

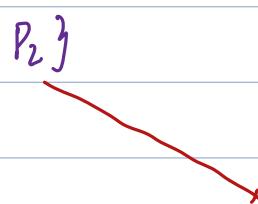
Today's Content:

8 Length of smallest string in A, which contains all occurrences B

If we want to apply 2 pointer on subarray, show me 4 of the below

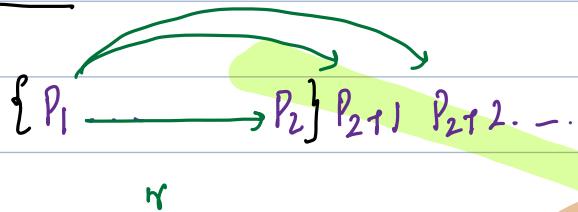


If $P_1 \dots P_2$ is valid
 $\{P_1 \longrightarrow P_2\}$

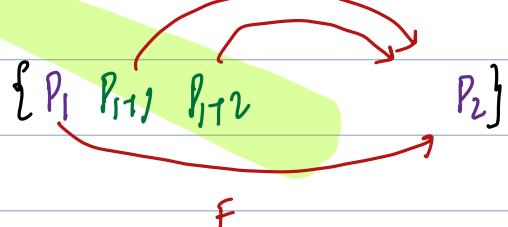
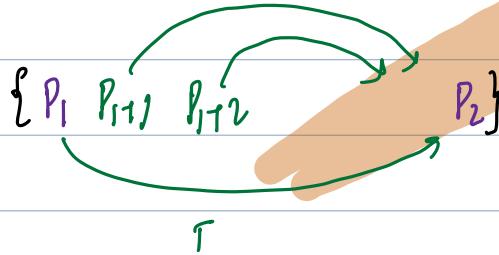
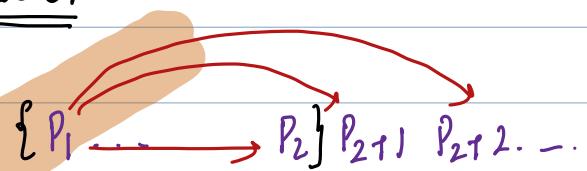


If $P_1 \dots P_2$ is valid
 $\{P_1 \longrightarrow P_2\}$

Case 1:



Case 1:



38: Minimum Window String:

Given two strings $S \sqsubseteq T$ of lengths N and K respectively.

Return length of smallest substring of S which contains all characters of T including duplicates

#Note: $S \sqsubseteq T$ contain only lower case.

Ex1: $T_K = b a b c$

$S_N = b d a c e b a n c b b a c$

Possible: len

$S[0:6]$ \dagger

$S[10:12]$ *

$S[9:12]$ γ

Ideas:

1. Insert $T[]$ in hMT : $\{b:2 \ c:1 \ a:1\}$

Generate all substrings of S :

for a substring of S , check if it contains all characters of T ?

#Substring $S[x:y] = a \ a \ c \ b \ c \ e \ b \ a$

$T[] = b \ a \ b \ c$

#Approach:

Insert $S[x:y]$ in hMS : $\{a:3 \ c:2 \ b:2 \ e:1\}$

$hMT: \{b:2 \ c:1 \ a:1\}$

for every char ch in hMT :

$hMT[ch] \leftarrow hMS[ch]$

TC: $O(K * N^2 * (N + 2b))$ SC: $O(2b) = O(1)$

To generate hMS \rightarrow Two iterate & compare 2 hashmaps.

At max, distinct keys are $2b$, because, Given $S \sqsubseteq T$ contain only smaller alphabets.

