LalCheetah ICPC Team Notebook (2016-17)

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1 Combinatorial optimization

1.1 Sparse max-flow(aka Modified Ford Fulkerson)

```
// Adjacency list implementation of Dinic's blocking flow
     algorithm.
// This is very fast in practice, and only loses to push-
     relabel flow.
// Running time:
      O(|V|^2 |E|)
      - graph, constructed using AddEdge()
       - source and sink
     - maximum flow value
      - To obtain actual flow values, look at edges with
         (zero capacity edges are residual edges).
#include<cstdio>
#include < vector >
#include<queue>
using namespace std;
typedef long long LL;
struct Edge {
 int u, v;
 LL cap, flow;
```

```
Edge(int u, int v, LL cap): u(u), v(v), cap(cap), flow(0)
struct Dinic {
 int N;
  vector<Edge> E;
  vector<vector<int>> g;
  vector<int> d, pt;
 \label{eq:definition} \mbox{Dinic(int N): } \mbox{N(N), } \mbox{E(0), } \mbox{g(N), } \mbox{d(N), } \mbox{pt(N) } \mbox{\{} \mbox{\}}
  void AddEdge(int u, int v, LL cap) {
    if (u != v) {
      E emplace_back(Edge(u, v, cap));
      g[u].emplace_back(E.size() - 1);
      E.emplace_back(Edge(v, u, 0));
      g[v].emplace_back(E.size() - 1);
 bool BFS(int S, int T) {
    queue<int> q({S});
    fill(d.begin(), d.end(), N + 1);
    d[S] = 0;
    while(!q.empty()) {
      int u = q.front(); q.pop();
      if (u == T) break;
      for (int k: g[u]) {
   Edge &e = E[k];
        if (e.flow < e.cap && d[e.v] > d[e.u] + 1) {
          d[e.v] = d[e.u] + 1;
           q.emplace(e.v);
    return d[T] != N + 1;
  LL DFS (int u, int T, LL flow = -1) {
    if (u == T || flow == 0) return flow;
    for (int &i = pt[u]; i < g[u].size(); ++i) {</pre>
      Edge &e = E[g[u][i]];
      Edge &oe = E[g[u][i]^1];
      if (d[e.v] == d[e.u] + 1)
        LL amt = e.cap - e.flow;
        if (flow !=-1 \&\& amt > flow) amt = flow;
        if (LL pushed = DFS(e.v, T, amt)) {
          e.flow += pushed;
           oe flow -= pushed;
           return pushed;
    return 0:
  LL MaxFlow(int S, int T) {
    LL total = 0;
    while (BFS(S, T)) {
      fill(pt.begin(), pt.end(), 0);
      while (LL flow = DFS(S, T))
    return total;
};
// The following code solves SPOJ problem #4110: Fast
     Maximum Flow (FASTFLOW)
int main()
 int N, E;
scanf("%d%d", &N, &E);
  Dinic dinic(N);
  for (int i = 0; i < E; i++)
    int u, v;
    LL cap; scanf("%d%d%lld", &u, &v, &cap);
    dinic.AddEdge(u - 1, v - 1, cap);
    dinic.AddEdge(v - 1, u - 1, cap);
  printf("%lld\n", dinic.MaxFlow(0, N - 1));
  return 0:
```

// END CUT

1.2 Global min-cut

```
// Adjacency matrix implementation of Stoer-Wagner min cut
     algorithm
// Running time:
      0(|V|^3)
// INPUT:
       - graph, constructed using AddEdge()
// OUTPUT:
       - (min cut value, nodes in half of min cut)
#include <cmath>
#include <vector>
#include <iostream>
using namespace std;
typedef vector<int> VI;
typedef vector<VI> VVI;
const int INF = 1000000000;
pair<int, VI> GetMinCut(VVI &weights) {
  int N = weights.size();
  VI used(N), cut, best_cut;
  int best_weight = -1;
  for (int phase = N-1; phase >= 0; phase--) {
   VI w = weights[0];
    VI added = used;
    int prev, last = 0;
    for (int i = 0; i < phase; i++) {</pre>
      prev = last;
last = -1;
      for (int j = 1; j < N; j++)
        if (!added[j] && (last == -1 || w[j] > w[last]))
      if (i == phase-1) {
        for (int j = 0; j < N; j++) weights[prev][j] +=</pre>
              weights[last][j];
        for (int j = 0; j < N; j++) weights[j][prev] =</pre>
        weights[prev][j];
used[last] = true;
cut.push_back(last);
        if (best_weight == -1 || w[last] < best_weight) {</pre>
          best_cut = cut;
          best_weight = w[last];
        for (int j = 0; j < N; j++)
        w[j] += weights[last][j];
added[last] = true;
  return make_pair(best_weight, best_cut);
// BEGIN CUT
// The following code solves UVA problem #10989: Bomb,
    Divide and Conquer
int main() {
 int N;
  cin >> N;
  for (int i = 0; i < N; i++) {
   int n, m;
    cin >> n >> m;
    VVI weights(n, VI(n));
    for (int j = 0; j < m; j++) {
     int a, b, c;
      cin >> a >> b >> c;
      weights[a-1][b-1] = weights[b-1][a-1] = c;
    pair<int, VI> res = GetMinCut(weights);
    cout << "Case #" << i+1 << ": " << res.first << endl;
// END CUT
```

