

Today's Content

1. Re-arrange arr[]
2. Count frequency of all elements.

Few Basics:

1. Say $a > 0$ & $a < M$:

$$a \% M = a; \quad \text{Ex: } 5 \% 7 = 5 \quad 2 \% 10 = 2$$

$$a / M = 0; \quad \text{Ex: } 5 / 7 = 0 \quad 2 / 3 = 0$$

Modular:

Given an $ar[N]$ re-arrange array value, such that $ar[i] = ar[ar[i]]$

Note: all array elements are unique.

Constraints:

$$1 \leq N \leq 10^5$$

$$0 \leq ar[i] < N$$

Ex: $ar[N] = \begin{matrix} & 0 & 1 & 2 & 3 & 4 & 5 & 6 & 7 \\ \{ & 6 & 4 & 2 & 1 & 7 & 0 & 3 & 5 \} \end{matrix}$

$$ar[i] = ar[ar[i]]$$

$$b[] = \{ 3, 7, 2, 4, 5, 6, 1, 0 \}$$

Idea1: 1. Create $b[]$;

$$TC: O(N+N) = O(N) \quad SC: O(N)$$

2. $i = 0; i < N; i++$


$$b[i] = ar[ar[i]]$$

3. Copy $b[] \rightarrow ar[]$

$i = 0; i < N; i++$

$$ar[i] = b[i]$$

Idea2: Iterate on $ar[i]$ & make $ar[i] = ar[ar[i]]$

$$ar[N] = \begin{matrix} & 0 & 1 & 2 & 3 & 4 & 5 & 6 & 7 \\ \left\{ \begin{array}{l} \cancel{6} \\ \underline{3} \end{array} \right. & \left\{ \begin{array}{l} \cancel{4} \\ \underline{7} \end{array} \right. & \left\{ \begin{array}{l} \cancel{2} \\ \underline{2} \end{array} \right. & \left\{ \begin{array}{l} \underline{1} \\ \cancel{7} \end{array} \right. & \left\{ \begin{array}{l} \cancel{7} \\ \underline{5} \end{array} \right. & \left\{ \begin{array}{l} \underline{0} \\ \cancel{3} \end{array} \right. & \left\{ \begin{array}{l} \underline{3} \\ \cancel{7} \end{array} \right. & \left\{ \begin{array}{l} \underline{5} \\ \cancel{3} \end{array} \right. \end{matrix}$$


Issue: If we update $ar[i] = ar[ar[i]]$ we will end up losing data

Catch: We need old & new value, without extra space?

#Iden2: No Extra Space

#hrs Since Bing Bang	Days	Time
100 hrs	4	4hrs = 4 am
40 hrs	1	16hrs = 4 pm
78 hrs	3	6hrs = 6 am
n hrs	$n/24$	$n\%24$

Obs: In n , Both day & Time are present
 $n/24 = \text{Days}$ $n\%24 = \text{Time}$

Hint: $0 \leq \text{arr}[i] < N \Rightarrow [0..N-1] \Rightarrow \text{Specifying } i, N = [0..N-1]$
In $\text{arr}[i]$: Store old & new value together

Case 1:

$$\text{arr}[i] \begin{cases} \rightarrow \text{arr}[i] \% N = \text{new} : \text{rem} \\ \rightarrow \text{arr}[i] / N = \text{old} : \text{quo} \end{cases}$$

$$\boxed{\text{arr}[i] = \text{old} * N + \text{new}}$$

$$\begin{aligned} \text{arr}[i] / N &= (\text{old} * N + \text{new}) / N \\ &= (\text{old} * N / N + \text{new} / N) \\ &= (\text{old} + 0) \\ &= \text{old} \end{aligned}$$

$$\begin{aligned} \text{arr}[i] \% N &= (\text{old} * N + \text{new}) \% N \\ &= (\text{old} * N \% N + \text{new} \% N) \% N \\ &= (0 + \text{new} \% N) \% N \\ &= (\text{new}) \% N = \text{new} \end{aligned}$$

Case 2:

$$\text{arr}[i] \begin{cases} \rightarrow \text{arr}[i] \% N = \text{old} : \text{rem} \\ \rightarrow \text{arr}[i] / N = \text{new} : \text{quo} \end{cases}$$

$$\boxed{\text{arr}[i] = N * \text{new} + \text{old}}$$

$$\begin{aligned} \text{arr}[i] / N &= (N * \text{new} + \text{old}) / N \\ &= (N * \text{new} / N + \text{old} / N) \\ &= (\text{new} + 0) \\ &= \text{new} \end{aligned}$$

$$\begin{aligned} \text{arr}[i] \% N &= (N * \text{new} + \text{old}) \% N \\ &= ((N * \text{new}) \% N + \text{old} \% N) \% N \\ &= (0 + \text{old} \% N) \% N \\ &= (\text{old} \% N) \\ &= \text{old} \end{aligned}$$

