is head