wooldridge-vignette

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Introduction

This vignette contains examples from every chapter of *Introductory Econometrics: A Modern Approach* by Jeffrey M. Wooldridge. Each example illustrates how to load data, build econometric models, and compute estimates with **R**.

Economics students new to both econometrics and **R** may find the introduction to both a bit challenging. In particular, the process of loading and preparing data prior to building one's first econometric model can present challenges. The wooldridge data package aims to lighten this task. It contains 105 data sets from Introductory Econometrics: A Modern Approach, and will load any set by typing its name into the data() function.

While the course companion site also provides publicly available data sets for Eviews, Excel, MiniTab, and Stata commercial software, \mathbf{R} is the open source option. Furthermore, using \mathbf{R} while building a foundation in econometrics, can become the first step in a student's journey toward using the most innovative new methods in statistical computing for handling larger, more modern data sets.

In addition, please visit the **Appendix** for sources on using R for econometrics. For example, an excellent reference is "Using R for Introductory Econometrics" by Florian Hess, written to compliment Introductory Econometrics: A Modern Approach. The full text can be viewed on the book website.

Now, install and load the wooldridge package and lets get started.

install.packages(wooldridge)

library(wooldridge)

Chapter 2: The Simple Regression Model

Example 2.10: A Log Wage Equation

$$\widehat{log(wage)} = \beta_0 + \beta_1 educ$$

Load the wage1 data.

Estimate a linear relationship between the \log of wage and education.

Print the results. I'm using the **stargazer** package to print the model results in a clean and easy to read format. See the bibliography for more information.

stargazer(log_wage_model, single.row = TRUE, header = FALSE)

Table 1:

	Dependent variable:
	lwage
educ	0.083*** (0.008)
Constant	$0.584^{***} (0.097)$
Observations	526
\mathbb{R}^2	0.186
Adjusted R^2	0.184
Residual Std. Error	0.480 (df = 524)
F Statistic	$119.582^{***} (df = 1; 524)$
Note:	*p<0.1; **p<0.05; ***p<0.01

Chapter 3: Multiple Regression Analysis: Estimation

Example 3.2: Hourly Wage Equation

$$\widehat{log(wage)} = \beta_0 + \beta_1 educ + \beta_3 exper + \beta_4 tenure$$

Estimate the model regressing education, experience, and tenure against log(wage).

```
hourly_wage_model <- lm(lwage ~ educ + exper + tenure, data = wage1)
```

Print the estimated model coefficients:

```
stargazer(hourly_wage_model, single.row = TRUE, header = FALSE)
```

Table 2:

	Dependent variable:
	lwage
educ	0.092*** (0.007)
exper	0.004** (0.002)
tenure	0.022*** (0.003)
Constant	0.284*** (0.104)
Observations	526
\mathbb{R}^2	0.316
Adjusted R^2	0.312
Residual Std. Error	0.441 (df = 522)
F Statistic	$80.391^{***} (df = 3; 522)$
Note:	*p<0.1; **p<0.05; ***p<

Chapter 4: Multiple Regression Analysis: Inference

Example 4.7 Effect of Job Training on Firm Scrap Rates

Load the jtrain data set and if you are using R Studio, View the data set.

```
data("jtrain")
```

View(jtrain)

Create a logical index, identifying which observations occur in 1987 and are non-union.

```
index <- jtrain$year == 1987 & jtrain$union == 0</pre>
```

Next, subset the jtrain data by the new index. This returns a data frame of jtrain data of non-union firms for the year 1987.

```
jtrain_1987_nonunion <- jtrain[index, ]</pre>
```

Now create the linear model regressing hrsemp(total hours training/total employees trained), the lsales(log of annual sales), and lemploy(the log of the number of the employees), against lscrap(the log of the scrape rate).

$$lscrap = \alpha + \beta_1 hrsemp + \beta_2 lsales + \beta_3 lemploy$$

```
linear_model <- lm(lscrap ~ hrsemp + lsales + lemploy, data = jtrain_1987_nonunion)</pre>
```

Finally, print the complete summary statistic diagnostics of the model.

stargazer(linear_model, single.row = TRUE, header = FALSE)

Table 3:

	Dependent variable:
	lscrap
hrsemp	-0.029 (0.023)
lsales	$-0.962^{**}(0.453)$
lemploy	$0.761^* \ (0.407)$
Constant	$12.458^{**} (5.687)$
Observations	29
\mathbb{R}^2	0.262
Adjusted \mathbb{R}^2	0.174
Residual Std. Error	1.376 (df = 25)
F Statistic	$2.965^* \text{ (df} = 3; 25)$
Note:	*p<0.1; **p<0.05; ***p<

