

## Today's Content

1. Count no: of elements with atleast 1  $u_i > \text{itself}$
2. Pair sum =  $k$
3. Vector Intro  $u_i$  pairs by value  $u_i$  pairs by reference.

Q: Given  $arr[N]$  return count no. of elements with atleast 1 ele  $>$  itself.

Constraints:

$$1 \leq N \leq 10^5$$

$$1 \leq arr[i] \leq 10^9$$

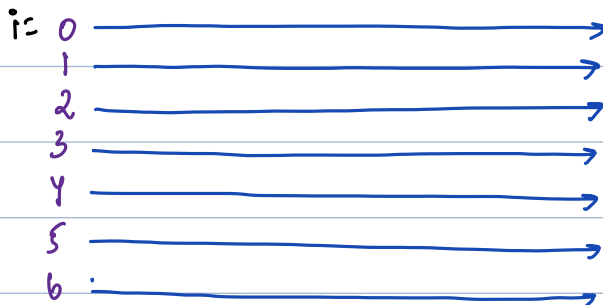
Ex:  $arr = \{7, 3, 10, 8, 9, 10, 6\}$  ans = 5

Ex:  $arr = \{9, 6, 4, 7, 9, 4\}$  ans = 4.

Idea: For every  $arr[i]$  element:

Iterate  $n$  array & check if there exists an element  $> arr[i]$

$arr = \{7, 3, 10, 8, 9, 10, 6\}$   $c = 4$ .



int greaterItself (int[] arr, int N) { Tc:  $O(N^2)$  Sc:  $O(1)$

int c = 0;

$\hookrightarrow N = 10^5 \Rightarrow N^2 = 10^{10} > 10^8$  TLE.

for (int i = 0; i < N; i++) {

// arr[i]: Check if there exists an element  $> arr[i]$ ;

bool isgreater = false;

for (int j = 0; j < N; j++) {

if (arr[j] > arr[i]) { // greater ele

isgreater = true;

} break;

}

if (isgreater == true) {

c++;

}

}

return c;

0 1 2 3 4 5 6 7 8  
 arr[] = { 7, 3, 10, 8, 9, 10, 6, 3, 10 }

obs1: In arr[] max element won't have element > itself

Idea2: 1. Iterate & get max  
 2. Iterate & get count of non-max elements. } Estimated TC:  $O(N)$

int greaterItself(int arr[], int n) { Calculated TC:  $O(N)$  SC:  $O(1)$   
 int m = INT\_MIN;  $\rightarrow N \leq 10^5; 10^5 < 10^8$   
 for(int i=0; i < n; i++) {  
 if(arr[i] > m) {  
 m = arr[i];  
 }  
 }  
 int c=0;  
 for(int i=0; i < n; i++) {  
 if(arr[i] != m) {  
 c++;  
 }  
 }  
 return c;  
}

TODO: Try to do it with 1 iteration.

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Given  $arr[N]$  elements &  $k$

Count no. of pairs  $(i, j)$  are there such  $arr[i] + arr[j] := k$

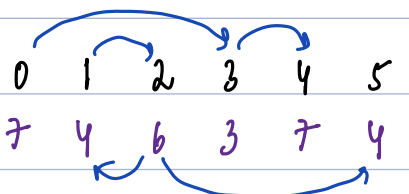
Note 1:  $(i, j)$  pair same as  $(j, i)$

Note 2:  $(i \neq j)$

Constraints:

$$1 \leq N \leq 10^3$$

$$1 \leq arr[i] \leq 10^9$$

Ex:   

 $arr[] = \{ 7, 4, 6, 3, 7, 4, 5, 5 \}$

$k = 10$

pairs =  $(0, 3)$   $(1, 2)$   $(2, 5)$   $(3, 4)$   $(4, 6)$   $(5, 7)$   $(6, 7)$

Idea: Generate all pairs, check if their sum =  $k$  & Inc C.

Tracing:  $arr[] = \{ 7, 4, 6, 3, 7 \}$

pairs:

$i \ j =$	0	1	2	3	4
0	$(0, 0)$	$(0, 1)$	$(0, 2)$	$(0, 3)$	$(0, 4)$
1	$(1, 0)$	$(1, 1)$	$(1, 2)$	$(1, 3)$	$(1, 4)$
2	$(2, 0)$	$(2, 1)$	$(2, 2)$	$(2, 3)$	$(2, 4)$
3	$(3, 0)$	$(3, 1)$	$(3, 2)$	$(3, 3)$	$(3, 4)$
4	$(4, 0)$	$(4, 1)$	$(4, 2)$	$(4, 3)$	$(4, 4)$

Note: In this idea  $(i, j)$  &  $(j, i)$  are considered, so for final ans/2 & return it.

