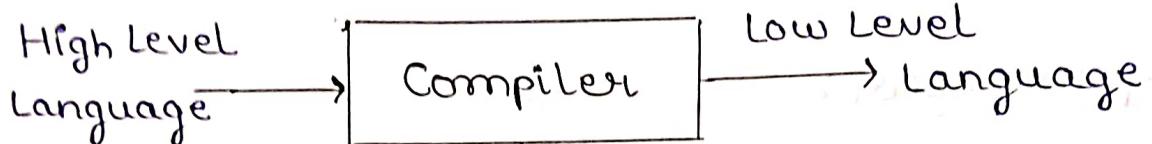


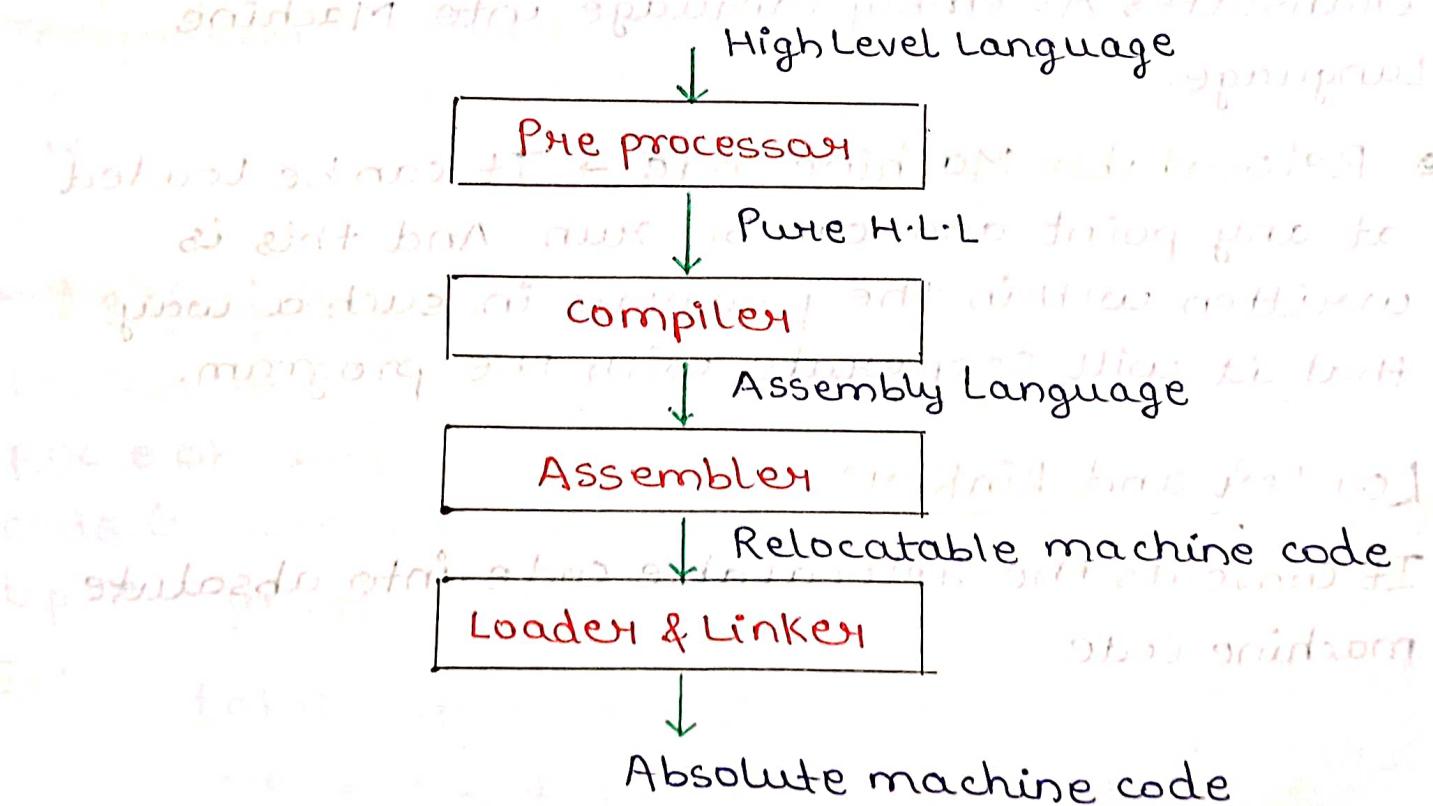
Compiler Design

UNIT 1



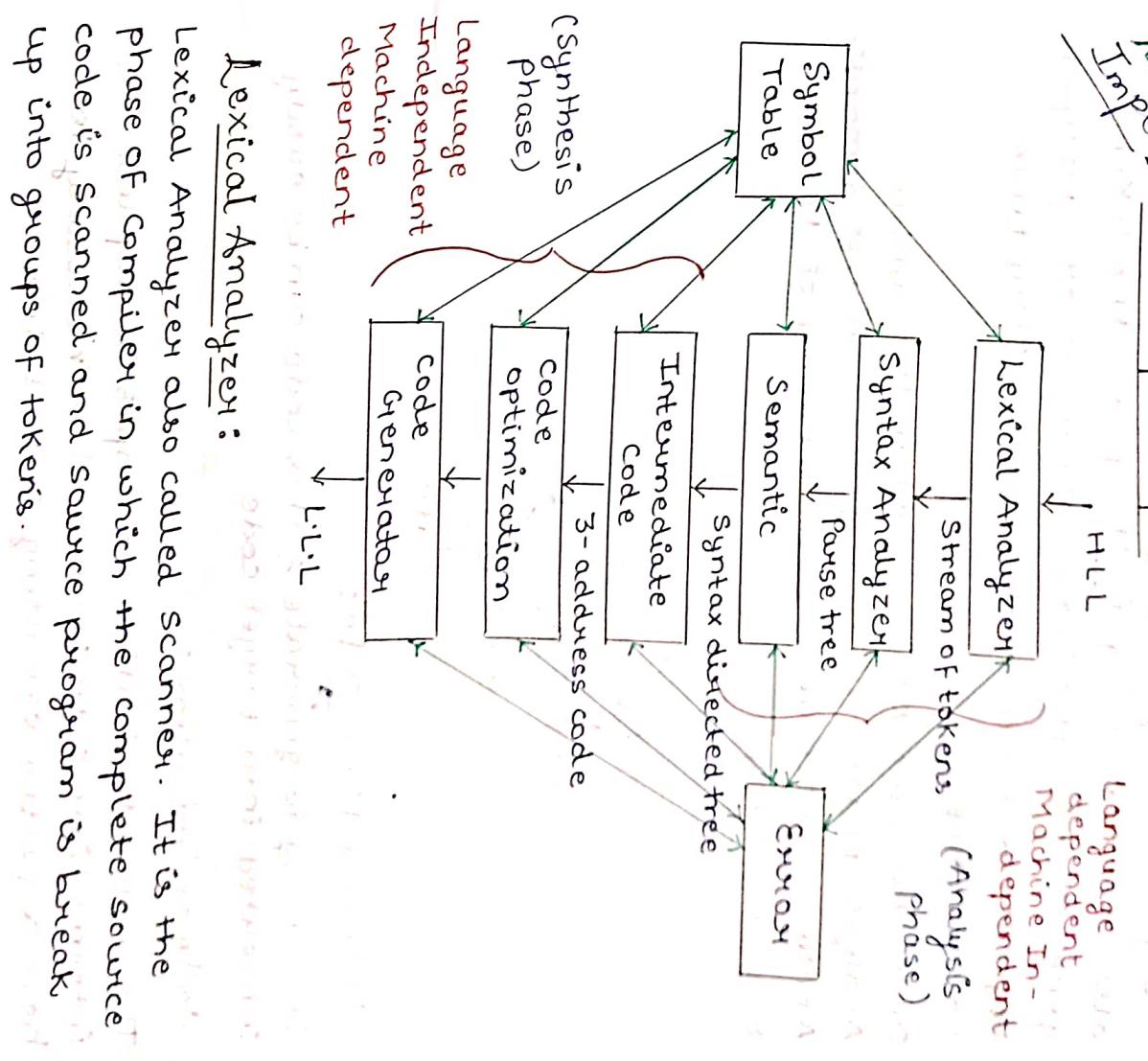
Compiler is a software that converts a program written in High Level Language into Low Level Language.

*** Language Processing Data:



Imp

Phases of Compiler:



Lexical Analyzer:

Lexical Analyzer also called scanner. It is the phase of compiler in which the complete source code is scanned and source program is broken up into groups of tokens.

Ex:

```

total = count + rate * 10;
string id1 = id2 + id3 * 10;
string name, date, location, job, address;
double age, balance, amount;

```

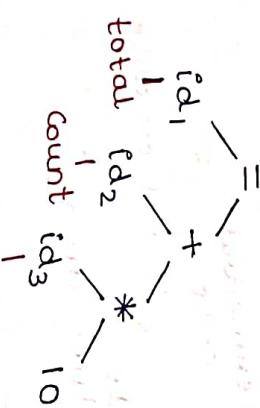
Output after lexical analysis:

tokens like +, *, =, <, >, <=, >=, ., , etc.

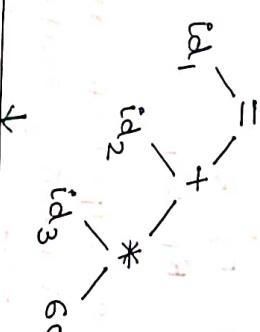
Syntax Analyzer: The Syntax Analyzer is also called **parsing**, in this phase the tokens generated by the Lexical Analyzer are grouped together to form a hierarchical structure called tree.

once, the syntax is checked in the Syntax Analyser phase, the next phase which is semantic Analysis, determines the meaning of the source string.

once, the Syntax is checked in the Syntax Analyser phase, the next phase which is semantic Analysis, determines the meaning of the source string.



Syntax Analyzer



Intermediate code:

It is easy to generate & this code can be easily converted into target code.

Code optimization:

he code optimization attempts to improve the intermediate code because it is necessary to have a faster executing code & less consumption of memory.

Code Generation: In the Code generation phase,

the target code get generated the intermediate code instructions are translated into sequence of machine instructions.

Ques: How an input $a = b + c * 60$ get translated by using compiler? Show the output of each stage of compiler? (consider c as real).

$$a = b + c * 60$$

Lexical Analyzer

$$id_1 = id_2 + id_3 * 60$$

Syntax Analyzer

$$\begin{aligned} t_1 &= \text{int to real} \\ t_2 &= id_3 * t_1 \\ t_3 &= id_2 + t_2 \\ id_1 &= t_3 \end{aligned}$$

Code Optimization

$$t_1 = id_3 * 60.0$$

$$id_1 = id_2 + t_1$$

Code Generator

```

MOV F id3, R2
MUL F #60.0, R2
MOV F id2, R1
ADD F R2, R1
MOV F R1, id1

```

ques2: Describe the output of various phases of compiler w.r.t following statement -

$$\text{Position} = \text{initial} * \text{Rate} * 60$$

(consider Rate as real).

$$\text{Position} = \text{initial} * \text{Rate} * 60$$

Lexical Analyzer

$$id_1 = id_2 * id_3 * 60$$

Syntax Analyzer

$$\begin{array}{c}
id_1 = \\
\downarrow \\
id_1 = id_2 * id_3 * 60
\end{array}$$

$$\begin{array}{c}
id_2 = \\
\downarrow \\
id_2 = id_3 * t_1
\end{array}$$

$$\begin{array}{c}
id_3 = \\
\downarrow \\
id_3 = 60
\end{array}$$

Semantic Analyzer

$$\begin{array}{c}
id_1 = \\
\downarrow \\
id_1 = id_2 * id_3
\end{array}$$

$$\begin{array}{c}
id_2 = \\
\downarrow \\
id_2 = t_1
\end{array}$$

$$\begin{array}{c}
id_3 = \\
\downarrow \\
id_3 = 60.0
\end{array}$$

Intermediate code

$$t_1 = \text{int to real}$$

$$t_2 = id_3 * t_1$$

$$t_3 = id_2 * t_2$$

Code Optimization

$$t_1 = id_3 * 60.0$$

$$id_1 = id_2 * t_1$$

Code Generator

```

MOV R1, id3
MUL R1, #60.0
MOV R2, id2
MUL R1, R2
MOV id1, R1

```

```

MOV id3, R1
MUL F #60.0, R1
MOV F id2, R2
MUL F R2, R1
MOV F R1, id1

```


Compiler can be characterized by -

language-

(a) Source Language

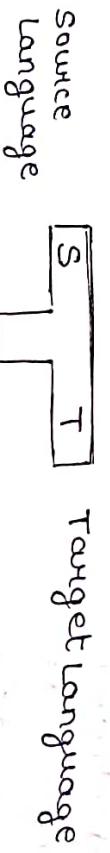
(b) Target Language

(c) Implementation Language

----- Intermediate Language



T-Diagram:



Error

Implementation Language

Example: Pascal Translation -

Source language : Pascal

Target language : C

Implementation language : C

P

C

Deterministic Finite Automata

Finite Automata

NT

Deterministic
finite automata

Non-Deterministic
Finite Automata

... Finite Automata:

A finite Automata is collection of 5 Tuple
(Q, Σ, S, q_0, F)

Q = A finite set of states

Σ = Input Alphabets indicates input set.

