

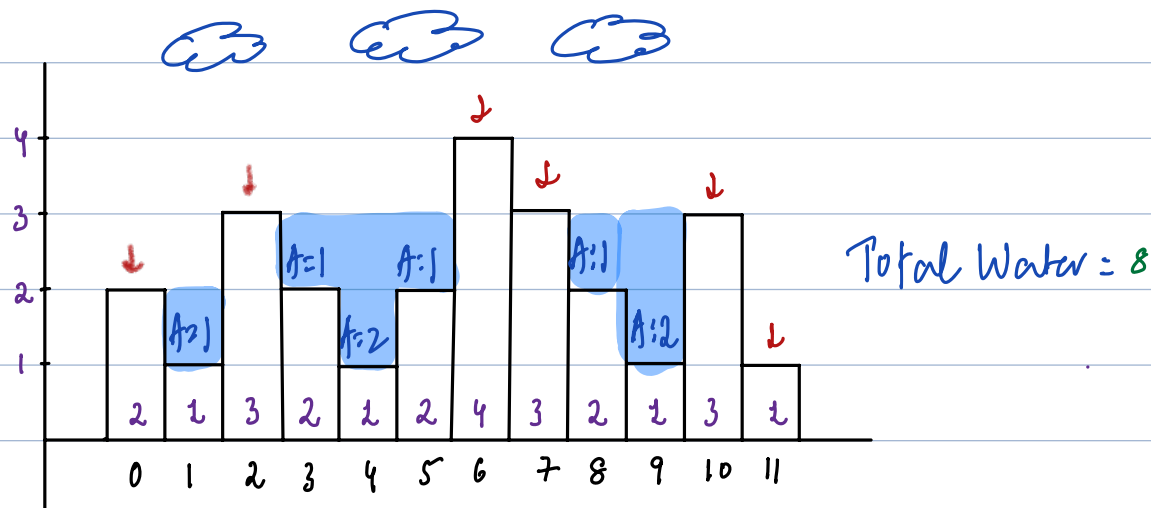
## Today's Content

1. Water Filling
2. Product Except current element
3. Majority Elements

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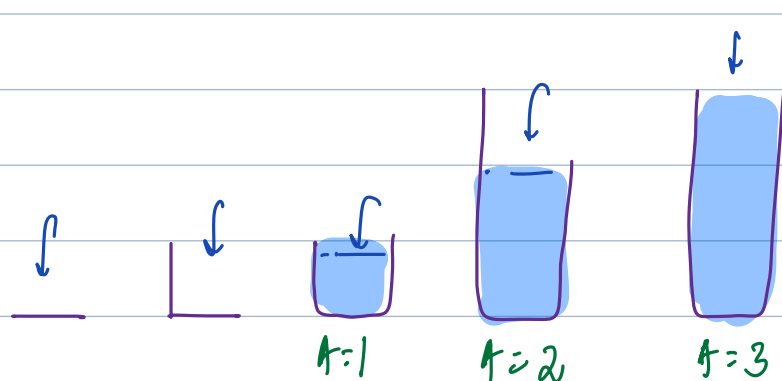
Given an  $arr[n]$  where  $arr[i]$  represent height of the building  
 Return amount of water trapped in our buildings  
 Note: Width of each building is 1

