

ME543
Assignment 1

Abhijeet
234103001

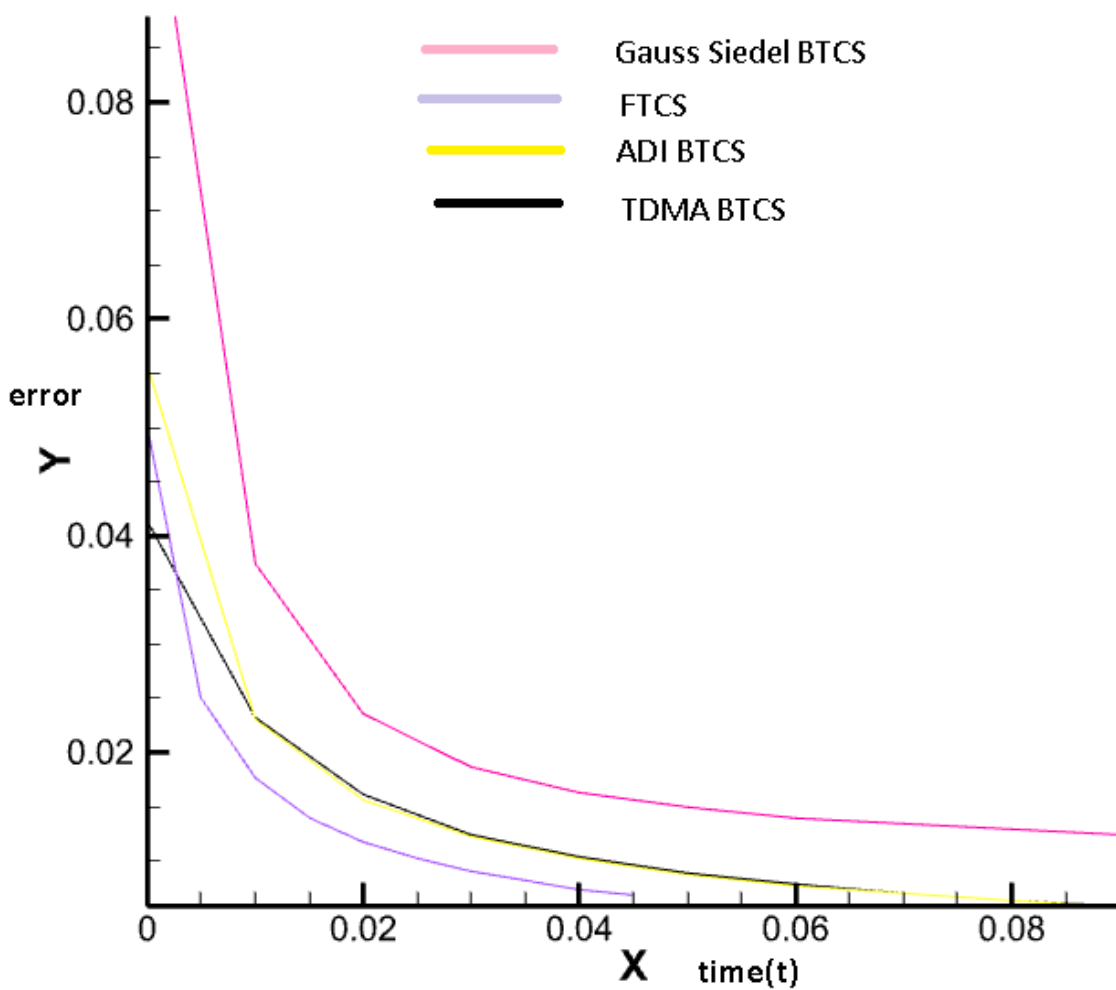
Couette Flow

$$\frac{\partial u}{\partial t} = \frac{1}{Re_H} \frac{\partial^2 u}{\partial y^2}$$