2 Geometry

2.1 Convex hull

```
// Compute the 2D convex hull of a set of points using the
     monotone chain
// algorithm. Eliminate redundant points from the hull if
      REMOVE REDUNDANT is
// #defined.
// Running time: O(n log n)
     INPUT: a vector of input points, unordered.
     OUTPUT: a vector of points in the convex hull,
     counterclockwise, starting
               with bottommost/leftmost point
#include <cstdio>
#include <cassert>
#include <vector>
#include <algorithm>
#include <cmath>
// BEGIN CUT
#include <map>
// END CUT
using namespace std;
#define REMOVE_REDUNDANT
typedef double T;
const T EPS = 1e-7:
struct PT {
 T x, y;
PT() {}
 PT(T x, T y) : x(x), y(y) {}
 bool operator<(const PT &rhs) const { return make_pair(y,</pre>
       x) < make_pair(rhs.y,rhs.x); }</pre>
 bool operator==(const PT &rhs) const { return make_pair(y
       ,x) == make_pair(rhs.y,rhs.x); }
T cross(PT p, PT q) { return p.x*q.y-p.y*q.x; }
T area2(PT a, PT b, PT c) { return cross(a,b) + cross(b,c)
      + cross(c,a); }
#ifdef REMOVE REDUNDANT
bool between (const PT &a, const PT &b, const PT &c) {
 return (fabs(area2(a,b,c)) < EPS && (a.x-b.x)*(c.x-b.x) 

<= 0 && (a.y-b.y)*(c.y-b.y) <= 0);
#endif
void ConvexHull(vector<PT> &pts) {
  sort(pts.begin(), pts.end());
  pts.erase(unique(pts.begin(), pts.end()), pts.end());
  vector<PT> up, dn;
  for (int i = 0; i < pts.size(); i++) {</pre>
    while (up.size() > 1 && area2(up[up.size()-2], up.back
         (), pts[i]) >= 0) up.pop_back();
    while (dn.size() > 1 && area2(dn[dn.size()-2], dn.back
         (), pts[i]) <= 0) dn.pop_back();
    up.push_back(pts[i]);
    dn.push_back(pts[i]);
  for (int i = (int) up.size() - 2; i >= 1; i--) pts.
       push_back(up[i]);
#ifdef REMOVE REDUNDANT
  if (pts.size() <= 2) return;</pre>
  dn.clear();
  dn.push_back(pts[0]);
  dn.push_back(pts[1]);
  for (int i = 2; i < pts.size(); i++) {</pre>
    if (between(dn[dn.size()-2], dn[dn.size()-1], pts[i]))
         dn.pop_back();
    dn.push_back(pts[i]);
  if (dn.size() >= 3 && between(dn.back(), dn[0], dn[1])) {
    dn[0] = dn.back();
    dn.pop_back();
```

```
pts = dn:
#endif
// BEGIN CUT
// The following code solves SPOJ problem #26: Build the
     Fence (BSHEEP)
int main() {
 int t:
  scanf("%d", &t);
  for (int caseno = 0; caseno < t; caseno++) {</pre>
    int n;
    scanf("%d", &n);
    vector<PT> v(n);
    for (int i = 0; i < n; i++) scanf("%lf%lf", &v[i].x, &v</pre>
    [i].y);
vector<PT> h(v);
    map<PT,int> index;
    for (int i = n-1; i >= 0; i--) index[v[i]] = i+1;
    ConvexHull(h);
    double len = 0;
    for (int i = 0; i < h.size(); i++) {</pre>
      double dx = h[i].x - h[(i+1)%h.size()].x;
      double dy = h[i].y - h[(i+1)%h.size()].y;
      len += sqrt (dx*dx+dy*dy);
    if (caseno > 0) printf("\n");
    printf("%.2f\n", len);
    for (int i = 0; i < h.size(); i++) {
      if (i > 0) printf(" ");
      printf("%d", index[h[i]]);
    printf("\n");
// END CUT
```

