

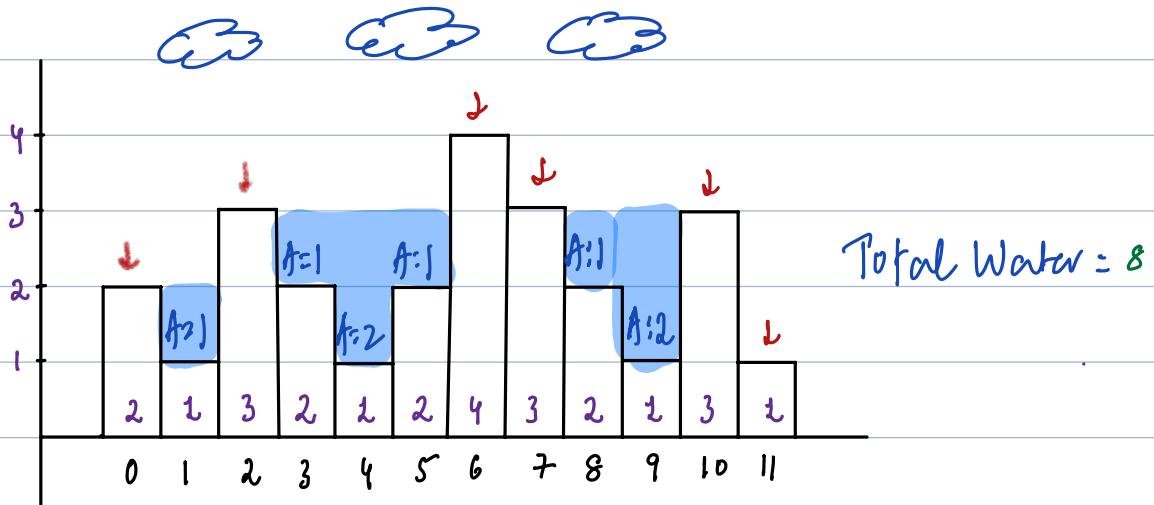
Todays Content

1. Water Filling
2. Product Except current element
3. Majority Elements.

18

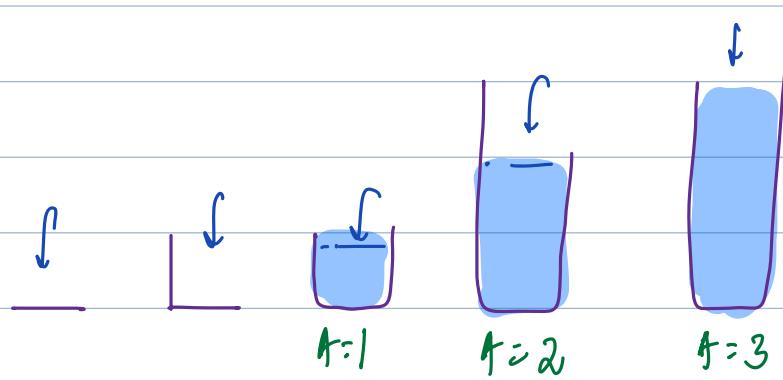
Given an arr[n] where arr[i] represent height of the building
 Return amount of water trapped on all buildings
 Note: Width of each building is 1