S = Transition Mapping function

q_0 = Initial state (q_0 is in Q , $q_0 \in Q$)

F = Set of Final states ($F \subset Q$)

... Representation:

A string & language can be accepted by finite automata when it reaches to the final state.

There are 2 representation for describing Automata -

1. Transition Diagram
2. Table form or Tabular form.

... Deterministic finite Automata:

1. The Finite Automata are called DFA if the machine reads an input string one symbol at a time.
2. Deterministic refers to the uniqueness of computation.
3. In DFA, there is only one path from a specific input from the current state to the next state.
4. DFA does not accept NULL move. DFA cannot change state without any IP character.

Formal Definition of DFA:

A DFA is a collection of 5 tuples (same as finite Automata)

Q = Finite set of states

Σ = Finite set of input

q_0 = Initial state

$$F = \text{Final state}$$

$$S = \text{Transition function } (Q \times \Sigma \rightarrow Q)$$

... Graphical Representation of DFA:

- The state is represented by vertex and the arc labeled with an input character shows the transition.
- The Initial state is marked with an arrow.
- The final state is denoted by double circle.

Let a DFA be -

$$Q = \{a, b, c\}$$

$$\Sigma = \{0, 1\}$$

$$q_0 = \{a\} \quad F = \{c\}$$



$Q \setminus \Sigma$	a	b	c
a	0	1	
b		0	1
c			0

Ques: construct a DFA starting with 'a'. $L = \{a, b\}^*$

accept string which accepts all strings
accept string which accepts all strings
 $\Sigma = \{a, b\}$

Ans: construct a DFA [$\Sigma = \{a, b\}$]

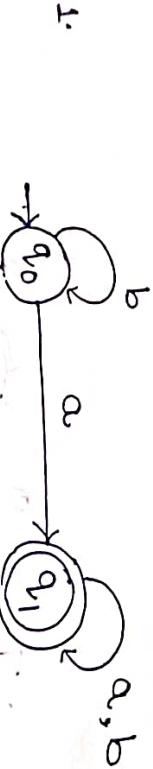
(i) containing a

(ii) End with a

(iii) Design a finite Automata which accepts

Ques: Design a DFA which checks that given binary number is even.

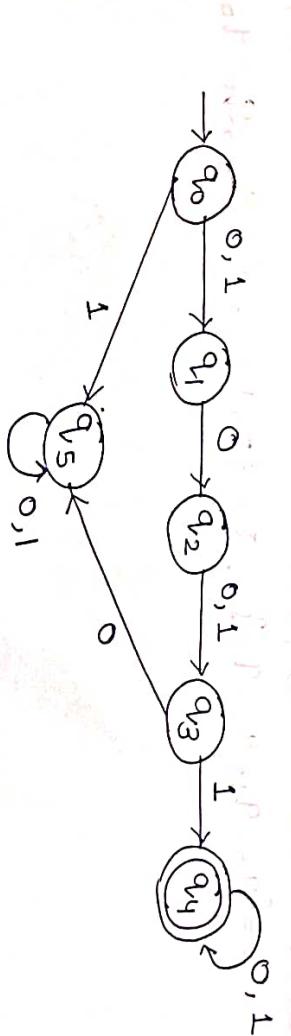
Ques: construct the finite state machine which accepts binary numbers ending with '0'.



Ques: construct a DFA which accepts a language of all strings starting with 'a' and ending with 'b'.

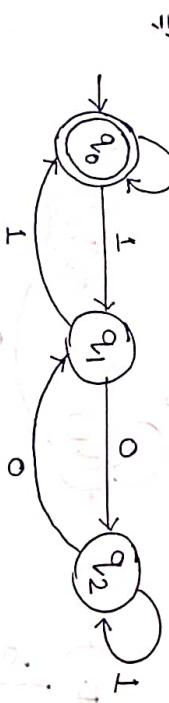


Ques: Design a DFA which accepts all strings in which 2nd symbol is 0 and 4th symbol is 1.



Ques: construct a DFA which accepts language of all strings not starting with 'a' and not ending with 'b'.

Ques: construct a DFA which accepts language of all strings (binary) divisible by 3. $[Z = \{0, 1\}]$



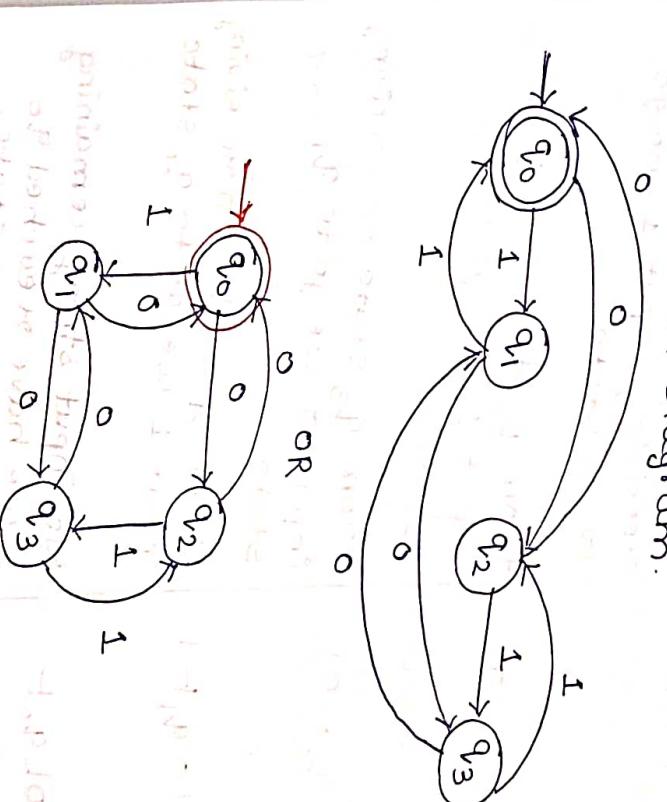
Possible remainders $\rightarrow 0, 1, 2$

$$0 \rightarrow q_0$$

$$1 \rightarrow q_1$$

$$2 \rightarrow q_2$$

Ques: consider a finite state machine in which $S = \{q_0, q_1, q_2, q_3\}$, $\Sigma = \{0, 1\}$, $F = q_0$, $S_0 = q_0$



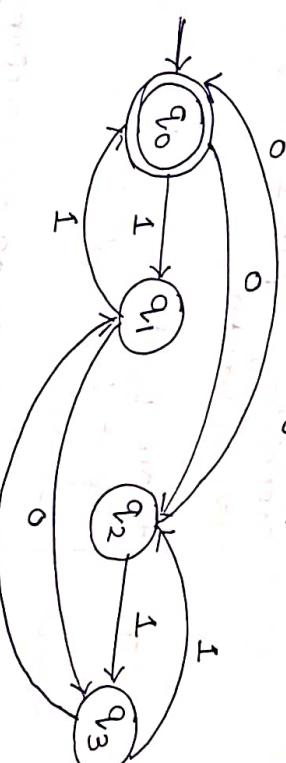
(i) Draw Transition Diagram.

101101

(ii) Find out the string among the following

- (a) 101101 (b) 11111 (c) 000000

(iii) Transition Diagram.



State	0	1
$\rightarrow q_0$	q_2	q_1
q_1	q_3	q_0
q_2	q_0	q_3
q_3	q_1	q_2

(iii) The entire sequence for 101101 is denoted by ' \vdash ', left to \vdash symbol is state in which the input is read and right to \vdash is the input to be processed.

Ques: Find the no. of Tokens.
 $\Rightarrow \text{printf}("i=%d, si=%c", i, si);$
 $\Rightarrow \text{No. of Tokens} = 9$

Step	Processing	Meaning
1.	$q_0 \vdash 101101$	Initially we are there in q_0 state read input 1 from q_0 with input 1 . we go to state q_1 .
2.	$1q_1 \vdash 01101$	From q_1 state on receiving input 0 we go to q_0 state.
3.	$10q_3 \vdash 1101$	From q_3 state on receiving input 1 we go to q_2 state.
4.	$101q_2 \vdash 101$	From q_2 state on receiving input 1 we go to q_3 state.
5.	$1011q_3 \vdash 01$	From q_3 state on receiving input 0 we go to q_1 state.
6.	$10110q_1 \vdash 1$	From q_1 state on receiving input 1 we go to q_0 state.
7.	$101101q_0 \vdash$	No input string remaining & we have reached q_0 which is a final state. Hence, it is a valid string.

- Regular Language:
A Regular expression is a method to represent a language. A language accepted by finite Automata can easily described by simple expression called Regular expression.
- It is most effective way to represent any language. The language accepted by some R.E are referred to as Regular language.

- A Regular expression can also be described as sequence of pattern that defines a string.
- For Instance: In R-E ∞^* means zero or more ∞ , we call it ∞ closure or Kleen closure.

• Operation on R.E :

Union: If 'L' and 'M' are two Regular languages, $L \cup M$ is also regular language.

Intersection: If 'L' and 'M' are two regular languages then $L \cap M$ is also regular.

Complement: If 'L' is a regular language then \bar{L} is also regular.

Ques: Construct DFA for a^*



$$a^* = \{ \epsilon, a, aa, aaa, \dots \}$$

Ques: $\Sigma = \{a, b\}$

- (1) Length 0 (2) Length 1 (3) Length 2
 (4) Length 3 (5) At most 1 (6) At most 2

\Rightarrow 1) Length 0

Ques: Construct DFA for $R \cdot E = a^+$

$$a^+ = \{ a, aa, aaa, \dots \}$$

2) Length 1 = {a, b}



Methods of Generating a Language:

Let 'R' be a Regular expression over alphabet Σ . If R is -

1. E is Regular expression denoted by the set $\{E\}$.

2. ϕ is Regular expression denoted by the empty set $\{\}$.

3. Each symbol $a \in \Sigma$, a is $R \cdot E$ denoted by $\{a\}$.

4. Union of $R \cdot E$ is also regular.

5. Concatenation of two ($R \cdot E$) expression is also regular.

6. Kleen closure of $R \cdot E$ is also regular.

- 7) All strings starting and ending with diff. symbol.
- 8) All strings starting and ending with two 'b'.
- 9) All strings having two 'b'.

