

Principles of Programming Languages - Homework 11

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1 Problem 1

(a)

$t_0 <: t_1$: type t_0 can be safely substituted by values of type t_1 .

(i) True: Number can safely be substituted by values of Number. Follows the SubRef rule.

(ii) False.

(iii) True: Number can safely be substituted by values of Any. Rule SubAny.

(iv) True: Var to Const is permitted by rule SubObjMut, and Number to Any by rule SubAny.

(v) False.

(vi) False.

(vii) False.

(viii) True.

(ix) False.

(b)

(i) (1): It will safely evaluate. It will produce a value. The value that `fun(x).f` would return would be 4. (2): TypeCall requires that the type of the argument in a call expression precisely matches the type of the function parameter that it is passed to. So it will not be well-typed with subtyping since that is not the case. The `const x` is missing the field `g` (which is a boolean). Also, `x` (declared on line 1) is not a subtype of `y` (in the parameter declared on line 2).

(ii) (1): It will safely evaluate. It will produce a value. The value that `fun(x).f` would return would be 3. (2): It is well-typed with subtype since `x` (declared on line 1) is a subtype of the parameter `y` (declared on line 2).

(iii) (1): It will safely evaluate. The function `fun` returns the argument that is passed into it (`x`), and thus accessing `g` will return `true`. (2): It is not well-typed with subtype since `fun` returns an object that is of type `{var f: number}`. This object does not have a field called `g`.

(iv) (1): It will safely evaluate. It will produce a value. The value would be 1. (2): It is well-typed. Both of the branches x and y can be resolved to any common supertype $\{\text{const } f: \text{any}, \text{const } g: \text{any}\}$ in accordance to the new `TypeIf` rule.