arr[12] = {2 1 3 2 1 2 4 3 2 1 3 1}



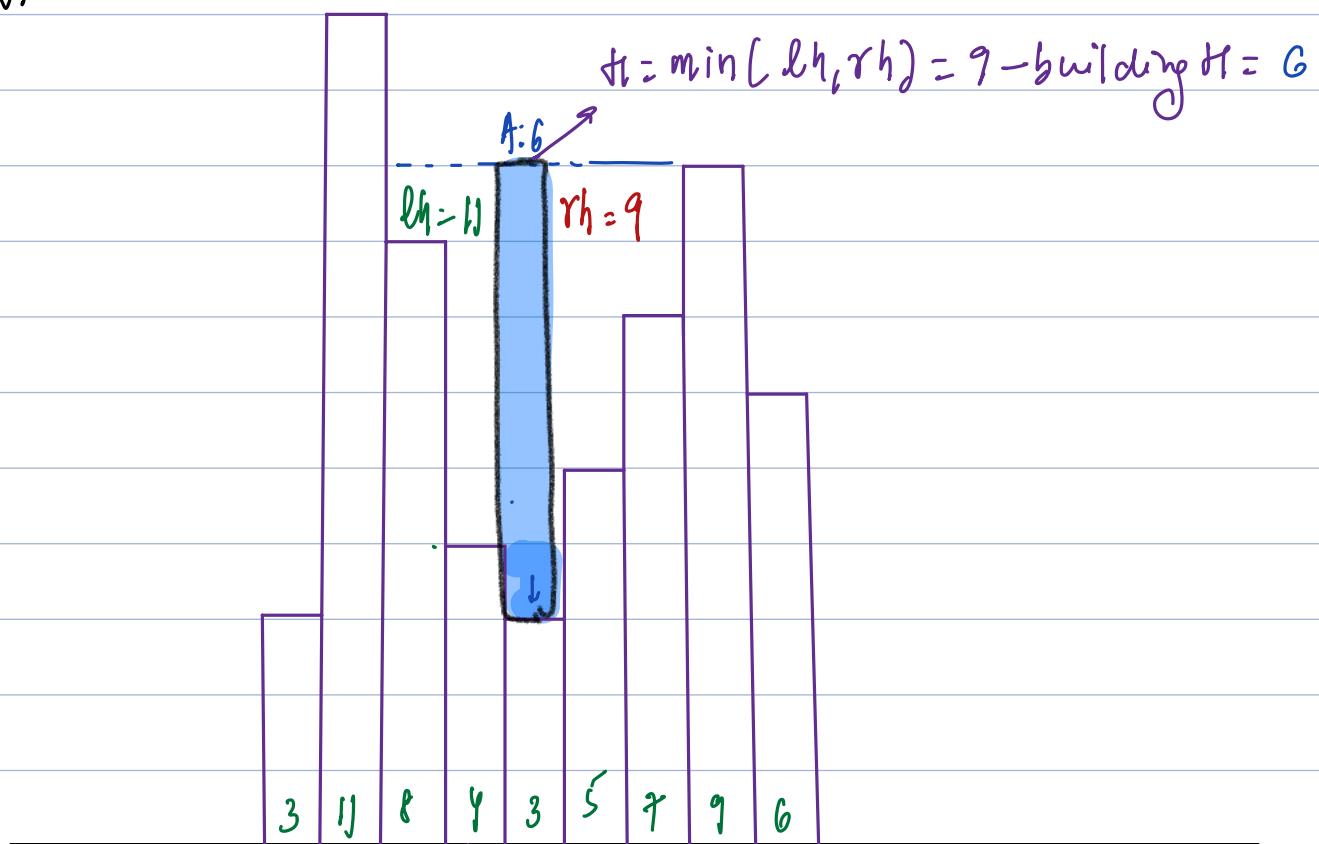
Idea: Add water accumulated on top of each building.

Dry Run 1:



Obs: Water in a building is minimum of (left, right) boundary.

Dry Run 2;



Idea:

int ans = 0; TC: $\Theta(N^2)$ SC: $\Theta(1)$

for all buildings: Add water accumulated.

Water in i^{th} building

$lh = \max \text{ height on left side } \{0 \dots i-1\}$

$rh = \max \text{ height on right side } \{i+1 \dots N-1\}$

$h = \min(lh, rh)$

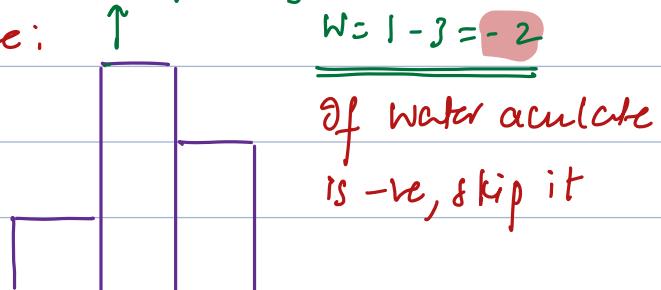
$W = h - \text{height}[i]$

$ans = ans + \max(W, 0);$

$lh = 1, rh = 2, h = 1.$

Edge Case:

$W = 1 - 3 = -2$



return ans;

Optimization: Using Precomputation.

For every element we want, man on left, man on right.

So precompute:

