

Todays Content

1. Count no: of elements with atleast 1 $\in \cup$ > itself
2. Pair sum = k
3. Vector Intro w/ pairs by value & pairs by reference.

Q8: Given $arr[n]$ return count no. of elements with atleast 1 ele $>$ itself.

Constraints:

$$\begin{aligned}1d = N &= 10^5 \\1 &\leq arr[i] \leq 10^9\end{aligned}\quad \left. \begin{array}{l} \\ \end{array} \right\} \text{Add in script}$$

Ex: $arr[] = \{7, 3, 10, 8, 9, 10, 6\}$ cnt = 5

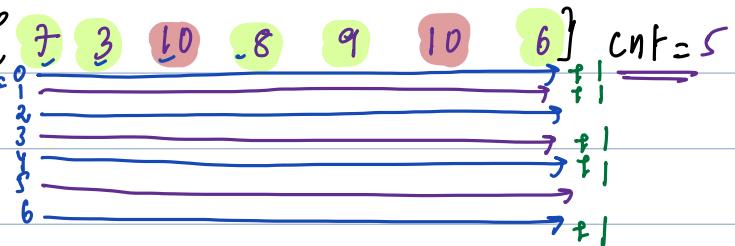
Ex: $arr[] = \{9, 6, 4, 7, 9, 4\}$ cnt = 4

Ideas: Iterate in $arr[]$:

For every $arr[i]$: Iterate q check if there an element $> arr[i]$.

$arr[] = \{7, 3, 10, 8, 9, 10, 6\}$ cnt = 5

Dry Run: $i=0$



int greaterThanSelf(int[] arr, int N) { TC: $O(N^2)$

int c = 0;

$$N \lambda = 10^5, N^2 \Rightarrow (10^5)^2 = 10^{10} > 10^8$$

for (int i = 0; i < N; i++) {

// For $arr[i]$: Check if there exists an element $> arr[i]$

bool isgre = false;

for (int j = 0; j < N; j++) {

if ($arr[j] > arr[i]$) {

isgre = true;

if (isgre == true) { // There is an ele $> arr[i]$.

isgre;

3 return c;

0 1 2 3 4 5 6 7 8
 $arr[0] = \{ 7 \ 3 \ 10 \ 8 \ 9 \ 10 \ 6 \ 3 \ 10 \}$

Observation: Max element will not have an element greater than itself,
 Other than max every element will have element > itself

Idea: Step 1: Iterate & calculate max

Step 2: Iterate & calculate no.-max elements counts & return.

int greaterItsself(int arr[], int N) { TC: O(2N) = O(N) SC: O(1)
 ↓

```
int max = arr[0] or INT_MIN;
for (int i = 0; i < N; i++) {
  if (arr[i] > max) {
    max = arr[i];
  }
}
```

```
int c = 0
for (int j = 0; j < N; j++) {
  if (arr[j] < max) {
    c++;
  }
}
return c;
```

TODO: Try to do it with 1 iteration.

Given $ar[n]$ elements a, k

Count no. of pairs indices (i, j) are there such that $ar[i] + ar[j] := k$

Note: $i \neq j$ are indices.

Note1: (i, j) pair same as (j, i)

Note2: $(i \neq j)$

Constraints: → Add in script

$$1 \leq N \leq 10^3 \longrightarrow TC: O(N^2) = (10^3)^2 = 10^6 \approx 10^8$$

$$1 \leq ar[i] \leq 10^9$$

Ex1:
 $ar[] = \{ 7, 4, 6, 3, 7, 4, 5, 5 \}$

$$k = 10$$

$$i=j$$

pairs = $(0, 3), (1, 2), (2, 5), (3, 4), (5, 2), (6, 7), (6, 6)$

Idea: Generate all pairs & calculate sum

if sum == k: inc count

0 1 2 3 4

Tracing: $ar[] = \{ 7, 4, 6, 3, 7 \}$

pairs:

