

generate a synthetic dataset

```
In [1]: import numpy as np
import pandas as pd

# Set the seed for reproducibility
np.random.seed(42)

# Generate data for two clusters
mean_1 = [2, 3]
cov_1 = [[1, 0.5], [0.5, 1]] # Covariance matrix for cluster 1

mean_2 = [8, 8]
cov_2 = [[1, -0.3], [-0.3, 1]] # Covariance matrix for cluster 2

# Generate points
data_1 = np.random.multivariate_normal(mean_1, cov_1, 150)
data_2 = np.random.multivariate_normal(mean_2, cov_2, 150)

# Combine the data into a single dataset
data = np.vstack((data_1, data_2))

# Save the dataset to a CSV file
df = pd.DataFrame(data, columns=['x', 'y'])
df.to_csv('synthetic_data.csv', index=False)

print("Dataset generated and saved as 'synthetic_data.csv'")
```

Dataset generated and saved as 'synthetic_data.csv'

Load the Dataset

```
In [3]: import pandas as pd

# Load the dataset
data = pd.read_csv('synthetic_data.csv')
print(data.head())
```

	x	y
0	1.638965	2.500701
1	0.677570	3.200600
2	2.319851	3.085714
3	0.248644	2.016079
4	2.135297	3.677857

Apply the EM Algorithm using a Gaussian Mixture Model

```
In [4]: #We'll use the GaussianMixture class from the sklearn.mixture module to apply EM
from sklearn.mixture import GaussianMixture
import matplotlib.pyplot as plt

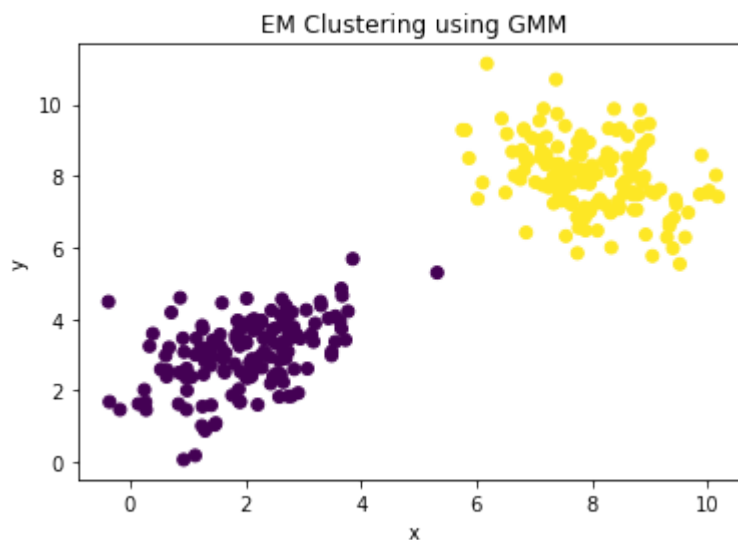
# Load the dataset
data = pd.read_csv('synthetic_data.csv')

# Convert the data to numpy array
X = data.values

# Apply Gaussian Mixture Model
gmm = GaussianMixture(n_components=2, covariance_type='full', random_state=42)
gmm.fit(X)

# Predict the cluster for each data point
labels = gmm.predict(X)

# Plot the results
plt.scatter(X[:, 0], X[:, 1], c=labels, cmap='viridis', marker='o')
plt.title('EM Clustering using GMM')
plt.xlabel('x')
plt.ylabel('y')
plt.show()
```



Analyzing the Gaussian Mixture Model

```
In [5]: print("Means of the clusters:\n", gmm.means_)  
        print("Covariances of the clusters:\n", gmm.covariances_)  
        print("Weights of each Gaussian:\n", gmm.weights_)
```

Means of the clusters:

```
[[2.01794373 3.04093116]  
 [7.95705197 7.97719282]]
```

Covariances of the clusters:

```
[[[ 0.9354123  0.4485924 ]  
 [ 0.4485924  0.95992804]]
```

```
[[ 0.89869926 -0.33498292]  
 [-0.33498292  0.9779328 ]]]
```

Weights of each Gaussian:

```
[0.49998898 0.50001102]
```

In []: