

Today's Content

1. Steps followed to solve a question
2. Importance of constraints
3. Idea/datatype using constraints
4. Space complexity

few Maths:

$$a^m * a^n = a^{m+n}$$

$$\frac{a^m}{a^n} = a^{m-n}$$

$$(a^m)^n = (a^{m*n})$$

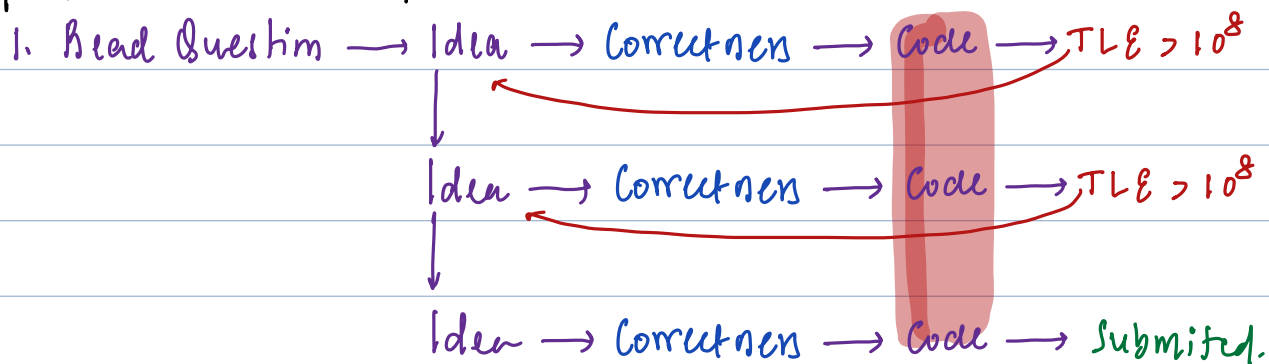
$$\text{int range} = \{-2 * 10^9 \dots 2 * 10^9\}$$

$$\text{long range} = \{-8 * 10^{18} \dots 8 * 10^{18}\}$$

Given Question:

1. Problem statement
2. Input format
3. Output format
4. Constraints
5. Sample Test Cases
6. Explanation of Testcases.

Steps followed to solve questions.



Q: Given an $arr[N]$ check if pair (i, j) exists such that their sum = k

Constraints:

$$1 \leq N \leq 10^6$$

$$1 \leq arr[i] \leq 10^9$$

Given $arr[N]$ & k

$$1 \leq N \leq 10^6$$

for (int i = 0; i < N; i++) TC: $O(N^2)$: TLE.

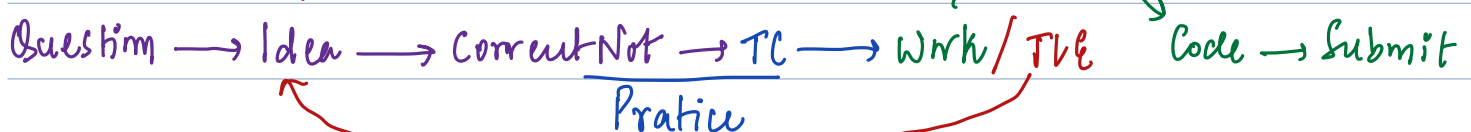
for (int j = 0; j < N; j++)

if ($arr[i] + arr[j] == k$)

return true;

return false;

\rightarrow Max $N = 10^6 \Rightarrow N^2 = 10^{12} > 10^8$ iterations



Idea based on Constraints

Ex1: $1 \leq N \leq 10^3$

$1 \leq arr[i] \leq 10^4$

Accepted TL:

Idea1: $O(N^3) = (10^3)^3 = 10^9 > 10^8 \text{ TLE}$

Idea2: $O(N^2) = (10^3)^2 = 10^6 \checkmark$

Idea3: $O(N \log N) = 10^3 \log_2 10^3 = 10^3 * 10 = 10^4 \checkmark$

Idea4: $O(N) = 10^3 \checkmark$

$$2^{10} = 1024 \approx 1000 = 10^3$$

$$\log_2 10^3 \approx \log_2 2^{10} = 10$$

$$\log_2^{AB} = \log_2 A + \log_2 B$$

$$\log_2 10^6 = \log_2 10^3 * 10^3 = \log_2 10^3 + \log_2 10^3 = 20$$

Ex2: $1 \leq N \leq 10^6$

$1 \leq arr[i] \leq 10^6$

Accepted TL:

Idea1: $O(N^2) = (10^6)^2 = 10^{12} > 10^8 \text{ TLE}$

Idea2: $O(N \log N) = 10^6 \log_2 10^6 = 10^6 * 20 = 2 * 10^7 \checkmark$

Ex3: $1 \leq N \leq 25$

$1 \leq arr[i] \leq 10^6$

Accepted TL:

Idea1: $O(N!) = 25! > 10^8 \text{ TLE}$

Idea2: $O(2^N) = 2^{25} = 10^3 * 10^3 * 32 = 3.2 * 10^7 \checkmark$

↳ Subsets.