2.2 Miscellaneous geometry

```
// C++ routines for computational geometry.
#include <iostream>
#include <vector>
#include <cmath>
#include <cassert>
using namespace std;
 double INF = 1e100;
double EPS = 1e-12;
struct PT {
   double x, y;
   PT() {}
   PT (double x, double y) : x(x), y(y) {}
  PT(const PT &p) : x(p.x), y(p.y)
PT operator + (const PT &p) con
                                     const { return PT(x+p.x, y+p
   PT operator - (const PT &p) const { return PT(x-p.x, y-p
   PT operator * (double c)
                                     const { return PT(x*c,
           ):
  PT operator / (double c)
                                     const { return PT(x/c, y/c
           ); }
};
double dot(PT p, PT q)
                                  return p.x*q.x+p.y*q.y; }
double dist2(PT p, PT q) { return dot(p-q,p-q)
double cross(PT p, PT q) { return p.x+q.y-p.y+
ostream &operator<<(ostream &o, const PT &p) {
  os << "(" << p.x << "," << p.y << ")";</pre>
                                { return dot(p-q,p-q); }
                                { return p.x*q.y-p.y*q.x; }
 // rotate a point CCW or CW around the origin
PT RotateCCW90(PT p) { return PT(-p.y,p.x);
PT RotateCW90 (PT p)
                            { return PT(p.y,-p.x); }
PT RotateCCW(PT p, double t) {
  return PT(p.x*cos(t)-p.y*sin(t), p.x*sin(t)+p.y*cos(t));
// project point c onto line through a and b
// assuming a != b
PT ProjectPointLine(PT a, PT b, PT c) {
```

```
return a + (b-a)*dot(c-a, b-a)/dot(b-a, b-a);
// project point c onto line segment through a and b
PT ProjectPointSegment (PT a, PT b, PT c) {
   double r = dot(b-a, b-a);
   if (fabs(r) < EPS) return a;</pre>
   r = dot(c-a, b-a)/r;
   if (r < 0) return a;</pre>
   if (r > 1) return b;
   return a + (b-a) *r;
// compute distance from c to segment between a and b
double DistancePointSegment(PT a, PT b, PT c) {
   return sqrt(dist2(c, ProjectPointSegment(a, b, c)));
// compute distance between point (x,y,z) and plane ax+by+
double d)
   return fabs(a*x+b*y+c*z-d)/sqrt(a*a+b*b+c*c);
// determine if lines from a to b and c to d are parallel
        or collinear
bool LinesParallel(PT a, PT b, PT c, PT d) {
   return fabs(cross(b-a, c-d)) < EPS;
bool LinesCollinear (PT a, PT b, PT c, PT d) {
   return LinesParallel(a, b, c, d)
&& fabs(cross(a-b, a-c)) < EPS</pre>
           && fabs(cross(c-d, c-a)) < EPS;
// determine if line segment from a to b intersects with
// line seament from c to d
bool SegmentsIntersect(PT a, PT b, PT c, PT d) {
   if (LinesCollinear(a, b, c, d)) {
       if (dist2(a, c) < EPS || dist2(a, d) < EPS ||</pre>
          dist2(b, c) < EPS || dist2(b, d) < EPS) return true;
       if (dot(c-a, c-b) > 0 \&\& dot(d-a, d-b) > 0 \&\& dot(c-b, d-b) > 0 && d
                d-b) > 0)
           return false;
       return true;
   if (cross(d-a, b-a) * cross(c-a, b-a) > 0) return false;
   if (cross(a-c, d-c) * cross(b-c, d-c) > 0) return false;
   return true;
\ensuremath{//} compute intersection of line passing through a and b
// with line passing through c and d, assuming that unique
// intersection exists; for segment intersection, check if
// segments intersect first
PT ComputeLineIntersection(PT a, PT b, PT c, PT d) {
   b=b-a; d=c-d; c=c-a;
assert(dot(b, b) > EPS && dot(d, d) > EPS);
   return a + b*cross(c, d)/cross(b, d);
// compute center of circle given three points
PT ComputeCircleCenter(PT a, PT b, PT c) {
   b = (a+b)/2;
   c = (a + c) / 2;
   return ComputeLineIntersection(b, b+RotateCW90(a-b), c, c
             +RotateCW90(a-c));
// determine if point is in a possibly non-convex polygon (
         by William
// Randolph Franklin); returns 1 for strictly interior
        points, 0 for
// strictly exterior points, and 0 or 1 for the remaining
        points.
// Note that it is possible to convert this into an *exact*
           test using
// integer arithmetic by taking care of the division
         appropriately
// (making sure to deal with signs properly) and then by
         writing exact
// tests for checking point on polygon boundary
bool PointInPolygon(const vector<PT> &p, PT q) {
   bool c = 0;
```

```
for (int i = 0; i < p.size(); i++) {</pre>
    int j = (i+1)%p.size();
    if ((p[i].y <= q.y && q.y < p[j].y ||</pre>
      p[j].y \le q.y \&\& q.y < p[i].y) \&\&
      q.x < p[i].x + (p[j].x - p[i].x) * (q.y - p[i].y) / (
           p[j].y - p[i].y)
  return c;
// determine if point is on the boundary of a polygon
bool PointOnPolygon(const vector<PT> &p, PT q) {
  for (int i = 0; i < p.size(); i++)</pre>
    if (dist2(ProjectPointSegment(p[i], p[(i+1)%p.size()],
         q), q) < EPS)
      return true;
    return false;
// compute intersection of line through points a and b with
// circle centered at c with radius r > 0
vector<PT> CircleLineIntersection(PT a, PT b, PT c, double
     r) {
  vector<PT> ret;
  b = b-a;
  double A = dot(b, b);
  double B = dot(a, b);
  double C = dot(a, a) - r*r;
  double D = B*B - A*C;
  if (D < -EPS) return ret;</pre>
  ret.push_back(c+a+b*(-B+sqrt(D+EPS))/A);
  if (D > EPS)
    ret.push_back(c+a+b*(-B-sqrt(D))/A);
  return ret;
// compute intersection of circle centered at a with radius
// with circle centered at b with radius R
vector<PT> CircleCircleIntersection(PT a, PT b, double r,
     double R) {
  vector<PT> ret;
  double d = sqrt(dist2(a, b));
  if (d > r+R \mid | d+min(r, R) < max(r, R)) return ret;
  double x = (d*d-R*R+r*r)/(2*d);
double y = sqrt(r*r-x*x);
  PT v = (b-a)/d;
  ret.push_back(a+v*x + RotateCCW90(v)*y);
    ret.push_back(a+v*x - RotateCCW90(v)*y);
  return ret;
// This code computes the area or centroid of a (possibly
     nonconvex)
// polygon, assuming that the coordinates are listed in a
     clockwise or
// counterclockwise fashion. Note that the centroid is
     often known as
// the "center of gravity" or "center of mass".
double ComputeSignedArea(const vector<PT> &p) {
  double area = 0;
  for(int i = 0; i < p.size(); i++) {</pre>
   int j = (i+1) % p.size();
    area += p[i].x*p[j].y - p[j].x*p[i].y;
  return area / 2.0;
double ComputeArea(const vector<PT> &p) {
  return fabs(ComputeSignedArea(p));
PT ComputeCentroid(const vector<PT> &p) {
  PT c(0,0);
  double scale = 6.0 * ComputeSignedArea(p);
  for (int i = 0; i < p.size(); i++) {</pre>
   int j = (i+1) % p.size();
    c = c + (p[i]+p[j])*(p[i].x*p[j].y - p[j].x*p[i].y);
  return c / scale;
// tests whether or not a given polygon (in CW or CCW order
     ) is simple
bool IsSimple(const vector<PT> &p) {
  for (int i = 0; i < p.size(); i++) {</pre>
```

```
int j = (i+1) % p.size();
     int 1 = (k+1) % p.size();
    if (i == 1 \mid \mid j == k) continue;
    if (SegmentsIntersect(p[i], p[j], p[k], p[l]))
      return false;
 return true;
int main() {
  // expected: (-5,2)
 cerr << RotateCCW90(PT(2,5)) << endl;</pre>
  // expected: (5,-2)
 cerr << RotateCW90(PT(2,5)) << endl;</pre>
  // expected: (-5,2)
 cerr << RotateCCW(PT(2,5),M_PI/2) << endl;</pre>
 // expected: (5,2)
 cerr << ProjectPointLine(PT(-5,-2), PT(10,4), PT(3,7)) <</pre>
 // expected: (5,2) (7.5,3) (2.5,1)
 << ProjectPointSegment(PT(-5,-2), PT(2.5,1), PT(3,7)
          ) << endl;
 // expected: 6.78903
 cerr << DistancePointPlane(4,-4,3,2,-2,5,-8) << endl;</pre>
 // expected: 1 0 1
 << LinesParallel(PT(1,1), PT(3,5), PT(2,0), PT(4,5))
<< " "
      << LinesParallel(PT(1,1), PT(3,5), PT(5,9), PT(7,13)
          ) << endl;
 // expected: 0 0 1
 << LinesCollinear(PT(1,1), PT(3,5), PT(2,0), PT(4,5)
         ) << " "
      << LinesCollinear(PT(1,1), PT(3,5), PT(5,9), PT
          (7,13)) << endl;
 // expected: 1 1 1 0
 << SegmentsIntersect(PT(0,0), PT(2,4), PT(4,3), PT (0,5)) << " "
      << SegmentsIntersect(PT(0,0), PT(2,4), PT(5,5), PT
          (1,7)) << endl;
 // expected: (1,2)
 cerr << ComputeLineIntersection(PT(0,0), PT(2,4), PT(3,1)</pre>
      , PT(-1,3)) << endl;
 cerr << ComputeCircleCenter(PT(-3,4), PT(6,1), PT(4,5))</pre>
      << end1:
 vector<PT> v;
 v.push_back(PT(0,0));
 v.push_back(PT(5,0));
 v.push_back(PT(5,5));
 v.push_back(PT(0,5));
 // expected: 1 1 1 0 0
 cerr << PointInPolygon(v, PT(2,2)) << " "</pre>
      << PointInPolygon(v, PT(2,0)) << " "
      << PointInPolygon(v, PT(0,2)) << " "
      << PointInPolygon(v, PT(5,2)) << " "
      << PointInPolygon(v, PT(2,5)) << endl;
 // expected: 0 1 1 1 1
 cerr << PointOnPolygon(v, PT(2,2)) << " "</pre>
      << PointOnPolygon(v, PT(2,0)) << " "
      << PointOnPolygon(v, PT(0,2)) << " "
      << PointOnPolygon(v, PT(5,2)) << " "
      << PointOnPolygon(v, PT(2,5)) << endl;
```

