Find the value of each of the following:

ii 7<sup>3</sup>

*iii* 3<sup>4</sup>

#### Solution:

We have

$$i 13^2 = 13 \times 13 = 169$$

$$ii 7^3 = 7 \times 7 \times 7 = 343$$

$$iii 3^4 = 3 \times 3 \times 3 \times 3 = 81$$

#### Question:2

Find the value of each of the following:

$$i - 7^{2}$$

$$ii - 3^4$$

$$iii-5^5$$

# Solution:

We know that if 'a' is natural number, then

- $-a^{\text{even number}}$  = Positive number
- $-a^{\mathrm{odd\ number}}$  = Negative number

We have

$$i - 7^2 = -7 \times -7 = 49$$

$$ii - 3^4 = -3 \times -3 \times -3 \times -3 = 81$$

$$iii - 5^5 = -5 \times -5 \times -5 \times -5 \times -5 = -3125$$

#### Question:3

Simplify:

 $i \, 3 \times 10^2$ 

 $ii\,2^2\times5^3$ 

 $ii\,3^3\times5^2$ 

# Solution:

We have

$$i \ 3 \times 10^2 = 3 \times 100 = 300$$
 [since  $10^2 = 10 \times 10 = 100$ ]

$$ii \ 2^2 \times 5^3 = 4 \times 125 = 500$$
 [since  $2^2 = 2 \times 2 = 4$  and  $5^3 = 5 \times 5 \times 5 = 125$ ]

$$iii \, 3^3 \times 5^2 = 27 \times 25 = 675$$
 [since  $3^3 = 3 \times 3 \times 3 = 27$  and  $5^2 = 5 \times 5 = 25$ ]

#### Question:4

Simplify:

$$i \, 3^2 \times 10^4$$

$$ii 2^4 \times 3^2$$

$$ii$$
  $5^2 \times 3^4$ 

Solution: We have

$$i \, 3^2 \times 10^4 = 9 \times 10000 = 90000$$
 [since  $3^2 = 3 \times 3 = 9$  and  $10^4 = 10 \times 10 \times 10 \times 10 = 10000$ ]

$$ii \ 2^4 \times 3^2 = 16 \times 9 = 144$$
 [since  $2^4 = 2 \times 2 \times 2 \times 2 = 16$  and  $3^2 = 3 \times 3 = 9$ ]

$$iii \ 5^2 \times 3^4 = 25 \times 81 = 2025$$
 [since  $5^2 = 5 \times 5 = 25$  and  $3^4 = 3 \times 3 \times 3 \times 3 = 81$ ]

### Question:5

Simplify:

$$i - 2 \times -3^3$$

$$ii-3^2\times -5^3$$

$$iii-2^5 \times -10^2$$

# Solution:

We know that if 'a' is natural number, then

$$-a^{\text{even number}} = \text{Positive number}$$

$$-a^{\text{odd number}}$$
 = Negative number

We have

$$i-2\times -3^3=-2-27=54$$
 [since  $(-3)^3=-3\times -3\times -3=-27$ ]  $ii-3^2\times -5^3=9-125=-1125$  [since  $(-3)^2=-3\times -3=9$  and  $-5^3=-5\times -5\times -5=-125$ ]  $iii-2^5\times -10^2=-32\times 100=-3200$  [since  $(-2)^5=-2\times -2\times -2\times -2=-32$  and  $-10^2=-10\times -10=100$ ]

#### Question:6

Simplify:

$$i\left(\frac{3}{4}\right)^2$$

$$ii\left(\frac{-2}{3}\right)^4$$

$$iii\left(\frac{-4}{5}\right)^5$$

# Solution:

We have

$$\begin{split} i\left(\frac{3}{4}\right)^2 &= \ \frac{3}{4} \times \frac{3}{4} \ = \frac{9}{16} \\ ii\left(\frac{-2}{3}\right)^4 &= \ \frac{-2}{3} \times \frac{-2}{3} \times \frac{-2}{3} \times \frac{-2}{3} = \ \frac{16}{81} \\ iii\left(\frac{-4}{5}\right)^5 &= \ \frac{-4}{5} \times \frac{-4}{5} \times \frac{-4}{5} \times \frac{-4}{5} \times \frac{-4}{5} = \frac{-1024}{3125} \end{split}$$

#### Question:7

Identify the greater number in each of the following:

 $i 2^5 \text{ or } 5^2$ 

ii  $3^4$  or  $4^3$ 

 $iii 3^5$  or  $5^3$ 

#### Solution:

We have

$$i \ 2^5 = 2 \times 2 \times 2 \times 2 \times 2 = 32 \text{ and } 5^2 = 5 \times 5 = 25$$

Therefore, 32 > 25.

