

Today's Content

1. Row wise & Column wise sum
2. Identity matrix
3. Diagonal Printing

Matrix: Declaration:

→ Rows / Horizontal

1. `int mat[4][5] → Columns / Vertical`

2. `vector<vector<int>> v(4, vector<int>(5));`
→ 4 rows

Matrix Index:

	0	1	2	3	4
0					
1			10		
2					20
3					

$$\rightarrow \text{mat}[1][2] = 10$$

$$\rightarrow \text{mat}[2][4] = 20$$

→ N rows

Q1: $\text{mat}[N][M] \rightarrow N \text{ Columns}$

$\text{mat}[0][0]$	0	1	i	$M-1$	$\text{mat}[0][M-1]$
0				$0, i$			
1				$1, i$			
⋮							
i	$i, 0$	$i, 1$	$i, 2$	i, i	...	$i, M-1$	
⋮							
$N-1$				$N-1, i$			$\text{mat}[N-1][M-1]$
$\text{mat}[N-1][0]$							

obj:

1. Iterate M in Row: Col range $\{0..M-1\}$

2. Iterate N in Col: Row range $\{0..N-1\}$

Q Sum of elements in each row

fn: `mat[4][5];`

	0	1	2	3	4
0	10	20	30	40	50
1	1	2	3	4	5
2	6	7	8	9	10
3	10	20	30	40	50

Output

150

15

40

150

Ideal: For every row, iterate & calculate sum & print

```
void sumRow(int mat[][], int N, int M){  
    for(int i=0; i<N; i++){  
        # i: Row; iterate & calculate sum.  
        long sum=0;  
        for(int j=0; j<M; j++){  
            sum = sum + mat[i][j];  
        }  
        print(sum);  
    }  
}
```

TC: $O(N \cdot M)$ SC: $O(1)$

Q Sum of elements in each col

fn: `mat[4][5];`

	0	1	2	3	4
0	10	20	30	40	50
1	1	2	3	4	5
2	6	7	8	9	10
3	10	20	30	40	50

void colRow(int mat[], int N, int M)

```
for(int j=0; j<M; j++){  
    # j: Column, iterate & calculate sum;  
    long sum=0;  
    for(int i=0; i<N; i++){  
        sum = sum + mat[i][j];  
    }  
    print(sum);  
}
```

TC: $O(N \cdot M)$ SC: $O(1)$

Output:

27 49 71 93 115

Identity Matrix: $N = M$

Given a square matrix, check if its identity matrix or Not.

An identity matrix, all main diagonal has only 1 and all other cells 0.
↳ $\text{mat}[r][c], r=c$.

Ex1:

$$I = 0 \begin{bmatrix} 0 & 1 & 2 & 3 \\ 1 & 0 & 0 & 0 \\ 2 & 0 & 0 & 1 \\ 3 & 0 & 0 & 0 \end{bmatrix}$$

Ex2:

$$I = 0 \begin{bmatrix} 0 & 1 & 2 \\ 1 & 0 & 0 \\ 2 & 0 & 1 \end{bmatrix}$$

Ex3:

$$I = 0 \begin{bmatrix} 0 & 1 & 2 \\ 1 & 0 & 0 \\ 2 & 0 & 1 \end{bmatrix}$$

Idea:

Note:

Ex3:

$$I = 0 \begin{bmatrix} 0 & 1 & 2 \\ 1 & 0 & 0 \\ 2 & 0 & 1 \end{bmatrix}$$

Ex4:

$$I = 0 \begin{bmatrix} 0 & 1 & 2 \\ 2 & 3 & 4 \\ 1 & 4 & 3 \\ 1 & 6 & 6 \end{bmatrix}$$

```
public int solve(int[][] A){
```

Dry Run:

$$I = 0 \begin{bmatrix} 0 & 1 & 2 \\ 1 & 0 & 0 \\ 0 & 1 & 0 \\ 1 & 0 & 1 \end{bmatrix}$$

2.8 Given a mat[N][N] print both main diagonals in new line.

fn1: mat[4][4]; square

	0	1	2	3
0	6	7	3	4
1	9	3	2	8
2	4	7	6	9
3	10	3	2	9

Output

d1 (L→R) : 6 3 6 9

d2 (R→L) : 4 2 7 10

1.1.1.1:

d1: (L→R)

	0	1	2	3
0	0,0	7	3	4
1	9	1,1	2	8
2	4	7	2,2	9
3	10	3	2	3,3

i=0;

print(mat[0][0]) i++

print(mat[1][1]) i++

print(mat[2][2]) i++

print(mat[3][3]) i++

i=4; stop

d2:

i=0, j=3

print(mat[0][3]) i++, j--

print(mat[1][2]) i++, j--

print(mat[2][1]) i++, j--

print(mat[3][0]) i++, j--

i=4, j=-1; stop.