Chapter 5: Multiple Regression Analysis: OLS Asymptotics

Example 5.3: Economic Model of Crime

```
narr86 = \beta_0 + \beta_1 pcnv + \beta_2 avgsen + \beta_3 tottime + \beta_4 ptime + \beta_5 qemp +
```

narr86: number of times arrested, 1986.

pcnv: proportion of prior arrests leading to convictions.

avgsen: average sentence served, length in months.

tottime: time in prison since reaching the age of 18, length in months.

ptime86: months in prison during 1986.

qemp86: quarters employed, 1986.

Load the crime1 data set.

```
data("crime1")
```

Estimate the model.

```
restricted_model <- lm(narr86 ~ pcnv + ptime86 + qemp86, data = crime1)
```

Create a new variable restricted_model_u containing the residuals $\tilde{\mu}$ from the above regression.

```
restricted_model_u <- restricted_model$residuals</pre>
```

Next, regress pcnv, ptime86, qemp86, avgsen, and tottime, against the residuals $\tilde{\mu}$ saved in restricted_model_u.

```
\tilde{\mu} = \beta_1 pcnv + \beta_2 avgsen + \beta_3 tottime + \beta_4 ptime 86 + \beta_5 qemp 86
```

[1] 0.001493846

$$LM = 2,725(0.0015)$$

```
LM_test <- nobs(LM_u_model) * 0.0015</pre>
```

[1] 4.0875

```
qchisq(1 - 0.10, 2)
```

[1] 4.60517

The p-value is:

$$P(X_2^2 > 4.09) \approx 0.129$$

```
1-pchisq(LM_test, 2)
```

[1] 0.129542

Chapter 6: Multiple Regression: Further Issues

Example 6.1: Effects of Pollution on Housing Prices, standardized.

$$price = \beta_0 + \beta_1 nox + \beta_2 crime + \beta_3 rooms + \beta_4 dist + \beta_5 stratio + \mu$$

price: median housing price.

nox: Nitrous Oxide concentration; parts per million.

crime: number of reported crimes per capita.

rooms: average number of rooms in houses in the community.

dist: weighted distance of the community to 5 employment centers.

stratio: average student-teacher ratio of schools in the community.

$$\widehat{zprice} = \beta_1 znox + \beta_2 zcrime + \beta_3 zrooms + \beta_4 zdist + \beta_5 zstratio$$

Load the hprice2 data.

```
data("hprice2")
```

Estimate the coefficient with the usual 1m regression model but this time, standardized coefficients by wrapping each variable with R's scale function:

Table 4:

	Dependent variable:
	scale(price)
scale(nox)	$-0.340^{***} (0.044)$
scale(crime)	$-0.143^{***} (0.031)$
scale(rooms)	$0.514^{***} (0.030)$
scale(dist)	-0.235***(0.043)
scale(stratio)	-0.270***(0.030)
Observations	506
\mathbb{R}^2	0.636
Adjusted R ²	0.632
Residual Std. Error	0.606 (df = 501)
F Statistic	$174.822^{***} (df = 5; 501)$
Note:	*p<0.1; **p<0.05; ***p<0.01

Example 6.2: Effects of Pollution on Housing Prices, Quadratic Interactive Term

Modify the housing model, adding a quadratic term in rooms:

 $log(price) = \beta_0 + \beta_1 log(nox) + \beta_2 log(dist) + \beta_3 rooms + \beta_4 rooms^2 + \beta_5 stratio + \mu$ housing_interactive <- lm(lprice ~ lnox + log(dist) + rooms+I(rooms^2) + stratio, data = hprice2)

Compare the results with the model from example 6.1.

stargazer(housing_standard, housing_interactive, single.row = TRUE, header = FALSE)

Table 5	:
---------	---

	Table 9:	
	Dependent variable:	
	scale(price)	lprice
	(1)	(2)
scale(nox)	$-0.340^{***} (0.044)$	
scale(crime)	$-0.143^{***} (0.031)$	
scale(rooms)	$0.514^{***} (0.030)$	
scale(dist)	-0.235^{***} (0.043)	
scale(stratio)	$-0.270^{***} (0.030)$	
lnox	` ,	-0.902^{***} (0.115)
log(dist)		$-0.087^{**} (0.043)$
rooms		$-0.545^{***}(0.165)$
I(rooms^2)		$0.062^{***} (0.013)$
stratio		-0.048***(0.006)
Constant		13.385*** (0.566)
Observations	506	506
\mathbb{R}^2	0.636	0.603
Adjusted \mathbb{R}^2	0.632	0.599
Residual Std. Error	0.606 (df = 501)	0.259 (df = 500)
F Statistic	$174.822^{***} (df = 5; 501)$	$151.770^{***} (df = 5; 500)$
Note:	*p.	<0.1; **p<0.05; ***p<0.01