for (int k = i+1; k < p.size(); k++) {</pre>

```
// expected: (1,6)
              (5,4) (4,5)
              blank line
              (4,5) (5,4)
              blank line
             (4,5) (5,4)
vector<PT> u = CircleLineIntersection(PT(0,6), PT(2,6),
     PT(1,1), 5);
for (int i = 0; i < u.size(); i++) cerr << u[i] << " ";</pre>
     cerr << endl:
  = CircleLineIntersection(PT(0,9), PT(9,0), PT(1,1), 5);
for (int i = 0; i < u.size(); i++) cerr << u[i] << " ";</pre>
     cerr << endl;
u = CircleCircleIntersection(PT(1,1), PT(10,10), 5, 5);
for (int i = 0; i < u.size(); i++) cerr << u[i] << " ";</pre>
     cerr << endl:
u = CircleCircleIntersection(PT(1,1), PT(8,8), 5, 5);
for (int i = 0; i < u.size(); i++) cerr << u[i] << "</pre>
     cerr << endl;
u = CircleCircleIntersection(PT(1,1), PT(4.5,4.5), 10,
     sqrt(2.0)/2.0);
for (int i = 0; i < u.size(); i++) cerr << u[i] << " ";</pre>
     cerr << endl;
u = CircleCircleIntersection(PT(1,1), PT(4.5,4.5), 5,
     sqrt(2.0)/2.0);
for (int i = 0; i < u.size(); i++) cerr << u[i] << " ";</pre>
     cerr << endl;
// area should be 5.0
// centroid should be (1.166666, 1.166666)
PT pa[] = { PT(0,0), PT(5,0), PT(1,1), PT(0,5) };
vector<PT> p(pa, pa+4);
PT c = ComputeCentroid(p);
cerr << "Area: " << ComputeArea(p) << endl;</pre>
cerr << "Centroid: " << c << endl;</pre>
```

3 Numerical algorithms

3.1 Fast Fourier transform

```
#include <cassert>
#include <cstdio>
#include <cmath>
struct cpx
 cpx(){}
 cpx (double aa):a(aa),b(0){}
  cpx(double aa, double bb):a(aa),b(bb){}
 double a;
 double b;
 double modsq(void) const
    return a * a + b * b;
  cpx bar (void) const
   return cpx(a, -b);
cpx operator + (cpx a, cpx b)
 return cpx(a.a + b.a. a.b + b.b);
cpx operator *(cpx a, cpx b)
 return cpx(a.a * b.a - a.b * b.b, a.a * b.b + a.b * b.a);
cpx operator / (cpx a, cpx b)
  cpx r = a * b.bar();
 return cpx(r.a / b.modsq(), r.b / b.modsq());
cpx EXP (double theta)
 return cpx(cos(theta), sin(theta));
```

```
const double two pi = 4 * acos(0);
// in:
           input array
// out:
           output array
// step:
           {SET TO 1} (used internally)
           length of the input/output {MUST BE A POWER OF
// size:
// dir:
           either plus or minus one (direction of the FFT)
// RESULT: out[k] = \sum_{j=0}^{size - 1} in[j] * exp(dir *
      2pi * i * j * k / size)
void FFT(cpx *in, cpx *out, int step, int size, int dir)
  if(size < 1) return;</pre>
  if(size == 1)
    out[0] = in[0];
    return:
  FFT(in, out, step * 2, size / 2, dir);
  FFT(in + step, out + size / 2, step \star 2, size / 2, dir);
  for (int i = 0; i < size / 2; i++)
    cpx even = out[i];
   cpx odd = out[i + size / 2];
   out[i] = even + EXP(dir * two pi * i / size) * odd;
    out[i + size / 2] = even + EXP(dir * two_pi * (i + size
          / 2) / size) * odd;
// f[0...N-1] and g[0..N-1] are numbers
// Want to compute the convolution h, defined by
// h[n] = sum of f[k]g[n-k] (k = 0, ..., N-1).
// Here, the index is cyclic; f[-1] = f[N-1], f[-2] = f[N
     -2], etc.
// Let F[0...N-1] be FFT(f), and similarly, define G and H.
// The convolution theorem says H[n] = F[n]G[n] (element-
// To compute h[] in O(N log N) time, do the following:
    1. Compute F and G (pass dir = 1 as the argument).
    2. Get H by element-wise multiplying F and G.
     3. Get h by taking the inverse FFT (use dir = -1 as
     the argument)
        and *dividing by N*. DO NOT FORGET THIS SCALING
     FACTOR.
int main (void)
  printf("If rows come in identical pairs, then everything
       works.\n");
  cpx \ a[8] = \{0, 1, cpx(1,3), cpx(0,5), 1, 0, 2, 0\};
  cpx b[8] = \{1, cpx(0,-2), cpx(0,1), 3, -1, -3, 1, -2\};
  cpx A[8];
 cpx B[8];
FFT(a, A, 1, 8, 1);
FFT(b, B, 1, 8, 1);
  for (int i = 0; i < 8; i++)
    printf("%7.21f%7.21f", A[i].a, A[i].b);
  printf("\n");
  for (int i = 0; i < 8; i++)
    cox Ai(0,0);
    for (int j = 0; j < 8; j++)
     Ai = Ai + a[j] * EXP(j * i * two_pi / 8);
    printf("%7.21f%7.21f", Ai.a, Ai.b);
  printf("\n");
  cpx AB[8];
  for (int i = 0; i < 8; i++)
   AB[i] = A[i] * B[i];
  cpx aconvb[8];
  FFT (AB, aconvb, 1, 8, -1);
  for (int i = 0; i < 8; i++)
    aconvb[i] = aconvb[i] / 8;
  for (int i = 0; i < 8; i++)
    printf("%7.21f%7.21f", aconvb[i].a, aconvb[i].b);
  printf("\n");
  for (int i = 0; i < 8; i++)
```

```
{
  cpx aconvbi(0,0);
  for(int j = 0; j < 8; j++)
  {
    aconvbi = aconvbi + a[j] * b[(8 + i - j) % 8];
    printf("%7.2lf%7.2lf", aconvbi.a, aconvbi.b);
  }
  printf("\n");
  return 0;
}</pre>
```

