

Question:1

Find the complement of each of the following angles:

i 35°

ii 47°

iii 60°

iv 73°

Solution:

i The given angle measures 35° .

Let the measure of its complement be x .

$$x + 35^\circ = 90^\circ$$

$$\text{or } x = 90 - 35^\circ = 55^\circ$$

Hence, the complement of the given angle will be 55° .

ii The given angle measures 47° .

Let the measure of its complement be x .

$$x + 47^\circ = 90^\circ$$

$$\text{or } x = 90 - 47^\circ = 43^\circ$$

Hence, the complement of the given angle will be 43° .

iii The given angle measures 60° .

Let the measure of its complement be x° .

$$x + 60^\circ = 90^\circ$$

$$\text{or } x = 90 - 60^\circ = 30^\circ$$

Hence, the complement of the given angle will be 30° .

iv The given angle measures 73° .

Let the measure of its complement be x .

$$x + 73^\circ = 90^\circ$$

$$\text{or } x = 90 - 73^\circ = 17^\circ$$

Hence, the complement of the given angle will be 17° .

Question:2

Find the supplement of each of the following angles:

i 80°

ii 54°

iii 105°

iv 123°

Solution:

i The given angle measures 80° .

Let the measure of its supplement be x .

$$x + 80^\circ = 180^\circ$$

$$\text{or } x = 180 - 80^\circ = 100^\circ$$

Hence, the complement of the given angle will be 100° .

ii The given angle measures 54° .

Let the measure of its supplement be x .

$$x + 54^\circ = 180^\circ$$

$$\text{or } x = 180 - 54^\circ = 126^\circ$$

Hence, the complement of the given angle will be 126° .

iii The given angle measures 105° .

Let the measure of its supplement be x .

$$x + 105^\circ = 180^\circ$$

$$\text{or, } x = 180 - 105^\circ = 75^\circ$$

Hence, the complement of the given angle will be 75° .

iv

The given angle measures 123° .

Let the measure of its supplement be x .

$$x + 123^\circ = 180^\circ$$

$$\text{or } x = 180 - 123^\circ = 57^\circ$$

Hence, the complement of the given angle will be 57° .

Question:3

Among two supplementary angles, the measure of the larger angle is 36° more than the measure of the smaller. Find their measures.

Solution:

Let the two supplementary angles be x° and $180 - x^\circ$.

Since it is given that the measure of the larger angle is 36° more than the smaller angle, let the larger angle be x° .

$$\therefore 180 - x^\circ + 36^\circ = x^\circ$$

$$\text{or } 216 = 2x$$

$$\text{or } 108 = x$$

$$\text{Larger angle} = 108^\circ$$

$$\begin{aligned}\text{Smaller angle} &= 108 - 36^\circ \\ &= 72^\circ\end{aligned}$$

Question:4

Find the angle which is equal to its supplement.

Solution:

Let the measure of the required angle be x .

Since it is its own supplement:

$$x + x = 180^\circ \text{ or } 2x = 180^\circ \text{ or } x = 90^\circ$$

Therefore, the required angle is 90° .

Question:5

Can two angles be supplementary if both of them are:

i acute?

ii obtuse?

iii right?

Solution:

i No. If both the angles are acute, i.e. less than 90° , they cannot be supplementary as their sum will always be less than 180° .

ii No. If both the angles are obtuse, i.e. more than 90° , they cannot be supplementary as their sum will always be more than 180° .

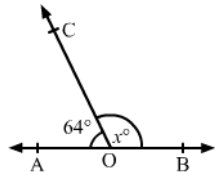
iii Yes. If both the angles are right, i.e. they both measure 90° , then they form a supplementary pair.

$$90^\circ + 90^\circ = 180^\circ$$

Question:6

In the given figure, AOB is a straight line and the ray OC stands on it.

If $\angle AOC = 64^\circ$ and $\angle BOC = x^\circ$, find the value of x .

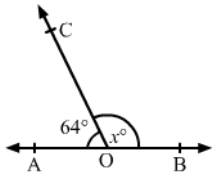


Solution:

By linear pair property:

$$\angle AOC + \angle COB = 180^\circ \quad 64^\circ + \angle COB = 180^\circ \quad \angle COB = x^\circ = 180^\circ - 64^\circ = 116^\circ$$

$$\therefore x = 116$$

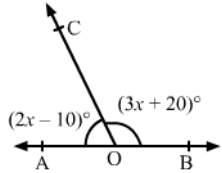


Question:7

In the given figure, AOB is a straight line and the ray OC stands on it.