$$Re_H = \frac{UH}{\nu}$$

$$\epsilon = \sqrt{\frac{\sum_{j=1}^M (u^{n+1} - u^n)^2}{M}}$$

$$\epsilon = 10^{-6}$$



1. Explicit Method :- FTCS

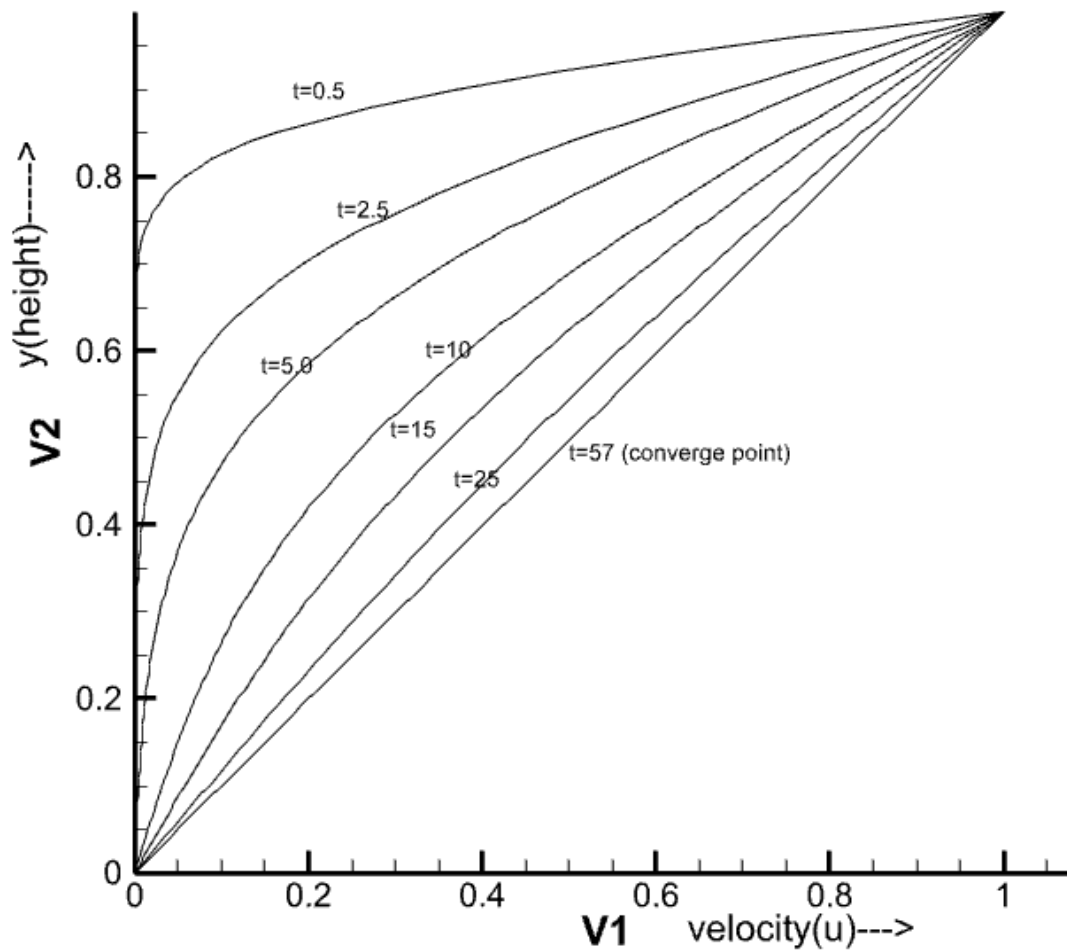
$$u_i^{n+1} = u_i^n + \gamma(u_{i+1}^n - 2u_i^n + u_{i-1}^n)$$

