

Today's Content:

Length of smallest string in A, which contains all occurrences B

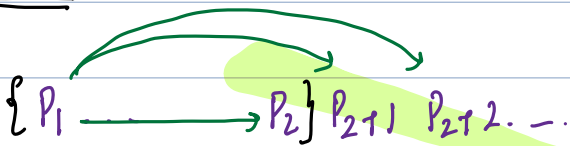
# If we want to apply 2 pointer on subarray, show me if the below

$\{P_1 \dots P_2\}$

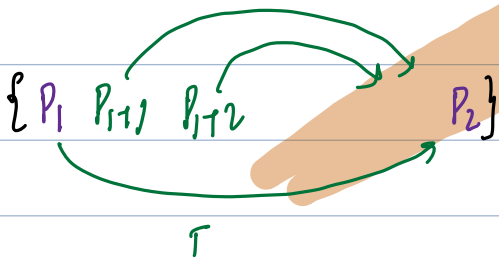
If  $P_1 \dots P_2$  is valid

$\{P_1 \longrightarrow P_2\}$

Case 1:



T

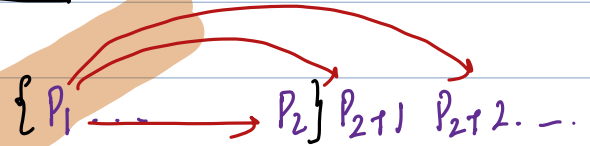


T

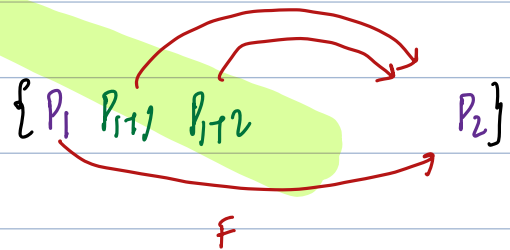
If  $P_1 \dots P_2$  is valid

$\{P_1 \longrightarrow P_2\}$

Case 1:



T



F

### 38: Minimum Window String:

Given two strings  $s$  &  $t$  of lengths  $N$  and  $k$  respectively.

Return length of smallest substring of  $s$  which contains all characters of  $T$  including duplicates

#Note:  $s$  &  $T$  contain only lower case.

Ex:  $T_k = b a b c$

0 1 2 3 4 5 6 7 8 9 10 11 12  
 $S_N = b d a c e b a n c b b a c$

Possible: len

$S[0 6]$  7

$S[10 12]$  \*

$S[9 12]$  4

Idea 1:

1. Insert  $T[]$  in  $hMT$ :  $\{b:2, c:1, a:1\}$

Generate all substrings of  $s$ :

For a substring of  $s$ , check if it contains all characters of  $T$ ?

# Substring  $s[n:y] = a a c b c e b a$

$T[] = b a b c$

# Approach:

Insert  $s[n:y]$  in  $hMS$ :  $\{a:3, c:2, b:2, e:1\}$

$hMT$ :  $\{b:2, c:1, a:1\}$

For every char  $ch$  in  $hMT$ :

$hMT[ch] \leq hMS[ch]$

TC:  $O(k + N^2 * (N + 26))$  SC:  $O(26) = O(1)$

To generate  $hMT$  → Two iterate & compare 2 hashmaps.

At max, distinct keys are 26, because, Given  $s$  &  $T$  contain only smaller alphabets.

## Idea 2: Optimize using carry forward

Say we have

$s[n..y] = a a c b c e b a$

$T[] = b a b c$

$s[1..4)$

$s[1..5)$

To compare both:

$hms: \{a:3 \ c:2 \ b:2 \ e:1\}$

$hmt: \{b:2 \ c:1 \ a:1\}$

Say we have

$s[n..y+1] = a a c b c e b a c$

Add, new char to hashmap  $hms$

$T[] = b a b c$

To compare both:

$hms: \{a:3 \ c:3 \ b:2 \ e:1\}$

$hmt: \{b:2 \ c:1 \ a:1\}$

$TC: O(k + N^2 \cdot (1 + 26))$

$SC: O(26) \approx O(1)$

↳ # To compare both  $hmt$  &  $hms$

↳ # To generate  $hms$  for each substring.