$arr[12] = \{ 2, 1, 3, 2, 1, 2, 4, 3, 2, 1, 3, 1 \}$



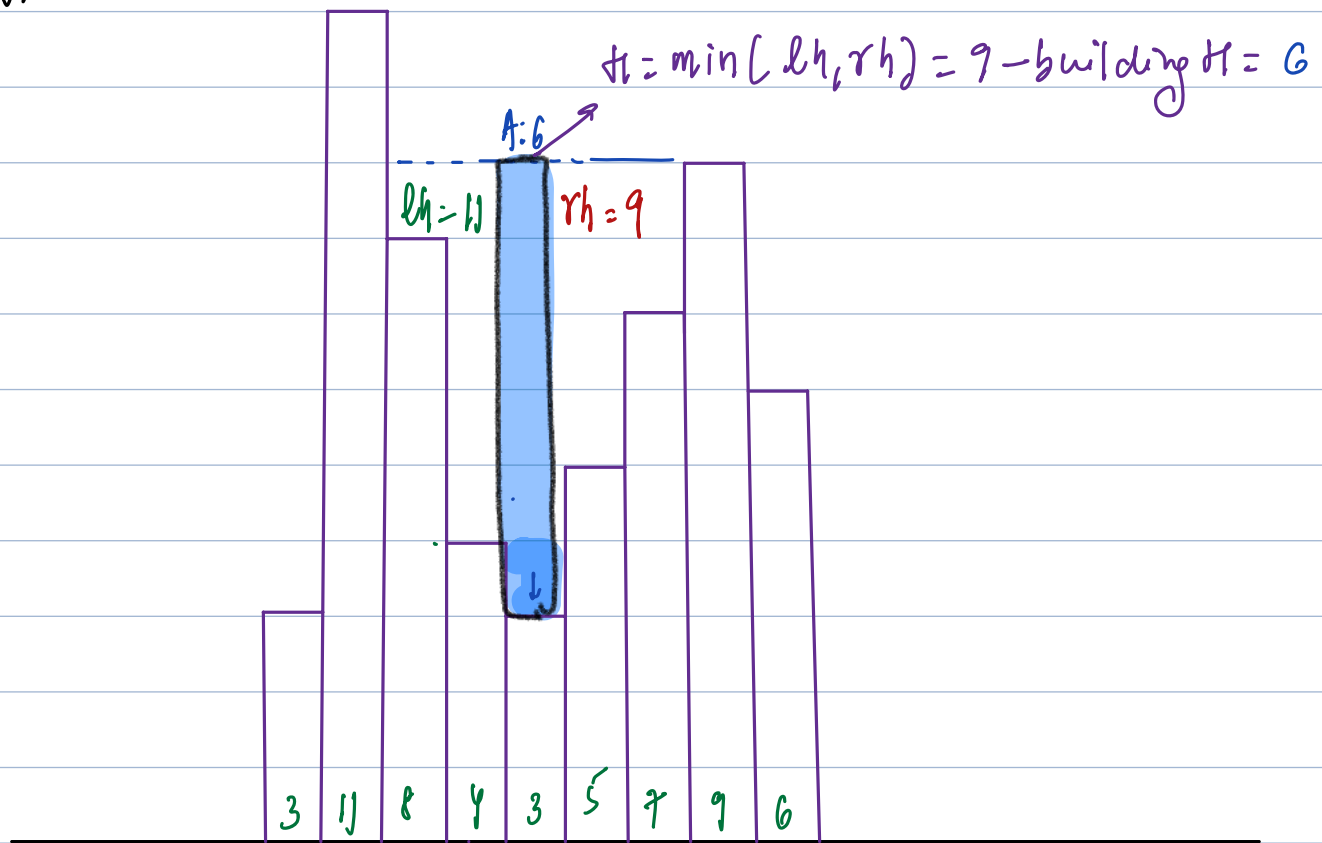
Idea: Add water accumulated on top of each building.

Dry Run 1:



Obs: Water in a building is minimum of (left, right) boundary.

Dry Run 2:



# Idea:

int ans = 0; TC:  $O(N^2)$  SC:  $O(1)$

For all buildings: Add water accumulated.

# Water in  $i^{th}$  building

lh = Max height on left side  $\{0 \dots i-1\}$

rh = Max height on right side  $\{i+1 \dots N-1\}$

H =  $\min(rh, lh)$

$W = H - \text{height}[i]$

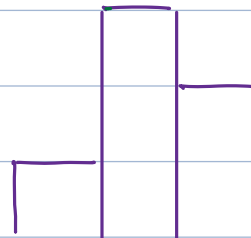
ans = ans +  $\max(W, 0)$ ;

# Edge Case:

lh = 1, rh = 2, H = 1.

$W = 1 - 3 = -2$

If water accumulate is -ve, skip it



return ans;

Optimization: Using Precomputation.

For every element we want, max on left, max on right.

So precompute:

