

# GATE 2023 EC

EE23BTECH11023-ABHIGNYA GOGULA

## Question28:

The Fourier transform  $X(\omega)$  of  $x(t) = e^{-t^2}$  is

Note:  $\int_{-\infty}^{\infty} e^{-y^2} dy = \sqrt{\pi}$

A)  $\sqrt{\pi} e^{\frac{\omega^2}{2}}$

B)  $\frac{e^{-\frac{\omega^2}{4}}}{2\sqrt{\pi}}$

C)  $\sqrt{\pi} e^{-\frac{\omega^2}{4}}$

D)  $\sqrt{\pi} e^{-\frac{\omega^2}{2}}$

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## Solution

$$x'(t) = -2te^{-t^2} \quad (1)$$

$$x'(t) = -2tx(t) \quad (2)$$

doing fourier transform

$$j2\pi f X(f) = -2j \frac{dX(f)}{df} \quad (3)$$

$$\int_0^f \frac{dX(f)}{X(f)} = \int_0^f \frac{2\pi f df}{-2} \quad (4)$$

$$\frac{X(f)}{X(0)} = e^{\frac{-(2\pi f)^2}{4}} \quad (5)$$

$$X(0) = \int_{-\infty}^{\infty} x(t) dt = \sqrt{\pi} \quad (6)$$

$$X(f) = \sqrt{\pi} e^{-\frac{(2\pi f)^2}{4}} \quad (7)$$

$$X(f) = \sqrt{\pi} e^{-\pi^2 f^2} \quad (8)$$

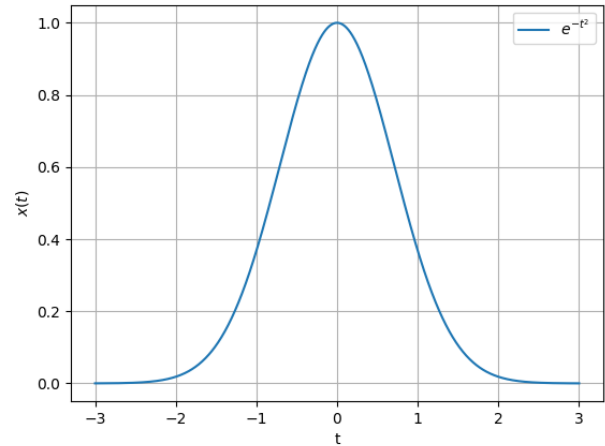


Fig. 0. Graph of  $e^{-t^2}$

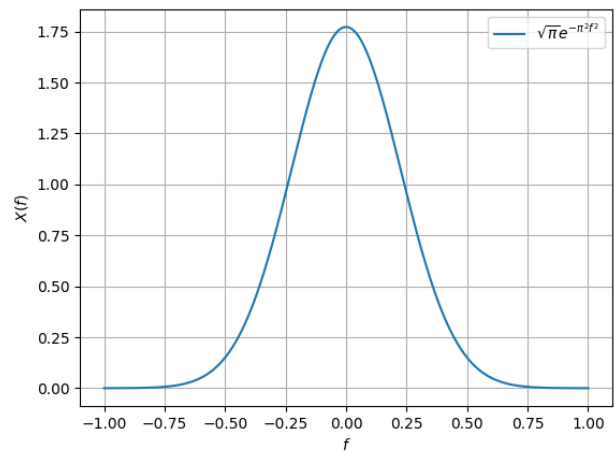


Fig. 0. Graph of  $X(f) = \sqrt{\pi} e^{-\pi^2 f^2}$