

## Todays Content

1. Longest subset inc order
2. Closest pair

10:35

28 Given  $\text{ar}(N)$  arr, calculate length of longest subset which can be re-arranged in strictly increasing Order by 1.

Note: Pick any no: of  $\text{arr}()$  elements in any order.

Constraints

$$1 \leq N \leq 10^6$$

$$-10^9 \leq \text{ar}[i] \leq 10^9$$

0 1 2 3 4 5 6 7

Ex:  $\text{ar}[] = \{-1, 8, 5, 3, 10, 2, 4, 9\}$

$$\text{ans1: } \{8, 10, 9\} = \{8, 9, 10\} \quad l=3$$

$$\text{ans2: } \{5, 3, 2, 4\} = \{2, 3, 4, 5\} \quad l=4$$

return 4.

0 1 2 3 4 5 6 7 8 9

Ex2:  $\text{ar}[] = \{3, 8, 2, 1, 9, 6, 5, 6, 7, 2\}$

$$\text{ans1: } \{8, 9, 5, 6, 7\} = \{5, 6, 7, 8, 9\} \quad l=5$$

$$\text{ans2: } \{3, 2, 1, 2\} = \{1, 2, 2, 3\} \quad \text{Not Increasing}$$

$$\text{ans3: } \{3, 2, 1, 3\} = \{1, 2, 3\} \quad l=3$$

return 5.

Ideas:

Dry Run: Sort arr[] & copy adj elements to get longest inc sequence

$$0 \ 1 \ 2 \ 3 \ 4 \ 5 \ 6 \ 7 \ 8 \\ \text{arr}[] = \{-1 \ 8 \ 5 \ 3 \ 10 \ 2 \ 4 \ 9 \ 0\}$$

$$\begin{array}{cccccccccc} 0 & 1 & 2 & 3 & 4 & 5 & 6 & 7 & 8 & \\ \{ -1 & 0 & 2 & 3 & 4 & 5 & 8 & 9 & 10 \} * \\ \text{cnt} = \underline{1} \ \underline{2} \ \underline{1} \ \underline{2} \ \underline{3} \ \underline{4} \ \underline{1} \ \underline{2} \ \underline{3} \\ \text{man} = \underline{2} \ \underline{4} \ \underline{3} \ \text{return } 4. \end{array}$$

$$0 \ 1 \ 2 \ 3 \ 4 \ 5 \ 6 \ 7 \ 8 \ 9 \\ \text{arr}[] = \{ 3 \ 8 \ 2 \ 1 \ 9 \ 6 \ 5 \ 6 \ 7 \ 2 \}$$

Dry Run 1:

$$\begin{array}{cccccccccc} 0 & 1 & 2 & 3 & 4 & 5 & 6 & 7 & 8 & 9 \\ \{ 1 & 2 & 2 & 3 & 4 & 5 & 6 & 6 & 7 & 8 & 9 \} * \\ \text{cnt} = \underline{1} \ \underline{2} \ \underline{1} \ \underline{2} \ \underline{1} \ \underline{2} \ \underline{1} \ \underline{2} \ \underline{3} \ \underline{4} \\ \text{man} = \underline{2} \ \underline{2} \ \underline{2} \ \underline{4} \ \text{return } 4 \end{array}$$

Reason: We stop sequence when element repeats, this is a mistake  
We continue when element repeats, we don't give count.

Dry Run 2:

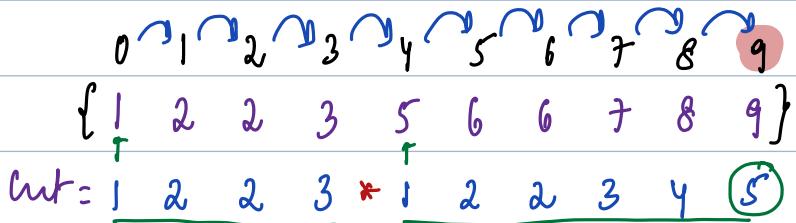
$$\begin{array}{cccccccccc} 0 & 1 & 2 & 3 & 4 & 5 & 6 & 7 & 8 & 9 \\ \{ 1 & 2 & 2 & 3 & 5 & 6 & 6 & 7 & 8 & 9 \} * \\ \text{cnt} = \underline{1} \ \underline{2} \ \underline{2} \ \underline{3} \ \underline{1} \ \underline{2} \ \underline{2} \ \underline{3} \ \underline{4} \ \underline{5} \\ \text{man} = \underline{3} \ \underline{5} \ \text{return } 5. \end{array}$$

```

int manlen(vector<int> &ar) { TC: O(N log N + N) = O(N log N)
    sort(ar.begin(), ar.end());
    int ans = 0, N = ar.size();
    int c = 1;            $\rightarrow i = N-1$ : Stop
    for (int i = 0; i < N-1; i++) {  $\# i = N-1$ , ar[i+1] - ar[i]  $\#$  Err.
         $\#$  compare ar[i] with ar[i+1]            $ar[N] - ar[N-1]$ 
        if (ar[i+1] - ar[i] == 1) {
            c++;  $\downarrow$  i++  $\downarrow$ 
        } else if (ar[i+1] - ar[i] == 0) {
            continue;  $\downarrow$ 
        } else {  $\# ar[i] \neq ar[i+1]$ 
            ans = man(ans, c);
            c = 1;  $\downarrow$ 
        }
    }
    return man(ans, c);  $\#$  last sequence will not be compared to
                        ans in loop, hence we compare it outside
                        loop & return biggest
}

```

Dry Run 3:



$$ans = 0 \quad ans = \max(c, ans)$$

$$ans = 3$$

Idea 2: for every  $ar[i]$

Calculate length of longest sequence starting from  $ar[i]$ .