Thus,  $2^5 > 5^2$ .

$$ii \ 3^4 = 3 \times 3 \times 3 \times 3 = 81 \ \text{and} \ 4^3 = 4 \times 4 \times 4 = 64$$

Therefore, 81 > 64.

Thus,  $3^4 > 4^3$ .

$$iii\ 3^5 = 3 \times 3 \times 3 \times 3 \times 3 = 243$$
 and  $5^3 = 5 \times 5 \times 5 = 125$ 

Therefore, 243 > 125.

Thus,  $3^5 > 5^3$ .

#### Question:8

Express each of the following in exponential form:

$$i$$
 (-5) × -5 × -5

$$ii\frac{-5}{2}\times\frac{-5}{2}\times\frac{-5}{2}\times\frac{-5}{2}$$

$$\begin{array}{c} ii \ \frac{-5}{7} \times \frac{-5}{7} \times \frac{-5}{7} \times \frac{-5}{7} \\ iii \ \frac{4}{3} \times \frac{4}{3} \times \ \frac{4}{3} \times \ \frac{4}{3} \times \ \frac{4}{3} \end{array}$$

#### Solution:

We have

$$i - 5 \times - 5 \times - 5 = -5^3$$

$$iirac{-5}{7} imesrac{-5}{7} imesrac{-5}{7} imesrac{-5}{7}=\left(rac{-5}{7}
ight)^4$$

$$iii \frac{4}{3} \times \frac{4}{3} \times \frac{4}{3} \times \frac{4}{3} \times \frac{4}{3} = \left(\frac{4}{3}\right)^5$$

#### Question:9

Express each of the following in exponential form:

$$ii$$
 (-2) × -2 × -2 × -2 × a × a × a

$$iii\left(rac{-2}{3}
ight) imes\left(rac{-2}{3}
ight) imes x imes x imes x$$

#### Solution:

We have

$$\begin{array}{l} i\;x\times\;x\times\;x\;\times\;x\;\times\;a\;\times a\;\times b\times b\times b=x^4a^2b^3\\ ii\;(-2)\;\times(-2)\;\times(-2)\;\times(-2)\;\times a\;\times a\;\times a=\left(-2\right)^4\times a^3\\ iii\;\left(\frac{-2}{3}\right)\times\left(\frac{-2}{3}\right)\times\;x\times\;x\times\;x=\;\left(\frac{-2}{3}\right)^2\times x^3 \end{array}$$

#### Question:10

Express each of the following numbers in exponential form:

i 512

ii 625

iii 729

# Solution:

We have

i Prime factorisation of 512 = 2 x 2 x 2 x 2 x 2 x 2 x 2 x 2 x 2 =  $2^9$ 

ii Prime factorisation of 625 = 5 x 5 x 5 x 5 =  $5^4$ 

iii Prime factorisation of 729 = 3 x 3 x 3 x 3 x 3 x 3 = 3<sup>6</sup>

#### Question:11

Express each of the following numbers as a product of powers of their prime factors:

i 36

*ii* 675

iii 392

#### Solution:

We have

i Prime factorisation of 36 =  $2 \times 2 \times 3 \times 3 = 2^2 \times 3^2$ 

ii Prime factorisation of 675 = 3 x 3 x 3 x 5 x 5 =  $3^3$  x  $5^2$ 

iii Prime factorisation of 392 = 2 x 2 x 2 x 7 x 7 =  $2^3$  x  $7^2$ 

# Question:12

Express each of the following numbers as a product of powers of their prime factors:

i 450

ii 2800

iii 24000

#### Solution:

We have

*i* Prime factorisation of  $450 = 2 \times 3 \times 3 \times 5 \times 5 = 2 \times 3^2 \times 5^2$ 

ii Prime factorisation of 2800 = 2 x 2 x 2 x 2 x 5 x 5 x 7 =  $2^4$  x  $5^2$  x 7

iii Prime factorisation of 24000 = 2 x 2 x 2 x 2 x 2 x 2 x 3 x 5 x 5 x 5 =  $2^6$  x 3 x  $5^3$ 

# Question:13

Express each of the following as a rational number of the form  $\frac{p}{a}$ :

$$i\left(\frac{3}{7}\right)^2$$

$$ii\left(\frac{7}{9}\right)^3$$

$$iii\left(\frac{-2}{3}\right)^4$$

# Solution:

$$\begin{split} i\left(\frac{3}{7}\right)^2 &= \frac{3}{7} \times \frac{3}{7} = \frac{9}{49} \\ ii\left(\frac{7}{9}\right)^3 &= \frac{7}{9} \times \frac{7}{9} \times \frac{7}{9} = \frac{343}{729} \end{split}$$

$$iii\left(\frac{-2}{3}\right)^4 = \frac{-2}{3} \times \frac{-2}{3} \times \frac{-2}{3} \times \frac{-2}{3} = \frac{16}{81}$$

