

EC 32

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QUESTION: A Simple closed path C in the Complex Plane is shown in the figure.

$$\oint_C \frac{2^z}{z^2 - 1} dz = -j\pi A$$

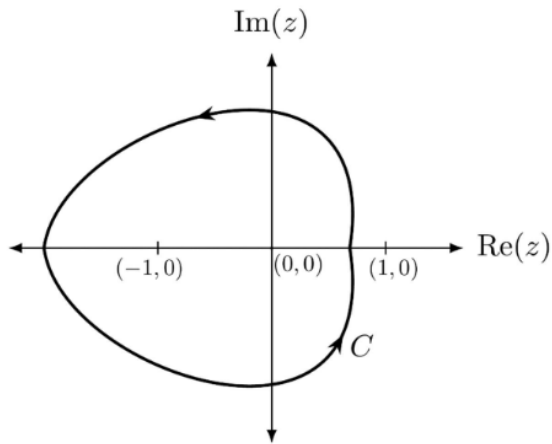
Where $j = \sqrt{-1}$, Then find the value of A is _____(Rounded of to two decimals) (GATE 2022)

By comparing

$$= 2\pi j \left(\frac{-1}{4} \right) \quad (5)$$

$$= -\pi j \left(\frac{1}{2} \right) \quad (6)$$

$$A = \frac{1}{2} = 0.50 \quad (7)$$



EC)

Solution:

Let

$$f(z) = \frac{2^z}{z^2 - 1}$$

For poles

$$z^2 - 1 = 0 \quad (1)$$

$$\Rightarrow z = \pm 1 \quad (2)$$

As $Z = -1$ lies inside the C and $z = 1$ lies outside C

$$\oint_C f(z) dz = \oint_C \frac{2^z}{z+1} dz \quad (3)$$

$$= 2\pi j \left(\frac{2^z}{z-1} \right) \text{ At } z = -1 \quad (4)$$

(By Cauchy's integral formula)