Notes:

1. If single variable based loops: Prefer for loop

2. If >1 variable based loops: Prefer while loop.

```
void printdiagonal (int mat[][], int N) {
```

#Printing d₁: L → R

```
for (int i = 0; i < N; i++) { TC: O(N)
```

```
    print (mat[i][i]);
```

}

#Printing d₂: R → L

```
int i = 0, j = N - 1;
```

```
while (i < N && j >= 0) {
```

```
    print (mat[i][j]);
```

```
    i++; j--;
```

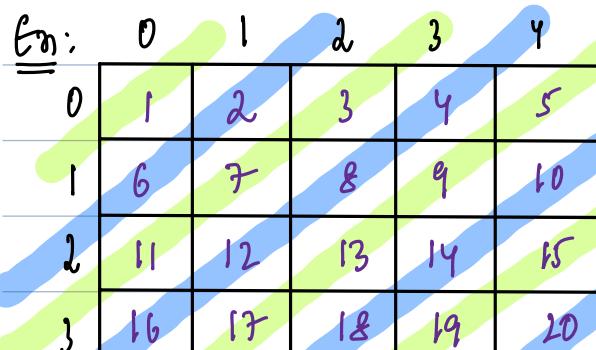
}

3

Q8

Given a $\text{mat}[N][N]$

Print all diagonals going from Right to Left & Top to down.

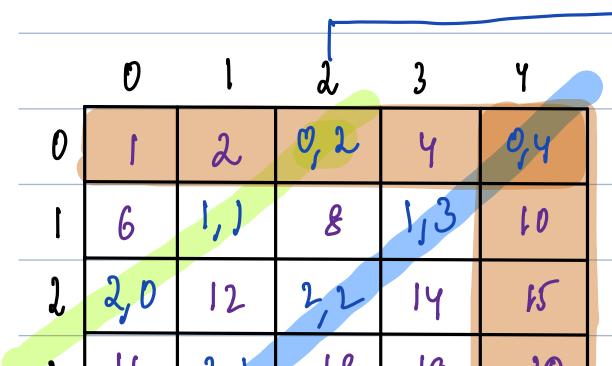
Ex: 

Output:

1
2 6
3 7 11
4 8 12 16
5 9 13 17
10 14 18
15 19

Hint:

20



Start # Start

i, j i, j
 $i+1, j$ $i+1, j$
 $i, j+1$ $i, j+1$
 $i+1, j+1$ $i+1, j+1$

Diagram showing the traversal order of the matrix. The matrix is 4x5. The traversal starts at (0,0) and moves right-to-left and top-to-bottom. The path is: (0,0) → (1,0) → (2,0) → (3,0) → (0,1) → (1,1) → (2,1) → (3,1) → (0,2) → (1,2) → (2,2) → (3,2) → (0,3) → (1,3) → (2,3) → (3,3) → (0,4) → (1,4) → (2,4) → (3,4).

void printRL(int mat[], int N, int M, int i, int j) {

(i, j) is start of R→L diagonal

while(i < N & & j >= 0) {

 print(mat[i][j]);

 i++; j--;

#Idea: R→L diagonals.

1. They can start at 0th row: Iterate q till every cell in 0th row is start point
2. They can start at last col: Iterate q till every cell in last col is start point

void printRL(int mat[][], int N, int M, int i, int j){

#(i, j) is start of R→L diagonal

while(i < N && j >= 0){

 print(mat[i][j]);

 i++; j--;

}

}

void printdiagonal(int mat[][], int N, int M){ TC: O(N*M) SC: O(1)}

#Step1: Print diagonals starting at 0th row j= 0

for(int j=0; j < M; j++) {

Start point = (0, j)

 printRL(mat, N, M, 0, j);

}

i=0	0	1	2	3	4
0	1	2	0, 2	4	0, 4
1	6	1, 1	8	1, 3	10
2	2, 0	12	2, 2	14	15
3	16	3, 1	18	19	20

#Step2: Print diagonals start at last col

for(int i=1; i < N; i++) {

Start point = (i, M-1)

 printRL(mat, N, M, i, M-1);

}

i=0	0	1	2	3	4
0	1	2	0, 2	4	0, 4
1	6	1, 1	8	1, 3	10
2	2, 0	12	2, 2	14	15
3	16	3, 1	18	19	20