Express each of the following rational numbers in power notation:

$$i_{\frac{49}{64}}$$

$$ii - \frac{64}{125} \\ iii - \frac{1}{216}$$

$$iii - \frac{1}{216}$$

Solution:

$$i \frac{49}{64} = \frac{7}{8} \times \frac{7}{8} = \frac{(7)^2}{(8)^2} = \left(\frac{7}{8}\right)^2$$

$$ii - \frac{64}{125} = -\frac{4}{5} \times -\frac{4}{5} \times -\frac{4}{5} = -\frac{(4)^3}{(5)^3} = \left(-\frac{4}{5}\right)^3$$

$$iii - \frac{1}{216} = \frac{-1}{6} \times \frac{-1}{6} \times \frac{-1}{6} = \frac{(-1)^3}{(6)^3} = \left(\frac{-1}{6}\right)^3$$

$$iii - \frac{1}{216} = \frac{-1}{6} \times \frac{-1}{6} \times \frac{-1}{6} = \frac{\left(-1\right)^3}{\left(6\right)^3} = \left(\frac{-1}{6}\right)^3$$

#### Question:15

Find the value of each of the following:

$$i\left(\frac{-1}{2}\right)^2 \times 2^3 \times \left(\frac{3}{4}\right)^2$$

$$ii\left(\frac{-3}{5}\right)^4 \times \left(\frac{4}{9}\right)^4 \times \left(\frac{-15}{18}\right)^2$$

#### Solution:

We have

$$i \left(\frac{-1}{2}\right)^2 \times 2^3 \times \left(\frac{3}{4}\right)^2 = \frac{1}{4} \times 8 \times \frac{9}{16} = \frac{1}{4} \times \frac{9}{2} = \frac{9}{8} \qquad \left[\text{Since } \left(\frac{-1}{2}\right)^2 \ = \ \frac{1}{4} \,, \ 2^3 \ = \ 8 \ \text{and} \ \left(\frac{3}{4}\right)^2 \ = \frac{9}{16}\right]$$

$$\frac{ii}{\left(\frac{-3}{5}\right)^4 \times \left(\frac{4}{9}\right)^4 \times \left(\frac{-15}{18}\right)^2} = \frac{\left(-3\right)^4}{5^4} \times \frac{4^4}{9^4} \times \left(\frac{-3 \times 5}{2 \times 9}\right)^2 = \frac{\left(-3\right)^4}{5^4} \times \frac{4^4}{9^2 \times 9^2} \times \left(\frac{-3 \times 5}{2 \times 9}\right)^2 = \frac{81}{5^4} \times \frac{4^4}{81 \times 9^2} \times \frac{\left(-3\right)^2 \times 5^2}{2^2 \times 9^2} = \frac{1}{5^4} \times \frac{4^4}{9^2} \times \frac{\left(-3\right)^2 \times 5^2}{2^2 \times 9^2} = \frac{1}{5^4} \times \frac{4^4}{9^2} \times \frac{9 \times 5^2}{4 \times 9^2} = \frac{1}{5^2} \times \frac{4^3}{9^2} \times \frac{1}{9} = \frac{1}{5^2} \times \frac{4^3}{9^2} \times \frac{1}{9^2} \times \frac$$

#### Question:16

If a = 2 and b = 3, then find the values of each of the following:

$$i(a+b)^a$$

$$iii\left(\frac{b}{a}\right)^b$$

$$iv\left(\frac{a}{b} + \frac{b}{a}\right)^a$$

We have a = 2 and b = 3.

$$i(a+b)^a = 2+3^2=5^2=25$$

$$ii (ab)^b = 2x3^3 = 6^3 = 216$$

$$iii\left(\frac{b}{a}\right)^b = \left(\frac{3}{2}\right)^3 = \frac{3}{2} \times \frac{3}{2} \times \frac{3}{2} = \frac{27}{8}$$

$$iv\left(\frac{a}{b} + \frac{b}{a}\right)^a = \left(\frac{2}{3} + \frac{3}{2}\right)^2 = \left(\frac{4+9}{6}\right)^2 = \left(\frac{13}{6}\right)^2 = \frac{169}{36}$$