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Chapter 7: Multiple Regression Analysis with Qualitative Information

Example 7.4: Housing Price Regression, Qualitative Binary variable

This time, use the hrprice1 data.

```
data("hprice1")
```

If you recently worked with hprice2, it may be helpful to view the documentation on this data set and read the variable names.

?hprice1

$$\widehat{log(price)} = \beta_0 + \beta_1 log(lotsize) + \beta_2 log(sqrft) + \beta_3 bdrms + \beta_4 colonial$$

Estimate the coefficients of the above linear model on the hprice data set.

Table 6:

	Dependent variable:
	lprice
llotsize	0.168*** (0.038)
lsqrft	$0.707^{***} (0.093)$
bdrms	0.027 (0.029)
colonial	$0.054\ (0.045)$
Constant	$-1.350^{**} (0.651)$
Observations	88
\mathbb{R}^2	0.649
Adjusted R^2	0.632
Residual Std. Error	0.184 (df = 83)
F Statistic	38.378*** (df = 4; 83)
Note:	*p<0.1; **p<0.05; ***p<0

Chapter 8: Heteroskedasticity

Example 8.9: Determinants of Personal Computer Ownership

$$\widehat{PC} = \beta_0 + \beta_1 hsGPA + \beta_2 ACT + \beta_3 parcoll + \beta_4 colonial$$

Load gpa1 and create a new variable combining the fathcoll and mothcoll, into parcoll. This new column indicates if either parent went to college.

```
data("gpa1")
gpa1$parcoll <- as.integer(gpa1$fathcoll==1 | gpa1$mothcoll)</pre>
GPA_OLS <- lm(PC ~ hsGPA + ACT + parcoll, data = gpa1)</pre>
```

Calculate the weights and then pass them to the weights argument.

```
weights <- GPA_OLS$fitted.values * (1-GPA_OLS$fitted.values)</pre>
GPA_WLS <- lm(PC ~ hsGPA + ACT + parcoll, data = gpa1, weights = 1/weights)
```

Compare the OLS and WLS model in the table below:

```
stargazer(GPA_OLS, GPA_WLS, single.row = TRUE, header = FALSE)
```

Table 7:

	$Dependent\ variable:$	
	PC	
	(1)	(2)
hsGPA	0.065 (0.137)	0.033(0.130)
ACT	$0.001\ (0.015)$	$0.004\ (0.015)$
parcoll	0.221**(0.093)	$0.215^{**} (0.086)$
Constant	-0.0004 (0.491)	$0.026 \ (0.477)$
Observations	141	141
\mathbb{R}^2	0.042	0.046
Adjusted R^2	0.021	0.026
Residual Std. Error $(df = 137)$	0.486	1.016
F Statistic (df $= 3; 137$)	1.979	2.224*

Note:

Chapter 9: More on Specification and Data Issues

Example 9.8: R&D Intensity and Firm Size

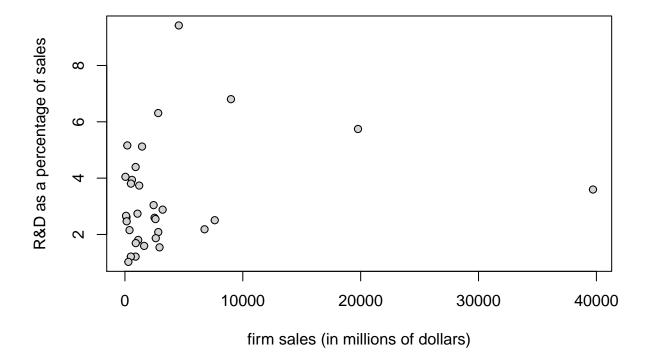
```
rdintens = \beta_0 + \beta_1 sales + \beta_2 prof marg + \mu
```

Load the data and estimate the model.

```
data("rdchem")
all_rdchem <- lm(rdintens ~ sales + profmarg, data = rdchem)</pre>
```

Plotting the data reveals the outlier on the far right of the plot, which will skew the results of our model.