$$\gamma = \frac{\Delta t}{\Re_H \Delta x^2} = 0.50$$

$$\Re_H = 100$$

$$\Delta t = 5 \times 10^{-3}$$

$$\Delta x = 0.01, \mathbf{M=100}$$



2. Implicite Methods :-

A. BTCS : Gauss- Siedel iterative method

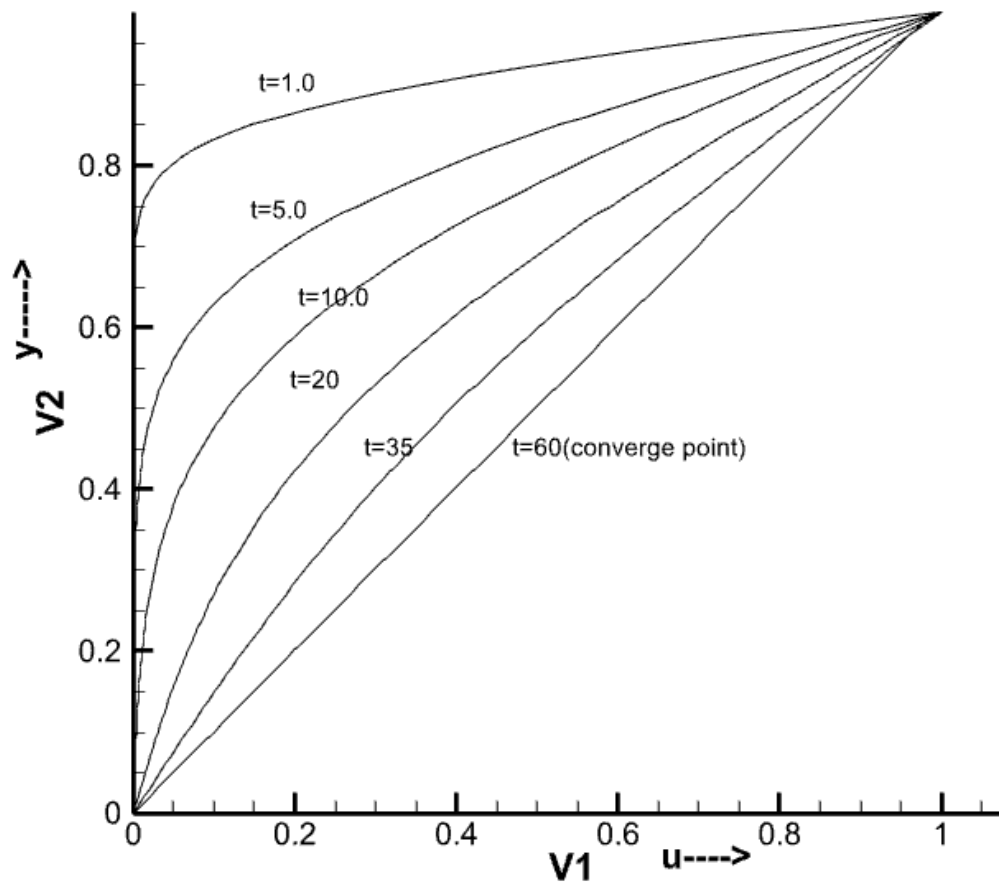
$$\gamma u_{i+1}^{n+1} - (1+2\gamma)u_i^{n+1} + \gamma u_{i-1}^{n+1} = -u_i^n$$