↳ #  $N^2$  substring

↳ To generate  $hmt$

Beacuz, we only need to add new char in  $hmt$

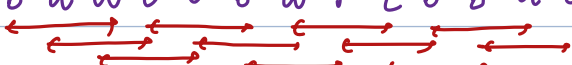
Idea 3: Using BS

0 1 2 3 4

$T_k = b a b c a$

0 1 2 3 4 5 6 7 8 9 10 11 12

$S_N = b d a c e b a n c b b a c$



Target = Min length of substring in  $S$

Search space =  $lo:1$   $hi: S.length;$

Discard ?

$l$   $h$   $m$

1 13 7 : Check if there exists substring of  $len=7$  which contains all character of  $T$ .

Q: We check all substrings of  $len=7$

7 8 9 10 ..

$low = m;$

$h = m-1;$

1 6 3 : Check if there exists substring of  $len=3$  which contains all character of  $T$ .

Q: We check all substrings of  $len=3$

1 2 3

$l = m+1;$

TC:  $O(\log^2 N \times N) \approx O(N \log^2 N)$  SC:  $O(26) \approx O(1)$

int pal(string s, string t) {

int l = 1, h = s.length(), ans = -1; # of no such substring exist.

while (l <= h) {

int m = (l+h)/2; # Check if there exists a substring of m

if (check(s, m, t)) { length is s, which contains all char in T.

ans = m;

h = m-1;

else {

l = m+1;

}

return ans;

}

Ty with sliding window TC:  $O(N)$

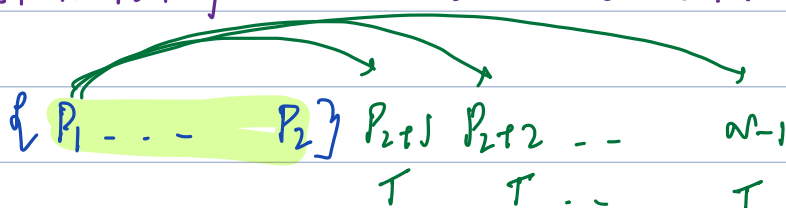
Idea 4: 2 pointers?

Say in  $S[P_1 \dots P_2]$  we take substring  $P_1 \dots P_2$ .

If it contains all character of T. It's a guarantee that

$P_1 \dots P_{2+1} [P_{2+2}] \dots$  will also contain all char of T.

Abse statement falls under below criteria:



Given:  $T_k = a a b b c$

$S_N =$

-1	0	1	2	3	4	5	6	7	8	9	10	11	12
c	a	b	a	a	c	c	e	b	a	b	a	c	
		$P_1$						$P_2$					

Does HMT contain all char of HMT

$P_1$	$P_2$	Valid	ans	Update	HMT: {a:2 b:2 c:1}
0	-1	*	*	$P_2++$ HMT[S[P <sub>2</sub> ]]++;	HMT: {c:2 a:2 b:2 e:1}
0	0	*	*	$P_2++$ HMT[S[P <sub>2</sub> ]]++;	
0	1	*	*	$P_2++$ HMT[S[P <sub>2</sub> ]]++;	
0	2	*	*	$P_2++$ HMT[S[P <sub>2</sub> ]]++;	
0	3	*	*	$P_2++$ HMT[S[P <sub>2</sub> ]]++;	
0	4	*	*	$P_2++$ HMT[S[P <sub>2</sub> ]]++;	
0	5	*	*	$P_2++$ HMT[S[P <sub>2</sub> ]]++;	
0	6	*	*	$P_2++$ HMT[S[P <sub>2</sub> ]]++;	
0	7	*	*	$P_2++$ HMT[S[P <sub>2</sub> ]]++;	
0	8	✓	q	HMT[S[P <sub>1</sub> ]]-- $P_1++$ ;	
1	8	✓	q	HMT[S[P <sub>1</sub> ]]-- $P_1++$ ;	
2	8	TODO			

Update length

Updating hashmap & pointer.