4 Graph algorithms

4.1 Fast Dijkstra's algorithm

```
// Implementation of Dijkstra's algorithm using adjacency
     lists
// and priority queue for efficiency.
// Running time: O(|E| log |V|)
#include <queue>
#include <cstdio>
using namespace std;
const int INF = 2000000000;
typedef pair<int, int> PII;
int main() {
        int N, s, t;
scanf("%d%d%d", &N, &s, &t);
        vector<vector<PII> > edges(N);
        for (int i = 0; i < N; i++) {
                int M;
scanf("%d", &M);
                 for (int j = 0; j < M; j++) {
                         int vertex, dist;
                         scanf("%d%d", &vertex, &dist);
                         edges[i].push_back(make_pair(dist,
                              vertex)); // note order of
                              arguments here
        // use priority queue in which top element has the
              "smallest" priority
        priority_queue<PII, vector<PII>, greater<PII> > Q;
        vector<int> dist(N, INF), dad(N, -1);
        Q.push(make_pair(0, s));
        dist[s] = 0;
        while (!Q.empty()) {
    PII p = Q.top();
                Q.pop();
                int here = p.second;
                 if (here == t) break;
                 if (dist[here] != p.first) continue;
                 for (vector<PII>::iterator it = edges[here
                      ].begin(); it != edges[here].end(); it
                         if (dist[here] + it->first < dist[</pre>
                              it->second1) {
                                 dist[it->second] = dist[
                                       here] + it->first;
                                  dad[it->second] = here;
                                  O.push (make pair (dist[it->
                                       second], it->second));
        printf("%d\n", dist[t]);
        if (dist[t] < INF)</pre>
                 for (int i = t; i != -1; i = dad[i])
                         printf("%d%c", i, (i == s ? '\n' :
    ' '));
        return 0;
```

```
/*
Sample input:
5 0 4
2 1 2 3 1
2 2 4 4 5
3 1 4 3 3 4 1
2 0 1 2 3
2 1 5 2 1

Expected:
5
4 2 3 0
*/
```

4.2 Strongly connected components

```
#include < memory.h>
struct edge{int e, nxt;};
int V, E;
edge e[MAXE], er[MAXE];
int sp[MAXV], spr[MAXV];
int group_cnt, group_num[MAXV];
bool v[MAXV];
int stk[MAXV];
void fill_forward(int x)
  for(i=sp[x];i;i=e[i].nxt) if(!v[e[i].e]) fill_forward(e[i
  stk[++stk[0]]=x;
void fill_backward(int x)
  group_num[x]=group_cnt;
  for(i=spr[x];i;i=er[i].nxt) if(v[er[i].e]) fill_backward(
void add_edge(int v1, int v2) //add edge v1->v2
  e [++E].e=v2; e [E].nxt=sp [v1]; sp [v1]=E;
  er[ E].e=v1; er[E].nxt=spr[v2]; spr[v2]=E;
void SCC()
  stk[0]=0;
  memset(v, false, sizeof(v));
  for (i=1; i <= V; i++) if (!v[i]) fill_forward(i);</pre>
  group_cnt=0;
  for (i=stk[0]; i>=1; i--) if (v[stk[i]]) {group_cnt++;
       fill_backward(stk[i]);}
```

4.3 Bellman Ford's algorithm

```
// This function runs the Bellman-Ford algorithm for single
// shortest paths with negative edge weights. The function
     returns
// false if a negative weight cycle is detected. Otherwise
// function returns true and dist[i] is the length of the
     shortest
  path from start to i.
// Running time: O(|V|^3)
            start, w[i][j] = cost of edge from i to j
    OUTPUT: dist[i] = min weight path from start to i
             prev[i] = previous node on the best path from
     the
                        start node
#include <iostream>
#include <queue>
#include <cmath>
#include <vector>
```

```
using namespace std;
typedef double T:
typedef vector<T> VT;
typedef vector<VT> VVT;
typedef vector<int> VI;
typedef vector<VI> VVI;
bool BellmanFord (const VVT &w, VT &dist, VI &prev, int
  int n = w \operatorname{size}():
 prev = VI(n, -1);
  dist = VT(n, 1000000000);
 dist[start] = 0;
  for (int k = 0; k < n; k++) {
    for (int i = 0; i < n; i++) {
      for (int j = 0; j < n; j++) {
        if (dist[j] > dist[i] + w[i][j]){
          if (k == n-1) return false;
          dist[j] = dist[i] + w[i][j];
          prev[j] = i;
  return true;
```

5 Miscellaneous

5.1 C++ template

```
#include <bits/stdc++.h>
using namespace std;
const long long Mod = 1e9 + 7;
const long long Inf = 1e18;
const long long Lim = 1e5 + 1e3;
const double eps = 1e-10;
typedef long long 11;
typedef vector <int> vi;
typedef vector <ll> vl;
typedef pair <int, int> pii;
typedef pair <ll, ll> pll;
typedef vector <pll> vll;
#define F first
#define S second
#define uint unsigned int
#define mp make_pair
#define pb push_back
#define pi 2*acos(0.0)
#define rep2(i,b,a) for(ll i = (ll)b, _a = (ll)a; i >= _a;
    i--)
#define rep1(i,a,b) for(ll i = (ll)a, _b = (ll)b; i <= _b;
     i++)
#define rep(i,n) for(ll i = 0, _n = (ll)n; i < _n; i++)
#define mem(a, val) memset(a, val, sizeof(a))
#define fast ios_base::sync_with_stdio(false),cin.tie(0),
     cout.tie(0);
```