Ques: Consider $\Sigma = \{a, b\}$ -

- 1) All string having a single 'b'.
- 2) All string having atleast 'b'.
- 3) All string having 'bbbb'.
- 4) All string end with 'ab'.
- 5) All string beginning and end with 'a'.
- 6) All string start with 'ba'.
- 7) All string containing 'aa'.
- 8) All strings starting and ending with diff. symbol.

$$\Rightarrow \text{ii) } R.E = a^* b a^*$$

$$\text{iii) } R.E = (a+b)^* b (a+b)^*$$

$$\text{iv) } R.E = (a+b)^* ab$$

$$\text{v) } R.E = ba(a+b)^*$$

$$\text{vi) } R.E = a(a+b)^* a$$

$$\text{vii) } R.E = (a+b)^* a (a+b)^*$$

$$\text{viii) } R.E = a(a+b)^* b + b(a+b)^* a$$

$$q. R.E = a^* ba^* ba^*$$

Ques: Write the R.E for a language containing strings which end with abb. over $\Sigma = \{a, b\}$

$$\Rightarrow R.E = (a+b)^* abb$$

Ques: Write a R.E to denote a language 'L' such that 3rd character from right end of the string is always 'a'. $\Sigma = \{a, b\}$

$$\Rightarrow R.E = (a+b)^* abb$$

$$R.E = (a+b)^* a (a+b) (a+b)$$

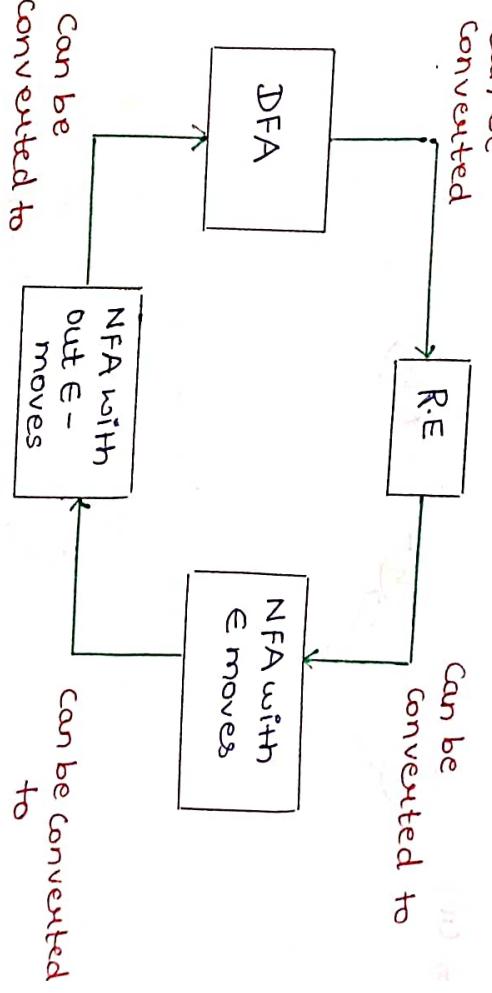
Conversion of R.E into finite Automata

1. To convert R.E to Finite Automata we use a method called subset method.

Step 1: Design a transition diagram for a given R.E using NFA with ϵ moves.

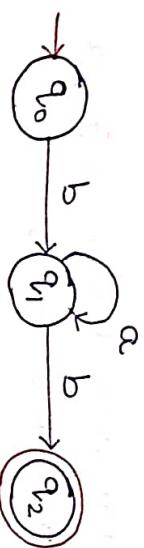
Step 2: Convert NFA with ϵ moves to NFA without ϵ -moves.

Step 3: Convert the obtained NFA into equivalent DFA.



Ques: Convert the following Regular Expressions to their equivalent finite Automata -

(i) $b a^* b$



(ii) $(a+b)c$

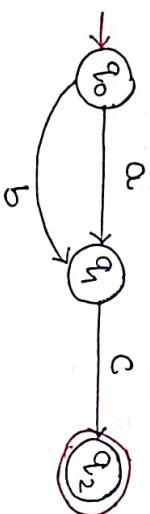
(iii) $a(bc)^*$

(iv) $10 + (0+11)0^*1$

(v) $1(1^*01^*01^*)^*$

(vi) 0^*1+10

⇒ (ii)



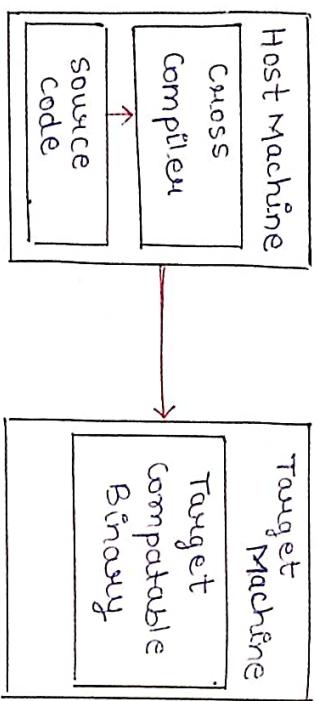
Cross Compiler:

It is a type of compiler that generates machine code targeted for the different system. For ex: A compiler that runs on Windows platform also generates a code that runs on Linux platform.

The process of generating executable code for different machine is called Retargeting code. Hence, the cross compiler is also known as Retargetable compiler.

GNU, GCC are the example of cross compiler.

Cross compiler operation

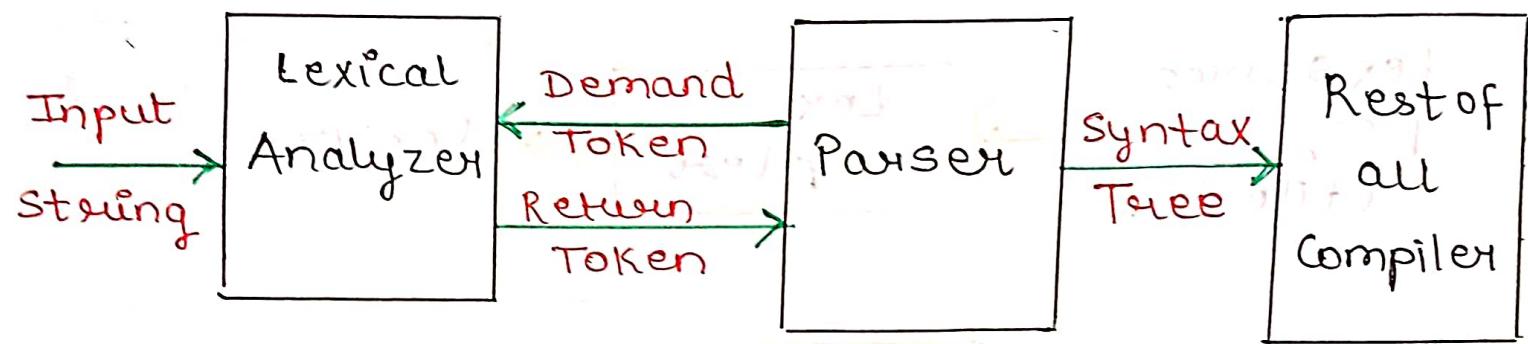


Implementation of Lexical Analyzer:

Lexical Analyzer is the first phase of compiler. The Lexical Analyzer reads the input source program from left to right one character at a time and generates the sequence of tokens, each token is a single lexical cohesive unit such as identifiers, Keywords, operators etc.

The parser to determine the syntax of source program can use these tokens.

The Role of Lexical Analyzer in the process of compilation is shown below-



The task of Lexical Analyzer apart from Token generation as follows -

- It eliminates Blanks and comments.
- It generates Symbol Table, which store the information about identifiers, constant.
- It keeps track of line number
- It reports the error encounter by generating the tokens.

Lexical Analyzer Generator:

The efficient design of compiler various tools are used to automate the phases of compiler.

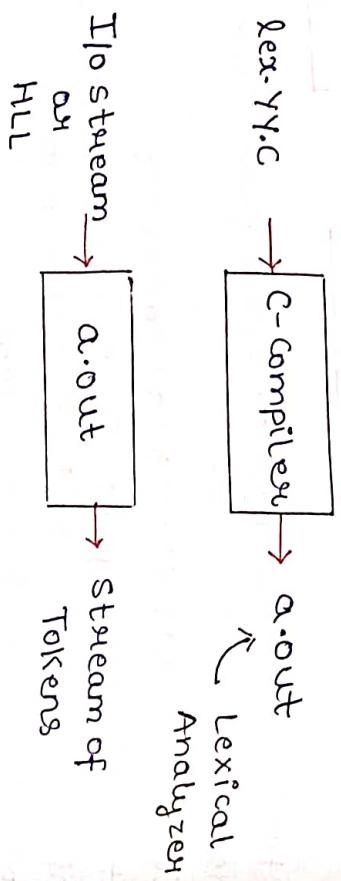
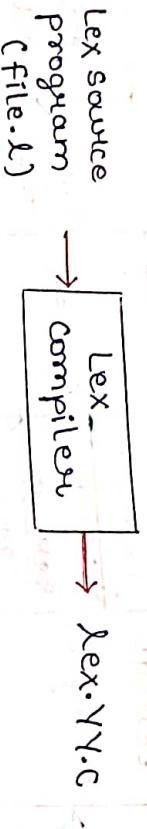
The Lexical Analyzer can be automate by using Lex tool.

Lex is a unix utility which generate lexical analyzer.

Lexical analyzer is generate with the help of R.E.

... LEX Tool in Compiler

LEX is a tool which generates Lexical Analyzer.
It will transfer input stream of character into transition diagram and generate code in a file called lex.yyc.



... Function of Lex:

- source code is in Lex language with file name (file.l). It is given to Lex compiler which is a Lex tool which generates lex.yyc. [it is a C program.]
- The C compiler runs this code (lex.yyc) and produce an output a.out.
- a.out transfers streams of character into stream of tokens.

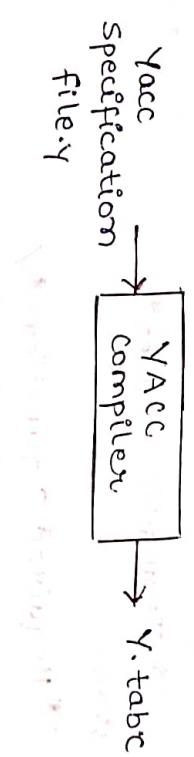
... YACC

YACC stand for 'Yet Another Compiler' or 'Left-to-right [LALR(1)].'

- It takes input from Lexical Analyzer and generates parse tree.

Syntax Analyzer / Parser:

It is second phase of compiler which takes input as token and generate parse tree.



- Input to YACC compiler will be compiled with .y extension. It will contains desired program in YACC format.
- YACC compiler will convert it into a C code & the OLP is y.tab.c.
- this y.tab.c is given as input to C compiler & the output will be LALR(1) parser.
- Token generated by Lexical Analyzer, using the Lex tool will be given as a.out

and we get parse tree.

Specification of YACC:

1. Declaration section
2. Translation tools
3. Auxiliary function

Syntax:

```
%{ /* Declaration */
```

```
%}
```

```
/* Transition rules */
```

```
%.
```

```
/* Required c function */
```

Ques: A CFG is given as -
 $E \rightarrow E + E / E - E / E * E / E / (CE) / id$
check whether the given sentence is a part of this grammar.

(i) $id + id * id$ (Valid)

(ii) $id + + id * id$ (Invalid)

Formal Grammar:

A Grammar is a set of rules which validates the correctness of sentence of a language.
Grammar can be defined by 4 tuples -

(V, T, P, S)

V = Variable or Non-Terminal

T = Terminal Symbol (Token)

P = Production rule

S = Start symbol

$E \rightarrow E + E / E - E / E * E / E / (CE) / id$ (CFG)
P1 P2 P3 P4 P5 P6
(i) $E \rightarrow id$ (Valid)
 $E \rightarrow E + E$ P1
 $E \rightarrow E + E * E$ P3 AND $E + E * id$ P6
 $E \rightarrow E + E * id$ P6 (Valid)
 $E \rightarrow id + id * id$ P6
It's a valid sentence

CFG and its Application:

CFG is used to define the syntactic structure of a programming language. It contains a set of rules called production rules.
CFG is used to check the syntax of programming language. (Algebraic expression, if-else statement, for loop, while loop, Array representation etc.)

Ex: In English language syntactic structure I am going.