Approach: $ar[i] = old * N + new$

0	1	2	3	4	5	6	7
6	4	2	1	7	0	3	5

$ar[N] = \{ 6 \quad 4 \quad 2 \quad 1 \quad 7 \quad 0 \quad 3 \quad 5 \}$

#Step1: Iterate on $ar[]$ multiply by N

0	1	2	3	4	5	6	7
6^*8	4^*8	2^*8	1^*8	7^*8	0^*8	3^*8	5^*8

$ar[N] = \{ 6^*8 \quad 4^*8 \quad 2^*8 \quad 1^*8 \quad 7^*8 \quad 0^*8 \quad 3^*8 \quad 5^*8 \}$

#Step2: Iterate on $ar[]$ & add new value to all elements

0	1	2	3	4	5	6	7
6^*8+3	4^*8+7	2^*8+2	1^*8+4	7^*8+5	0^*8+6	3^*8+1	5^*8+0

$ar[N] = \{ 6^*8+3 \quad 4^*8+7 \quad 2^*8+2 \quad 1^*8+4 \quad 7^*8+5 \quad 0^*8+6 \quad 3^*8+1 \quad 5^*8+0 \}$

$$ar[0] += ar[ar[0]/N] = ar[6]/N = 3$$

$$ar[1] += ar[ar[1]/N] = ar[4]/N = 7$$

$$ar[2] += ar[ar[2]/N] = ar[2]/N = 2$$

$$ar[3] += ar[ar[3]/N] = ar[1]/N = 6$$

$$ar[i] += ar[ar[i]/N]/N$$

#Step3: Iterate on $ar[]$ & update $ar[i] = ar[i] \% N$

0	1	2	3	4	5	6	7
6^*8+3	4^*8+7	2^*8+2	1^*8+4	7^*8+5	0^*8+6	3^*8+1	5^*8+0

$ar[N] = \{ 6^*8+3 \quad 4^*8+7 \quad 2^*8+2 \quad 1^*8+4 \quad 7^*8+5 \quad 0^*8+6 \quad 3^*8+1 \quad 5^*8+0 \}$

0	1	2	3	4	5	6	7
3	7	2	4	5	6	1	0

$ar[N] = \{ 3 \quad 7 \quad 2 \quad 4 \quad 5 \quad 6 \quad 1 \quad 0 \}$

vector<int> re-arrange(vector<int> &arr) { Tc: $O(N)$ Sc: $O(1)$

TODD

}

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Constraints:

$$0 \leq ar[i] < N$$

Ex: $ar[5] = \{ \overset{0}{2} \overset{1}{4} \overset{2}{4} \overset{3}{0} \overset{4}{3} \}$

Output

0: 1

1: 0

2: 1

3: 1

4: 2

Idea1: For every element from $[0..N-1]$:

Iterate on array & get frequency & print it.

TC: $O(N*N) = O(N^2)$ SC: $O(1)$

Idea2: At $ar[i]$: Store ele & its freq information.

Way1: $ar[i] \begin{cases} \rightarrow ar[i]/N = ele : quo \\ \rightarrow ar[i]\%N = freq : rem \end{cases}$

$$ar[i] = N * ele + freq$$

$$ar[i]\%N = (N * ele + freq)\%N$$

$$= [(N * ele)\%N + freq\%N]\%N$$

$$(0 + freq\%N)\%N$$

$(freq\%N)$: Is ele: At max $freq = N$. If all ele are same

if $freq = N$: $(freq\%N) = 0$

Way 2: $ar[i] \begin{cases} \rightarrow ar[i]/N = \text{freq} : Qu \\ \rightarrow ar[i]\%N = ele : rem \end{cases}$

$$ar[i] = \text{freq} * N + ele$$

$$ar[i]\%N$$

$$(\text{freq} * N + ele) \% N$$

$$((\text{freq} * N) \% N + ele \% N) \% N$$

$$= (0 + ele \% N) \% N$$

$$= (ele) \% N$$

$$= ele$$

$$ar[i]/N$$

$$(\text{freq} * N + ele) / N$$

$$(\text{freq} * N / N + \underline{ele / N})$$

$$(\text{freq} + 0)$$

$$= \text{freq}$$

#DryRun $ar[i] = \text{freq} * N + ele$

	0	1	2	3	4	5	6	7
Ex: $ar[8] = \{$	2	4	4	5	2	3	5	2

Step 1: Iterate $ar[]$ & store freq

	0	1	2	3	4	5	6	7
Ex: $ar[8] = \{$	2	4	4 + 3N	5 + N	2 + 2N	3 + 2N	5	2

$$\begin{aligned} & i = 0; i < N; i++ \{ \\ & \quad ar[ar[i]\%N] += N \end{aligned}$$

Step 2: Iterate m $ar[]$ & print freq

	0	1	2	3	4	5	6	7
Ex: $ar[8] = \{$	2 0	4 0	4 + 3N	5 + N	2 + 2N	3 + 2N	5	2

$ar[] = \{$	0	0	3	1	2	2	0	0
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$$\begin{aligned} & i = 0; i < N; i++ \{ \\ & \quad ar[i] = ar[i] / N \end{aligned}$$