FIGURE 9.1: Scatterplot of R&D intensity against firm sales



So, we can estimate the model without that data point to gain a better understanding of how sales and profmarg describe rdintens for most firms. We can use the subset argument of the linear model function to indicate that we only want to estimate the model using data that is less than the highest sales.

The table below compares the results of both models side by side. By removing the outlier firm, sales become a more significant determination of R&D expenditures.

stargazer(all_rdchem, smallest_rdchem, single.row = TRUE, header = FALSE)

Table 8:

	Dependent variable: rdintens	
	(1)	(2)
sales	0.0001 (0.00004)	0.0002** (0.0001)
profmarg	0.045(0.046)	$0.048 \ (0.044)$
Constant	2.625^{***} (0.586)	$2.297^{***} (0.592)$
Observations	32	31
\mathbb{R}^2	0.076	0.173
Adjusted R ²	0.012	0.114
Residual Std. Error	1.862 (df = 29)	1.792 (df = 28)
F Statistic	$1.195 \ (df = 2; 29)$	2.925* (df = 2; 28)

Note:

Chapter 10: Basic Regression Analysis with Time Series Data

Example 10.2: Effects of Inflation and Deficits on Interest Rates

$$\hat{i3} = \beta_0 + \beta_1 inf_t + \beta_2 def_t$$

```
data("intdef")

tbill_model <- lm(i3 ~ inf + def, data = intdef)

stargazer(tbill_model, single.row = TRUE, header = FALSE)</pre>
```

Table 9:

	Dependent variable:
	i3
inf	0.606*** (0.082)
def	$0.513^{***} (0.118)$
Constant	1.733*** (0.432)
Observations	56
\mathbb{R}^2	0.602
Adjusted R ²	0.587
Residual Std. Error	1.843 (df = 53)
F Statistic	$40.094^{***} (df = 2; 53)$
Note:	*p<0.1; **p<0.05; ***p<0.0

Example 10.11: Seasonal Effects of Antidumping Filings

```
data("barium")
barium_imports <- lm(lchnimp ~ lchempi + lgas + lrtwex + befile6 + affile6 +
    afdec6, data = barium)</pre>
```

Estimate a new model, barium_seasonal which accounts for seasonality by adding dummy variables contained in the data. Compute the anova between the two models.

```
barium_seasonal <- lm(lchnimp ~ lchempi + lgas + lrtwex + befile6 + affile6 +
    afdec6 + feb + mar + apr + may + jun + jul + aug + sep + oct + nov + dec,
    data = barium)

barium_anova <- anova(barium_imports, barium_seasonal)

stargazer(barium_imports, barium_seasonal, single.row = TRUE, header = FALSE)

stargazer(barium_anova, single.row = TRUE, header = FALSE)</pre>
```

Table 10:

	Dependent variable:	
	lchnimp	
	(1)	(2)
lchempi	3.117*** (0.479)	3.265*** (0.493)
lgas	$0.196 \ (0.907)$	-1.278(1.389)
lrtwex	0.983** (0.400)	$0.663 \ (0.471)$
befile6	$0.060 \ (0.261)$	$0.140 \ (0.267)$
affile6	-0.032(0.264)	$0.013\ (0.279)$
afdec6	-0.565*(0.286)	$-0.521^{*}(0.302)$
feb	` '	$-0.418\ (0.304)$
mar		$0.059 \ (0.265)^{'}$
apr		$-0.451^{\circ}(0.268)$
may		$0.033 \ (0.269)$
jun		-0.206(0.269)
jul		$0.004 \ (0.279)$
aug		-0.157(0.278)
sep		$-0.134\ (0.268)$
oct		$0.052 \ (0.267)^{'}$
nov		-0.246(0.263)
dec		$0.133\ (0.271)$
Constant	$-17.803 \ (21.045)$	16.779 (32.429)
Observations	131	131
\mathbb{R}^2	0.305	0.358
Adjusted R ²	0.271	0.262
Residual Std. Error	0.597 (df = 124)	0.601 (df = 113)
F Statistic	$9.064^{***} (df = 6; 124)$	$3.712^{***} (df = 17; 113)$

Note:

Table 11:

Statistic	N	Mean	St. Dev.	Min	Max
Statistic	1.4	Mean	Dr. Dev.	1/1111	Max
Res.Df	2	118.500	7.778	113	124
RSS	2	42.545	2.406	40.844	44.247
Df	1	11.000		11	11
Sum of Sq	1	3.403		3.403	3.403
F	1	0.856		0.856	0.856
Pr(>F)	1	0.585		0.585	0.585

