

Today's Content

1. Sorting Intro
2. Bubble Sort
3. Selection Sort
4. Insertion Sort

Sorting: Arranging data in inc/dec order passed in parameter

0 1 2 3 4 5
Ex1: $A[] = \{2, 3, 9, 12, 17, 19\}$: Inc based on value

0 1 2 3 4 5
Ex2: $A[] = \{19, 6, 5, 2, -1, -19\}$: Dec based on value

0 1 2 3 4 5
Ex3: $A[] = \{2, 7, 4, 9, 6, 10\}$: Inc based on factor
#factor 2 2 3 3 4 4

Sorting library? TC: $O(N \log N)$ To sort N elements.

1. To sort $\text{int arr}[]$:

$\text{sort}(\text{arr}, \text{arr} + n)$; # It will sort $\text{arr}[]$ from $\text{arr}[0]$ to $\text{arr}[N-1]$ in Inc

$\text{sort}(\text{arr}, \text{arr} + n, \text{greater}(\text{int})())$; # It will sort $\text{arr}[]$ in Dec

#include <function> #for greater

2. To sort $\text{vector}(\text{int}) v$:

$\text{sort}(v.\text{begin}(), v.\text{end}())$; # Sort in increasing order

$\text{sort}(v.\text{begin}(), v.\text{end}(), \text{greater}(\text{int})())$; # Sort in Decreasing order

#include <function> #for greater

Stable Sorting: When 2 data points have same value, their relative order should be same, before & after sorting, that type of sorting algo is called stable sorting Algo.

Ex: $\text{arr}[5] = \{1, 5, 2, 6, 2\}$ # Sort inc based on value;

#Sort1 = $\{1, 2, 2, 5, 6\}$ # Sort1 is stable

#Sort2 = $\{1, 2, 2, 5, 6\}$ # Sort2 is unstable

Inplace Sorting:

Sorting Algo with $SC: O(1)$ It is considered as Inplace Sorting.

All Sorting Algorithms

Basic: Selection Sort < Bubble Sort < Insertion Sort

TC : $O(N^2)$ $O(N^2)$ $O(N^2)$

Stable Sort : * ✓ ✓

Inplace Sort : ✓ ✓ ✓

Optimized: Merge Sort Quick Sort Heap Sort

TC :

Stable Sort :

Inplace Sort :

Linear: Count Sort Radix Sort

TC :

Stable Sort :

Inplace Sort :

Selection Sort:

At each step:

Iterate n $arr[]$ select min & bring to its correct position.

$arr[] = \{ 9 \ 8 \ 4 \ 10 \ 6 \ 2 \}$ $mini$: Index with min value

$i=0 \ j:[0 \ 5]$ $\{ 9 \ 8 \ 4 \ 10 \ 6 \ 2 \}$
 $mini=0 \ 1 \ 2 \ 2 \ 2 \ 5$ $MinInd \ 5$ $Swap(arr[0] \ arr[5]);$

$i=1 \ j:[1 \ 5]$ $\{ 2 \ 8 \ 4 \ 10 \ 6 \ 9 \}$
 $mini=1 \ 2 \ 2 \ 2 \ 2$ 2 $Swap(arr[1] \ arr[2]);$

$i=2 \ j:[2 \ 5]$ $\{ 2 \ 4 \ 8 \ 10 \ 6 \ 9 \}$
 $mini=2 \ 2 \ 4 \ 4$ 4 $Swap(arr[2] \ arr[4]);$

$i=3 \ j:[3 \ 5]$ $\{ 2 \ 4 \ 6 \ 10 \ 8 \ 9 \}$
 $mini=3 \ 4 \ 4$ 4 $Swap(arr[3] \ arr[4]);$

$i=4 \ j:[4 \ 5]$ $\{ 2 \ 4 \ 6 \ 8 \ 10 \ 9 \}$
 $mini=4 \ 5$ 5 $Swap(arr[4] \ arr[5]);$

$i=5 \ j:[5 \ 5]$ $\{ 2 \ 4 \ 6 \ 8 \ 9 \ 10 \}$
 $mini=5 \ 5$ 5 $Swap(arr[5] \ arr[5]);$

#Pseudo Code:

$i: 0$ to $N-1$:

Iterate $j: i$ to $N-1$ & calculate $mini$:

$Swap \ arr[mini] \ \& \ arr[i];$

void selection(int ar[], int N) { Tc: $O(N^2)$ Sc: $O(1)$

```

for(int i=0; i<N; i++) {
    # i: j = [i..N-1] & calculate mini j
    int mini = i;
    for(int j=i; j<N; j++) {
        # ar[mini] & ar[j]
        if(ar[j] < ar[mini]) {
            mini = j;
        }
    }
    swap(ar[i], ar[mini]);
}