Ex 1: 0 1 2 3 4 5 6 7 8

$$ar[] = \{ -1, 8, 5, 3, 10, 2, 4, 9, 0 \} \text{ ans} = 4$$

Start:

-1: 0 1 \* 2

8: 9 10 11 \* 3

5: 6 \* 1

3: 4 5 6 \* 3

10: 11 \* 1

2: 3 4 5 6 \* 4

1: 5 6 \* 2

hint: Store all  $ar[i]$  in hash set,

it can search if an element

exists or not in  $O(1)$

9: 10 11 \* 2

0: 1 \* 1

Ex 2:

$$ar[] = \{ 9, 7, 6, 8, 10 \} \text{ Insert in ts: } \{ 6, 8, 9, 10, 7 \}$$

Start:

9: 10 11 \*  $l=2$

Iterations =  $2+4+5+3+1$

7: 8 9 10 11 \*  $l=4$

$= 1+2+3+4+5 \quad S(5) = 15$

6: 7 8 9 10 11 \*  $l=5$  for  $ar[N]$

8: 9 10 11 \*  $l=3$

TC:  $1+2+3+\dots+N = \frac{(N)(N+1)}{2} = O(N^2)$

10: 11 \*  $l=1$

Issue: We iterate on same sequence multiple times hence it's going till  $O(N^2)$

Hint 1: We start sequence from  $ar[i]$  when  $ar[i]-1$  doesn't exist

$$ar[] = \{ 9, 7, 6, 8, 10 \}$$

8: 9:

6: 7:

\* 5: 6: 7: 8: 9: 10: 11 \*  $l=5$

7: 8:

9: 10:

Err2:

0	1	2	3	4	5	6	7
---	---	---	---	---	---	---	---

$\text{arr}[] = \{6, 6, 6, 6, 8, 9, 7, 10\}$

\* 5 6: 7 8 9 10 11 \* l=5

\* 5 6: 7 8 9 10 11 \* l=5

\* 5 6: 7 8 9 10 11 \* l=5

\* 5 6: 7 8 9 10 11 \* l=5

Issue: Because arr[] elements are repeating, same sequence will repeat multiple times

Hint2: To avoid above we iterate on hashset

Final Idea:

Iterate on hashset;

for element n: We start sequence if n-1 doesn't exist

Dry Run;

0	1	2	3	4	5	6	7	8	9
---	---	---	---	---	---	---	---	---	---

$\text{arr}[] = \{-1, 8, 5, 3, 10, 2, 4, 9, 2, 5\}$

HS = { -1, 8, 5, 3, 10, 2, 4, 9 }

-2 → -1 → 0 \* l=1

Total iterations =  $O(N+N) = O(N)$  SC:  $O(N)$

7 → 8 → 9 → 10 → 11 \* l=3

Outer loop: Iterating on hashset =  $O(N)$

4 → 5:

Inner loop: Sum of all sequence length:  $O(n)$

2 → 3:

9 → 10

# Instructr: TC need more detailed explanation

\* 2 → 3 → 4 → 5 → 6 \* l=4 → 4

3 → 4

6 → 9

int longestSequence(vector<int> &ar) TC:  $O(N+N) = O(N)$   
SC:  $O(N)$

```
unordered_set<int> hs;
for(int i=0; i< ar.size(); i++) {
    hs.insert(ar[i]);
```

int ans=0;

```
for(auto x: hs) {
```

# we start sequence from  $x$ , if  $x-1$  doesn't exist

```
if(hs.find(x-1) == hs.end()) {
```

# Start seq of  $\underline{x}$  :

```
int s=x, c=0
```

```
while(hs.find(s) != hs.end()) {
```

c++ # find seq length

s++ # go to next elem search

```
ans=max(ans, c);
```

}

```
return ans;
```

3

28 Given arr

find min abs[i-j] such that arr[i] == arr[j] & i ≠ j

Ex1 : arr = {0, 1, 2, 3, 4, 5, 6, 3, 4, 7, 3}

Pairs:

Ideas:

Ex2 : arr = {0, 1, 2, 3, 4, 5, 6, 7, 8, 9, 3}

hint: highlight 3s

Show for every 3 we compare with latest owner.

for every client compare with its latest owner.

By Run:

HashMap:



int minClosest(vector<int> &arr) {

3