# Question:17

Using laws of exponents, simplify and write the answer in exponential form:

$$i \ 2^3 \times 2^4 \times 2^5$$

$$ii \, 5^{12} \div 5^3$$

$$iii~(7^2)^3$$

$$iv (3^2)^5 \div 3^4$$

$$v 3^7 \times 2^7$$

$$vi~(5^{21} \div 5^{13}) \times 5^7$$

# Solution:

$$i \ 2^3 \times 2^4 \times 2^5 = 2^{3+4+5} = 2^{12}$$
 [since  $a^m + a^n + a^p = a^{m+n+p}$ ]

$$\begin{array}{ll} ii \ 5^{12} \div 5^3 = \frac{5^{12}}{5^3} = 5^{12 - 3} = 5^9 & \qquad [ \text{ since } \mathbf{a}^{\mathbf{m}} \div \mathbf{a}^{\mathbf{n}} = \mathbf{a}^{\mathbf{m} \cdot \mathbf{n}} ] \\ iii \ (7^2)^3 = 7^6 & \qquad [ \text{ since } (\mathbf{a}^{\mathbf{m}})^{\mathbf{n}} = \mathbf{a}^{\mathbf{m} \cdot \mathbf{n}} ] \\ iv (3^2)^5 \div 3^4 = 3^{10} \div 3^4 & \qquad [ \text{ since } (\mathbf{a}^{\mathbf{m}})^{\mathbf{n}} = \mathbf{a}^{\mathbf{m} \cdot \mathbf{n}} ] \\ = 3^{10 - 4} = 3^6 & \qquad [ \text{ since } \mathbf{a}^{\mathbf{m}} \div \mathbf{a}^{\mathbf{n}} = \mathbf{a}^{\mathbf{m} \cdot \mathbf{n}} ] \\ v \ 3^7 \times 2^7 = 3x2^7 = 6^7 & \qquad [ \text{ since } \mathbf{a}^{\mathbf{m}} \times \mathbf{b}^{\mathbf{m}} = \mathbf{a}xb^{\mathbf{m}} ] \\ vi \ (5^{21} \div 5^{13}) \times 5^7 = 5^{21 - 13} \times 5^7 & \qquad [ \text{ since } \mathbf{a}^{\mathbf{m}} \div \mathbf{a}^{\mathbf{n}} = \mathbf{a}^{\mathbf{m} \cdot \mathbf{n}} ] \\ = 5^8 \times 5^7 & \qquad [ \text{ since } \mathbf{a}^{\mathbf{m}} \times \mathbf{b}^{\mathbf{n}} = \mathbf{a}^{\mathbf{m} \cdot \mathbf{n}} ] \\ = 5^8 \times 5^7 & \qquad [ \text{ since } \mathbf{a}^{\mathbf{m}} \times \mathbf{b}^{\mathbf{n}} = \mathbf{a}^{\mathbf{m} \cdot \mathbf{n}} ] \\ = 5^8 \times 5^7 & \qquad [ \text{ since } \mathbf{a}^{\mathbf{m}} \times \mathbf{b}^{\mathbf{n}} = \mathbf{a}^{\mathbf{m} \cdot \mathbf{n}} ] \\ = 5^8 \times 5^7 & \qquad [ \text{ since } \mathbf{a}^{\mathbf{m}} \times \mathbf{b}^{\mathbf{n}} = \mathbf{a}^{\mathbf{m} \cdot \mathbf{n}} ] \\ = 5^8 \times 5^7 & \qquad [ \text{ since } \mathbf{a}^{\mathbf{m}} \times \mathbf{b}^{\mathbf{n}} = \mathbf{a}^{\mathbf{m} \cdot \mathbf{n}} ] \\ = 5^8 \times 5^7 & \qquad [ \text{ since } \mathbf{a}^{\mathbf{m}} \times \mathbf{b}^{\mathbf{n}} = \mathbf{a}^{\mathbf{m} \cdot \mathbf{n}} ] \\ = 5^8 \times 5^7 & \qquad [ \text{ since } \mathbf{a}^{\mathbf{m}} \times \mathbf{b}^{\mathbf{n}} = \mathbf{a}^{\mathbf{m} \cdot \mathbf{n}} ] \\ = 5^8 \times 5^7 & \qquad [ \text{ since } \mathbf{a}^{\mathbf{m}} \times \mathbf{b}^{\mathbf{n}} = \mathbf{a}^{\mathbf{m} \cdot \mathbf{n}} ] \\ = 5^8 \times 5^7 & \qquad [ \text{ since } \mathbf{a}^{\mathbf{m}} \times \mathbf{b}^{\mathbf{n}} = \mathbf{a}^{\mathbf{m} \cdot \mathbf{n}} ] \\ = 5^8 \times 5^7 & \qquad [ \text{ since } \mathbf{a}^{\mathbf{m}} \times \mathbf{b}^{\mathbf{n}} = \mathbf{a}^{\mathbf{m} \cdot \mathbf{n}} ] \\ = 5^8 \times 5^7 & \qquad [ \text{ since } \mathbf{a}^{\mathbf{m}} \times \mathbf{b}^{\mathbf{n}} = \mathbf{a}^{\mathbf{m} \cdot \mathbf{n}} ] \\ = 5^8 \times 5^7 & \qquad [ \text{ since } \mathbf{a}^{\mathbf{m}} \times \mathbf{b}^{\mathbf{n}} = \mathbf{a}^{\mathbf{m} \cdot \mathbf{n}} ] \\ = 5^8 \times 5^7 & \qquad [ \text{ since } \mathbf{a}^{\mathbf{m}} \times \mathbf{b}^{\mathbf{n}} = \mathbf{a}^{\mathbf{m} \cdot \mathbf{n}} ] \\ = 5^8 \times 5^7 & \qquad [ \text{ since } \mathbf{a}^{\mathbf{m}} \times \mathbf{b}^{\mathbf{n}} = \mathbf{a}^{\mathbf{m} \cdot \mathbf{n}} ] \\ = 5^8 \times 5^7 & \qquad [ \text{ since } \mathbf{a}^{\mathbf{m}} \times \mathbf{b}^{\mathbf{n}} = \mathbf{a}^{\mathbf{m} \cdot \mathbf{n}} ] \\ = 5^8 \times 5^7 & \qquad [ \text{ since } \mathbf{a}^{\mathbf{m}} \times \mathbf{b}^{\mathbf{n}} = \mathbf{a}^{\mathbf{m} \cdot \mathbf{n}} ] \\ = 5^8 \times 5^7 & \qquad [ \text{ since } \mathbf{a}^{\mathbf{m}} \times \mathbf{b}^{\mathbf{n}} = \mathbf{a}^{\mathbf{m} \cdot \mathbf{n}} ] \\ = 5^8 \times 5^7 & \qquad [ \text{ since } \mathbf{a}^{\mathbf{m}} \times \mathbf{b}^{\mathbf{n}} = \mathbf{a}^{\mathbf{m} \cdot \mathbf{n}} ] \\ = 5$$