Ex4: $1 \leq N \leq 10$

$1 \leq arr[i] \leq 10^5$

Accepted TL:

Idea1: $O(N!) = 10! = 3.6 * 10^6 \checkmark$

↳ Permutations

Datatype based constraints

Q1: Given arr[] calculate sum of array elements

Constraints:

$$\left. \begin{array}{l} 1 \leq N \leq 10^5 \\ 1 \leq \text{arr}[i] \leq 10^9 \end{array} \right\} \begin{array}{l} \text{sum range: } \{1..10^{14}\} \gg \text{int range} \\ \text{Min: } \text{arr}[1] = \{1\} = 1 \\ \text{Max: } \text{arr}[10^5] = \{10^9 + 10^9 + 10^9 + \dots + 10^9\} = 10^5 \times 10^9 = 10^{14} \end{array}$$

```
int sum = 0;
```

```
for (int i = 0; i < N; i++) {  
    sum = sum + arr[i];  
}  
print(sum);
```

$$10^9 + 10^9 = 2 \times 10^9$$

$$10^9 + 10^9 + 10^9 = 3 \times 10^9$$

Note: Constraints will also tell about range of variables, based on that we can estimate datatype of variable.

Q: For below constraints, range of sum variable

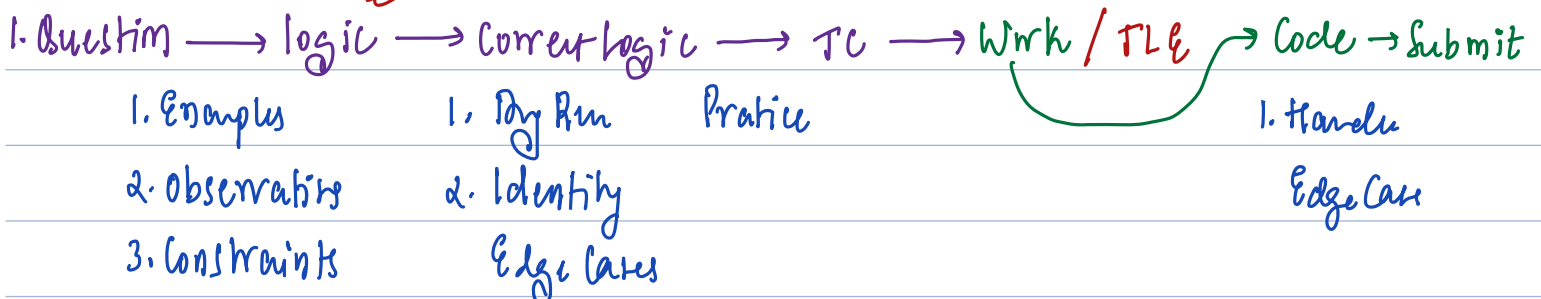
$$1 \leq N \leq 10^5$$

$$-10^9 \leq \text{arr}[i] \leq 10^9$$

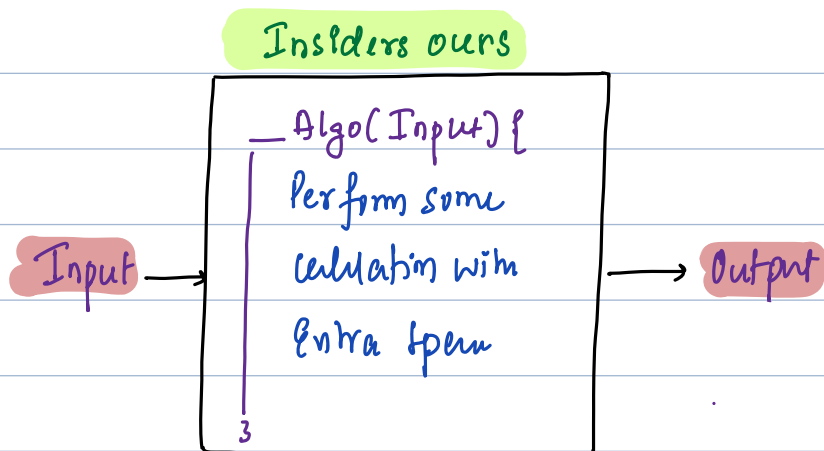
$$\text{Min: } \text{arr}[10^5] = \{-10^9 -10^9 -10^9 \dots -10^9\} = -10^9 \times 10^5 = -10^{14}$$

$$\text{Max: } \text{arr}[10^5] = \{10^9 10^9 10^9 \dots 10^9\} = 10^9 \times 10^5 = 10^{14}$$

Steps



Space Complexity: Main extra space used by algorithm during its execution.



Note 1: We neglect Input & Output space, & only consider extra space taken by Algo

Note 2: We use BigO to analyze space complexity as well

↗ Input

```
void Algo1(int n) {  
    int x = n;  ↗ 4B  
    int y = x * n  ↗ 4B  
    long z = x * y  ↗ 8B  
}
```

int = 4B long = 8B

Total space = 16B → Constant space = $O(1)$

```
void fun(int n) {  
    int arr[10];  ↗ 40B  
    int x, y;     ↗ 8B  
    long z;       ↗ 8B  
    int a[n];     ↗ 4N  
}
```

Total space = $56 + 4N \rightarrow O(N)$

void func(int N) {

int x = N; $\rightarrow 4B$

int y = x * x; $\rightarrow 4B$

long z = x * y; $\rightarrow 8B$

int arr[N]; $\rightarrow 4N$

long d[N][N]; $\rightarrow 8N^2$

Total space = $16B + 4N + 8N^2 = O(N^2)$

}

\hookrightarrow matrix size = $N \times N$

Q: Given an arr[N] return max of an array.

Input

int maxarr(int arr[], int N) {

int max = INT_MIN;

Iteration = $N \rightarrow O(N)$

for(int i = 0; i < N; i++) {

Total space = $4B \rightarrow O(1)$

if(arr[i] > max) {

max = arr[i];

}

return max;

}