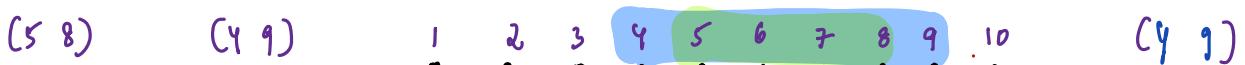
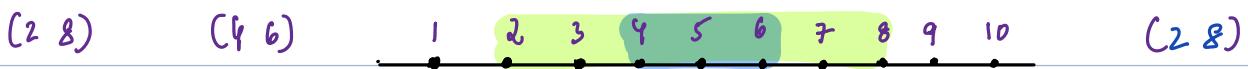
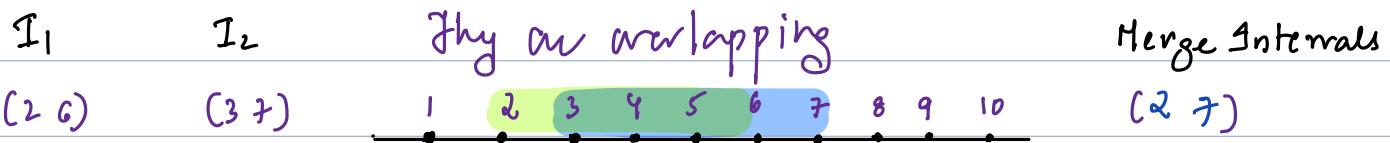


Todays Content

- 1. Overlapping Intervals
- 2. Insert in overlapping intervals.

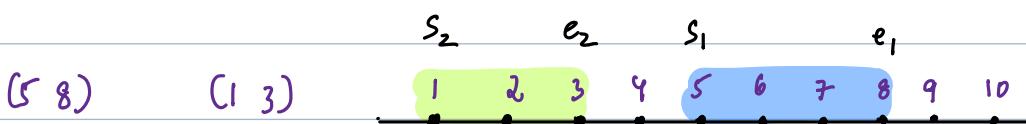
Merge Intervals: Any Interval: $[s \dots e]$



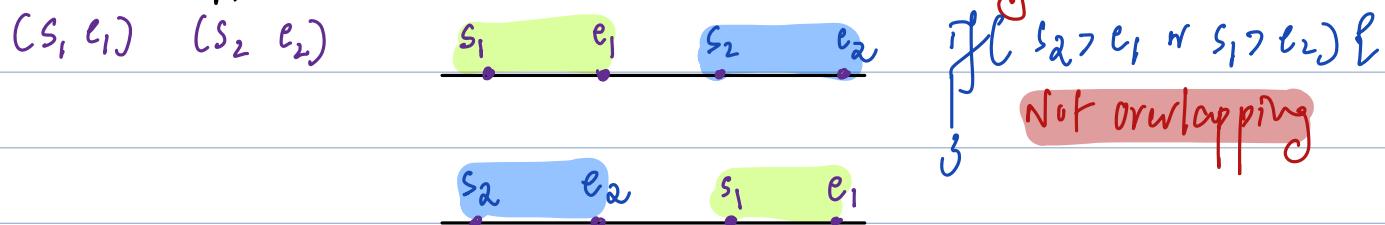
Overlapping Intervals:

I_1 I_2 Say Overlapping New Interval
 (s_1, e_1) (s_2, e_2) $(\min(s_1, s_2), \max(e_1, e_2))$

Non Overlapping:



Non Overlapping Case:



Q1: Given collection of intervals in a 2D array format, which are sorted-based on their start time.

Merge all overlapping intervals & return set of non-overlapping intervals

Note: If intervals are not already sorted, sort them.

Ex1: Intervals:

	0	1	Current Interval	New Interval
0	0	2	$\{0, 2\}$	$\{0, 1\}$
1	1	4	$\{0, 2\} = \{0, 4\}$	$\{0, 4\}$
2	5	6	$\{0, 4\} = \{5, 6\}$	$\{5, 10\}$
3	6	8	$\{5, 6\} = \{5, 8\}$	$\{12, 14\}$
4	7	10	$\{5, 8\} = \{5, 10\}$	
5	8	9	$\{5, 10\} = \{5, 10\}$	
6	12	14	$\{5, 10\} = \{12, 14\}$	
↗ #outside stop			$\{12, 14\}$	

Ex2: Intervals:

	0	1	Current Interval	New Interval
0	0	3	$\{0, 3\}$	$\{0, 1\}$
1	1	5	$\{0, 3\} \quad \{0, 5\}$	$\{0, 7\}$
2	4	7	$\{0, 5\} \quad \{0, 7\}$	$\{9, 14\}$
3	9	12	$\{0, 7\} \quad \{9, 12\}$	$\{17, 34\}$
4	10	14	$\{9, 12\} \quad \{9, 14\}$	
5	17	20	$\{9, 14\} \quad \{17, 20\}$	
6	19	24	$\{17, 20\} \quad \{17, 24\}$	
7	21	25	$\{17, 24\} \quad \{17, 25\}$	
8	24	34	$\{17, 25\} \quad \{17, 34\}$	
↗ #outside stop			$\{17, 34\}$	

TC: O(n) SC: O(1)

s e

vector<pair<int, int>> MergeAll(vector<pair<int, int>> arr){
 sort(arr.begin(), arr.end()); // Sorting based on start time

vector<pair<int, int>> newInterval;
 pair<int, int> cg = arr[0]; // cg current interval

```

for(int i=1; i < arr.size(); i++) {
  // current Interval cg arr[i].s arr[i].e cg.s cg.e
  // latest Interval arr[i]
  if(cg.e < arr[i].s || arr[i].e < cg.s) { # Not overlapping
    newInterval.push_back(cg); # inserting
    cg = arr[i]; # updating
  } else { # overlapping merge
    cg.s = min(arr[i].s, cg.s);
    cg.e = max(arr[i].e, cg.e);
  }
}
newInterval.push_back(cg);
return newInterval;
  
```

Note: In above code

$$cg.s = cg.\text{first}, cg.e = cg.\text{second}$$

$$arr[i].s = arr[i].\text{first}, arr[i].e = arr[i].\text{second}.$$

Q. Given N sorted non overlapping Interval, Insert a new Interval in them, { Merge if Necessary }
 Return set of non-overlapping Intervals

	Interval	Insert [12 22]	ans Interval
0	[1 3]	{[12, 22]}	{[1 3]}
1	[4 7]	{[12, 22]}	{[4 7]}
2	[10 14]	{[12, 22]} {[10, 22]}	{[10 29]}
3	[16 19]	{[10, 22]} {[10, 22]}	[27 30]
4	[21 24]	{[10, 22]} {[10, 24]}	[32 35]
5	[27 30]	{[10, 24]}	[38 41]
6	[32 35]		[43 50]
7	[38 41]		
8	[43 50]		

	Interval	Insert [12 22]	ans Interval
0	[1 5]	{[12, 22]}	{[1 5]}
1	[8 10]	{[12, 22]}	[8 10]
2	[11 14]	{[12, 22]} {[11, 22]}	{[11, 24]}
3	[15 20]	{[11, 22]} {[11, 22]}	[27 30]
4	[21 24]	{[11, 22]} {[11, 24]}	[32 36]
5	[27 30]	{[11, 24]}	
6	[32 36]		

#Idea: TC: O(N) SC: O(1)

Insert new interval $\{ns, ne\}$

Iterate on current interval: $\{cs, ce\}$

if ($ce < ns$ or $ne < cs$) { #Not overlapping

 if ($ce = ns$) { #current interval comes first $\{cs, ce\}$ $\{ns, ne\}$

 Insert current interval in ans ✓✓

 } else { $\{ns, ne\}$ $\{cs, ce\}$

 Insert new interval in ans;

 Iterate & insert all current intervals in ans

 return ans;

}

else { #overlapping. ✓✓✓

 ns = min(cs, ns);

 ne = max(ce, ne);

}

Insert new interval in ans; #Edge Case, if we come outside loop.
return ans;

Ex3: Interval

Insert $[12, 22]$

ans Interval

$[1, 5]$ $[12, 22]$

$[1, 5]$

$[8, 10]$ $[12, 22]$

$[8, 10]$

$[11, 14]$ $[12, 22]$ $\{11, 22\}$

$\{11, 22\}$

$[15, 20]$ $\{11, 22\}$ $\{11, 22\}$

$[21, 24]$ $\{11, 22\}$

$\{11, 22\}$

#outside

$\{11, 22\}$

`vector<pair<int, int>> Insert (vector<pair<int, int>> &arr, pair<int, int> p)`