Ideas: Optimize using carry forward

Say we have

$s[n..y] = a a c b c e b a$

$T[] = b a b c$

$s[1..y]$

$T_1 =$

To compare both:

trms: $\{a:3 \ c:2 \ b:2 \ e:1\}$

tmt: $\{b:2 \ c:1 \ a:1\}$

Say we have

$s[n..y] = a a c b c e b a \boxed{c}$

Add, new char to hashing trms

$T[] = b a b c$

To compare both:

trms: $\{a:3 \ \boxed{c:3} \ b:2 \ e:1\}$

tmt: $\{b:2 \ \boxed{c:1} \ \boxed{a:1}\}$

TC: $O(k + N^2(1 + 2b))$ SC: $O(2b) \approx O(1)$

To compare both tmt & trms

To generate trms for each substring.

N^2 substring

To generate tmt

Because, we only need to add new char in trms

Ideas: Using BS

0 1 2 3 4

$T_k = b a b c a$

0 1 2 3 4 5 6 7 8 9 10 11 12

$S_N = b d a c e b a n c b b a c$



Target = Min length of substring in S

Search for $m = \text{lo : } 1 \text{ hi : } S.length(); j$

Discard?

$l \quad h \quad m$

1 13 7 : Check if there exists substring of $l \leq m = 7$ which contains all character of T .

Q: We check all substrings of $l \leq m = 7$

7 8 9 10 ..

$ans = m;$

$h = m - 1;$

1 6 3 : Check if there exists substring of $l \leq m = 3$ which contains all character of T .

Q: We check all substrings of $l \leq m = 3$

1 2 3

$l = m + 1;$

TC: $O(\log_2^N \#N) = O(N \log_2 N)$ SC: $O(26) \approx O(1)$

int pair(string s, string t) {

int l = 1, h = s.length(), ans = -1; # if no such substring exist.

while (l <= h) {

int m = (l + h) / 2; # there exists a substring of m

if (check(s, m, t)) { # length in s, which contains all chars in t.

ans = m;

h = m - 1;

else

l = m + 1;

else

return ans;

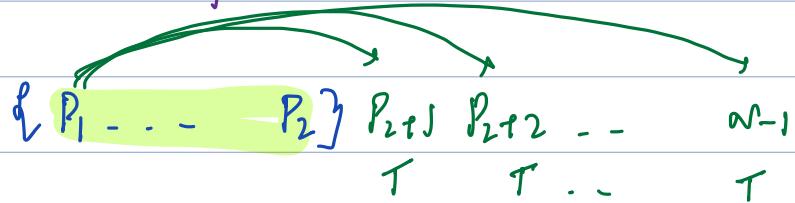
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Ideas: 2 pointers?

say in $s[P_1 \dots P_2]$ we take substring $P_1 \dots P_2$.

if it contains all characters of T . It's a guarantee that $P_1 \dots P_{2+1} \dots P_{2+2} \dots$ will also contain all chars of T .

Above statement falls under below criteria:



Dry Run: $T_k = a \ a \ b \ b \ c$

$P_1 \ 0 \ 1 \ 2 \ 3 \ 4 \ 5 \ 6 \ 7 \ 8 \ 9 \ 10 \ 11 \ 12$

$S_N = c \ a \ b \ a \ a \ c \ c \ e \ b \ a \ b \ a \ c$

P_1

P_2

→ Does TMS contain all char of HMT

$P_1 \ P_2$ Valid ans Update

HMT: {a: 2, b: 2, c: 1}

0 -1 ✗ ✗ P_2++ TMS[s[P2]]++;

TMS: {c: 2, a: 2, b: 2, e: 1}

0 0 ✗ ✗ P_2++ TMS[s[P2]]++;

0 1 ✗ ✗ P_2++ TMS[s[P2]]++;

0 2 ✗ ✗ P_2++ TMS[s[P2]]++;

0 3 ✗ ✗ P_2++ TMS[s[P2]]++;

0 4 ✗ ✗ P_2++ TMS[s[P2]]++;

0 5 ✗ ✗ P_2++ TMS[s[P2]]++;

0 6 ✗ ✗ P_2++ TMS[s[P2]]++;

0 7 ✗ ✗ P_2++ TMS[s[P2]]++;

0 8 ✓ 9 TMS[s[TP1]] -- P1++;

1 8 ✓ 8 TMS[s[TP1]] -- P1++;

2 8 TODO

→ Update high

→ Updating hashmap & pointer.