Simplify and express each of the following in exponential form:

$$\begin{split} i\left\{ \left(2^{3}\right)^{4} \times 2^{8} \right\} & \div 2^{12} \\ ii\left(8^{2} \times 8^{4}\right) & \div 8^{3} \\ iii\left(\frac{5^{7}}{5^{2}}\right) \times 5^{3} \\ iv\left.\frac{5^{4} \times x^{10} y^{5}}{5^{4} \times x^{7} y^{4}}\right. \end{split}$$

$$iv \frac{5^4 \times x^{10}y^5}{5^4 \times x^7 u^4}$$

# Solution:

We have

$$i \{(2^3)^4 \times 2^8\} \div 2^{12}$$

$$= \{2^{12} \times 2^8\} \div 2^{12}$$

$$= 2^{12} + 8 \div 2^{12}$$

$$= 2^{20} \div 2^{12}$$

$$= 2^{20} - 1^2 = 2^8$$

$$ii (8^2 \times 8^4) \div 8^3$$

$$= 8^2 + ^4 \div 8^3$$

$$= 8^6 \div 8^3$$

$$= 8^6 - ^3 = 8^3 = (2^3)^3 = 2^9$$

$$iii \left(\frac{5^7}{5^2}\right) \times 5^3 = 5^7 - 2 \times 5^3$$
  
=  $5^5 \times 5^3$   
=  $5^5 + 3 = 5^8$ 

$$\begin{split} iv \ &\frac{5^4 \times x^{10} y^5}{5^4 \times x^7 y^4} = 5^{\left(4-4\right)} \times x^{\left(10-7\right)} \times y^{\left(5-4\right)} \\ &= 5^0 \times x^3 \times y \\ &= 1 \times x^3 y = x^3 y \end{split} \text{ [since 5}^0 = 1\text{]}$$

Simplify and express each of the following in exponential form:

$$\begin{split} i\left\{\left(3^2\right)^3 \times 2^6\right\} \times 5^6 \\ ii\left(\frac{x}{y}\right)^{12} \times y^{24} \times \left(2^3\right)^4 \\ iii\left(\frac{5}{2}\right)^6 \times \left(\frac{5}{2}\right)^2 \\ iv\left(\frac{2}{3}\right)^5 \times \left(\frac{3}{5}\right)^5 \end{split}$$