If else Grammar:

→ if expression then, statement

→ if expression then, statement

→ else statement

(i) Example:

Sentence -

* if (a < b) then printf("Yes") else printf("No")

S → if expression then statement else

statement

→ if (a < b) then statement else statement

→ if (a < b) then printf("Yes") else printf("No")

statement

→ if (a < b) then printf("Yes") else printf("No")

→ if (a < b) then printf("Yes") else printf("No")

↓
P " BNF Notation : (Backus - Naur Form)

Developed by John Backus and Peter Naur.

It is a notation technique for CFG, this notation is useful for specifying the syntax of the language. BNF Specification is given below -

< symbol > : = Exp₁ | Exp₂ | Exp₃ | ... | ...
where,

< symbol > is a non-terminal and
Exp₁ | Exp₂ | Exp₃ | ... and so on are the

Sequence of symbol.

This symbol can be combination of Terminal and Non-terminal.

For example :

< Address > : = < first Name > " " < street > " " full < zip code >

< full Name > : = < first Name > " " < middle Name > " " < sury Name >

P ... Commonly used Notations in BNF :

1. Optional symbols are written within square brackets.

2. For repeating the symbol for 0 or more number of time asterisk (*) can be used as -

(name)* , ab* = {a, ab, abb...}

3. For repeating the symbol for at least 1 or more occurrence -

a(bc)⁺ = {abc, abcb, abcabc...}

4. The Alternative rules are separated by vertical bar.

5. The group of items must be enclosed within brackets.

Ambiguity:

A grammar is said to be ambiguous grammar if it can produce either more than one right most derivation or more than one right most derivation.

LMD: In LMD replace the leftmost non-terminal with a suitable production rule starting with start symbol.

Ex: $E \rightarrow E+E / E*E / id$

$P_1 \quad P_2 \quad P_3$

Sentence: $id + id * id$

$\Rightarrow LMD_1 \quad E \rightarrow E_* E \quad P_2$

P_1

$E \rightarrow E+E * E \quad P_1$

P_3

$E \rightarrow E+id * id \quad P_3$

$E \rightarrow id + id * id \quad P_3$

$E \rightarrow id + id * id \quad P_3$

RMD_1

$E \rightarrow E+E \quad P_1$

$E \rightarrow E*id \quad P_3$

$E \rightarrow E+E * id \quad P_1$

$E \rightarrow E+id * id \quad P_3$

$E \rightarrow id + id * id \quad P_3$

Check whether the Grammar is Ambiguous or not:

1. G: $E \rightarrow E+E / E*E / id$

Sentence: $E+E$

$id + id * id$

\Rightarrow Solution is explained above -

\therefore Given grammar is Ambiguous.

LMD_2

$E \rightarrow E+E \quad P_1$

P_3

$E \rightarrow id + E * E \quad P_2$

P_3

$E \rightarrow id + id * id \quad P_3$

P_3

RMD: In RMD, replace the rightmost non-terminal with a suitable production rule starting with start symbol.

Ex: $E \rightarrow E+E / E*E / id$

$P_1 \quad P_2 \quad P_3$

LMD_2 is not possible for this grammar therefore, the grammar that is given to us is ambiguous.

Elimination of Ambiguity:

Ambiguity can be eliminated by the following method -

1. By defining Precedence level of Arithmetic operation * is having more/higher precedence than +.
2. By defining Associativity of Arithmetic operations.

* & + both are Left associative.
^ is Right Associative.

Ques: check the following grammar is ambiguous or not.

$$G_1: S \rightarrow aS \mid Sa \mid a$$

Sentence : aa

$$\Rightarrow LMD_1 \quad S \rightarrow aS \quad P_1 \\ S \rightarrow aa \quad P_3$$

$$LMD_2 \quad S \rightarrow Sa \quad P_2 \\ S \rightarrow aa \quad P_3$$

Since, two left most Derivation are possible for this grammar, therefore the grammar is ambiguous.

Ques: $E \rightarrow E+E \mid E-E \mid id$

Sentence: $id+id-id$

LMD₁ $E \rightarrow E+E \quad P_1$

$E \rightarrow id+E \quad P_3$

$E \rightarrow id+E-E \quad P_2$

$E \rightarrow id+id-E \quad P_3$

$E \rightarrow id+id-id \quad P_3$

LMD₂

$E \rightarrow E-E \quad P_2$

$E \rightarrow E+E-E \quad P_1$

$E \rightarrow id+E-E \quad P_3$

$E \rightarrow id+id-E \quad P_3$

$E \rightarrow id+id-id \quad P_3$

Since, there is two LMD possible, therefore the grammar is ambiguous.

Ques: $S \rightarrow aSb \mid ss, \quad S \rightarrow E$

$P_1 \quad P_2, \quad P_3$

Sentence: $aabb$

LMD₁ $S \rightarrow aSb \quad P_1$

$S \rightarrow aasbb \quad P_1$

$S \rightarrow aaebb \quad P_3$

$S \rightarrow aabb$

Since, there exists two LMD for same sentence therefore, the grammar is ambiguous.

LMD₂ $S \rightarrow ss \quad P_2$

$S \rightarrow aSbs \quad P_1$

$S \rightarrow aasbbs \quad P_1$

$S \rightarrow aabbe \quad P_3$

Since, there exist two LMD therefore, the grammar is ambiguous.

Ques: $S \rightarrow Sas$

$S \rightarrow b$

LMD₁ $S \rightarrow Sas \quad P_1$

$S \rightarrow sasas \quad P_1$

$S \rightarrow basas \quad P_2$

$S \rightarrow babas \quad P_2$

$S \rightarrow babab \quad P_2$

LMD₂

$S \rightarrow sas \quad P_1$

$S \rightarrow bas \quad P_2$

$S \rightarrow basas \quad P_1$

$S \rightarrow babas \quad P_2$

$S \rightarrow babab \quad P_2$



Ambiguous to unambiguous

We can make a grammar unambiguous if we take care of two things-

1. Associativity
2. Precedence

Ex: $G_1: E + E \mid E * E \mid id$

This grammar is both left and right associative because we can draw our tree in any direction.

If we want to achieve Left Associativity then we have to restrict our tree to grow in Left direction only.

So, if we want operator to be Left Associative we have to make that grammar is Left recursive always.

For the Left Associative Recursion, Left most symbol of RHS must be equal to LHS.

For Precedence problem-

We should take care that highest precedence operators should be at least level.

So, we will introduce several different symbols like -

once we have reached T we can not generate +

$$\begin{aligned} E &\rightarrow E + T \mid T \\ T &\rightarrow T * F \mid F \\ F &\rightarrow id \end{aligned}$$

\Rightarrow NOT > AND > OR

$$\begin{aligned} E &\rightarrow E \text{ OR } F \\ F &\rightarrow F \text{ AND } G \\ G &\rightarrow \text{NOT } G \mid \text{True} \mid \text{False} \end{aligned}$$

Ques: $A \rightarrow A \$ B \mid B$
 $B \rightarrow B \# C \mid C$
 $C \rightarrow C @ D \mid D$
 $D \rightarrow id$

$$@ > \# > \$$$

Find Associativity and precedence of given grammar-

\Rightarrow Left Associative and @ has higher precedence since, it is far away from starting symbol A.

Ques $E \rightarrow E + E \mid E * E \mid F$
 $F \rightarrow F - G \mid G$
 $G \rightarrow id$

\Rightarrow NOT > AND > OR > PRECEDENCE

Ques: change according to precedence & Associativity rule - and generate grammar-

$$\begin{aligned} b \text{ Exp} &\rightarrow b \text{ Exp OR } b \text{ Exp} \\ &\quad / \text{ Exp AND } b \text{ Exp } / \text{ NOT } b \text{ Exp } / \text{ True } / \\ &\quad \text{ False} \end{aligned}$$

Recursive Grammar:

A grammar is said to be recursive if it produce itself again & again. Recursion can be of two types-

- Direct
- Indirect

Left Recursion:

A production of grammar is said to have left recursion if the left most variable of its RHS is same as variable of its LHS.

Ex: 1. $A \rightarrow A\alpha | \beta$ /* Direct Left Recursive

2. $S \rightarrow A\alpha$
 $A \rightarrow S\mu$

/* Indirect

Ques: Why it is important to remove Left Recursion?

\Rightarrow It is because top-down parser can not accept the grammar having left recursion. Hence, they do not allow left recursive grammar, that's why we have to remove left recursion from the grammar.

Conversion of Left Recursive Grammar:

Ques: Eliminate left Recursion from the given grammar -

1. $A \rightarrow A\alpha | \beta$ [Format 1] $\Rightarrow A \rightarrow \beta A' \quad [\text{Right Recursive}]$
 $A' \rightarrow \alpha A' | \epsilon$
2. $E \rightarrow E + T | T$ $\Rightarrow E \rightarrow T \cdot E'$
 $E' \rightarrow + T \cdot E' | \epsilon$
3. $S \rightarrow SOS1O / O1S$ $\Rightarrow S \rightarrow O1S'$
 $S' \rightarrow OS1OS' | \epsilon$
4. $S \rightarrow (L) / \alpha$
 $L \rightarrow L, S | S$ $\Rightarrow S \rightarrow (L) / \alpha$
 $L \rightarrow SL'$
 $L' \rightarrow ,SL' | \epsilon$
5. $A \rightarrow A\alpha_1 | A\alpha_2 | A\alpha_3 | \dots | A\alpha_n$ [Format 2] $\Rightarrow A \rightarrow \beta_1 A' | \beta_2 A' | \beta_3 A' | \dots | \beta_m A'$
 $A' \rightarrow \alpha_1 A' | \alpha_2 A' | \alpha_3 A' | \dots | \alpha_n A' | \epsilon$

This right recursive grammar is equivalent to given left recursive grammar.

$$E \rightarrow E + T \mid T$$

$$T \rightarrow T * F \mid F$$

$$F \rightarrow \text{id}$$

$$\Rightarrow E \rightarrow T E' \\ E' \rightarrow + T E' \mid e$$

$$T \rightarrow T * F \mid F$$

$$\underline{A} \quad \underline{A} \quad \underline{\alpha} \quad \underline{\beta}$$

$$T' \rightarrow * F T' \mid e$$

$$F \rightarrow \text{id}$$

Ques: Consider the following grammar:-

$$A \rightarrow ABD \mid Aa \mid a$$

$$B \rightarrow Be \mid b$$

Remove left Recursion

\Rightarrow

$$A \rightarrow ABd \mid a$$

$$A \rightarrow Aa \mid a$$

$$B \rightarrow Be \mid b$$

\therefore

$$A' \rightarrow \alpha A'$$

$$B \rightarrow bB'$$

$$B' \rightarrow eB' \mid e$$

$$A' \rightarrow \alpha A' \mid e$$

$$\left\{ \begin{array}{l} A \rightarrow ABD \mid a \\ A \rightarrow Aa \mid \alpha \\ B \rightarrow Be \mid b \end{array} \right.$$

Production will be -

$$S \rightarrow AaB$$

$$A \rightarrow bB \mid a$$

$$A \rightarrow \alpha A'$$

$$A' \rightarrow \alpha A' \mid e$$

$$(a) A \rightarrow AaA \mid b$$

$$\Rightarrow A \rightarrow bA'$$

$$A' \rightarrow \alpha A' \mid e$$

$$\Rightarrow E \rightarrow E + T \mid T$$

$$(b) S \rightarrow sss \mid o$$

$$S \rightarrow OS'$$

$$S' \rightarrow SSS' \mid e$$

$$S \rightarrow SSS \mid o$$

$$\underline{A} \quad \underline{A} \quad \underline{\alpha} \quad \underline{\beta}$$

$$(c) S \rightarrow SOS \mid 1s \mid$$

$$S' \rightarrow OS1s' \mid e$$

$$S \rightarrow SOS \mid o \mid 1$$

$$\underline{A} \quad \underline{A} \quad \underline{\alpha} \quad \underline{\beta_1} \quad \underline{\beta_2}$$

$$A \rightarrow \beta_1 A' \mid \beta_2 A'$$

$$A' \rightarrow \alpha_1 A' \mid \alpha_2 A'$$

Assignment

(e) $E \rightarrow F + T \mid T$
 $T \rightarrow T * F \mid F$
 $F \rightarrow (E) \mid id$

(f) $R \rightarrow R^* \mid RR \mid (R) \mid id$

(g) $S \rightarrow (L) \mid a$
 $L \rightarrow L, S \mid s$

Sol(e) $T \rightarrow T * F \mid F$

$T \rightarrow FT'$
 $T' \rightarrow *FT'E$

∴ final production will be -

$E \rightarrow F + T \mid T$

$T \rightarrow FT'$

$T' \rightarrow *FT'E$
 $F \rightarrow (E) \mid id$

$\begin{array}{c} T \rightarrow T * F \mid F \\ \sqcup \quad \sqcup \quad \sqcup \\ A \quad A \quad \alpha \quad \beta \end{array}$

Ques 1: What is the language generated by the following grammar?

