

Todays Content

1. SCRT ✓

2. Painter Partition.

Q: Given τ find $SQRT(N)$

Find greatest i such that $i^2 \leq N$

$SQRT(25)$: return 5

$SQRT(37)$: $5^2 \leq 37$, $6^2 \leq 37$, $7^2 \leq 37$ return 6.

$N = 30$

i $i^2 \leq N$ ans =

1 $1^2 \leq 30$ ans = 1 ✓

2 $2^2 \leq 30$ ans = 2 ✓

3 $3^2 \leq 30$ ans = 3 ✓

4 $4^2 \leq 30$ ans = 4 ✓

5 $5^2 \leq 30$ ans = 5 ✓

6 $6^2 \leq 30$ return ans = 5

int $SQRT(\text{int } N)$ { TC: $O(\sqrt{N})$ SC: $O(1)$

int $i=1$, ans = 0; $\rightarrow i^2 \leq N \Rightarrow i \leq \sqrt{N}$

while [$i^2 \leq N$]

 ans = i ; # update ans

$i+1$; # looks for better ans

return ans;

}

Ideas:

1. Target: Greatest i , with $i^2 \leq N$.

2. Search Space: Space where we search for target, it can be imaginary

$S_1: [1.. \sqrt{N}] \rightarrow$ We don't know \sqrt{N}

$S_2: [1.. N/2]$, if $N=1$, search space $[1.. 0] *$

$S_3: [1.. N]$, if $N=1$, search spa $[1.. 1]$ ✓

Note: In your search space it should contain target for every el.

3. Discard

$N=30$ Search Space $[1.. N]$ # Imaginary: No need to store

l	h	m	l	m	h	
1	30	15	$M^2 m \leq 30$	{ 1	15 16 17 ... 30 }	$h=m-1$;
1	14	7	$M^2 m \leq 30$	{ 1	7 8 9 ... 14 }	$h=m-1$;
1	6	3	$M^2 m \leq 30$	{ 1	3	$ans=3, l=m+1$
4	6	5	$M^2 m \leq 30$	{ 4	5	$ans=5, l=m+1$
6	6	6	$M^2 m \leq 30$	{ 6	6	$h=m-1$;
6	5					return ans = 5.

Constraints:

$$1 \leq N \leq 10^{18} \rightarrow \text{sqrt} = \left[\frac{1}{10^9}, \frac{10^{18}}{10^9} \right] \# \text{ if we take } 1..10^9, \text{ product of } m^*m \text{ will be in long range}$$

int Sqrt(int N){

int l=1, h=N $\sqrt{10^9}$, min(N, 10⁹), ans=0;

Note: Think about datatype

while(l <= h){

long m = (l+h)/2;

if(m*m <= N){

ans=m;

l=m+1;

else { # m*m > N goto left }

h=m-1;

} return ans;

Note: #Search Space Size {1..N} : # N Elements

Tc: $O(\log_2 N)$ Sc: $O(1)$

Q1:

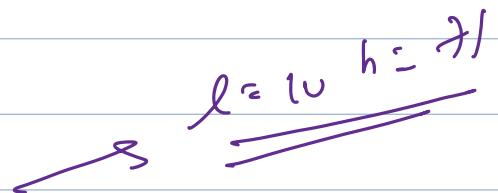
We have to paint N boards of length $\{c_0, c_1, c_2, \dots, c_{N-1}\}$

There are W painters available and each of them takes 1 unit of time to paint 1 unit of board

Calculate & return the minimum time required to paint all boards

Notes:

1. Two painters cannot share a board to paint, A board cannot be painted partially by 1 painter & partially by another.
2. A painter can only paint contiguous boards
3. All painters start work at same time.



$E_n:$	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	<u>Time Taken</u>
$N=15$	3	5	1	7	8	2	5	3	10	1	4	7	5	4	6	34.
$W=3$	$W_1=34$						$W_2=15$				$W_3=22$					31.
	$W_1=31$						$W_2=18$				$W_3=22$					25
	$W_1=24$						$W_2=25$				$W_3=22$					

$E_{n2}:$ 0 1 2 3 4 5

$ar[6] = 1 1 1 1 1 101$ Time Taken

$W=2$ $W_1=5$ $W_2=101$: 101

Idea: Average Time will not work, as seen in above example

$l = \text{smallest val pos}$

$h = \text{greatest val pos.}$

Search:

Target: Min time taken to paint all boards

Search Space: Should be based on time:

