

→ Z-Test

- Used when

- Sample size large ($n \geq 30$) or
- Population variance (σ^2) known or we know standard deviation (σ)

$$\text{Margin Error (ME)} = Z_{\alpha/2} \frac{\sigma}{\sqrt{n}}$$

$$C_{\text{lower}} = PE - ME$$

$$C_{\text{upper}} = PE + ME$$

$$Z = \frac{\bar{X} - \mu}{\sigma / \sqrt{n}}$$

- To perform the Z-test

- Calculate ME, C_{lower} , C_{upper} , Z
- Use Z-table to get Z values
- Take decision from standard rules of test statistic
- Make conclusion

- If population standard deviation not known and still want Z-test we can use sample standard deviation (s).

Formulas: σ will be replaced by s.

- Comparing two different groups,

$$Z = \frac{(\bar{X}_1 - \bar{X}_2) - (\mu_1 - \mu_2)}{\sqrt{(\sigma_1^2/n_1) + (\sigma_2^2/n_2)}}$$

→ T-Test

- Used when

- sample size small ($n < 30$) and
- Sample variance (s^2) known or standard deviation (s) known

$$\text{Margin Error (ME)} = t_{\alpha/2} \frac{s}{\sqrt{n}}$$

$$C_{\text{lower}} = PE - ME$$

$$C_{\text{upper}} = PE + ME$$

$$t = \frac{\bar{X} - \mu}{s / \sqrt{n}}$$

- To perform the T-test

- Calculate ME, C_{lower} , C_{upper} , t
- Use T-table to get t values
- Take decision from standard rules of test statistic
- Make conclusion

- To perform T table we also need degree of freedom (df)

$$df = n - 1$$

- Comparing two different groups,

$$t = \frac{(\bar{X}_1 - \bar{X}_2) - (\mu_1 - \mu_2)}{s_p \sqrt{1/n_1 + 1/n_2}}$$

$$s_p^2 = \frac{(n_1 - 1)s_1^2 + (n_2 - 1)s_2^2}{n_1 + n_2 - 2}$$

$$df = n_1 + n_2 - 2$$

→ Chi-Square Test

- Used when data is chi-square distributed

- Used to check whether variables in population are independent or not

- This test checks the difference between observed (o) and expected (e) value which can be calculated using observed frequency (f_o) and expected frequency (f_e)

- Its non parametric test performed on categorical data.

$$\text{number of categories} = \text{Total categories (C)}$$

$$df = C - 1$$

$$\chi^2 = \sum_{i=1}^n \frac{(f_o - f_e)^2}{f_e}$$

- To perform chi-square tests

- calculate C , df , χ^2
- Get critical value (C_v) from χ^2 table using α and df

- If $\chi^2 > C_v$, reject H_0

- $\chi^2 < C_v$, fail to reject H_0