

Today's Content

1. Peak Element
2. Find Unique Element

Google:

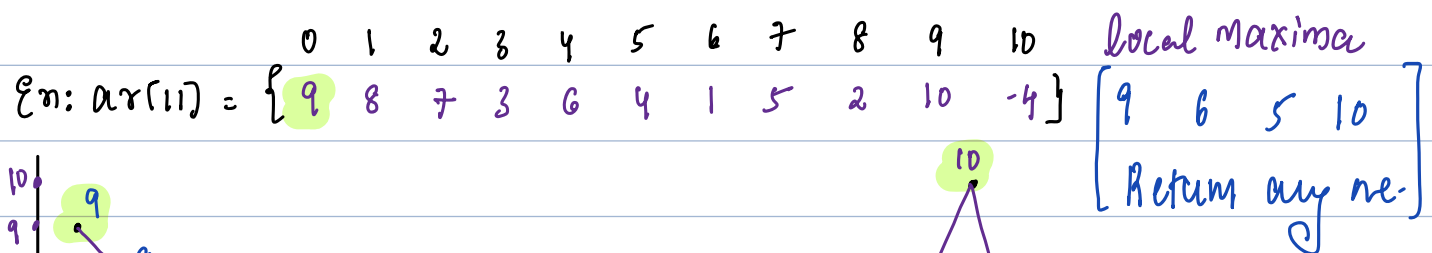
Given a unsorted arr[] with all distinct elements return any one local maxima

local maxima: An element is said to be local maxima, if $>$ than its adjacent elements {immediate left & right}

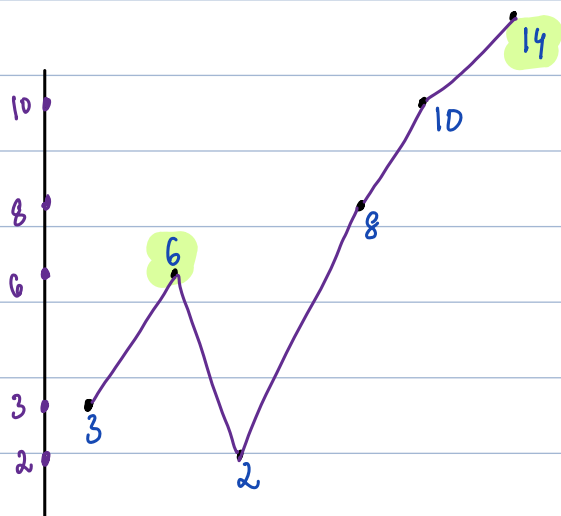
$arr[i]$ local maxima: $arr[i] > arr[i-1]$ & $arr[i] > arr[i+1]$

$arr[0]$ local maxima: $arr[0] > arr[1]$

$arr[n-1]$ local maxima: $arr[n-1] > arr[n-2]$



Ex: $arr[6] = \{3, 6, 2, 8, 10, 14\}$ local maxima = 6, 14 Return any one



Idea 1: Iterate on $arr[]$ TC: $O(N)$ SC: $O(1)$

for every $arr[i]$: Compare with adj
if its local maxima return it

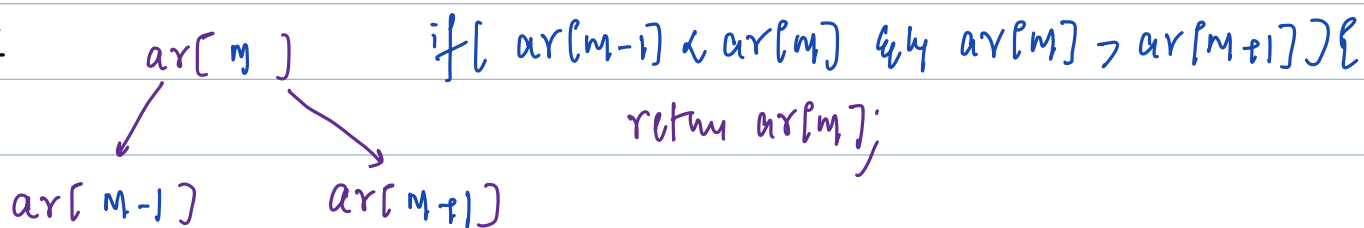
Idea 2: Iterate on $arr[]$: TC: $O(N)$ SC: $O(1)$

calculate & return max of $arr[]$

Idea:

Target = Any One local maxima Search Space = $\ln arr[]$

Case-1



Case-2 if $[arr[m] < arr[m+1]]$ { #go to right, it's a guarantee, local maxima }

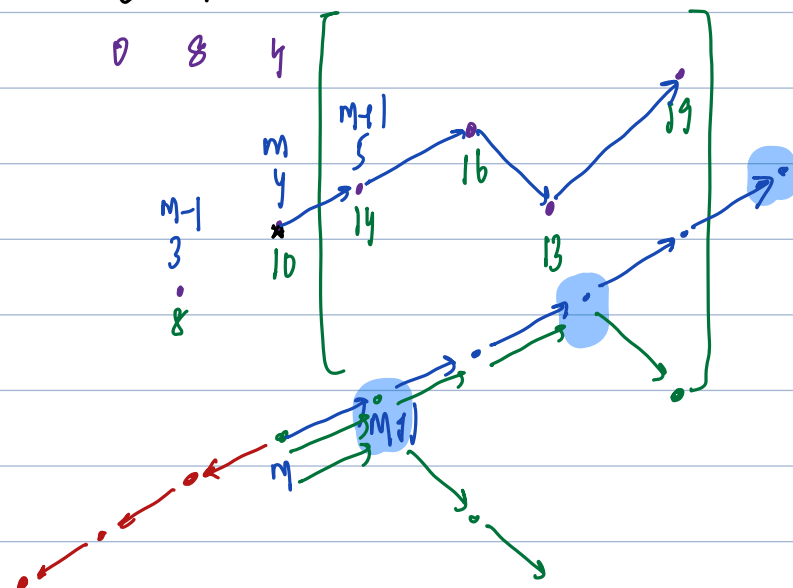
$arr[m+1]$

0 1 2 3 4 5 6 7 8 cnits

6 4 12 8 10 14 16 13 19

l h m

0 8 4



Case-3 if $[arr[m-1] > arr[m]]$ {

#go to left

$arr[m-1]$

$arr[m]$

$arr[m+1]$

Case-IV: If Both sides are inc, go anywhere to get local maxima

$arr[m-1]$

$arr[m+1]$

$arr[m]$

#obs: Go to side where data increases.

1
int localmaxima(vector<int> &arr) { T.C: $O(\log N)$ S.C: $O(1)$

int N = arr.size();

if (N == 1) { return arr[0]; }

if (arr[0] > arr[1]) { return arr[0]; }

if (arr[N-1] > arr[N-2]) { return arr[N-1]; }

int l = 1, h = N-2;

while (l <= h) {

int m = (l+h)/2;

if (arr[m-1] < arr[m] && arr[m] > arr[m+1]) { return arr[m]; }

else if (arr[m] < arr[m+1]) { # goto right

l = m+1;

else { # arr[m-1] > arr[m] goto left

h = m-1;

}

}

Note: Comparing adj elements,
take care of corner elements

if m == 0: arr[-1] < arr[0]: Err.

if m == N-1: arr[N-1] > arr[N]: Err.

Given a unsorted arr[] return any one local maxima

local maxima: An element is said to be local maxima, if \geq than its adjacent elements [immediate left & right]

$$\underline{arr[i] \geq arr[i-1]} \text{ \& \& } \underline{arr[i] \geq arr[i+1]}$$

If $i=0$: $arr[0]$ is local maxima $\Rightarrow arr[0] \geq arr[1]$

If $i=N-1$: $arr[N-1]$ is local maxima $\Rightarrow arr[N-1] \geq arr[N-2]$

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int localMaximaRepetition (vector<int> &arr) {
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}
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18. Every element occurs twice, except for 1, find a unique element

Note: Duplicates are adjacent to each other

Ex1: 0 1 2 3 4 5 6 7 8 9 10

$arr[] = \{ 6, 6, 2, 2, 7, 9, 9, 4, 4, 10, 10 \}$ ans = 7

0 1 2 3 4 5 6 7 8 9 10 11 12 13 14

$arr[] = \{ 3, 3, 1, 1, 8, 8, 10, 10, 19, 6, 6, 2, 2, 4, 4 \}$ ans = 19

Idea1: 1. Calculate XOR of all elements

2. Iterate on $arr[]$: compare adj elements & return unique ele

TC: $O(N)$ SC: $O(1)$

Idea2:

Target: Unique element SearchSpace: In $arr[]$

Discard?

l m h
 $arr[] = \{ 3, 3, 1, 1, 8, 8, 10, 10, 19, 6, 6, 2, 2, 4, 4 \}$

if m is here:

goto right

if 1st occurrence is Even:

on left

goto right

if m is here

goto left

if 1st occurrence is Odd:

on right

goto left

Note: It is possible that m can find m 2nd occurrence

Con: if m is m 2nd occ: Bring to 1st

if ($arr[m-1] == arr[m]$) {

$m = m - 1$

}

$arr[m-1]$ 1st $arr[m]$ 2nd

	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14
ar[] =	3	3	1	1	8	8	10	10	19	6	6	2	2	4	4
							m		lh	m		m			h

l	h	m	1 st or 2 nd Occ	Even or Odd
0	14	7	ar[m] == ar[m-1]; m = m-1; m = 6	m: Even: goto right, l = m+2;
8	14	11	1 st occurrence	m: Odd: goto left, h = m-1;
8	10	9	1 st occurrence	m: Odd: goto left, h = m-1;
8	8	8	unique ele; return ar[m];	

int unique(vector<int> &ar) { T.C: $O(\log N)$ S.C: $O(1)$

int n = ar.size();

if (n == 1) { return ar[0]; }

if (ar[0] != ar[1]) { return ar[0]; }

if (ar[n-1] != ar[n-2]) { return ar[n-1]; }

int l = 1, h = n-2;

while (l <= h)

int m = (l+h)/2;

if (ar[m-1] != ar[m] & ar[m] != ar[m+1]) { return ar[m]; }

if (ar[m-1] == ar[m]) { # m m 2nd occ: Bring to 1st occ
m = m-1;

if (m%2 == 0) { # on left
l = m+2; # goto right
else { # m%2 == 1, m right
h = m-1;