5.2 C++ input/output

```
cout.setf(ios::fixed); cout << setprecision(5);
cout << 100.0/7.0 << endl;
cout.unsetf(ios::fixed);

// Output the decimal point and trailing zeros
cout.setf(ios::showpoint);
cout.v100.0 << endl;
cout.unsetf(ios::showpoint);

// Output a '+' before positive values
cout.setf(ios::showpos);
cout << 100 << " " << -100 << endl;
cout.unsetf(ios::showpos);
// Output numerical values in hexadecimal
cout << hex << 100 << " " << 1000 << " " << 1000 << ded </pre>
```

5.3 Longest increasing subsequence

```
// Given a list of numbers of length n, this routine
// longest increasing subsequence.
// Running time: O(n log n)
     INPUT: a vector of integers
    OUTPUT: a vector containing the longest increasing
     subsequence
#include <iostream>
#include <vector>
#include <algorithm>
using namespace std;
typedef vector<int> VI;
typedef pair<int, int> PII;
typedef vector<PII> VPII;
#define STRICTLY_INCREASNG
VI LongestIncreasingSubsequence(VI v) {
 VI dad(v.size(), -1);
 for (int i = 0; i < v.size(); i++) {</pre>
#ifdef STRICTLY_INCREASNG
    PII item = make_pair(v[i], 0);
    VPII::iterator it = lower_bound(best.begin(), best.end
         (), item);
    item.second = i;
#else
    PII item = make_pair(v[i], i);
    VPII::iterator it = upper_bound(best.begin(), best.end
         (), item);
#endif
    if (it == best.end()) {
     dad[i] = (best.size() == 0 ? -1 : best.back().second)
      best.push_back(item);
     else {
     dad[i] = dad[it->second];
      *it = item:
 VI ret:
  for (int i = best.back().second; i >= 0; i = dad[i])
   ret.push_back(v[i]);
  reverse(ret.begin(), ret.end());
 return ret;
```

5.4 Knuth-Morris-Pratt

```
/*
Searches for the string w in the string s (of length k).
Returns the
```

```
0-based index of the first match (k if no match is found).
     Algorithm
runs in O(k) time.
#include <iostream>
#include <string>
#include <vector>
using namespace std;
typedef vector<int> VI;
void buildTable(string& w, VI& t)
  t = VI(w.length());
 int i = 2, j = 0;
t[0] = -1; t[1] = 0;
  while(i < w.length())</pre>
    if(w[i-1] == w[j]) { t[i] = j+1; i++; j++; }
    else if(j > 0) j = t[j];
    else { t[i] = 0; i++; }
int KMP (string& s, string& w)
  int m = 0, i = 0;
  VI t;
  buildTable(w, t);
  while(m+i < s.length())</pre>
    if(w[i] == s[m+i])
      if(i == w.length()) return m;
    else
     m += i-t[i];
      if(i > 0) i = t[i];
  return s.length();
int main()
  string a = (string) "The example above illustrates the
       general technique for assembling "+
    "the table with a minimum of fuss. The principle is
         that of the overall search: "+
    "most of the work was already done in getting to the
         current position, so very "+
    "little needs to be done in leaving it. The only minor
         complication is that the "+
    "logic which is correct late in the string erroneously
         gives non-proper "+
    "substrings at the beginning. This necessitates some
         initialization code.";
  string b = "table";
 int p = KMP(a, b);
cout << p << ": " << a.substr(p, b.length()) << " " << b</pre>
       << endl;
```

5.5 Topological sort (C++)

```
which represents an ordering of the nodes
     which
              is consistent with w
// If no ordering is possible, false is returned.
#include <iostream>
#include <queue>
#include <cmath>
#include <vector>
using namespace std;
typedef double T;
typedef vector<T> VT;
typedef vector<VT> VVT;
typedef vector<int> VI;
typedef vector<VI> VVI;
bool TopologicalSort (const VVI &w, VI &order) {
 int n = w.size();
  VI parents (n);
 queue<int> q;
order.clear();
  for (int i = 0; i < n; i++) {</pre>
    for (int j = 0; j < n; j++)
     if (w[i][i]) parents[i]++;
      if (parents[i] == 0) q.push (i);
  while (q.size() > 0) {
   int i = q.front();
    q.pop();
    order.push_back (i);
    for (int j = 0; j < n; j++) if (w[i][j]) {</pre>
     parents[j]--;
      if (parents[j] == 0) q.push (j);
 return (order.size() == n);
```

5.6 Fast exponentiation

```
Uses powers of two to exponentiate numbers and matrices.
     Calculates
n^k in O(\log(k)) time when n is a number. If A is an n x n
    matrix.
calculates A^k in O(n^3*log(k)) time.
#include <iostream>
#include <vector>
using namespace std;
typedef double T;
typedef vector<T> VT;
typedef vector<VT> VVT;
T power(T x, int k) {
  T ret = 1;
  while(k) {
    if(k & 1) ret *= x;
    k >>= 1; x *= x;
  return ret;
VVT multiply(VVT& A, VVT& B) {
 int n = A.size(), m = A[0].size(), k = B[0].size();
  VVT C(n, VT(k, 0));
  for (int i = 0; i < n; i++)
    for (int j = 0; j < k; j++)
      for (int 1 = 0; 1 < m; 1++)
       C[i][j] += A[i][1] * B[1][j];
 return C:
```

```
VVT power(VVT& A, int k) {
  int n = A.size();
  VVT ret(n, VT(n)), B = A;
  for(int i = 0; i < n; i++) ret[i][i]=1;</pre>
  while(k) {
    if(k & 1) ret = multiply(ret, B);
    k >>= 1; B = multiply(B, B);
  return ret;
int main()
  /* Expected Output:
     2.37^48 = 9.72569e+17
     550 376 529 285 484
     484 265 376 264 285
     285 220 265 156 264
     529 285 484 265 376 */
  double n = 2.37;
  int k = 48;
  cout << n << "^" << k << " = " << power(n, k) << endl;
  double At [5] [5] =
     0, 0, 1, 0, 0 },
1, 0, 0, 1, 0 },
0, 0, 0, 0, 1 },
1, 0, 0, 0, 0 },
    { 0, 1, 0, 0, 0 } };
  vector <vector <double> > A(5, vector <double>(5));
  for(int i = 0; i < 5; i++)
    for (int j = 0; j < 5; j++)
      A[i][j] = At[i][j];
  vector <vector <double> > Ap = power(A, k);
  cout << endl:
  for(int i = 0; i < 5; i++) {
    for (int j = 0; j < 5; j++)
      cout << Ap[i][j] << " ";
    cout << endl;
```

