

# Assignment-1

EE:1205 Signals and Systems  
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## I. QUESTION 11.14.8

A spring balance has a scale that reads from 0 to 50 kg. The length of the scale is 20 cm. A body is suspended from this balance, when displaced and released, oscillates with a period of 0.6 s. What is weight of the body?

## II. SOLUTION

TABLE 0  
INPUT PARAMETERS

Parameter	Value
Mass ( $M$ )	50 kg
Maximum displacement of the spring ( $l$ )	0.2 m
Time period ( $T$ )	0.6 s

The maximum mass that the scale can read is given by:

$$M = 50 \text{ kg} \quad (1)$$

The maximum displacement of the spring is equal to the length of the scale, given by:

$$l = 20 \text{ cm} = 0.2 \text{ m} \quad (2)$$

The time period is given as:

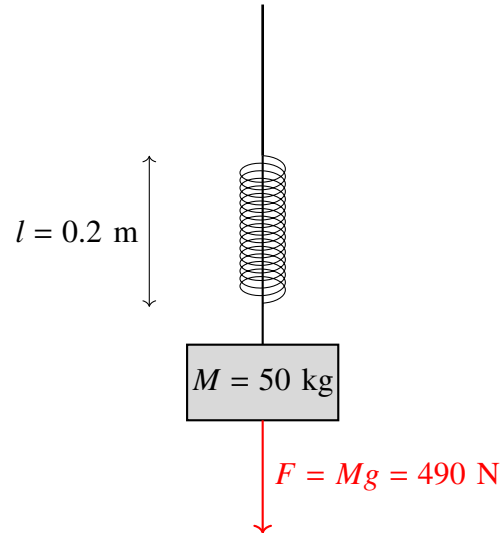
$$T = 0.6 \text{ s} \quad (3)$$

The maximum force exerted on the spring is calculated using:

$$F = Mg \quad (4)$$

where  $g$  is the acceleration due to gravity ( $9.8 \text{ m/s}^2$ ):

$$F = 50 \times 9.8 = 490 \text{ N} \quad (5)$$



The spring constant,  $k$ , is calculated as:

$$k = \frac{F}{l} = \frac{490}{0.2} = 2450 \text{ N/m}^{-1} \quad (6)$$

The time period,  $t$ , for mass  $m$  suspended from the balance is given by:

$$t = 2\pi \sqrt{\frac{m}{k}} \quad (7)$$

Hence, solving for  $m$ :

$$m = \left(\frac{T}{2\pi}\right)^2 \times k = \left(\frac{0.6}{2 \times 3.14}\right)^2 \times 2450 = 22.36 \text{ kg} \quad (8)$$

The weight of the body is defined as:

$$\text{Weight} = mg = 22.36 \times 9.8 = 219.16 \text{ N} \quad (9)$$

Therefore, the weight of the body is approximately 219 N.

Starting with Newton's second law of motion ( $F = ma$ ) and Hooke's law ( $F = -kx$ ) for the mass attached to a spring:

Newton's second law:  $F = ma$  and Hooke's law:  $F = -kx$   
(10)

Given values:

$$m = 50 \text{ kg}$$

$$k = 2450 \text{ N/m}$$

Equating these forces, where  $m$  is the mass,  $a$  is the acceleration,  $k$  is the spring constant, and  $x$  is the displacement from the equilibrium position:

$$ma = -kx \quad (11)$$

Here,  $a$  represents the second derivative of displacement with respect to time, denoted as  $\frac{d^2x}{dt^2}$ .

Therefore, substituting  $a = \frac{d^2x}{dt^2}$  into the equation  $ma = -kx$ , we get the differential equation governing the motion of the mass on the spring:

$$50 \frac{d^2x}{dt^2} + 2450x = 0 \quad (12)$$

This equation describes the simple harmonic motion of the mass attached to the spring with the given mass and spring constant values.