Chapter 11: Further Issues in Using OLS with with Time Series Data

Example 11.7: Wages and Productivity

$$log(\widehat{hrwage_t}) = \beta_0 + \beta_1 log(outphr_t) + \beta_2 t + \mu_t$$

```
data("earns")
wage_time <- lm(lhrwage ~ loutphr + t, data = earns)
wage_diff <- lm(diff(lhrwage) ~ diff(loutphr), data = earns)
stargazer(wage_time, wage_diff, single.row = TRUE, header = FALSE)</pre>
```

Table 12:

	$Dependent\ variable:$	
	lhrwage	diff(lhrwage)
	(1)	(2)
loutphr	1.640*** (0.093)	
t	$-0.018^{***}(0.002)$	
diff(loutphr)	, ,	$0.809^{***} (0.173)$
Constant	-5.328**** (0.374)	$-0.004 \ (0.004)$
Observations	41	40
\mathbb{R}^2	0.971	0.364
Adjusted R^2	0.970	0.348
Residual Std. Error $(df = 38)$	0.029	0.017
F Statistic	$641.224^{***} (df = 2; 38)$	$21.771^{***} (df = 1; 38)$
	·	·

Note:

Chapter 12: Serial Correlation and Heteroskedasticiy in Time Series Regressions

Example 12.4: Prais-Winsten Estimation in the Event Study

```
data("barium")
barium_model <- lm(lchnimp ~ lchempi + lgas + lrtwex + befile6 + affile6 + afdec6,
    data = barium)
# Load the `prais` package, use the `prais.winsten` function to estimate.
library(prais)
barium_prais_winsten <- prais.winsten(lchnimp ~ lchempi + lgas + lrtwex + befile6 +
   affile6 + afdec6, data = barium)
barium_model
##
## Call:
## lm(formula = lchnimp ~ lchempi + lgas + lrtwex + befile6 + affile6 +
       afdec6, data = barium)
##
## Coefficients:
## (Intercept)
                   lchempi
                                                           befile6
                                   lgas
                                               lrtwex
    -17.80300
##
                   3.11719
                                0.19635
                                              0.98302
                                                           0.05957
##
      affile6
                    afdec6
      -0.03241
                   -0.56524
barium_prais_winsten
## [[1]]
##
## Call:
## lm(formula = fo)
##
## Residuals:
##
       Min
                      Median
                                    3Q
                                            Max
                 1Q
## -2.01146 -0.39152 0.06758 0.35063 1.35021
##
## Coefficients:
             Estimate Std. Error t value Pr(>|t|)
## Intercept -37.07771 22.77830 -1.628
                                           0.1061
                                   4.647 8.46e-06 ***
## lchempi
              2.94095
                        0.63284
## lgas
              1.04638
                         0.97734
                                  1.071
                                           0.2864
## lrtwex
             1.13279 0.50666
                                   2.236
                                           0.0272 *
## befile6
             -0.01648
                         0.31938 -0.052
                                           0.9589
## affile6
             -0.03316
                         0.32181 -0.103
                                           0.9181
## afdec6
             -0.57681
                         0.34199 -1.687
                                           0.0942 .
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 0.5733 on 124 degrees of freedom
## Multiple R-squared: 0.9841, Adjusted R-squared: 0.9832
## F-statistic: 1096 on 7 and 124 DF, p-value: < 2.2e-16
##
## [[2]]
         Rho Rho.t.statistic Iterations
##
                    3.483363
## 0.2932171
```

Example 12.8: Heteroskedasticity and the Efficient Markets Hypothesis

$$return_t = \beta_0 + \beta_1 return_{t-1} + \mu_t$$

```
data("nyse")
return_AR1 <-lm(return ~ return_1, data = nyse)</pre>
```

$$\hat{\mu_t^2} = \beta_0 + \beta_1 return_{t-1} + residual_t$$

```
return_mu <- residuals(return_AR1)
mu2_hat_model <- lm(return_mu^2 ~ return_1, data = return_AR1$model)
stargazer(return_AR1, mu2_hat_model, single.row = TRUE, header = FALSE)</pre>
```

Table 13:

	$Dependent\ variable:$	
	return	$return_mu^2$
	(1)	(2)
return_1	0.059 (0.038)	-1.104^{***} (0.201)
Constant	0.180** (0.081)	4.657*** (0.428)
Observations	689	689
\mathbb{R}^2	0.003	0.042
Adjusted R^2	0.002	0.041
Residual Std. Error ($df = 687$)	2.110	11.178
F Statistic (df = 1 ; 687)	2.399	30.055***