# Solution:

$$i \ \{(3^2)^3 \times 2^6\} \times 5^6$$
  
=  $\{3^6 \times 2^6\} \times 5^6$  [since  $(a^m)^n = a^{mn}$ ]  
=  $6^6 \times 5^6$  [since  $a^m \times b^m = axb^m$ ]  
=  $30^6$ 

$$egin{aligned} ii \ \left(rac{x}{y}
ight)^{12} imes y^{24} imes \left(2^3
ight)^4 \ &= rac{x^{12}}{y^{12}} imes y^{24} imes 2^{12} \end{aligned}$$

$$\begin{array}{l} = x^{12} \times \frac{y^{24}}{y^{12}} \times 2^{12} \\ = x^{12} \times y^{24-12} \times 2^{12} \\ = x^{12} \times y^{12} \times 2^{12} \\ = (2xy)^{12} \left[ \text{since } a^m \times b^m \times c^m = (a \times b \times c)^m \right] \\ iii \\ \left( \frac{5}{2} \right)^6 \times \left( \frac{5}{2} \right)^2 \\ = \left( \frac{5}{2} \right)^8 \left[ \text{since } a^m \times a^n = a^{m+n} \right] \end{array}$$

$$egin{aligned} & iv \ \left(rac{2}{3}
ight)^5 imes \left(rac{3}{5}
ight)^5 \ &= \left(rac{2}{3} imes rac{3}{5}
ight)^5 \left[ ext{since } a^m imes b^m = \left(a imes b
ight)^m 
ight] \end{aligned}$$

Write  $9 \times 9 \times 9 \times 9$  in exponential form with base 3.

#### Solution:

We have

$$9 \times 9 \times 9 \times 9 \times 9 = 9^5 = (3^2)^5 = 3^{10}$$

#### Question:21

Simplify and write each of the following in exponential form:

i 
$$25^3 \div 5^3$$
  
ii  $81^5 \div (3^2)^5$ 

iii iv

# Solution:

We have

$$i 25^3 \div 5^3$$
  
=  $(5^2)^3 \div 5^3$ 

 $=5^6\div 5^3$ 

=

ii 
$$81^5 \div (3^2)^5$$

$$=(3^4)^5 \div (3^2)^5$$

$$= 3^{20} \div 3^{10}$$

\_

iii

$$^{16-12}$$
×  $(x)^{10-6} = 3^4$ ×  $x^4 = (3x)^4$ 

iv

# Question:22

Simplify:

i

ii

iii

iv

# Solution:

$$i (3^5)^{11} \times (3^{15})^{4} - (3^5)^{18} \times (3^5)^{5}$$
$$= 3^{55} \times 3^{60} - 3^{90} \times 3^{25}$$

```
= 3^{55+60} - 3^{90+25}
= 3^{115} - 3^{115}
= 0
ii
```

iii

iv

#### Question:23

Find the values of n in each of the following:

ii

iii iv

IV

Vİ

# Solution:

We have

$$5^{2n} \times 5^3 = 5^{11}$$
  
=  $5^{2n+3} = 5^{11}$ 

On equating the coefficients, we get

$$2n + 3 = 11$$

ii 
$$9 \times 3^n = 3^7$$

$$= 3^2 \times 3^n = 3^7$$

$$= 3^{2+n} = 3^7$$

On equating the coefficients, we get

$$2 + n = 7$$

$$\Rightarrow$$
 n = 7 - 2 = 5

iii 
$$8 \times 2^{n+2} = 32$$

$$= 2^3 \times 2^{n+2} = 2^5$$
 [since  $2^3 = 8$  and  $2^5 = 32$ ]

$$=2^{3+n+2}=2^5$$

On equating the coefficients, we get

$$3 + n + 2 = 5$$

$$\Rightarrow$$
 n + 5 = 5

$$\Rightarrow$$
 n = 5 -5

$$\Rightarrow$$
 n = 0

$$i \vee 7^{2n+1} \div 49 = 7^3$$

$$=7^{2n+1} \div 7^2 = 7^3$$
 [since  $49 = 7^2$ ]

 $=7^{2n-1}=7^3$ 

On equating the coefficients, we get

2n - 1 = 3

 $\Rightarrow$  2n = 3 + 1

⇒ 2n = 4

⇒ n =

. .

On equating the coefficients, we get

2n + 1 = 9

⇒ 2n = 9 - 1

⇒ 2n = 8

⇒ n =

vi

On equating the coefficients, we get

⇒ 0 = 2n - 2

⇒ 2n = 2

⇒ n =

#### Question:24

If , find the value of n.