5.7 Longest common subsequence

```
Calculates the length of the longest common subsequence of
    two vectors.
Backtracks to find a single subsequence or all subsequences
     . Runs in
O(m*n) time except for finding all longest common
     subsequences, which
may be slow depending on how many there are.
#include <iostream>
#include <vector>
#include <set>
#include <algorithm>
using namespace std;
typedef int T;
typedef vector<T> VT;
typedef vector<VT> VVT;
typedef vector<int> VI:
typedef vector<VI> VVI;
void backtrack (VVI& dp, VT& res, VT& A, VT& B, int i, int j
 if(!i || !j) return;
 if(A[i-1] == B[j-1]) \{ res.push_back(A[i-1]); backtrack(
       dp, res, A, B, i-1, j-1); }
   if(dp[i][j-1] \ge dp[i-1][j]) backtrack(dp, res, A, B, i
         , j-1);
```

```
else backtrack(dp, res, A, B, i-1, j);
void backtrackall(VVI& dp, set<VT>& res, VT& A, VT& B, int
 if(!i || !j) { res.insert(VI()); return; }
  if(A[i-1] == B[j-1])
    set<VT> tempres;
    backtrackall(dp, tempres, A, B, i-1, j-1);
    for(set<VT>::iterator it=tempres.begin(); it!=tempres.
         end(); it++)
     VT temp = *it;
      temp.push_back(A[i-1]);
      res.insert(temp);
  else
    if(dp[i][j-1] >= dp[i-1][j]) backtrackall(dp, res, A, B
         , i, j-1);
    if(dp[i][j-1] <= dp[i-1][j]) backtrackall(dp, res, A, B</pre>
        , i-1, j);
VT LCS(VT& A, VT& B)
  VVI dp;
  int n = A.size(), m = B.size();
  dp.resize(n+1);
  for(int i=0; i<=n; i++) dp[i].resize(m+1, 0);</pre>
  for (int i=1; i<=n; i++)</pre>
    for(int j=1; j<=m; j++)</pre>
      if(A[i-1] == B[j-1]) dp[i][j] = dp[i-1][j-1]+1;
      else dp[i][j] = max(dp[i-1][j], dp[i][j-1]);
  backtrack(dp, res, A, B, n, m);
  reverse(res.begin(), res.end());
  return res;
set < VT > LCSall (VT& A, VT& B)
  VVI dp;
  int n = A.size(), m = B.size();
  dp.resize(n+1);
  for(int i=0; i<=n; i++) dp[i].resize(m+1, 0);</pre>
  for (int i=1; i<=n; i++)</pre>
    for(int j=1; j<=m; j++)</pre>
      if(A[i-1] == B[j-1]) dp[i][j] = dp[i-1][j-1]+1;
      else dp[i][j] = max(dp[i-1][j], dp[i][j-1]);
  set<VT> res;
  backtrackall(dp, res, A, B, n, m);
  return res;
int main()
  int a[] = { 0, 5, 5, 2, 1, 4, 2, 3 }, b[] = { 5, 2, 4, 3,
  2, 1, 2, 1, 3 };
VI A = VI(a, a+8), B = VI(b, b+9);
  VI C = LCS(A, B);
  for(int i=0; i<C.size(); i++) cout << C[i] << " ";</pre>
  cout << endl << endl;
  set <VI> D = LCSall(A, B);
  for(set<VI>::iterator it = D.begin(); it != D.end(); it
    for(int i=0; i<(*it).size(); i++) cout << (*it)[i] << "</pre>
    cout << endl;
```

5.8 Miller-Rabin Primality Test (C)

```
// Randomized Primality Test (Miller-Rabin):
   Error rate: 2^(-TRIAL)
   Almost constant time. srand is needed
#include <stdlib.h>
#define EPS 1e-7
typedef long long LL;
LL ModularMultiplication(LL a, LL b, LL m)
        LL ret=0, c=a;
        while(b)
                if(b&1) ret=(ret+c)%m;
                b>>=1; c=(c+c)%m;
        return ret:
LL ModularExponentiation(LL a, LL n, LL m)
        LL ret=1, c=a;
        while(n)
                if(n&1) ret=ModularMultiplication(ret, c, m
                n>>=1; c=ModularMultiplication(c, c, m);
        return ret;
bool Witness(LL a, LL n)
        LL u=n-1;
  int t=0;
        while (!(u&1))\{u>>=1; t++;\}
        LL x0=ModularExponentiation(a, u, n), x1;
        for (int i=1; i<=t; i++)</pre>
                x1=ModularMultiplication(x0, x0, n);
                if (x1==1 \&\& x0!=1 \&\& x0!=n-1) return true;
                x0=x1:
        if(x0!=1) return true;
        return false;
LL Random(LL n)
  LL ret=rand(); ret*=32768;
        ret+=rand(); ret*=32768;
        ret+=rand(); ret*=32768;
        ret += rand();
 return ret%n;
bool IsPrimeFast(LL n, int TRIAL)
  while (TRIAL--)
    LL a=Random(n-2)+1;
    if(Witness(a, n)) return false;
  return true;
```