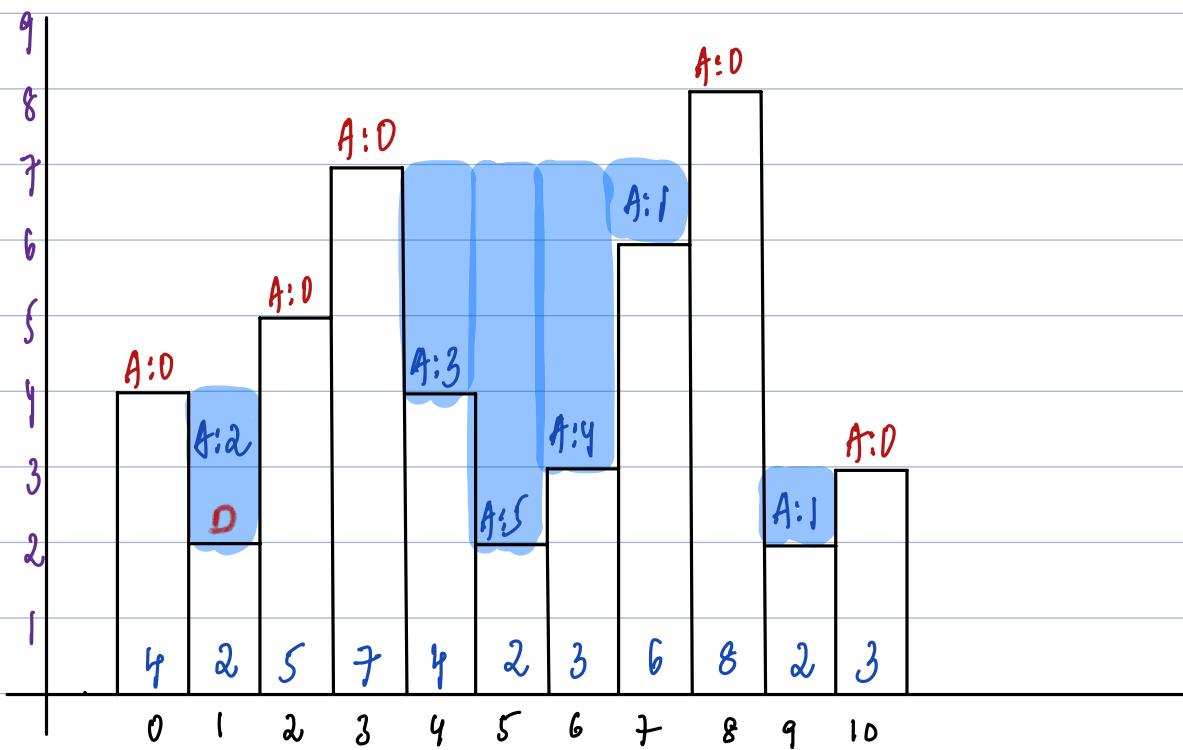
Man on left: PrefixMan

$Pf[i]$ = Man of all elements $[0..i]$

Man on right: SuffixMan

$Sf[i]$ = Man of all elements $[i..N-1]$

DyRun2:



$$Pf[] = \{ 4, 4, 5, 7, 7, 7, 7, 7, 8, 8, 8 \}$$

$$Sf[] = \{ 8, 8, 8, 8, 8, 8, 8, 8, 8, 3, 3 \}$$

Water in i^{th} Building:

$$lh = \text{man on left } [0..i-1] = Pf[i-1]$$

$$rh = \text{man on right } [i+1..N-1] = Sf[i+1]$$

$$h = \min(lh, rh)$$

$$W = h - \text{height}[i]$$

$$Ans = Ans + \max(W, 0)$$

$Pf[i]$ = Man of all elements $[0..i]$

$Sf[i]$ = Man of all elements $[i..N-1]$

int water(vector<int> &h) { TC: $O(N + N + N) = O(N)$ SC: $O(N + N) = O(N)$

vector<int> leftm = pfmax(h);

vector<int> rightm = sfmax(h);

int N = h.size();

0th N-1th building will not have any water accumulated

int ans = 0;

for (int i = 1, i < N - 1, i++) {

Water accumulated in h[i];

int lh = leftm[i - 1]; # max from [0..i-1] # Edge Case i == 0

int rh = rightm[i + 1]; # max from [i + 1..N - 1] # Edge Case i == N - 1

int bh = min(lh, rh);

int w = bh - h[i];

ans = ans + min(w, 0);

}

return ans;

}

Product Array Puzzle:

Given a $\text{arr}()$ Construct a $\text{prod}()$

Such that $\text{prod}[i] = \text{product of all } \underline{\text{arr}[j] \text{ except arr}[i]}$

Note: Cannot use / operator.

Ex1: $\text{arr}[] = \{ 10, 3, 5, 6, 2 \}$

$\text{prod}[] = \{ 180, 600, 360, 300, 900 \}$

Ex2: $\text{arr}[] = \{ 3, 4, 2, 5, 6, 2 \}$

$\text{prod}[] = \{ \quad \}$

Idea!

For every $\text{arr}[i]$:

$\text{prod} = \text{product of all elements from } [0..i-1]$

$\text{prod} = \text{product of all elements from } [i+1..n-1]$

$\text{prod}[i] = \text{prod} * \text{prod}$

return prod

TC: $O(N^2)$ SC: $O(1)$

Optimization: Precomputation.

For every element we want, prod on left & prod on right

So precompute;

Prod on left: Prefix Prod

$pf[i] = \text{Product of all elements } [0..i]$

Prod on right: Suffix Prod

$sf[i] = \text{Product of all elements } [i..N-1]$

For i^{th} element =

$prod = \text{product of elements from } [0..i-1] = pf[i-1]$

$prod = \text{product of elements from } [i+1..N-1] = sf[i+1]$

$prod[i] = pf[i-1] * sf[i+1];$

vector<long> productArray (vector<long> ar) {

vector<long> pf = prefinProduct(ar);

vector<long> sf = suffixProduct(ar);

int N = ar.size();

vector<long> prod[N, 0];

if (N == 1) { prod[0] = 1; return; } $ar[] = \{10\}$
 $pf[] = \{1\}$

prod[0] = sf[1]; # product of elements [1.. N-1]

prod[N-1] = pf[N-2]; # product of elements [0.. N-2]

for (int i = 1; i < N-1; i++) {
 prod[i] = pf[i-1] * sf[i+1];

Edge Cases: i = 0, i = N-1;

return prod;