If $\angle AOC = (2x - 10)^\circ$ and $\angle BOC = (3x + 20)^\circ$, find the value of x .

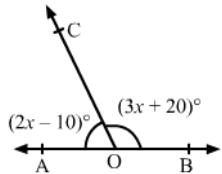
Also, find $\angle AOC$ and $\angle BOC$



Solution:

By linear pair property:

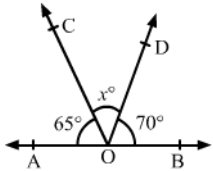
$$\angle AOC + \angle BOC = 180^\circ \text{ or } (2x - 10)^\circ + (3x + 20)^\circ = 180^\circ \quad (\text{given}) \text{ or } 5x + 10 = 180 \text{ or } 5x = 170 \text{ or } x = 34. \therefore \angle AOC = (2x - 10)^\circ = (2 \times 34 -$$



Question:8

In the given figure, AOB is a straight line and the rays OC and OD stand on it.

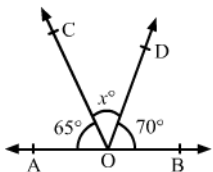
If $\angle AOC = 65^\circ$, $\angle BOD = 70^\circ$ and $\angle COD = x^\circ$ find the value of x .



Solution:

Since AOB is a straight line, we have:

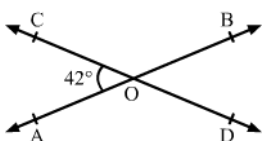
$$\angle AOC + \angle BOD + \angle COD = 180^\circ \text{ or } 65^\circ + 70^\circ + x^\circ = 180^\circ \quad (\text{given}) \text{ or } 135^\circ + x^\circ = 180^\circ \text{ or } x^\circ = 45^\circ \text{ Thus, the value of } x \text{ is } 45$$



Question:9

In the given figure, two straight lines AB and CD intersect at a point O .

If $\angle AOC = 42^\circ$, find the measure of each of the angles:

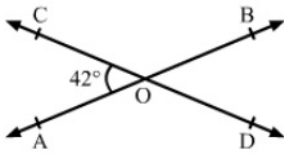


i $\angle AOD$

ii $\angle BOD$

iii $\angle COB$

Solution:



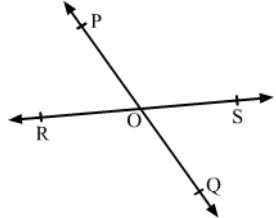
AB and CD intersect at O and CD is a straight line.

(i) $\angle COA + \angle AOD = 180^\circ$ (linear pair) $42^\circ + \angle AOD = 180^\circ$ $\angle AOD = 138^\circ$ (ii) $\angle COA$ and $\angle BOD$ are vertically opposite angles. $\therefore \angle COA$

Question:10

In the given figure, two straight line PQ and RS intersect at a O .

If $\angle POS = 114^\circ$, find the measure of each of the angles:



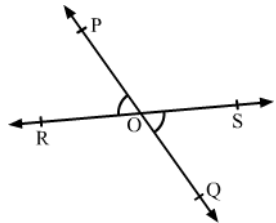
i $\angle POR$

ii $\angle ROQ$

iii $\angle QOS$

Solution:

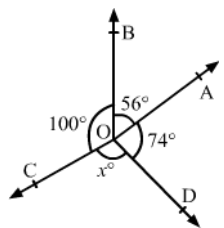
(i) $\angle POS + \angle POR = 180^\circ$ (linear pair) or $114^\circ + \angle POR = 180^\circ$ or $\angle POR = 180^\circ - 114^\circ = 66^\circ$ (ii) Since $\angle POS$ and $\angle QOR$ are vertically



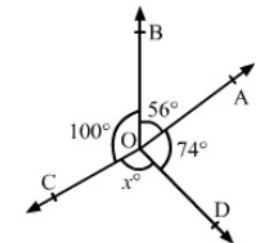
Question:11

In the given figure, rays OA , OB , OC and OD are such that $\angle AOB = 56^\circ$, $\angle BOC = 100^\circ$, $\angle COD = x^\circ$ and $\angle DOA = 74^\circ$.

Find the value of x .



Solution:



Sum of all the angles around a point is 360° .

$\therefore \angle AOB + \angle BOC + \angle COD + \angle DOA = 360^\circ$ or $56^\circ + 100^\circ + x^\circ + 74^\circ = 360^\circ$ (given) or $230^\circ + x^\circ = 360^\circ$ or $x^\circ = 130^\circ$ or $x = 130$