$S \rightarrow osi \mid oi$
 $S \rightarrow +ss \mid -ss \mid a$
 $S \rightarrow S(Ss)S \mid e$

Justify your answer in each case -

Ques 2: Write short note on context free grammar. Give example.

(b) Parse tree., give example.

Ques 3: How is Finite Automata useful for Lexical Analysis. Construct NFA and DFA for following Regular Expression -

(a+b)*abb

Sol(g) $S \rightarrow (L) \mid a$
 $L \rightarrow SL'$
 $L' \rightarrow ,SL' \mid E$

∴ final production will be -

$R \rightarrow idR'$
 $R \rightarrow RR'E$
 $R \rightarrow (R) \mid id$

Ques 4: Write short note on Cross compiler.

Ques 5: Discuss the implementation of Look Ahead operator while doing the Lexical Analyser.

Ques 6: Explain all necessary phases and passes of compiler design.

Ques 7: What is Bootstrapping? How does bootstrapping is done on more than one machine?

Ques: Why translators are needed?

Left Factoring:

(Deterministic & Non-Deterministic Grammars)

If a grammar can not decide a production by using single input it is non-deterministic grammar else Deterministic grammar.

Ex 1: $A \rightarrow \alpha | \beta | \gamma$

$$\begin{array}{l} A \rightarrow \alpha \\ A \rightarrow \beta \\ A \rightarrow \gamma \end{array}$$

(Deterministic)

Ex 2: $A \rightarrow \alpha\beta_1 | \alpha\beta_2 | \alpha\beta_3 | \alpha\beta_4 \dots$

input $\alpha\beta_3$

Back tracking is required.

Ex 1: $S \rightarrow iEts | iEses | a$

$$\Rightarrow \begin{array}{l} S \rightarrow iEts \\ E \rightarrow b \\ S' \rightarrow \epsilon | es \\ E \rightarrow b \end{array}$$

Left Factoring

Process of making Non-Deterministic Grammar - to Deterministic Grammar is called

Ex 2:

$A \rightarrow \alpha\beta_1 | \alpha\beta_2 | \alpha\beta_3 | \alpha\beta_4$

$\Rightarrow \begin{array}{l} A \rightarrow \alpha A' \\ A' \rightarrow \beta_1 | \beta_2 | \beta_3 | \beta_4 \end{array}$

Steps to Make Non-Deterministic Grammar to Deterministic Grammar:

1. Make one production for common prefix.
2. one production for remaining part of production.

1. $A \rightarrow \alpha\beta_1 | \alpha\beta_2 | \alpha\beta_3 | \alpha\beta_4$ [format] convert the given Non-Deterministic grammar into deterministic.

$$\Rightarrow \begin{array}{l} A \rightarrow \alpha A' \\ A' \rightarrow \beta_1 | \beta_2 | \beta_3 | \beta_4 \end{array}$$

Ex 2: $S \rightarrow assbs | assbs | abb | b$

$$\Rightarrow \begin{array}{l} S \rightarrow assb' \\ S \rightarrow aB' \\ B' \rightarrow ssbs | asb | bb \end{array}$$

$S \rightarrow \alpha S \beta$

$S' \rightarrow SS'' | bb$

$S'' \rightarrow Sbs | asb$

$\beta_1 = ssbs$
 $\beta_2 = sasb$
 $\beta_3 = bb$
 $A = S$

For production 3

$A = S'$

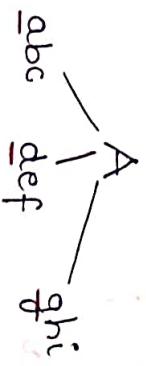
$\alpha = S$

$\beta_1 = sbs$

$\beta_2 = asb$

... Finding First Function:

1. $A \rightarrow abc | def | ghi$



$first(A) = \{a, d, g\}$

2. $B \rightarrow AC | abcghi$



$first(B) = \{a, g\}$

$= \{ first(A), a, g\}$

$first(A)$ is set of terminal symbols that are first symbol appears at LHS in derivation of A. If $A \rightarrow E$ then,

$first(A) = E$

Ques: find first function in given grammar:

ω $E \rightarrow TE'$

$E' \rightarrow +TE' | e$

$T \rightarrow FT'$

$T' \rightarrow *FT' | e$

$F \rightarrow id | CE)$

$\Rightarrow first(E) = first(T) = first(F) = \{id, (\}$

$first(E') = \{+, \in\}$

$first(T) = first(F) = \{id, (\}$

$first(T') = \{*, \in\}$

$first(F) = \{id, (\}$

(ii) $S \rightarrow ABC | ghi jkl$

$A \rightarrow a | b | c$

$B \rightarrow b$
 $D \rightarrow d$

$\Rightarrow first(S) = \{first(A), g, j\} = \{a, b, c, g, j\}$

$first(A) = \{a, b, c\}$

$first(B) = \{b\}$

$first(D) = \{d\}$

(iii) $S \rightarrow ABC$

$A \rightarrow a|b|e$

$B \rightarrow c|d|e$

$C \rightarrow e|f|e$

$\Rightarrow \text{first}(S) = \text{first}(A) = \{a, b, e, d, e, f\}$

$\text{first}(A) = \{a, b, e\}$

$\text{first}(B) = \{c, d, e\}$

$\text{first}(C) = \{e, f, e\}$

$\Rightarrow \text{follow of } (S) = \{\$\}$

$\text{follow of } (A) = \{a, d, \$\}$

$\text{follow}(D) = \text{follow}(S) = \{\$\}$

$\text{follow}(C) = \text{first}(D) = \{d, \$\}$

(iv) $A \rightarrow BCD$

$B \rightarrow bcfe$

$C \rightarrow cegele$

$D \rightarrow d$

$\text{first}(D) = \{d\}$

$\text{first}(C) = \{c, e\}$

$\text{first}(B) = \{b, e\}$

$\text{first}(A) = \{b, c, d, e\}$

Ques: Find first and follow of the following-

1) $S \rightarrow AaAb|BbBa$

$A \rightarrow e$

$B \rightarrow e$

$\Rightarrow \text{first of } B = \{e\}$

$\text{first of } A = \{e\}$

$\text{first of } S = \{a, b\}$

$\text{follow}(S) = \{\$\}$

$\text{follow}(A) = \{a, b\}$

$\text{follow}(B) = \{a, b\}$

... finding follow ...

$\text{Follow}(A)$ contains set of all terminals present immediate in right of A.

Rule 1:

Follow of start symbol is $\$\$

Rule 2:

Follow never contain ϵ

2) $S \rightarrow ABCDE$

$A \rightarrow a|e$

$B \rightarrow b|e$

$C \rightarrow c$

$D \rightarrow d|e$

$E \rightarrow e|e$

$\Rightarrow \text{first}(E) = \{e, e\}$

$\text{first}(D) = \{d, e\}$

$\text{first}(C) = \{c\}$

$\text{first}(B) = \{b, e\}$

$\text{first}(A) = \{a, e\}$

$\text{first}(S) = \{a, b, c\}$

$\text{follow}(S) = \{\$\}$

$\text{follow}(E) = \{\$\}$

$\text{follow}(T) = \{+, \$\}$

$\text{follow}(B) = \{c\}$

$\text{follow}(E') = \{\$\}$

$\text{follow}(D) = \{e, \$\}$

$\text{follow}(T') = \{+, \$\}$

$\text{follow}(C) = \{d, e, \$\}$

$\text{follow}(E) = \{\$\}$

$S \rightarrow Bb | Cc$

$B \rightarrow ab | e$

$C \rightarrow cc | e$

$\Rightarrow \text{first}(S) = \{a, b, c, d\}$

$\text{first}(B) = \{a, e\}$

$\text{first}(C) = \{c, e\}$

$\text{follow}(S) = \{\$\}$

$\text{follow}(B) = \{b\}$

$\text{follow}(C) = \{d\}$

4)

$E \rightarrow TE'$

$E' \rightarrow +TE' | e$

$T \rightarrow FT'$

$T' \rightarrow *FT' | e$

$F \rightarrow id | CE$

$\text{first}(F) = \{id, C\}$

$\text{first}(CT') = \{*, e\}$

$\text{first}(CE) = \{+, e\}$

\Rightarrow
first

follow

$\text{follow}(S) = \{\$\}$

$\text{follow}(A) = \{h, g, \$\}$

$\text{follow}(B) = \{\$, g, a, h\}$

$\text{follow}(C) = \{g, \$, b, \}$

$\text{first}(C) = \{h, e\}$

$\text{first}(B) = \{g, e\}$

$\text{first}(A) = \{d, g, h, e\}$

$\text{first}(S) = \{d, g, h, \$\}$

b, a, h

h

\Rightarrow

$S \rightarrow ACB | CBB | Ba$

$A \rightarrow da | BC$

$B \rightarrow g | e$

$C \rightarrow h | e$

\Rightarrow
first

follow

$\text{follow}(S) = \{\$\}$

$\text{follow}(A) = \{h, g, \$\}$

$\text{follow}(B) = \{\$, g, a, h\}$

$\text{follow}(C) = \{g, \$, b, \}$

Ques: $S \rightarrow aBDh$

$$\begin{array}{l} B \rightarrow CC \\ C \rightarrow bC | e \\ D \rightarrow EF \\ E \rightarrow g | e \\ F \rightarrow f | e \end{array}$$

$$\Rightarrow \text{first}(F) = \{f, e\}$$

$$\text{first}(E) = \{g, e\}$$

$$\text{first}(D) = \{g, f, e\}$$

$$\text{first}(C) = \{b, e\}$$

$$\text{first}(B) = \{c\}$$

$$\text{first}(S) = \{a\}$$

$$\text{follow}(S) = \{\$\}$$

$$\text{follow}(B) = \{g, f, h\}$$

$$\text{follow}(C) = \{g, f, h\}$$

$$\text{follow}(D) = \{h\}$$

$$\text{follow}(E) = \{f, h\}$$

$$\text{follow}(F) = \{h\}$$

~~To find out whether the given grammar is LL(1) or not:~~

$$1. \quad S \rightarrow aSbS \mid bSas \mid e$$

$$\Rightarrow \text{first}(S) = \{a, b, e\}$$

$$\text{follow}(S) = \{\$, b, a\}$$

LL(1) Parsing Table

S	a	b	$\$$
$S \rightarrow aSbS$		$S \rightarrow bSas$	$S \rightarrow \$$
$S \rightarrow e$			

This grammar is not LL(1) grammar.