Solution:

We have

On equating the coefficients, we get

3n - 15 = -3

 $\Rightarrow$  3n = -3 + 15

⇒ 3n = 12

⇒ n =

### Question:25

Express the following numbers in the standard form:

i 3908.78

ii 5,00,00,000

iii 3,18,65,00,000

 $iv 846 \times 10^{7}$ 

v 723 × 10<sup>9</sup>

# Solution:

We have

i 3908.78 = 3.90878 x 10<sup>3</sup>

since the decimal point is moved 3 places to the left

ii  $5,00,00,000 = 5,00,00,000.00 = 5 \times 10^7$ 

since the decimal point is moved 7 places to the left

 $= 3.1865 \times 10^9$ 

since the decimal point is moved 9 places to the left

iv  $846 \times 10^7 = 8.46 \times 10^2 \times 10^7$ 

since the decimal point is moved 2 places to the left

 $= 8.46 \times 10^9$ 

 $v 723 \times 10^9 = 7.23 \times 10^2 \times 10^9$ = 7.23 x 10<sup>11</sup> since the decimal point is moved 2 places to the left

[ since  $a^m \times a^n = a^{m+n}$ ]

[since  $a^m \times a^n = a^{m+n}$ ]

#### Question:26

Write the following numbers in the usual form:

 $i 4.83 \times 10^{7}$ 

ii  $3.21 \times 10^5$ 

iii 3.5 × 10<sup>3</sup>

#### Solution:

We have

i 
$$4.83 \times 10^7 = 483 \times 10^{7-2}$$
 since the decimal point is moved two places to the right =  $483 \times 10^5 = 4,83,00,000$ 

ii 
$$3.21 \times 10^5 = 321 \times 10^{5-2}$$
  
=  $321 \times 10^3 = 3,21,000$ 

since the decimal point is moved two places to the right

iii  $3.5 \times 10^3 = 35 \times 10^{3-1}$  since the decimal point is moved one place to the right

$$= 35 \times 10^2 = 3,500$$

### Question:27

Express the numbers appearing in the following statements in the standard form:

- i The distance between the Earth and the Moon is 384,000,000 metres.
- ii Diameter of the Earth is 1,27,56,000 metres.
- iii Diameter of the Sun is 1,400,000,000 metres.
- iv The universe is estimated to be about 12,000,000,000 years old.

### Solution:

We have

The distance between the Earth and the Moon is 3.84 x 10<sup>8</sup> metres.

Since the decimal point is moved 8 places to the left.

ii The diameter of the Earth is 1.2756 x 10<sup>7</sup> metres.

Since the decimal point is moved 7 places to the left.

iii The diameter of the Sun is 1.4 x 10<sup>9</sup> metres.

Since the decimal point is moved 9 places to the left.

iv The universe is estimated to be about 1.2x  $10^{10}$  years old.

Since the decimal point is moved 10 places to the left.

#### Question:28

Write the following numbers in the expanded exponential forms:

i 20068

ii 420719

iii 7805192

iv 5004132

v 927303

#### Solution:

We have

$$i\ 20068 = 2\ x\ 10^4 + 0\ x\ 10^3 + 0\ x\ 10^2 + 6\ x\ 10^1 + 8\ x\ 10^0$$

ii 
$$420719 = 4 \times 10^5 + 2 \times 10^4 + 0 \times 10^3 + 7 \times 10^2 + 1 \times 10^1 + 9 \times 10^0$$

iii 
$$7805192 = 7 \times 10^6 + 8 \times 10^5 + 0 \times 10^4 + 5 \times 10^3 + 1 \times 10^2 + 9 \times 10^1 + 2 \times 10^0$$

iv 
$$5004132 = 5 \times 10^6 + 0 \times 10^5 + 0 \times 10^4 + 4 \times 10^3 + 1 \times 10^2 + 3 \times 10^1 + 2 \times 10^0$$

$$\sqrt{927303} = 9 \times 10^5 + 2 \times 10^4 + 7 \times 10^3 + 3 \times 10^2 + 0 \times 10^1 + 3 \times 10^0$$

**Note**:  $a^0 = 1$ 

Find the number from each of the following expanded forms:

$$\begin{split} &i~7\times10^4+6\times10^3+0\times10^2+4\times10^1+5\times10^0\\ ⅈ~5\times10^5+4\times10^4+2\times10^3+3\times10^0\\ &iii~9\times10^5+5\times10^2+3\times10^1\\ &iv~3\times10^4+4\times10^2+5\times10^0\\ \end{split}$$

