

## Today's Content

1. Overlapping Intervals

2. Insert in overlapping Intervals.

Merge Intervals: Any Interval:  $[s \dots e]$

$I_1$	$I_2$	Why are overlapping	Merge Intervals
(2 6)	(3 7)		(2 7)
(2 8)	(4 6)		(2 8)
(3 7)	(4 10)		(3 10)
(3 6)	(6 10)		(3 10)
(5 8)	(4 9)		(4 9)

Overlapping Interval:

$I_1$	$I_2$	Say Overlapping	New Interval
$(s_1, e_1)$	$(s_2, e_2)$		$(\min(s_1, s_2), \max(e_1, e_2))$

Non Overlapping:

(2 5)	(8 10)	
(5 8)	(1 3)	

Non Overlapping Case:

$(s_1, e_1)$	$(s_2, e_2)$	

#Way 1:

if  $(s_2 > e_1 \text{ or } s_1 > e_2)$  {  
 Not overlapping

Q1: Given collection of intervals in a 2D array format, which are sorted-based on their start time.

Merge all overlapping intervals & return set of non-overlapping intervals

Note: If intervals are not already sorted, sort them.

Ex1: Intervals:

	0	1	Current Interval	New Interval
0	0	2	$\rightarrow \{0, 2\}$	
1	1	4	$\{0, 2\} = \{0, 4\}$	$\{0, 4\}$
2	5	6	$\{0, 4\} = \{5, 6\}$	$\{5, 10\}$
3	6	8	$\{5, 6\} = \{5, 8\}$	$\{12, 14\}$
4	7	10	$\{5, 8\} = \{5, 10\}$	
5	8	9	$\{5, 10\} = \{5, 10\}$	
6	12	14	$\{5, 10\} = \{12, 14\}$	

7 #outside stop

Ex2: Intervals:

	0	1	Current Interval	New Interval
0	0	3	$\rightarrow \{0, 3\}$	
1	1	5	$\{0, 3\} \{0, 5\}$	$\{0, 7\}$
2	4	7	$\{0, 5\} \{0, 7\}$	$\{9, 14\}$
3	9	12	$\{0, 7\} \{9, 12\}$	$\{17, 24\}$
4	10	14	$\{9, 12\} \{9, 14\}$	
5	17	20	$\{9, 14\} \{17, 20\}$	
6	19	24	$\{17, 20\} \{17, 24\}$	
7	21	25	$\{17, 24\} \{17, 25\}$	
8	24	34	$\{17, 25\} \{17, 34\}$	

9 #outside stop

TC:  $O(N)$  SC:  $O(1)$

vector<pair<int, int>> MergeAll(vector<pair<int, int>> arr) {  
 sort(arr.begin(), arr.end()); // Sorting based on start time

vector<pair<int, int>> newInterval;  
pair<int, int> ci = arr[0]; // ci current interval

```
for (int i = 1; i < arr.size(); i++) {  
    // current interval ci      arr[i].s arr[i].e      ci.s      ci.e  
    // latest interval arr[i]  
    if (ci.e < arr[i].s || arr[i].e < ci.s) { // Not overlapping  
        newInterval.push_back(ci); // inserting  
        ci = arr[i]; // updating  
    } else { // overlapping merge  
        ci.s = min(arr[i].s, ci.s); // [arr[i].s arr[i].e]  
        ci.e = max(arr[i].e, ci.e); // [ci.s ci.e]  
    }  
}  
newInterval.push_back(ci);  
return newInterval;  
}
```

# Note: In above code

$ci.s = ci.first$ ,  $ci.e = ci.second$

$arr[i].s = arr[i].first$ ,  $arr[i].e = arr[i].second$ .

28. Given  $N$  sorted non overlapping Interval, Insert a new Interval  
 In them, { Merge if Necessary }  
 Return set of non-overlapping Intervals

Ex1: Interval      Insert [12 22]      ans Interval

0	[1 3]	{12, 22}	<div>[</div> <div>[1 3]</div> <div>]</div>
1	[4 7]	{12, 22}	
2	[10 14]	{12, 22}    {10, 22}	
3	[16 19]	{10, 22}    {10, 22}	
4	[21 24]	{10, 22}    {10, 24}	
5	[27 30]	{10, 24}	
6	[32 35]		
7	[38 41]		
8	[43 50]		

Ex2: Interval      Insert [12 22]      ans Interval

0	[1 5]	{12, 22}	<div>[</div> <div>[1 5]</div> <div>]</div>
1	[8 10]	{12, 22}	
2	[11 14]	{12, 22}    {11, 22}	
3	[15 20]	{11, 22}    {11, 22}	
4	[21 24]	{11, 22}    {11, 24}	
5	[27 30]	<del>{11, 24}</del>	
6	[32 36]		

#Idea:  $T: O(N)$   $SC: O(1)$

Insert new Interval  $[ns, ne]$

Iterate in current Interval:  $[cs, ce]$

```
if(  $ce < ns$  or  $ne < cs$  ) { #Not overlapping
    if(  $ce < ns$  ) { #current Interval comes first  $[cs, ce]$   $[ns, ne]$ 
        Insert current Interval in ans ✓✓
    }
    else {  $[ns, ne]$   $[cs, ce]$ 
        Insert new Interval in ans;
        Iterate & insert all current Intervals in ans
        return ans;
    }
}
else { #overlapping. ✓✓✓
     $ns = \min(cs, ns);$ 
     $ne = \max(ce, ne);$ 
}
```

Insert new Interval in ans; #Edge Case, if we come outside loop.  
return ans;

Ans: Interval	Insert $[12, 22]$	ans Interval
$[1, 5]$	$[12, 22]$	$[1, 5]$
$[8, 10]$	$[12, 22]$	$[8, 10]$
$[11, 14]$	$[12, 22]$ $\{11, 22\}$	$\{11, 24\}$
$[15, 20]$	$\{11, 22\}$ $\{11, 22\}$	
$[21, 24]$	$\{11, 22\}$	
#outside	$\{11, 24\}$	

vector<pair<int, int>> Insert (vector<pair<int, int>> &arr, pair<int, int> j) {