TC: $O(k + 2N * \{2b + 1 + 1 + 1\})$

SC: $O(2b) \approx O(1)$

↳ # Comparing 2 hashmaps

↳ # Total 2 pointer iterating

TC: $O(k, S_N)$ SC: $O(1)$

$\approx O(k + N)$

→ TLE, if can exceed $> 10^8$ iterations

Dyfny: $Tc: O(k + 2N * \lceil \frac{1}{\epsilon} \rceil + \lceil \frac{1}{\epsilon} \rceil)$ \rightarrow match val $Tc: O(k + N) = O(N + k)$

$T_k = a \ a \ b \ b \ c$ $\xrightarrow{\text{valid}}$ ans \rightarrow hashmap & pr

0 1 2 3 4 5 6 7 8 9 10 11 12

$S_N = \underset{P_1}{\cancel{a}} \underset{P_1}{\cancel{a}} \underset{P_2}{\cancel{a}} \underset{P_2}{\cancel{a}} c \ b \ c \ e \ a \ b \ a \ c$

keep a track of how many of char of tms are matching tmt

psf match := length of T

tmt: {a: 2, b: 2, c: 1}

tms: {c: 1, a: 2, b: 1}

P_1	P_2	match	Valid	ans	Update	Referent	
0	-1	0	*	*	$P_{q+1} \ hms[S[P_2]] + 1$	✓	match _{i+1}
0	0	1	*	*	$P_{q+1} \ hms[S[P_2]] + 1$	✓	match _{i+1}
0	1	2	*	*	$P_{q+1} \ hms[S[P_2]] + 1$	✓	match _{i+1}
0	2	3	*	*	$P_{q+1} \ hms[S[P_2]] + 1$	✓	match _{i+1}
0	3	4	*	*	$P_{q+1} \ hms[S[P_2]] + 1$	*	
0	4	5	*	*	$P_{q+1} \ hms[S[P_2]] + 1$	*	
0	5	4	*	*	$P_{q+1} \ hms[S[P_2]] + 1$	✓	match _{i+1}
0	6	5	✓	7	$hms[S[P_1]] - j \ P_{1+q}$	*	
1	6	5	✓	6	$hms[S[P_1]] - j \ P_{1+q}$	*	
2	6	5	✓	5	$hms[S[P_1]] - j \ P_{1+q}$	✓	match _{--j}

obs:

Add referent char: ch

if ($hms[ch] \leq hmt[ch]$) {

ch is and & it's correct char, Inc count of match by 1

3. $match_{i+1}$

Remove referent char: ch

if ($hmt[ch] > hms[ch]$) {

ch is removed & it's correct char, Dec count of match by 1

match_{--j}

```
int smallestString(string s, string t) {
```

```
    unordered_map<char, int> hmt;  
    for (int i = 0; i < t.size(); i++) {  
        hmt[t[i]]++; // Insert t[i] in hmt;
```

```
    int match = 0;
```

```
    int i = 0, j = -1, ans = INT_MAX;
```

```
    unordered_map<char, int> hms;
```

```
    while (j < s.size()) {
```

```
        if (match == t.size()) { // i..j
```

```
            ans = min(ans, j - i + 1);
```

```
            hms[s[i]]--;
```

```
        if (hms[s[i]] < hmt[s[i]]) {
```

```
            match--;
```

```
        i++;
```

```
    } // i..j
```

```
    if (j == s.size()) { break; }
```

```
    hms[s[j]]++;
```

```
    if (hms[s[j]] <= hmt[s[j]]) {
```

```
        match++;
```

```
    return ans;
```