#### Solution:

We have

$$\begin{array}{l} i \ 7 \times 10^4 + 6 \times 10^3 + 0 \times 10^2 + 4 \times 10^1 + 5 \times 10^0 \\ = 7 \times 10000 + 6 \times 1000 + 0 \times 100 + 4 \times 10 + 5 \times 1 = 76045 \\ \\ ii \ 5 \times 10^5 + 4 \times 10^4 + 2 \times 10^3 + 3 \times 10^0 \\ = 5 \times 100000 + 4 \times 10000 + 2 \times 1000 + 3 \times 1 = 542003 \\ \\ iii \ 9 \times 10^5 + 5 \times 10^2 + 3 \times 10^1 \\ = 9 \times 100000 + 5 \times 100 + 3 \times 10 = 900530 \\ \\ iv \ 3 \times 10^4 + 4 \times 10^2 + 5 \times 10^0 \end{array}$$

#### Question:30

Mark the correct alternative in the following question:

 $= 3 \times 10000 + 4 \times 100 + 5 \times 1 = 30405$ 

#### Solution:

Hence, the correct alternative is option b.

# Question:31

Mark the correct alternative in the following question:

# Solution:

Since,

Hence, the correct alternative is option d.

#### Question:32

Mark the correct alternative in the following question:

### Solution:

Hence, the correct alternative is option c.

#### Question:33

Mark the correct alternative in the following question:

# Solution:

Since,

Hence, the correct alternative is option  $\ensuremath{\text{c}}.$ 

#### Question:34

Mark the correct alternative in the following question:

# Solution:

Since,

Hence, the correct alternative is option is d.
Question:35  Mark the correct alternative in the following question:  Solution:  Since,
Hence, the correct alternative is option b.
Question:36  Mark the correct alternative in the following question:  Solution:  Since,
Hence, the correct alternative is option a.
Question:37  Mark the correct alternative in the following question:
Solution: Since,
Hence, the correct alternative is option b.
Question:38  Mark the correct alternative in the following question:  Solution:  Since,
Hence, the correct alternative is option $\ensuremath{\mathtt{c}}$ .
Question:39  Mark the correct alternative in the following question:
Solution:
Hence, the correct alternative is option a.
Question:40 Mark the correct alternative in the following question:

Solution: Since,

Hence, the correct alternative is option b.
Question:41 Mark the correct alternative in the following question:
Solution: Since,
Hence, the correct alternative is option b.
Question:42 Mark the correct alternative in the following question:
Solution:
Question:43 Mark the correct alternative in the following question:
Solution: Since,
Hence, the correct alternative is option c.
Question:44  Mark the correct alternative in the following question:
Solution: Since,
Hence, the correct alternative is option c.
Question:45 Mark the correct alternative in the following question:
Solution: Since,
Hence, the correct alternative is option a.
Question:46  Mark the correct alternative in the following question:
Solution:
Hence, the correct alternative is option a.

Mark the correct alternative in the following question:

# Solution: So, 6<sup>5</sup> should be multiplied. Hence, the correct alternative is option b. Question:48 Mark the correct alternative in the following question: Solution: Since, Hence, the correct option is $\boldsymbol{a}$ . Question:49 Choose the correct alternative in the following question: Solution: Hence, the correct alternative is option a. Question:50 Choose the correct alternative in the following question: The number 4,70,394 in standard form is written as a 4.70394 10<sup>5</sup> b 4.70394 10<sup>4</sup> c 47.0394 10<sup>4</sup> d 4703.94 10<sup>2</sup> Solution: Since, $4,70,394 = 4.70394 \ 100000 = 4.70394 \ 10^5$ . So, the number 4,70,394 in standard form is written as $4.70394 \cdot 10^5$ . Hence, the correct alternative is option a. Question:51 Choose the correct alternative in the following question: The number 2.35 10<sup>4</sup> in the usual form is written as a 2.35 10<sup>3</sup> $d 235 10^4$ b 23500 c 2350000 Solution: Since, $2.35 \ 10^4 = 2.35 \ 10000 = 23500$ So, the number 2.35 10<sup>4</sup> in the usual form is written as 23500. Hence, the correct alternative is option b. Question:52 Choose the correct alternative in the following question:

Hence, the correct alternative is option b.

Solution:

Question:53	
Choose the correct alternative in the following question:	
Solution:	

Hence, the correct alternative is option  ${\sf b}$ .

# Question:54

Choose the correct alternative in the following question:

# Solution:

Since,

Hence, the correct alternative is option d.

Typesetting math: 54%