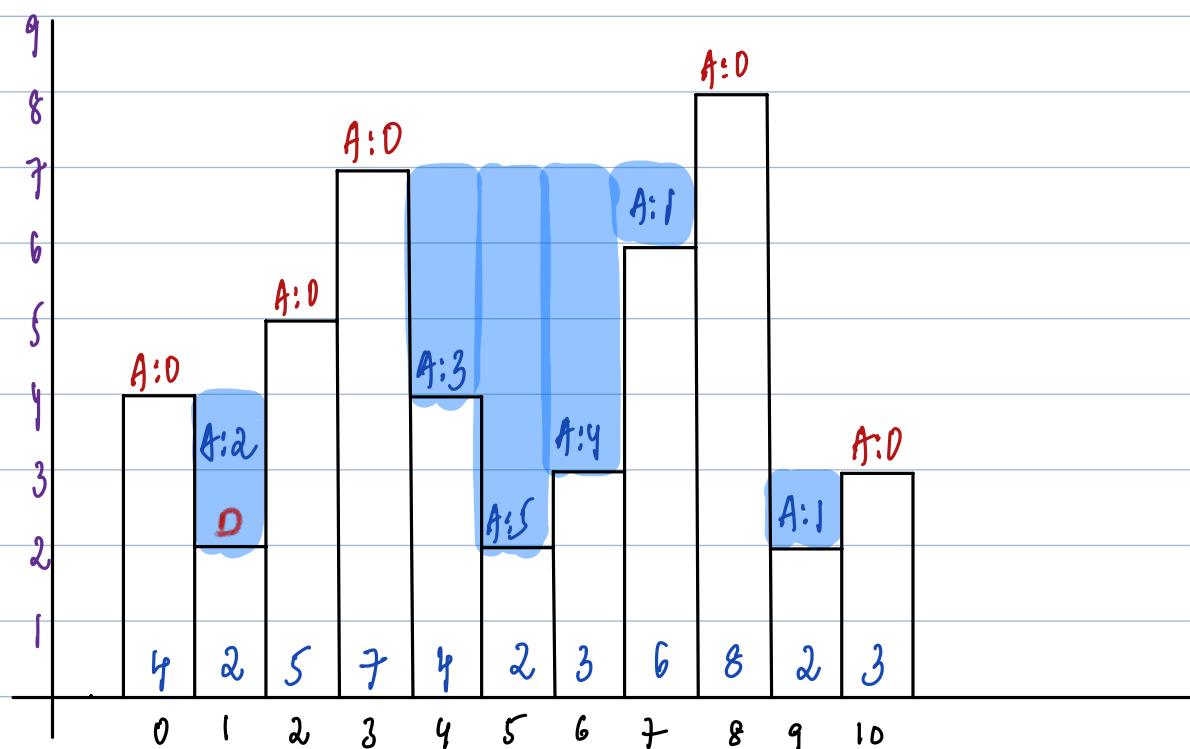
Max on left: Prefix Max

$pf[i] = \text{Max of all elements } [0..i]$

Max on right: Suffix Max

$sf[i] = \text{Max of all elements } [i..n-1]$

Dry Run 2:



$pf[] = \{ 4, 4, 5, 7, 7, 7, 7, 7, 8, 8, 8 \}$

$sf[] = \{ 8, 8, 8, 8, 8, 8, 8, 8, 8, 3, 3 \}$

# Water in  $i^{\text{th}}$  Building:

$lh = \text{max on left } [0..i-1] = pf[i-1]$

$rh = \text{max on right } [i+1..n-1] = sf[i+1]$

$h = \min(lh, rh)$

$w = h - \text{height}[i]$

$ans = ans + \text{max}(w, 0)$

$pf[i] = \text{Max of all elements } [0..i]$

$sf[i] = \text{Max of all elements } [i..n-1]$

int water(vector<int> h) { TC:  $O(N+N+N) = O(N)$  SC:  $O(N+N) = O(N)$

vector<int> leftm = pfman(h);

vector<int> rightm = sfman(h);

int N = h.size();

# 0<sup>th</sup> & N-1<sup>st</sup> building will not have any water accumulated

int ans = 0;

for(int i = 1, i < N-1; i++) {

# Water accumulated on h[i];

int lh = leftm[i-1];

# max from [0..i-1] # Edge case i==0

int rh = rightm[i+1];

# max from [i+1..N-1] # Edge case i==N-1

int bh = min(lh, rh);

int W = bh - h[i];

ans = ans + max(W, 0);

}

return ans;

}

## Product Array Puzzle:

Given an array Construct a product array

Such that  $prod[i] = \text{product of all } arr[] \text{ except } arr[i]$

Note: Cannot use / operator.

Ex1:  $arr[] = \begin{matrix} 0 & 1 & 2 & 3 & 4 \\ 10 & 3 & 5 & 6 & 2 \end{matrix}$   
 $prod[] = \begin{matrix} 180 & 600 & 360 & 300 & 900 \end{matrix}$

Ex2:  $arr[] = \begin{matrix} 0 & 1 & 2 & 3 & 4 & 5 \\ 3 & 4 & 2 & 5 & 6 & 2 \end{matrix}$   
 $prod[] = \{ \quad \quad \quad \quad \quad \quad \}$

# Idea 1

for every  $arr[i]$ :

$prod = \text{product of all elements from } [0..i-1]$

$prod = \text{product of all elements from } [i+1..n-1]$

$prod[i] = prod * prod$

return prod;

TC:  $O(N^2)$  SC:  $O(1)$

Optimization: Precomputation.

For every element we want, prod on left & prod on right

So precompute:

Prod on left: Prefix Prod

$pf[i] =$  Product of all elements  $[0..i]$

Prod on right: Suffix Prod

$sf[i] =$  Product of all elements  $[i..n-1]$

for  $i^{\text{th}}$  element =

prod = product of elements from  $[0..i-1] = pf[i-1]$

pror = product of elements from  $[i+1..n-1] = sf[i+1]$

$prod[i] = pf[i-1] * sf[i+1];$

```
vector<long> productArray(vector<long> ar){
```

```
    vector<long> pf = prefixProduct(ar);
```

```
    vector<long> sf = suffixProduct(ar);
```

```
    int N = ar.size();
```

```
    vector<long> prod(N, 0);
```

```
    if(N==1){ prod[0]=1; return }
```

0  
ar[] = {10}

pf[] = {1}

```
    prod[0] = sf[1]; # product of elements [1.. N-1]
```

```
    prod[N-1] = pf[N-2]; # product of elements [0.. N-2]
```

```
    for(int i=1; i<N-1; i++){
```

Edge Cases:  $i=0, i=N-1$

```
        prod[i] = pf[i-1] * sf[i+1]
```

```
    return prod;
```

}