$i, j = 0 \ 1 \ 2 \ 3 \ 4$

$i=0$ $(0, 0), (0, 1), (0, 2), (0, 3), (0, 4)$ Note: When we generate all

$i=1$ $(1, 0), (1, 1), (1, 2), (1, 3), (1, 4)$ pairs, valid pair are

$i=2$ $(2, 0), (2, 1), (2, 2), (2, 3), (2, 4)$ counted twice

$i=3$ $(3, 0), (3, 1), (3, 2), (3, 3), (3, 4)$ Before returning final ans/2;

$i=4$ $(4, 0), (4, 1), (4, 2), (4, 3), (4, 4)$

→ Script

int pairSum(int arr[], int N, int K) { TC: O(N^2) SC: O(1) }

$$\hookrightarrow N^2 = 10^3 : (10^3)^2 = 10^6 \ll 10^8$$

int c = 0;

for (int i = 0; i < N; i++) {

 for (int j = 0; j < N; j++) {

 if (arr[i] + arr[j] == 2 * K && i != j) {

 c++;

 3

 return c / 2;

3

obs: Iterate only in 1 half of pairs. { upper or lower half }
TODO.

0 1 2 3 4

Tracing: arr[] = { 7 4 6 3 7 }

pairs:

i j= 0 1 2 3 4

i=0 (0 0) (0 1) (0 2) (0 3) (0 4) i=0 j=1 2 .. N-1

i=1 (1 0) (1 1) (1 2) (1 3) (1 4) i=1 j=2 ... N-1

i=2 (2 0) (2 1) (2 2) (2 3) (2 4) i=2 j=3 ... N-1

i=3 (3 0) (3 1) (3 2) (3 3) (3 4) :

i=4 (4 0) (4 1) (4 2) (4 3) (4 4) i j = i+1 ... N-1

int pairSum(int arr[], int N, int k) { TC: $O\left(\frac{N^2 + N}{2}\right) = O(N^2)$ SC: O(1)}

int c = 0;

for (int i = 0; i < N; i++) {

 for (int j = i + 1; j < N; j++) {

 if (arr[i] + arr[j] == k) {

 c++;

 }

return c;

}

Issues in Arrays:

`int arr[5];`

0	1	2	3	4
10	20	30	40	50

`arr[0]=10; arr[1]=20; arr[2]=30; arr[3]=40 arr[4]=50`

Size is not dynamic.

Dynamic Arrays: Size is dynamic

In C++:

In Java:

In Python:

vector

ArrayList

List

Create a Vector:

Way 1: `vector<datatype> vname;` // vname = []

`vector<int> v1; // v1: []` : Can only int

`vector<float> v2; // v2: []` : Can only float

Way 2: `vector<datatype> vname2(initial-size, initial-value);`

`vector<int> v(5, 10); // v: 0 1 2 3 4`

Access: `vname[index]`

`v[2]=9; v[1]=14 v[3]=19`

10	14	9	19	10
----	----	---	----	----

Insert into a vector:

`vname.push_back(val);` // Adds new element after last index

`v.push_back(60);` // v: 0 1 2 3 4 5 6

`v.push_back(3);`

10	14	9	19	10	60	3
----	----	---	----	----	----	---

Size of Vector

`vname.size();` // return size of vector

`int n = v.size();` // n = 7;

Remove from vector

`vname.pop_back();` // It will delete last index

`v.pop_back();` // v: 0 1 2 3 4 5 6

10	14	9	19	10	60	3
----	----	---	----	----	----	---

Note: Check inserting & deleting from middle

Iterate in Vector

```
int N = v.size();  
for(int i=0; i<N; i++) {  
    |    cout << v[i];  
}|}
```

Sort a vector

```
sort(vname.begin(), vname.end());
```

```
sort(v.begin(), v.end());
```

v: 0 1 2 3 4 5


v: 0 1 2 3 4 5


TC: Vector:

TC: for 1 single call

- 1. push_back(n) $O(1)$
- 2. pop_back() $O(1)$
- 3. size() $O(1)$
- 4. sort(v.begin(), v.end()) $O(N \log N)$
 $\hookrightarrow N = \text{size of Vector.}$

Q: Given vector add all elements by +2 & return vector.

vector<int> modify(vector<int> &v) {

}