Note:

Example 12.9: ARCH in Stock Returns

$$\hat{\mu_t^2} = \beta_0 + \hat{\mu_{t-1}^2} + residual_t$$

We still have return_mu in the working environment so we can use it to create $\hat{\mu_t^2}$, (mu2_hat) and $\hat{\mu_{t-1}^2}$ (mu2_hat_1). Notice the use R's matrix subset operations to perform the lag operation. We drop the first observation of mu2_hat and squared the results. Next, we remove the last observation of mu2_hat_1 using the subtraction operator combined with a call to the NROW function on return_mu. Now, both contain 688 observations and we can estimate a standard linear model.

```
mu2_hat <- return_mu[-1]^2
mu2_hat_1 <- return_mu[-NROW(return_mu)]^2
arch_model <- lm(mu2_hat ~ mu2_hat_1)
stargazer(arch_model, single.row = TRUE, header = FALSE)</pre>
```

Table 14:

	Dependent variable:
	$mu2_hat$
mu2_hat_1	$0.337^{***} (0.036)$
Constant	2.947*** (0.440)
Observations	688
\mathbb{R}^2	0.114
Adjusted R ²	0.112
Residual Std. Error	10.759 (df = 686)
F Statistic	$87.923^{***} (df = 1; 686)$
Note:	*p<0.1; **p<0.05; ***p<0.

Chapter 13: Pooling Cross Sections across Time: Simple Panel Data Methods

Example 13.7: Effect of Drunk Driving Laws on Traffic Fatalities

$$\widehat{\Delta dthrte} = \beta_0 + \Delta open + \Delta admin$$

```
data("traffic1")

DD_model <- lm(cdthrte ~ copen + cadmn, data = traffic1)

stargazer(DD_model, single.row = TRUE, header = FALSE)</pre>
```

Table 15:

	Dependent variable:
	$\operatorname{cdthrte}$
copen	$-0.420^{**} (0.206)$
cadmn	-0.151 (0.117)
Constant	$-0.497^{***} (0.052)$
Observations	51
\mathbb{R}^2	0.119
Adjusted R ²	0.082
Residual Std. Error	0.344 (df = 48)
F Statistic	$3.231^{**} (df = 2; 48)$
Note:	*p<0.1: **p<0.05: ***p<0.0

Chapter 14: Advanced Panel Data Methods

Example 14.1: Effect of Job Training on Firm Scrap Rates

In this section, we will estimate a linear panel modeg using the plm function from the plm: Linear Models for Panel Data package. See the bibliography for more information.

Table 16:

	Dependent variable:
	lscrap
d88	-0.080 (0.109)
d89	$-0.247^* (0.133)$
grant	-0.252^* (0.151)
grant_1	$-0.422^{**} (0.210)$
Observations	162
\mathbb{R}^2	0.201
Adjusted R ²	-0.237
F Štatistic	$6.543^{***} (df = 4; 104)$
Note:	*p<0.1; **p<0.05; ***p<0.0

Chapter 15: Instrumental Variables Estimation and Two Stage Least Squares

Example 15.1: Estimating the Return to Education for Married Women

$$log(wage) = \beta_0 + \beta_1 educ + \mu$$

```
data("mroz")
wage_educ_model <- lm(lwage ~ educ, data = mroz)</pre>
```

$$\widehat{educ} = \beta_0 + \beta_1 fatheduc$$

We run the typical linear model, but notice the use of the subset argument. inlf is a binary variable in which a value of 1 means they are "In the Labor Force". By sub-setting the mroz data frame by observations in which inlf==1, only working women will be in the sample.

```
fatheduc_model <- lm(educ ~ fatheduc, data = mroz, subset = (inlf==1))</pre>
```

In this section, we will perform an **Instrumental-Variable Regression**, using the **ivreg** function in the AER (Applied Econometrics with R) package. See the bibliography for more information.

```
library("AER")
wage_educ_IV <- ivreg(lwage ~ educ | fatheduc, data = mroz)
stargazer(wage_educ_model, fatheduc_model, wage_educ_IV, single.row = TRUE,
    header = FALSE)</pre>
```

Table 17:

	$Dependent\ variable:$		
	lwage	educ	lwage
	OLS	OLS	$instrumental\\variable$
	(1)	(2)	(3)
educ	0.109*** (0.014)		0.059*(0.035)
fatheduc	, ,	$0.269^{***} (0.029)$, ,
Constant	$-0.185 \ (0.185)$	10.237*** (0.276)	$0.441 \ (0.446)$
Observations	428	428	428
\mathbb{R}^2	0.118	0.173	0.093
Adjusted R ²	0.116	0.171	0.091
Residual Std. Error ($df = 426$)	0.680	2.081	0.689
F Statistic ($df = 1; 426$)	56.929***	88.841***	

Note:

Example 15.2: Estimating the Return to Education for Men

$$\widehat{educ} = \beta_0 + sibs$$

```
data("wage2")
educ_sibs_model <- lm(educ ~ sibs, data = wage2)</pre>
```

$$\widehat{log(wage)} = \beta_0 + educ$$

Again, estimate the model using the ivreg function in the AER (Applied Econometrics with R) package. library("AER")

educ_sibs_IV <- ivreg(lwage ~ educ | sibs, data = wage2)
stargazer(educ_sibs_model, educ_sibs_IV, wage_educ_IV, single.row = TRUE, header = FALSE)</pre>

Table 18:

	$Dependent\ variable:$		
	educ	lwage	
	$OLS \hspace{1cm} instrumental \ variable$		
	(1)	(2)	(3)
sibs	-0.228***(0.030)		
educ	` ,	$0.122^{***} (0.026)$	0.059*(0.035)
Constant	$14.139^{***} (0.113)$	$5.130^{***} (0.355)$	$0.441 \ (0.446)$
Observations	935	935	428
\mathbb{R}^2	0.057	-0.009	0.093
Adjusted R ²	0.056	-0.010	0.091
Residual Std. Error	2.134 (df = 933)	0.423 (df = 933)	0.689 (df = 426)
F Statistic	$56.667^{***} (df = 1; 933)$		

Note:

Example 15.5: Return to Education for Working Women

$$\widehat{log(wage)} = \beta_0 + \beta_1 educ + \beta_2 exper + \beta_3 exper^2$$

Use the ivreg function in the AER (Applied Econometrics with R) package to estimate.

```
data("mroz")
wage_educ_exper_IV <- ivreg(lwage ~ educ + exper + expersq | exper + expersq +
    motheduc + fatheduc, data = mroz)</pre>
```

Table 19:

	Dependent variable:
	lwage
educ	$0.061^* \ (0.031)$
exper	$0.044^{***} (0.013)$
expersq	-0.001**(0.0004)
Constant	0.048 (0.400)
Observations	428
\mathbb{R}^2	0.136
Adjusted R^2	0.130
Residual Std. Error	0.675 (df = 424)
Note:	*p<0.1; **p<0.05; ***p<0.01

Chapter 16: Simultaneous Equations Models

Example 16.4: INFLATION AND OPENNESS

$$inf = \beta_{10} + \alpha_1 open + \beta_{11} log(pcinc) + \mu_1$$
$$open = \beta_{20} + \alpha_2 inf + \beta_{21} log(pcinc) + \beta_{22} log(land) + \mu_2$$

Example 16.6: INFLATION AND OPENNESS

library(AER)

Note:

$$\widehat{open} = \beta_0 + \beta_1 log(pcinc) + \beta_2 log(land)$$

```
data("openness")
open_model <-lm(open ~ lpcinc + lland, data = openness)</pre>
```

$$\widehat{inf} = \beta_0 + \beta_1 open + \beta_2 log(pcinc)$$

Use the ivreg function in the AER (Applied Econometrics with R) package to estimate.

inflation_IV <- ivreg(inf ~ open + lpcinc | lpcinc + lland, data = openness)</pre>

stargazer(open_model, inflation_IV, single.row = TRUE, header = FALSE)

Table 20:

	$Dependent\ variable:$		
	open	inf	
	OLS	$instrumental\\variable$	
	(1)	(2)	
open		-0.337**(0.144)	
lpcinc	0.546 (1.493)	0.376(2.015)	
lland	-7.567**** (0.814)		
Constant	117.085*** (15.848)	26.899* (15.401)	
Observations	114	114	
\mathbb{R}^2	0.449	0.031	
Adjusted R^2	0.439	0.013	
Residual Std. Error $(df = 111)$	17.796	23.836	
F Statistic	$45.165^{***} (df = 2; 111)$		

Chapter 17: Limited Dependent Variable Models and Sample Selection Corrections

Example 17.3: POISSON REGRESSION FOR NUMBER OF ARRESTS

```
data("crime1")
```

Sometimes, when estimating a model with many variables, defining a model object containing the formula makes for much cleaner code.

```
formula <- (narr86 ~ pcnv + avgsen + tottime + ptime86 + qemp86 + inc86 + black +
   hispan + born60)
```