```

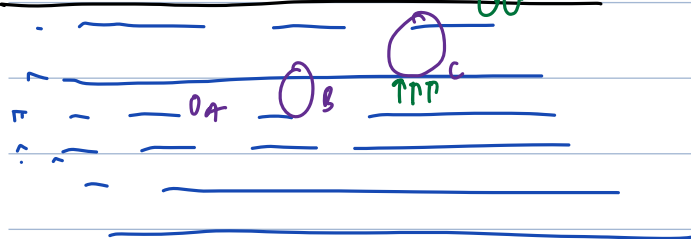
Selection Sort:

	0	1	2	3	4	5			
i=0 j:[0 5] {	6	5	6	3	8	7	}	MinInd	Swap(ar[0] ar[3]);
mini =	0	1	1	3	3	3		3	swap(ar[0] ar[3])

	0	1	2	3	4	5			
i=1 j:[1 5] {	3	5	6	6	8	7	}		
mini =		1	1	1	1	1		1	swap(ar[1] ar[1])

	0	1	2	3	4	5			
i= j:[] {	3	5	6	6	8	7	}	# Issue: Relative order between	
mini =								6 & 6 is changed	

Idea Bubble Sort: Bigger bubble will come out on top.



Bubble Sort : At each iteration

Compare adj elements, if not in correct order swap

Increasing

Note:	0	1	2	3	4	5	
arr[] :	9	8	4	10	6	2	#small optim
i=0:	8	4	9	6	2	10	i=0, j<5; j:=5 stop
i=1:	4	8	6	2	9	10	i=1, j<4; j:=5-1;
i=2:	4	6	2	8	9	10	i=2, j<3; j:=5-2;
i=3:	4	2	6	8	9	10	i=3, j<2; j:=5-3;
i=4:	2	4	6	8	9	10	i → j < N-i-1;
i=5:	2	4	6	8	9	10	

void bubbleSort(int[] arr, int N) { Tc: $O(N^2)$ Sc: $O(1)$

for(int i=0; i<N; i++) {

for(int j=0; j<N-i-1; j++) {

if(arr[j] > arr[j+1]) { # j = N-1: arr[N-1] > arr[N]: Err.
swap arr[j] & arr[j+1];

}

Stability : # Relative order maintained in small elements

arr[] = { 6 3 5 6 4 }

i=0 { 3 5 6 4 6 }

i=1 { 3 5 4 6 6 }

i=2 { 3 4 5 6 6 }

3

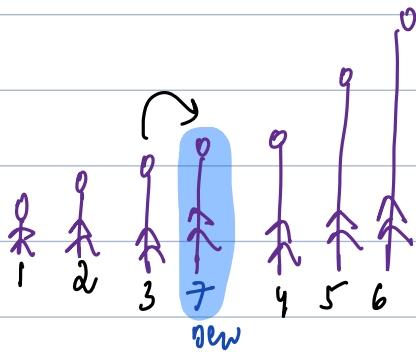
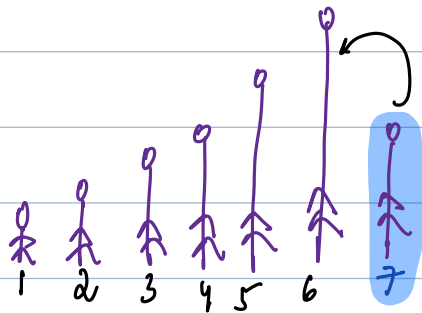
TODO: Check inplace or not.

Insertion Sort:

We insert 1 element in existing sorted data to make entire data sorted.

while (prev person > new person && if no prev ele we stop) {
 We swap

↓
if new person at start position,
no prev person so we can stop



Insertion Sort:

Day Run: Sort Insert
i = [] arr[] arr[] = { 10 | 9 4 8 6 2 }

i = [] arr[]

i = [] arr[]

i = [] arr[]

i = [] arr[]

i = []

void Insertion(int ar[], int N) { TC: $O(N^2)$ SC: $O(1)$

for(int i=0; i < N-1; i++) {

 // i = [0..i] is sorted [0 1 2 .. i] } i+1

 int j = i+1; // Insert in sorted data [0..i];

 while(j > 0 && ar[j-1] > ar[j]) { ~~// j=0 { ar[-1] > ar[0] }~~

 swap ar[j-1] & ar[j]

 j--;

 }

}

}