TC:  $O(N^2)$  SC:  $O(1)$

$\hookrightarrow N=10^3 \Rightarrow (10^3)^2 = 10^6 < 10^8$

int pairSum(int arr[], int N, int k)

int c=0;

for(int i=0; i<N; i++)

for(int j=0; j<N; j++)

if (arr[i] + arr[j] == k && (i != j))

c++;

}

return c/2;

obs: Iterate on only upper part or lower part to avoid extra iterations  
TODO

Tracing: arr[] = { 7, 4, 6, 3, 7 }

pairs:

i \ j =	0	1	2	3	4
0	(0,0)	(0,1)	(0,2)	(0,3)	(0,4)
1	(1,0)	(1,1)	(1,2)	(1,3)	(1,4)
2	(2,0)	(2,1)	(2,2)	(2,3)	(2,4)
3	(3,0)	(3,1)	(3,2)	(3,3)	(3,4)
4	(4,0)	(4,1)	(4,2)	(4,3)	(4,4)

obs:  $i, j = i+1 \dots N-1$

$i=0, j=1$

$i=1, j=2$

$i=2, j=3$

$i=3, j=4$

int pairSum(int[] arr, int N, int k) { Tc:  $O(N^2)$  Sc:  $O(1)$

int c = 0;

for(int i = 0; i < N; i++) {

for(int j = i + 1; j < N; j++) {

if(arr[i] + arr[j] == k) {

c++;

}

}

return c;

Iterations: Construct Table

i	j: [i+1..N-1]
0	j: [1..N-1] = N-1
1	j: [2..N-1] = N-2
⋮	
N-1	j: [N..N-1] = 0

Outer loop: N

Inner loop:  $N-1 + N-2 + N-3 + \dots + 1 + 0$

$$= \frac{(N-1)N}{2}$$

$$\text{Total Iterations} = \frac{N(N+1)}{2}$$

## Issues in Arrays:

```
int arr[5];
```

0	1	2	3	4
10	20	30	40	50

$arr[0]=10; arr[1]=20; arr[2]=30; arr[3]=40; arr[4]=50;$

Issue: We cannot include size according to situation.

Dynamic Arrays: Size can be changed according to situation.

In C++

Vector

In Java

ArrayList

In Python

List

## Create a Vector:

Way 1: `Vector<datatype> vname;`

Ex1: `Vector<int> v1;`

Ex2: `Vector<float> v2;`

Way 2: `Vector<datatype> vname2(initial-size, initial-value);`

Ex1: `Vector<int> v(5, 10);` // v: 

0	1	2	3	4
10	10	10	10	10

## Insert into a vector:

`vname.push_back(val);` // Adds element at last

`v.push_back(15);`

// v: 

0	1	2	3	4	5
10	10	10	10	10	15

## Size of Vector

`vname.size();` // return size of vector

`int N = v.size();` //  $s = 6$ . `arr[i];`

## Iterate on Vector: `vname[indx];`

`for(int i=0; i<N; i++){`

`print(v[i]);`

}

## Remove from vector

`vname.pop-back()`; It will delete last element

`v.pop-back()`;

// v: 

0	1	2	3	4	5
10	10	10	10	10	15

## Sort a vector

`sort(vname.begin(), vname.end())`; // Sort v from start  $\rightarrow$  end

`sort(v.begin(), v.end())`;

// v: 

0	1	2	3	4
10	10	10	10	10

## Vector

### TC for Single call

- |                             |                                       |
|-----------------------------|---------------------------------------|
| 1. <code>push-back()</code> | $O(1)$                                |
| 2. <code>pop-back()</code>  | $O(1)$                                |
| 3. <code>size()</code>      | $O(1)$                                |
| 4. <code>sort()</code>      | $N \log N$ ; // N: number of elements |
| 5. <code>v[i]</code>        | $O(1)$                                |

## Pass vector to a function.

1. Pass by value;

2. Pass by reference;

Q: Given vector add all elements by +2 & return vector.

```
vector<int> modify(vector<int> &v){
```

```
}
```