Then, pass the formula object into the lm function, and define the data argument as usual.

```
econ_crime_model <- lm(formula, data = crime1)</pre>
```

To estimate the poisson regression, use the general linear model function glm and define the family argument as poisson.

```
econ_crim_poisson <- glm(formula, data = crime1, family = poisson)</pre>
```

Use the stargazer package to easily compare diagnostic tables of both models.

stargazer(econ_crime_model, econ_crim_poisson, single.row = TRUE, header = FALSE)

Table 21:

	$Dependent\ variable:$		
	narr86		
	OLS	Poisson	
	(1)	(2)	
pcnv	$-0.132^{***} (0.040)$	$-0.402^{***} (0.085)$	
avgsen	$-0.011 \ (0.012)$	-0.024 (0.020)	
tottime	0.012 (0.009)	0.024*(0.015)	
ptime86	$-0.041^{***} (0.009)$	$-0.099^{***} (0.021)$	
qemp86	-0.051^{***} (0.014)	-0.038(0.029)	
inc86	$-0.001^{***} (0.0003)$	-0.008***(0.001)	
black	$0.327^{***} (0.045)$	0.661***(0.074)	
hispan	$0.194^{***} (0.040)$	0.500***(0.074)	
born60	-0.022 (0.033)	-0.051 (0.064)	
Constant	$0.577^{***} (0.038)$	$-0.600^{***} (0.067)$	
Observations	2,725	2,725	
\mathbb{R}^2	0.072		
Adjusted R ²	0.069		
Log Likelihood		-2,248.761	
Akaike Inf. Crit.		4,517.522	
Residual Std. Error	0.829 (df = 2715)		
F Statistic	$23.572^{***} (df = 9; 2715)$		
Note:	*p<0.1; **p<0.05; ***p<0.01		

Chapter 18: Advanced Time Series Topics

Example 18.8: FORECASTING THE U.S. UNEMPLOYMENT RATE

data("phillips")

$$\widehat{unemp}_t = \beta_0 + \beta_1 unem_{t-1}$$

Estimate the linear model in the usual way and note the use of the subset argument to define data equal to and before the year 1996.

$$\widehat{unemp_t} = \beta_0 + \beta_1 unem_{t-1} + \beta_2 inf_{t-1}$$

Table 22:

	Dependen	t variable:	
	unem		
	(1)	(2)	
unem_1	0.732*** (0.097)	0.647*** (0.084)	
inf_1	` ,	0.184***(0.041)	
Constant	$1.572^{***} (0.577)$	1.304** (0.490)	
Observations	48	48	
\mathbb{R}^2	0.554	0.691	
Adjusted R ²	0.544	0.677	
Residual Std. Error	1.049 (df = 46)	0.883 (df = 45)	
F Statistic	$57.132^{***} (df = 1; 46)$	$50.219^{***}(df = 2; 45)$	

Note:

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Appendix

Using R for Introductory Econometrics

This is an excellent open source complimentary text to "Introductory Econometrics" by Jeffrey M. Wooldridge and should be your number one resource. This excerpt from the book's website:

This book introduces the popular, powerful and free programming language and software package R with a focus on the implementation of standard tools and methods used in econometrics. Unlike other books on similar topics, it does not attempt to provide a self-contained discussion of econometric models and methods. Instead, it builds on the excellent and popular textbook "Introductory Econometrics" by Jeffrey M. Wooldridge.

Hess, Florian. *Using R for Introductory Econometrics*. ISBN: 978-1-523-28513-6, CreateSpace Independent Publishing Platform, 2016, Dusseldorf, Germany.

url: https://urfie.net.

Applied Econometrics with R

From the publisher's website:

This is the first book on applied econometrics using the R system for statistical computing and graphics. It presents hands-on examples for a wide range of econometric models, from classical linear regression models for cross-section, time series or panel data and the common non-linear models of microeconometrics such as logit, probit and tobit models, to recent semiparametric extensions. In addition, it provides a chapter on programming, including simulations, optimization, and an introduction to R tools enabling reproducible econometric research. An R package accompanying this book, AER, is available from the Comprehensive R Archive Network (CRAN) at http://CRAN.R-project.org/package=AER.

Kleiber, Christian and Achim Zeileis. *Applied Econometrics with R.* ISBN 978-0-387-77316-2, Springer-Verlag, 2008, New York. http://www.springer.com/us/book/9780387773162