2. $S \rightarrow (S) \mid e$

$$\Rightarrow \begin{array}{l} \text{first}(S) = \{c, e\} \\ \text{follow}(S) = \{\$\} \end{array}$$

S	$($	$)$	$\$$
$S \rightarrow (S)$		$S \rightarrow e$	
$S \rightarrow e$			

As each cell in the above table contains unique entries, the given grammar is LL(1) grammar.

$$3. \quad S \rightarrow AaAb \mid BbBa$$

$$\begin{array}{l} A \rightarrow e \\ B \rightarrow e \end{array}$$

$$\Rightarrow \text{first}(A) = \{e\}$$

$$\text{first}(B) = \{e\}$$

$$\text{first}(S) = \{a, b\}$$

$$\text{follow}(S) = \{\$\}$$

$$\text{follow}(A) = \{a, b\}$$

$$\text{follow}(B) = \{b, a\}$$

S	a	b	$\$$
$S \rightarrow AaAb$		$S \rightarrow BbBa$	$\$$
$S \rightarrow e$			

$\text{first}(\alpha_1) \cap \text{first}(\alpha_2) = \emptyset$

or

$\text{first}(\alpha_1) \cap \text{first}(\alpha_2) = \emptyset$

$\text{first}(\alpha_2) \cap \text{first}(\alpha_3) = \emptyset$

\Rightarrow

$\text{first}(A) = \{a, \epsilon\}$

$\text{first}(S) = \{a, b, \epsilon\}$

$\text{follow}(S) = \{\$\}$

$\text{follow}(A) = \{b, \$\}$

$\text{follow}(B) = \{ \$\}$

$$\begin{aligned} & S \rightarrow aB \\ & B \rightarrow bC \\ & C \rightarrow c\$ \end{aligned}$$

$$\text{first}(C) = \{c, \epsilon\}$$

$$\text{first}(B) = \{b, \epsilon\}$$

$$\text{first}(S) = \{a, \epsilon\}$$

$$\text{follow}(S) = \{\$\}$$

$$\text{follow}(B) = \{ \$\}$$

$$\text{follow}(C) = \{ \$\}$$

$$S \rightarrow aB$$

$$B \rightarrow bC$$

$$C \rightarrow c\$$$

Since, each cell of each column has a single entry so, this grammar is L(1) grammar.

5. $S \rightarrow AB$
 $A \rightarrow a|\epsilon$
 $B \rightarrow b|\epsilon$

$$\begin{array}{c|ccccc} S & a & b & \$ & \\ \hline A & A \rightarrow a & & & \\ B & & B \rightarrow b & & \\ C & & & B \rightarrow \epsilon & \\ \hline & S \rightarrow AB & S \rightarrow AB & S \rightarrow AB & \end{array}$$

$$\begin{array}{c|ccccc} S & a & b & \$ & \\ \hline A & A \rightarrow a & & & \\ B & & B \rightarrow b & & \\ C & & & B \rightarrow \epsilon & \\ \hline & S \rightarrow AB & S \rightarrow AB & S \rightarrow AB & \end{array}$$

$$S \rightarrow AB$$

$$A \rightarrow a$$

$$A \rightarrow \epsilon$$

$$B \rightarrow b$$

$$B \rightarrow \epsilon$$

$$C \rightarrow \epsilon$$

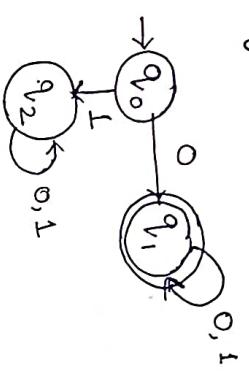
7.

$$S \rightarrow aAa|\epsilon$$

$$A \rightarrow ab|\epsilon$$

8.

Ques: DFA with $\Sigma = \{0, 1\}$ starting with 0.



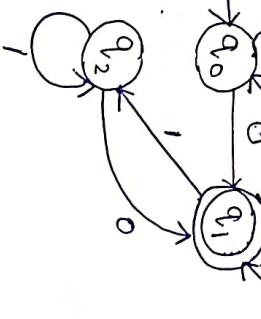
$$Q = \{q_0, q_1, q_2\}$$

$$\Sigma = \{0, 1\}$$

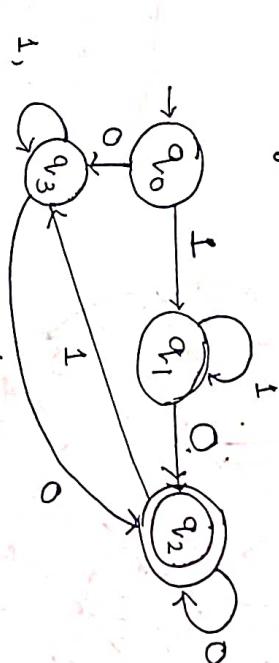
$$q_0 = \{q_0\}$$

$$F = \{q_1\}$$

Ans: DFA with $\Sigma = \{0, 1\}$ accepts all strings ending with 0.



Ques: DFA with $\Sigma = \{0, 1\}$ accepts all strings starting with 1, ending with 0.



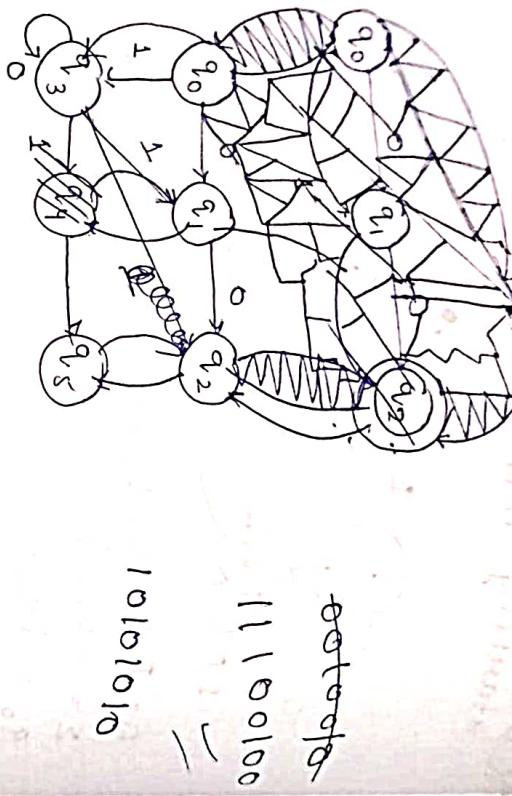
$$Q = \{q_0, q_1, q_2, q_3\}$$

$$\Sigma = \{0, 1\}$$

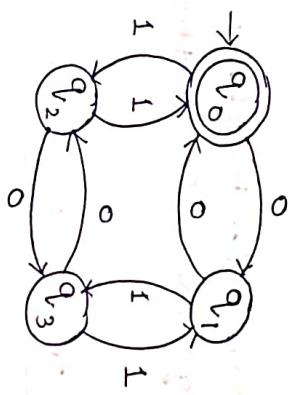
$$q_0 = \{q_0\}$$

$$F = \{q_2\}$$

Ques: DFA with $\Sigma = \{0, 1\}$ accepts all strings starting with 1 and ending with 0.



Ques: DFA with $\Sigma = \{0, 1\}$ accepts all strings with even no. of 0 and 1.



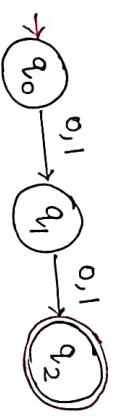
$$\begin{aligned} Q &= \{q_0, q_1, q_2, q_3\} \\ \Sigma &= \{0, 1\} \\ q_0 &= \{q_0\} \\ F &= \{q_0\} \end{aligned}$$

Ques: Draw a NFA

all strings of length atleast 2.

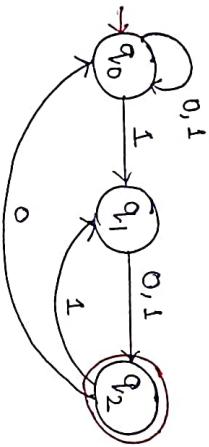
$$L = \{00, 11, 01, 10\}$$

\Rightarrow



Ques: Draw a NFA in which second last bit

is 1, with $\Sigma = \{0,1\}$

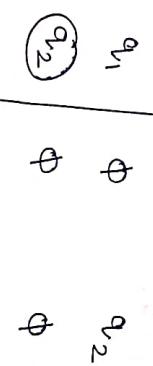
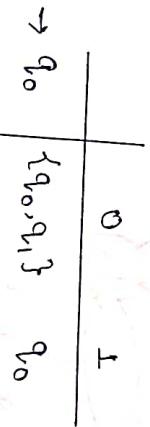


$$L = \{010, 111, 10, 11, 110, \dots\}$$

Ques: Conversion from NFA to DFA :

{set of all strings over $\{0,1\}$ that ends with '1'}

\Rightarrow NFA :

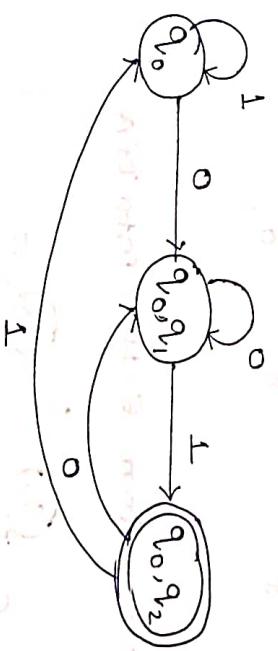


$$\Rightarrow \begin{array}{c|cc} & 0 & 1 \\ \hline q_0 & \{q_0, q_1\} & q_0 \\ q_1 & \emptyset & q_2 \\ q_2 & \emptyset & \end{array}$$

DFA Transition Table -

	0	1
$\{q_0, q_1\}$	$\{q_0, q_1\}$	q_0
$\{q_0, q_2\}$	$\{q_0, q_2\}$	$\{q_0, q_2\}$
$\{q_0, q_1, q_2\}$	$\{q_0, q_1, q_2\}$	q_0
q_0	q_0	q_0

Transition diagram :



Ques: Conversion from ϵ -NFA to DFA.



$$\Rightarrow \epsilon\text{-closure}(q_0) = \{q_0, q_1, q_2\}$$

$$\epsilon\text{-closure}(q_1) = \{q_1, q_2\}$$

$$\epsilon\text{-closure}(q_2) = \{q_2\}$$

E-NFA

\Rightarrow E-closure(q_0) = $\{q_0, q_1, q_2, q_5\}$

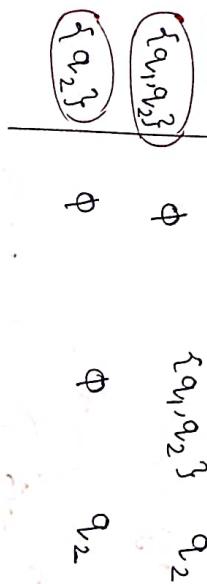
E-closure(q_1) = $\{q_1, q_2, q_5\}$

E-closure(q_3) = $\{q_3, q_1, q_2, q_5\}$

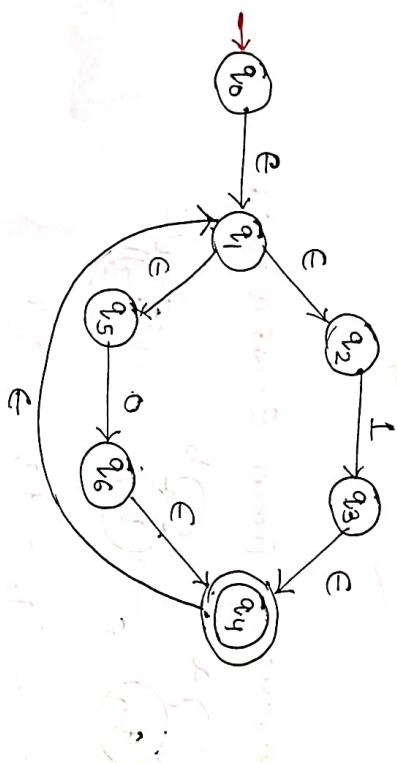
E-closure(q_4) = $\{q_4, q_1, q_2, q_5\}$

