

Problem Name: Rotating Tree

Topic: Trees

Tags: Trees, Array

Language used: C++

Difficulty: Hard

Problem Statement:

You are given a binary tree with N nodes and $N-1$ edges rooted at node 1, but this tree has a unique property of cyclically rotating its nodes at every level after each second. For example if nodes at level 3 are [4, 5, 6, 7] then after 1 second they will be [7, 4, 5, 6]. You need to find the sum of middle elements of all the levels of the tree after K seconds. If there are X nodes at some level then the middle node would be $((X/2)+1)^{\text{th}}$ node. Initially the nodes at each level are in ascending order of node value.

Note: Here floor division is used for finding the middle element.

Input Format:

The first line of input contains N denoting the number of nodes.

Next $N-1$ lines contain two integers u, v denoting an edge between nodes u and v .

Next line contains an integer K , denoting the seconds.

Output Format:

Output the sum of middle elements of all the levels of the tree after K seconds.

Constraints:

$1 \leq N \leq 1000$

$1 \leq u, v \leq N$

$1 \leq K \leq 10^7$

Sample Input 1:

7

1 2

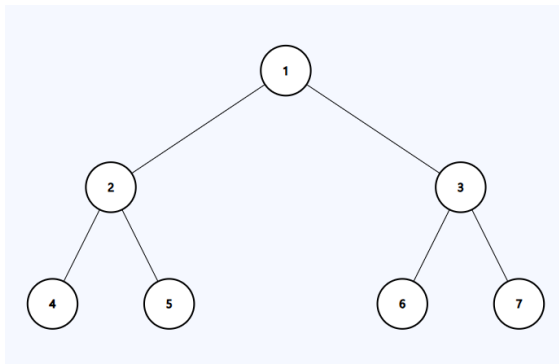
1 3
2 4
2 5
3 6
3 7
2

Sample Output 1:

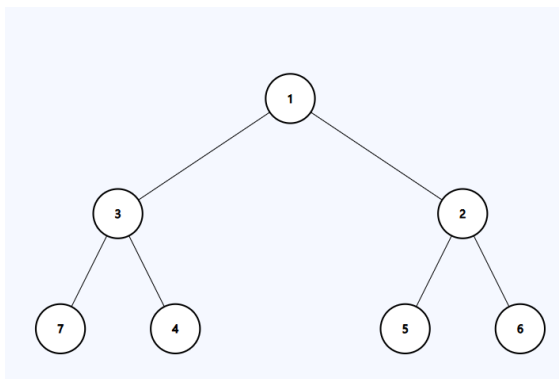
8

Explanation of Sample Input 1:

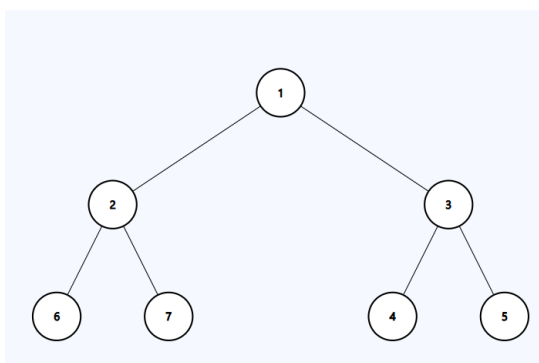
Initially the tree would look like this,



After 1 second, tree would be like,



After 2 seconds, tree would be like,



Now the middle element at level 0 is 1.

Middle element at level 1 is 3, as there are 2 nodes at level 1 and the middle node would be $((2/2)+1)^{\text{th}}$ node, which would be the second node of level 1.

Middle element at level 2 is 4, as there are 4 nodes at level 2 and the middle node would be $((4/2)+1)^{\text{th}}$ node, which would be the third node of level 2.

Thus, $\text{sum} = 1 + 3 + 4 = 8$.

Sample Input 2:

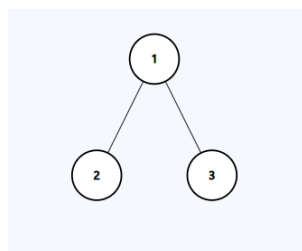
3
1 3
1 2
1

Sample Output 2:

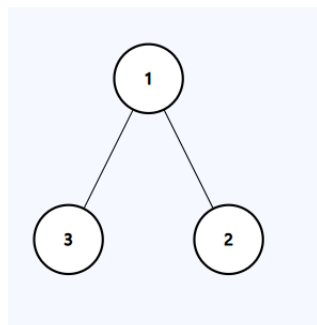
3

Explanation of Sample Input 1:

Initially the tree would look like this,



After 1 second, it would be like,



Now the sum of middle elements is $1 + 2 = 3$.

Code:

```
#include <bits/stdc++.h>

using namespace std;
long int calculate(vector<long int>& temp, long int K){
    sort(temp.begin(),temp.end());
    int middle= temp.size()/2 + 1;
    int size = temp.size();
    K%=size;
    int index;
    if (K >= middle)
        index = (size - K) + (middle - 1);
    else
        index = (middle - K - 1);
    return temp[index];
}
int main()
{
    long int n,u,v,ans=0,i,K;
    cin>>n;
    vector<long int>adj[n+1];
    for(i=0;i<n-1;i++){
        cin>>u>>v;
        adj[u].push_back(v);
    }
    cin>>K;
    queue<vector<long int>>>q;
    q.push({1, 0});
    int cur=0;
    vector<long int>temp;
    while(!q.empty()){
        long int node = q.front()[0];
        long int level = q.front()[1];
        q.pop();
        if(level==cur)temp.push_back(node);
        else{
            ans+= calculate(temp, K);
            temp.clear();
            cur=level;
            temp.push_back(node);
        }
        for(auto it:adj[node]){
            q.push({it, level+1});
        }
    }
    ans+= calculate(temp, K);
    cout<<ans<<endl;

    return 0;
}
```

C++

Python

Java