$$\gamma = \frac{\Delta t}{\Re_H \Delta x^2} = 1.0$$

$$\Re_H = 100$$

$$\Delta t = 10^{-2}$$

$$\Delta x = 0.01, \mathbf{M} = 100$$



B. BTCS : TriDiagonal Matrix Algorithm

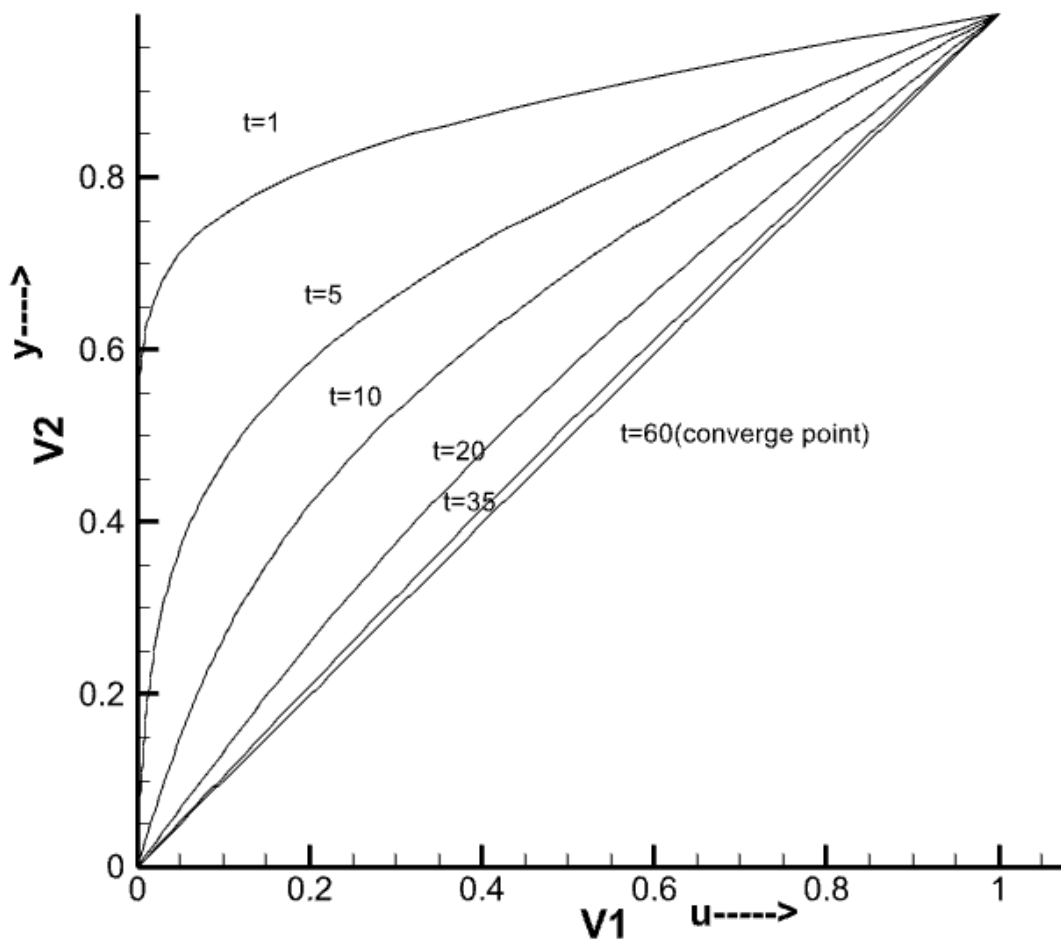
$$\gamma u_{i+1}^{n+1} - (1+2\gamma) u_i^{n+1} + \gamma u_{i-1}^{n+1} = -u_i^n$$

$$\gamma = \frac{\Delta t}{\Re_H \Delta x^2} = 1.0$$

$$\Re_H = \mathbf{100}$$

$$\Delta t = 10^{-2}$$

$$\Delta x = 0.01, \mathbf{M} = \mathbf{100}$$



C. Crank - Nicolson: TriDiagonal Matrix Algorithm

$$\frac{\gamma}{2}u_{i+1}^{n+1}-(1+\gamma)u_i^{n+1}+\frac{\gamma}{2}u_{i-1}^{n+1}=-\left(\frac{\gamma}{2}u_{i+1}^n-(1-\gamma)u_i^n+\frac{\gamma}{2}u_{i-1}^n\right)$$

$$\gamma=\frac{\Delta t}{\Re_H\Delta x^2}=1.0$$

$$\Re_H=\mathbf{100}$$

$$\Delta t=10^{-2}$$

$$\Delta x=0.01\text{ , }\mathbf{M=100}$$