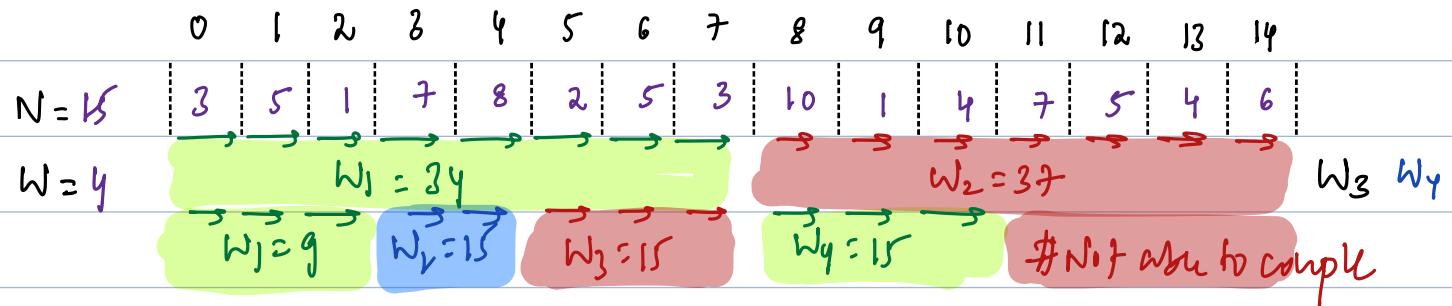
{ l } { h }

A smallest time to paint all boards l : Min of ar[6]

A greatest time to paint all boards l : Sum of ar[6]

} $\left\{ \begin{array}{l} \text{for every input} \\ \text{ar[6] in search space} \end{array} \right\}$

Discard?



$l \quad h \quad m$

10 71 40 : Check if we can paint all boards $x=40$ mins ✓

ans = 40; goto left

[$l \quad m \quad m+1 \quad m+2 \dots \quad h$]

if we can do task in m time:

We can do task in $m+1, m+2 \dots$

update m & goto better ans m left.

#Sorry $m = 15$.

m

15: Check if we can paint all boards $x=15$ mins

[$l \dots m-1 \quad m \quad m+1 \dots \dots \quad h$]

if we cannot do task in m time:

We cannot do task in $m-1, m-2 \dots$

goto right

Check function Idea:

$W=4$	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14
$N=15$	3	5	1	7	8	2	5	3	10	1	4	7	5	4	6
$M=40; S=0 \rightsquigarrow 3 \rightsquigarrow 8 \rightsquigarrow 9 \rightsquigarrow 16 \rightsquigarrow 24 \rightsquigarrow 26 \rightsquigarrow 3 \rightsquigarrow 34 \rightsquigarrow 10 \rightsquigarrow 11 \rightsquigarrow 15 \rightsquigarrow 22 \rightsquigarrow 27 \rightsquigarrow 31 \rightsquigarrow 37 \dots$															

$p=1 \longrightarrow p_{11} \quad 2 \quad p=2 \leftarrow 4$

$W=4$	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14
$N=15$	3	5	1	7	8	2	5	3	10	1	4	7	5	4	6
$M=24; S=0 \rightsquigarrow 3 \rightsquigarrow 8 \rightsquigarrow 9 \rightsquigarrow 16 \rightsquigarrow 24 \rightsquigarrow 26 \rightsquigarrow 2 \rightsquigarrow 10 \rightsquigarrow 11 \rightsquigarrow 21 \rightsquigarrow 4 \rightsquigarrow 11 \rightsquigarrow 16 \rightsquigarrow 20 \rightsquigarrow 26 \rightsquigarrow 6$															

$p=1 \longrightarrow p_{11} \quad 2 \longrightarrow p_{11} \quad 3 \longrightarrow p_{11} \quad y \quad p=4 \leftarrow 4$

$W=4$	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14
$N=15$	3	5	1	7	8	2	5	3	10	1	4	7	5	4	6
$M=16; S=0 \rightsquigarrow 3 \rightsquigarrow 8 \rightsquigarrow 9 \rightsquigarrow 16 \rightsquigarrow 24 \rightsquigarrow 10 \rightsquigarrow 15 \rightsquigarrow 3 \rightsquigarrow 18 \rightsquigarrow 13 \rightsquigarrow 14 \rightsquigarrow 4 \rightsquigarrow 11 \rightsquigarrow 16 \rightsquigarrow 9 \rightsquigarrow 10$															

$p=1 \longrightarrow p_{11} \quad 2 \rightarrow p_{11} \quad 3 \rightarrow p_{11} \quad 4 \rightarrow p_{11} \quad 5 \quad p=5 > 4$

$b \quad h \quad m: \text{Job } b/2$ Can we finish tasks in m time update

10 71 40: Can we finish tasks in 40m $ans = 40; h = m - 1;$

10 39 24: Can we finish tasks in 24m $ans = 24; h = m - 1;$

10 23 16: Can we finish tasks in 16m $b = m + 1;$

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int minTime(restrint) b; int N, int w){
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int l = max of b, h = sum of b, ans = 0;
while(l <= h){

int m = (l + h)/2;

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if( check(b, m, w)){
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ans = m;

h = m - 1;

else{

l = m + 1;

return ans;

}

```
bool check(restrint) rb, int m, int w){
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int p = 1, s = 0,

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for( int i = 0; i < b.size(); i++) {
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s = s + b[i];

if(s > m){ # i^th task allocates new person

p++;

s = b[i];

}

return p <= w; # p = person used & w = workers allocated

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