TC:  $O(k + 2N * \{2b + 1 + 1 + 1\})$

SC:  $O(2b) \approx O(1)$

↳ # Comparing 2 hashmaps  
↳ # Total 2 pointer iterations

TC:  $O(k + 5N)$  SC:  $O(1)$

$\approx O(k + N)$

↳ TLE, if can exceed  $> 10^8$  iterations

Dry Run: TC:  $O(k + 2N * (1 + 1 + 1 + 1)) \rightarrow$  Match value TC:  $O(k + N) = O(N + k)$   
 $T_k = a a b b c \rightarrow$  valid  $\rightarrow$  ans  $\rightarrow$  hashmap & ptr

0 1 2 3 4 5 6 7 8 9 10 11 12  
 $S_N = \cancel{a} \cancel{a} \cancel{b} a a c b c e a b a c$   
 $P_1$   $P_2$

Keep a track of how many of  
 char of TMS are matching HMT

HMT: {a: 2 b: 2 c: 1}

HMS: {c: 1 a: 2 b: 1}

if match == length of T

$P_1$	$P_2$	match	Valid	ans	Update	Relevant
0	-1	0	*	*	$P_2 + 1$ hms[S[P <sub>2</sub> ]]++	✓ match++;
0	0	1	*	*	$P_2 + 1$ hms[S[P <sub>2</sub> ]]++	✓ match++;
0	1	2	*	*	$P_2 + 1$ hms[S[P <sub>2</sub> ]]++	✓ match++;
0	2	3	*	*	$P_2 + 1$ hms[S[P <sub>2</sub> ]]++	✓ match++;
0	3	4	*	*	$P_2 + 1$ hms[S[P <sub>2</sub> ]]++	*
0	4	5	*	*	$P_2 + 1$ hms[S[P <sub>2</sub> ]]++	*
0	5	4	*	*	$P_2 + 1$ hms[S[P <sub>2</sub> ]]++	✓ match++;
0	6	5	✓	7	hms[S[P <sub>1</sub> ]]--; $P_1++$	*
1	6	5	✓	6	hms[S[P <sub>1</sub> ]]--; $P_1++$	*
2	6	5	✓	5	hms[S[P <sub>1</sub> ]]--; $P_1++$	✓ match--;

#Obs:

Add relevant char: ch

if (hms[ch] <= hmt[ch]) {

#ch is add & it's correct char, Inc count of match by 1  
 match++;

Remove relevant char: ch

if (hmt[ch] > hms[ch]) {

#ch is removed & it's correct char, Dec count of match by 1  
 match--;

```
int smallestString(string s, string T){
```

```
    unordered_map<char, int> hmt;
```

```
    for(int i = 0; i < T.size(); i++) {
```

```
        hmt[T[i]]++; // insert T[i] in hmt;
```

```
    int match = 0;
```

```
    int i = 0, j = -1, ans = INT_MAX;
```

```
    unordered_map<char, int> hms;
```

```
    while(j < s.size()) {
```

```
        if( match == T.size() ) { // [i..j]
```

```
            ans = min(ans, j - i + 1);
```

```
            hms[s[i]]--;
```

```
            if( hms[s[i]] < hmt[s[i]] ) {
```

```
                match--;
```

```
                i++;
```

```
            }
```

```
        else {
```

```
            j++;
```

```
            if( j == s.size() ) { break; }
```

```
            hms[s[j]]++;
```

```
            if( hms[s[j]] == hmt[s[j]] ) {
```

```
                match++;
```

```
            }
```

```
        }
```

```
    return ans;
```

```
}
```