6 Data structures

6.1 Suffix array

```
// Suffix array construction in O(L log^2 L) time. Routine
    for
// computing the length of the longest common prefix of any
    two
// suffixes in O(log L) time.
//
// INPUT: string s
//
// OUTPUT: array suffix[] such that suffix[i] = index (
    from 0 to L-1)
//    of substring s[i...L-1] in the list of sorted
    suffixes.
```

```
That is, if we take the inverse of the
     permutation suffix[],
            we get the actual suffix array.
#include <vector>
#include <iostream>
#include <string>
using namespace std;
struct SuffixArray {
 const int L:
  string s;
  vector<vector<int> > P;
  vector<pair<int,int>,int> > M;
  SuffixArray(const string &s) : L(s.length()), s(s), P(1,
       vector<int>(L, 0)), M(L) {
    for (int i = 0; i < L; i++) P[0][i] = int(s[i]);</pre>
    for (int skip = 1, level = 1; skip < L; skip *= 2,</pre>
         level++) {
      P.push_back(vector<int>(L, 0));
      for (int i = 0; i < L; i++)</pre>
        M[i] = make_pair(make_pair(P[level-1][i], i + skip
             < L ? P[level-1][i + skip] : -1000), i);
      sort(M.begin(), M.end());
      for (int i = 0; i < L; i++)
        P[level][M[i].second] = (i > 0 && M[i].first == M[i]
             -1].first) ? P[level][M[i-1].second] : i;
  vector<int> GetSuffixArray() { return P.back(); }
  // returns the length of the longest common prefix of s[i
       \dots L-1] and s[j\dots L-1]
  int LongestCommonPrefix(int i, int j) {
    int len = 0;
    if (i == j) return L - i;
    for (int k = P.size() - 1; k >= 0 && i < L && j < L; k
      if (P[k][i] == P[k][j]) {
       i += 1 << k;
        j += 1 << k;
        len += 1 << k;
    return len;
};
// BEGIN CUT
// The following code solves UVA problem 11512: GATTACA.
#define TESTING
#ifdef TESTING
int main() {
 int T;
  for (int caseno = 0; caseno < T; caseno++) {</pre>
    string s;
    cin >> s;
    SuffixArray array(s);
    vector<int> v = array.GetSuffixArray();
    int bestlen = -1, bestpos = -1, bestcount = 0;
    for (int i = 0; i < s.length(); i++) {</pre>
      int len = 0, count = 0;
      for (int j = i+1; j < s.length(); j++) {</pre>
        int l = array.LongestCommonPrefix(i, j);
        if (1 >= len) {
          if (1 > len) count = 2; else count++;
      if (len > bestlen || len == bestlen && s.substr(
           bestpos, bestlen) > s.substr(i, len)) {
        bestlen = len;
        bestcount = count;
        bestpos = i;
    if (bestlen == 0) {
      cout << "No repetitions found!" << endl;</pre>
      cout << s.substr(bestpos, bestlen) << " " <<</pre>
           bestcount << endl;
```

```
#else
// END CUT
int main() {
  // bobocel is the 0'th suffix
 // obocel is the 5'th suffix
      bocel is the 1'st suffix
       ocel is the 6'th suffix
        cel is the 2'nd suffix
         el is the 3'rd suffix
          l is the 4'th suffix
 SuffixArray suffix("bobocel");
 vector<int> v = suffix.GetSuffixArray();
  // Expected output: 0 5 1 6 2 3 4
 for (int i = 0; i < v.size(); i++) cout << v[i] << " ";</pre>
 cout << endl;
 cout << suffix.LongestCommonPrefix(0, 2) << endl;</pre>
// BEGIN CUT
#endif
```

6.2 Binary Indexed Tree

```
#include <iostream>
using namespace std;
#define LOGSZ 17
int tree[(1<<LOGSZ)+1];</pre>
int N = (1 << LOGSZ);
// add v to value at x
void set(int x, int v) {
  while (x \le N) {
   tree[x] += v;
    x += (x \& -x);
// get cumulative sum up to and including x
int get(int x) {
 int res = 0;
  while(x) {
    res += tree[x];
    x = (x \& -x);
  return res;
// get largest value with cumulative sum less than or equal
// for smallest, pass x-1 and add 1 to result
int getind(int x) {
  int idx = 0, mask = N;
  while (mask && idx < N)
    int t = idx + mask;
    if(x >= tree[t]) {
      idx = t;
      x -= tree[t];
    mask >>= 1:
  return idx:
```

6.3 Union-find set(aka DSU)

```
#include <iostream>
#include <vector>
using namespace std;
int find(vector<int> &C, int x) { return (C[x] == x) ? x :
        C[x] = find(C, C[x]); }
void merge(vector<int> &C, int x, int y) { C[find(C, x)] =
        find(C, y); }
```

```
int main()
{
    int n = 5;
    vector<int> C(n);
    for (int i = 0; i < n; i++) C[i] = i;
    merge(C, 0, 2);
    merge(C, 1, 0);
    merge(C, 1, 0);
    merge(C, 3, 4);
    for (int i = 0; i < n; i++) cout << i << " " << find(C, i) << endl;
    return 0;
}</pre>
```

6.4 Lowest common ancestor

```
const int max_nodes, log_max_nodes;
int num_nodes, log_num_nodes, root;
vector<int> children[max_nodes];
                                        // children[i]
     contains the children of node i
int A[max_nodes][log_max_nodes+1];
                                        // A[i][j] is the
     2^j-th ancestor of node i, or -1 if that ancestor does
      not exist
int L[max_nodes];
                                        // L[i] is the
     distance between node i and the root
// floor of the binary logarithm of n
int lb (unsigned int n)
    if(n==0)
       return -1;
    int p = 0;
   if (n >= 1<<16) { n >>= 16; p += 16; }
```

```
if (n >= 1<< 8) { n >>= 8; p += 8; }
   if (n >= 1<< 4) { n >>= 4; p += 4; }
    if (n >= 1<< 2) { n >>= 2; p += 2; }
   if (n >= 1<< 1) {
                              p += 1; }
   return p;
void DFS(int i, int 1)
    L[i] = 1;
   for(int j = 0; j < children[i].size(); j++)</pre>
       DFS(children[i][j], 1+1);
int LCA(int p, int q)
    // ensure node p is at least as deep as node q
   if(L[p] < L[q])
       swap(p, q);
    // "binary search" for the ancestor of node p situated
         on the same level as q
    for(int i = log_num_nodes; i >= 0; i--)
       if(L[p] - (1<<i) >= L[q])
           p = A[p][i];
    if(p == g)
       return p;
    // "binary search" for the LCA
    for(int i = log_num_nodes; i >= 0; i--)
       if(A[p][i] != -1 && A[p][i] != A[q][i])
           p = A[p][i];
           q = A[q][i];
```

```
return A[p][0];
int main(int argc,char* argv[])
    // read num_nodes, the total number of nodes
    log_num_nodes=1b(num_nodes);
    for(int i = 0; i < num_nodes; i++)</pre>
        // read p, the parent of node i or -1 if node i is
             the root
        A[i][0] = p;
        if (p ! = -1)
        children[p].push_back(i);
else
            root = i;
    // precompute A using dynamic programming
    for(int j = 1; j <= log_num_nodes; j++)</pre>
        for(int i = 0; i < num_nodes; i++)</pre>
            if(A[i][j-1] != -1)
                A[i][j] = A[A[i][j-1]][j-1];
            else
                A[i][j] = -1;
   // precompute L
DFS(root, 0);
    return 0;
```