E-closure(q_5) = $\{q_6, q_4, q_1, q_2, q_5\}$

DFA
 \rightarrow $(\{q_0, q_1, q_2\}, \{q_1, q_2\}, q_2)$



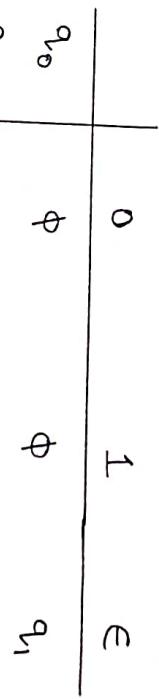
Ques conversion from E-NFA into DFA



E-NFA

\Rightarrow E-closure(q_0) = $\{q_0, q_1, q_2, q_3, q_4, q_5, q_6\}$

E-NFA
 \rightarrow $(0, 1, \epsilon, q_1)$



Ques: Remove left Recursion : Spanning (1) 1

$$E \rightarrow E + T \mid T$$

$$T \rightarrow T * F \mid F$$

$$F \rightarrow (E) \mid id$$

$$\Rightarrow E \rightarrow E + T \mid T$$

$$\therefore E \rightarrow T E'$$

$$E' \rightarrow + T E' \mid \epsilon$$

$$\boxed{E \rightarrow \boxed{E + T} \mid T}$$

$$\boxed{T \rightarrow \boxed{T * F} \mid F}$$

$$T \rightarrow T * F \mid F$$

$$\therefore T \rightarrow F T'$$

$$T' \rightarrow * F T' \mid \epsilon$$

\therefore Production will be -

$$E \rightarrow T E'$$

$$E' \rightarrow + T E' \mid \epsilon$$

$$T \rightarrow F T'$$

$$T' \rightarrow * F T' \mid \epsilon$$

$$F \rightarrow (E) \mid id$$

(ii) $A \rightarrow ABD \mid A\alpha\beta\alpha$

$$B \rightarrow Belb$$

$$\boxed{A \rightarrow \boxed{ABD} \mid \boxed{A\alpha\beta\alpha}}$$

$$\Rightarrow A \rightarrow \alpha A'$$

$$A' \rightarrow BdA' \mid \alpha A' \mid \epsilon$$

$$B \rightarrow bB'$$

$$B' \rightarrow eB' \mid \epsilon$$

LL(1) → look ahead symbol

$\swarrow \downarrow$ left to leftmost right derivative

First

- $E \rightarrow TE'$
- $E' \rightarrow +TE' | \epsilon$
- $T \rightarrow FT'$
- $T' \rightarrow *FT' | \epsilon$
- $F \rightarrow (\epsilon) | id$

First

- $first(E) = \{ id, (\}$
 $first(E') = \{ +, \epsilon \}$
 $first(T) = \{ id, (\}$
 $first(T') = \{ *, \epsilon \}$
 $first(F) = \{ (, id \}$

Follow

- $follow(E) = \{ \$,) \}$
 $follow(E') = \{ +, \$,) \}$
 $follow(T) = \{ +, \$,) \}$
 $follow(T') = \{ +, \$,) \}$
 $follow(F) = \{ *, +, \$,) \}$

First

- $$\begin{array}{l} A \rightarrow cCA' | CA' \\ A' \rightarrow cBA' | \epsilon \\ B \rightarrow bB | id \\ C \rightarrow BBC' | BC' \\ C' \rightarrow aBC' | \epsilon \end{array}$$

$A \rightarrow AcB | cc | C$
 $B \rightarrow bB | id$
 $A \rightarrow AcB | C$

Production	+	*	()	id	\$
E						
E'	$E' \rightarrow +TE'$		$E \rightarrow TE'$		$E \rightarrow TE'$	
T			$T \rightarrow FT'$		$E' \rightarrow \epsilon$	
T'	$T \rightarrow E$	$T' \rightarrow *FT'$		$T \rightarrow FT'$		
F			$T \rightarrow E$		$T \rightarrow E$	
					$F \rightarrow (E)$	
						$F \rightarrow id$

Bottom up Parsing: (Pruning)

1.	$S \rightarrow aABe$	$+ id_3 \$$	Replace by $E \rightarrow id$
	$A \rightarrow Abc b$	$+ id_3 \$$	shift
	$B \rightarrow d$	$id_3 \$$	
	Input string - abbcde	(RMD) in reverse order	
	\downarrow		
	abbcde	$A \rightarrow b$	
	\downarrow		
	aAbcde	$A \rightarrow Abc$	
	\downarrow		
	aAde	$B \rightarrow d$	
	\downarrow		
	aABe	$S \rightarrow aABe$	
	\downarrow		
	S		

Shift Reduce Parser:

1. $E \rightarrow E + E$
 $E \rightarrow E * E$
 $E \rightarrow id$

Input string: $id_1 + id_2 + id_3$

\Rightarrow stack

Action

Input Buffer	Action
$\$$	shift
id_1	Replace by $E \rightarrow id$
$+ id_2 + id_3 \$$	
$+ id_2 + id_3 \$$	shift
$id_2 + id_3 \$$	shift

2. $E \rightarrow E + T | T$

$T \rightarrow F * F | F$

$F \rightarrow (E) | id$

Input string: $id * id$

$\$ E + id_3 \$$	$+ id_3 \$$	Replace by $E \rightarrow id$
$\$ E +$	$id_3 \$$	shift
$id_2 + id_3 \$$	$id_2 + id_3 \$$	Accept
$id_2 + id_3 \$$	$id_2 + id_3 \$$	

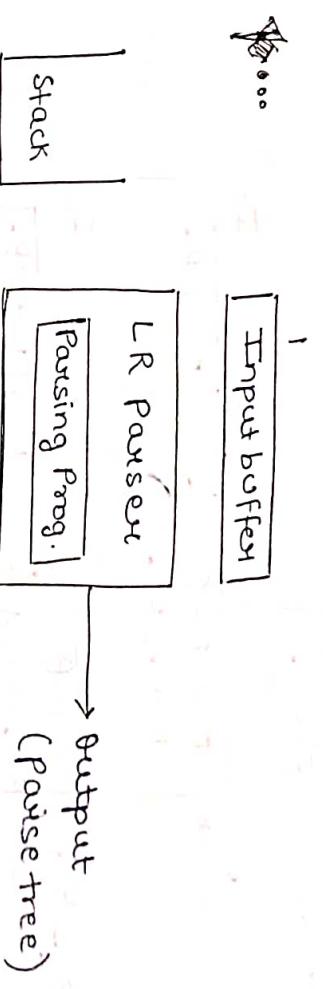
Operator Precedence

Rule1: In RHS, there should not present \in
Rule2: And no two Non-terminals must be together at RHS.

<u>Guess:</u> $E \rightarrow E+E \mid E*E \mid id$	[Terminals have high priority then - operator then - \$]
$+ > < < >$	
$* > > < >$	
$id > > > >$	
$< < < Accept$	

LR Parser:

$L \rightarrow R \rightarrow$ Right most derivative
 Left to Right



Start	Relation	Input String	Operation
\$	<	id + id * id \$	shift id
\$ id	>	+ id * id \$	Reduce $E \rightarrow id$
\$ E	<	id * id \$	shift +
\$ E +	<	id * id \$	shift id
\$ E + id	>		Reduce $E \rightarrow id$
\$ E + E	<		Shift *
\$ E + E *	<		Shift id
\$ E + E * id	>		Reduce $E \rightarrow id$
\$ E + E * E	>		$E \rightarrow E + E$

Guess: $E \rightarrow BB \mid B \rightarrow cB \mid d$

Input string: ccdd\$

\Rightarrow Step1: Augment the grammar take.

Action	Goto
Instructions	

$\left\{ \begin{array}{l} \text{if we have} \\ \text{commas} \\ \text{then,} \\ S' \rightarrow S \end{array} \right.$
Augment

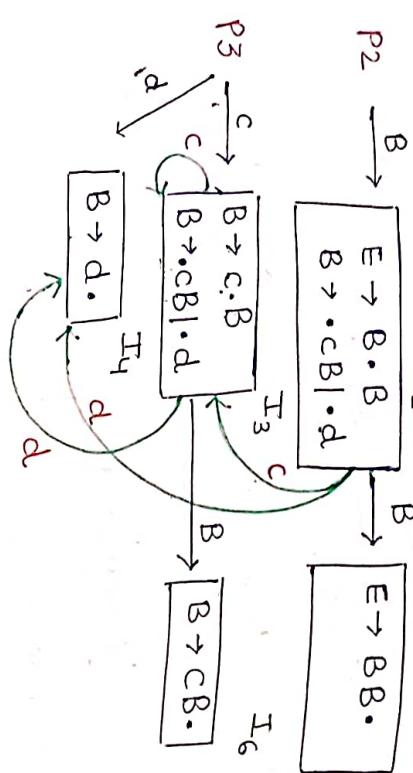
Step 2: Draw canon.

item:

$$\begin{array}{l} I_0 \\ P1 \quad E' \rightarrow E \\ P2 \quad E \rightarrow \bullet BB \\ P3 \quad B \rightarrow \bullet cB | \bullet d \end{array}$$

canonical form

$$\left. \begin{array}{l} E' \rightarrow E \\ E' \rightarrow \bullet E \end{array} \right\} LR(0)$$



Step 3: Name the production

$$\begin{array}{l} E \xrightarrow{1} E' \\ B \xrightarrow{2} \bullet B B \\ B \xrightarrow{3} \bullet cB | \bullet d \end{array}$$

Step 4: Create the parsing table

States	c	d	\$	Action
I ₀	S ₃	S ₄		
I ₁				Accept
I ₂	S ₃	S ₄		
I ₃	h ₃	h ₃		
I ₄	h ₁	h ₁		
I ₅	h ₁	h ₁		
I ₆	h ₂	h ₂		

stack	Input	Action
\$0	c	shift c and goto statement 3
\$0c3	3	shift c and goto statement 3
\$0c3c3d4	d	shift d → 4
\$0c3c3B6	B	reduced B → cB
\$0c3B6	d	reduced B → cB
\$QB2	d	Shift d → 4
\$QB2d	d	Shift d → 4

Reduced E_{RL}

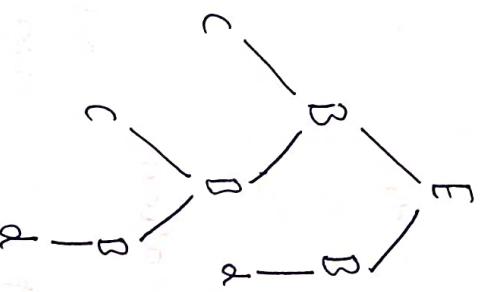
Guess:

$$E \rightarrow T + E | T$$

\$ OBS₅

\$ Q_{E1}

Step 6: Parse tree



\$

\$

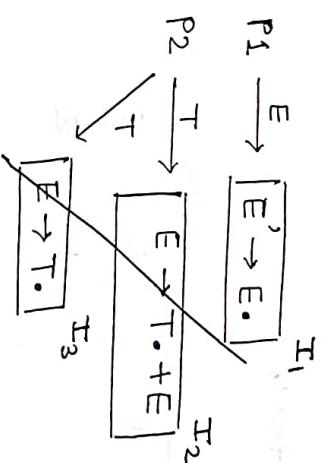
Accept

⇒ Step 1: Augment the grammar

$$\begin{array}{l} E' \rightarrow E \\ E \rightarrow T + E | T \\ T \rightarrow id \end{array}$$

Step 2: Draw canonical collection of LR(0) items:

$$\begin{array}{ll} P_1 & \boxed{E' \rightarrow \cdot E} \quad I_1 \\ P_2 & \boxed{E \rightarrow \cdot T + E | \cdot T} \quad I_2 \\ P_3 & \boxed{T \rightarrow \cdot id} \quad I_3 \end{array}$$



SLR Parser:

Step 4 Parsing table

→ follow of canonical collection

→ Then write producing name as x_1, x_2, \dots

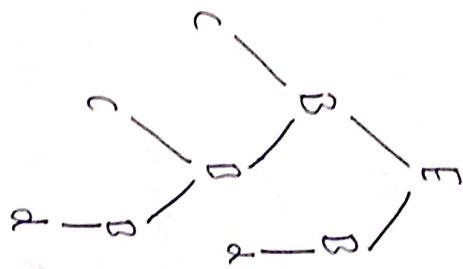
Reduced $E \Rightarrow_L$

Ques: $E \rightarrow T + E \mid T$
 $T \rightarrow id$

\$0\beta\beta\\$

\$OEI

Step: Parse tree



⇒ Step 1: Augment the grammar

$$\begin{aligned} E' &\rightarrow E \\ E &\rightarrow T + E \mid T \\ T &\rightarrow id \end{aligned}$$

Step 2: Draw canonical collection of LR(0) items:

$$\begin{array}{|l|} \hline P_1 \\ \hline E \rightarrow \cdot E \\ \hline P_2 \\ \hline E \rightarrow \cdot T + E \cdot \mid T \\ \hline P_3 \\ \hline T \rightarrow \cdot id \\ \hline \end{array} I_0$$

$$\begin{array}{c} P_1 \xrightarrow{E} [E \rightarrow E \cdot] \\ \downarrow \\ P_2 \xrightarrow{T} [E \rightarrow T \cdot + E] \\ \diagdown \\ \boxed{[E \rightarrow T \cdot]} \quad I_3 \end{array} I_1$$

$$\begin{array}{c} P_1 \xrightarrow{E} [E \rightarrow E \cdot] \\ \downarrow \\ P_2 \xrightarrow{T} [E \rightarrow T \cdot + E] \\ \diagup \\ \boxed{[E \rightarrow T \cdot]} \quad I_3 \end{array} I_2$$

SLR Parser:

Step 4 Parsing table

→ follow of canonical collection

→ Then write producing name as x_1, x_2, \dots

$$P_1 \xrightarrow{E} [E' \rightarrow E \cdot]^{T_1}$$

$$P_2 \xrightarrow{T} [E \rightarrow T \cdot + E \mid T \cdot]^{T_2} + \xrightarrow{+} [E \rightarrow T \cdot + \cdot E \mid T \cdot]^{T_3} \xrightarrow{T} [E \rightarrow \cdot T + E \cdot \mid T \cdot]^{T_4} \xrightarrow{E} [E \rightarrow T \cdot + E \cdot \mid T \cdot]^{T_5}$$

$$P_3 \xrightarrow{id} [\overline{T \rightarrow id \cdot}]^{T_3}$$

$\text{first}(E) = \{\text{id}\}$
 $\text{first}(T) = \{\text{id}\}$

$\text{follow}(E) = \{\$\}$
 $\text{follow}(T) = \{+, \$\}$

SLR parser:

States	Action			
	id	\$	E	T
I_0				
I_1				
I_2				
I_3	s_4			
I_4	s_3			
I_5	s_3			
	h_1	h_1	h_1	

- Step 3: Name the production.
- $E \rightarrow \frac{1}{T+E} \mid \frac{2}{T}$
 $T \rightarrow \frac{3}{id}$

Step 4: Create the parsing table (LR(0))

States	Action			
	id	\$	E	T
I_0				
I_1				
I_2				
I_3				
I_4				
I_5				

CLR parser

Ans: $S \rightarrow CC$

$C \rightarrow cC$

$C \rightarrow d$

\Rightarrow Step 1: Augment the grammar -

$S' \rightarrow S$

$S \rightarrow CC$

$C \rightarrow cC$

$C \rightarrow d$

Step 2: Draw canonical collection

$P_1 \left[S' \rightarrow \cdot S, \$ \right]$
 $P_2 \left[S \rightarrow \cdot CC, \$ \right]$
 $P_3 \left[C \rightarrow \cdot cC, cld \right]$
 $P_4 \left[C \rightarrow \cdot d, cld \right]$

follow(S') = $\$$
 follow(S) = $\$$
 follow(C) = c, d

\downarrow
 I_1

$P_1 \xrightarrow{S} [S' \rightarrow S, \$]$
 I_2

$P_2 \xrightarrow{C} \left[\begin{array}{l} S \rightarrow C \cdot C, \$ \\ C \rightarrow \cdot cC, \$ \\ C \rightarrow \cdot d, \$ \end{array} \right]$
 I_3

$P_3 \xrightarrow{C} \left[\begin{array}{l} S \rightarrow CC \cdot, \$ \\ C \rightarrow c \cdot C, \$ \\ C \rightarrow \cdot d, \$ \end{array} \right]$
 I_4

$P_4 \xrightarrow{C} \left[\begin{array}{l} S \rightarrow CC \cdot, \$ \\ C \rightarrow cC \cdot, \$ \\ C \rightarrow \cdot d, \$ \end{array} \right]$
 I_5

$P_3 \xrightarrow{C} \left[\begin{array}{l} C \rightarrow c \cdot C, cld \\ C \rightarrow \cdot cC, cld \\ C \rightarrow \cdot d, cld \end{array} \right]$
 I_6

$P_4 \xrightarrow{C} \left[\begin{array}{l} C \rightarrow d \cdot, \$ \\ C \rightarrow cC \cdot, cld \end{array} \right]$
 I_7

$P_4 \xrightarrow{d} \left[\begin{array}{l} C \rightarrow d \cdot, cld \end{array} \right]$
 I_8

Action	state	s	d	\$	s	c
Accept	s_3	s_4			1	2
	s_6	s_7			5	
	s_3	s_4			8	
	s_6	s_7				
	s_3	s_3				
	s_6	s_7				
	s_2	s_2				
	s_2	s_2				

Stack Implementation:

Stack

Input

return

$E \rightarrow \text{digit}$

$E \rightarrow E + T$

$E \rightarrow E - T$

$E \rightarrow T$

$T \rightarrow T * F$

$T \rightarrow T / F$

$F \rightarrow (E)$

$F \rightarrow \text{digit}$

$E \rightarrow \text{digit} * \text{digit}$

$E \rightarrow \text{digit} - \text{digit}$

$E \rightarrow \text{digit}$

$T \rightarrow \text{digit} * \text{digit}$

$T \rightarrow \text{digit} / \text{digit}$

$F \rightarrow (\text{digit})$

$F \rightarrow \text{digit}$

$E \rightarrow \text{digit} . \text{digit}$

$E \rightarrow \text{digit} . \text{digit} * \text{digit}$

$E \rightarrow \text{digit} . \text{digit} / \text{digit}$

$E \rightarrow \text{digit} . \text{digit} (\text{digit})$

$E \rightarrow \text{digit} . \text{digit} . \text{digit}$

$E \rightarrow \text{digit} . \text{digit} . \text{digit} * \text{digit}$

$E \rightarrow \text{digit} . \text{digit} . \text{digit} / \text{digit}$

$E \rightarrow \text{digit} . \text{digit} . \text{digit} (\text{digit})$

$E \rightarrow \text{digit} . \text{digit} . \text{digit} . \text{digit}$

$E \rightarrow \text{digit} . \text{digit} . \text{digit} . \text{digit} * \text{digit}$

$E \rightarrow \text{digit} . \text{digit} . \text{digit} . \text{digit} / \text{digit}$

$E \rightarrow \text{digit} . \text{digit} . \text{digit} . \text{digit} (\text{digit})$

$E \rightarrow \text{digit} . \text{digit} . \text{digit} . \text{digit} . \text{digit}$

$E \rightarrow \text{digit} . \text{digit} . \text{digit} . \text{digit} . \text{digit} * \text{digit}$

$E \rightarrow \text{digit} . \text{digit} . \text{digit} . \text{digit} . \text{digit} / \text{digit}$

$E \rightarrow \text{digit} . \text{digit} . \text{digit} . \text{digit} . \text{digit} (\text{digit})$

$E \rightarrow \text{digit} . \text{digit} . \text{digit} . \text{digit} . \text{digit} . \text{digit}$

• LALR parser:

Given: $S \rightarrow A \alpha b \beta c \delta d \gamma$

$A \rightarrow d$

• SDT : (Syntax Directed Translation):

Given semantic rules = SDT

- 1. Synthesized attribute
- 2. Inherited attribute

- If a node takes values from child node then it is synthesized attribute.

SDD:

Given: Construct parse tree/ Syntax tree and annotated parse tree for the input string

$S \rightarrow E$

$E \rightarrow E + T$

$E \cdot \text{val} = E \cdot \text{val} + T \cdot \text{val}$

$E \rightarrow E - T$

$E \cdot \text{val} = E \cdot \text{val} - T \cdot \text{val}$

$E \rightarrow T$

$E \cdot \text{val} = T \cdot \text{val}$

$T \rightarrow T * F$

$T \cdot \text{val} = T \cdot \text{val} * F \cdot \text{val}$

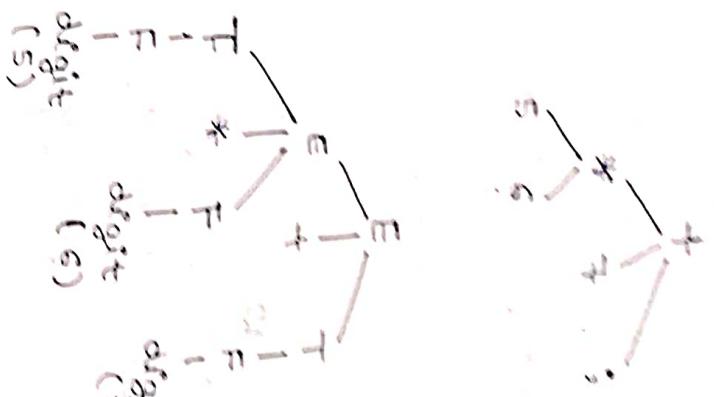
$T \rightarrow T / F$

$T \cdot \text{val} = T \cdot \text{val} / F \cdot \text{val}$

$F \rightarrow (E)$

$F \cdot \text{val} = E \cdot \text{val}$

$F \cdot \text{val} = \text{digit}$



S. on

carried forward by concatenation

ques: Annotated parse tree

$5 + 3 * 4$

Production Rule

$E \rightarrow E + F$

$E \rightarrow T$

$T \rightarrow T * F$

$T \rightarrow F$

$F \rightarrow \text{digit}$

Semantic Actions

$E.\text{val} = E.\text{val} + T.\text{val}$

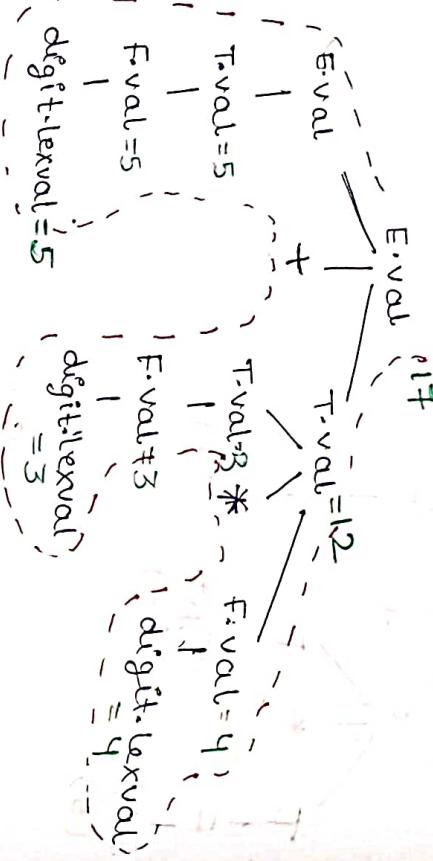
$E.\text{val} = T.\text{val}$

$T.\text{val} = T.\text{val} * F.\text{val}$

$T.\text{val} = F.\text{val}$

$F.\text{val} = \text{digit}.lexval$

\Rightarrow



Ques: dependency graph:

Production rule

Semantic Actions

$S \rightarrow T L$

$T \rightarrow \text{int}$

$T \rightarrow \text{float}$

$T \rightarrow \text{char}$

$T \rightarrow \text{double}$

$L \rightarrow \text{cd}$

value obtained from child to parent

value obtained from parent to child

