$$E(\max(r_1 + p_M, r_2)) = \int_{-\infty}^{\infty} x f(x) dx$$

where f(x) = F'(x)

F being the cumulative distribution function

$$F(x) = \int_0^x f(x)dx \tag{1}$$

$$= prob\{\max\{r_1 + p_M, r_2\} < x\}$$
 (2)

$$= prob\{r_1 + p_M < x\} * prob\{r_2 < x\}$$
 (3)

$$= \begin{cases} (x^{2} - p_{M}x), & p_{M} < x < 1\\ (x - p_{M}), & 1 < x < p_{M}\\ 1, & x > 1 + p_{M}\\ 0, & otherwise \end{cases}$$

$$(4)$$

Thus,

$$f(x) = \begin{cases} 2x - p_M, & p_M < x < 1\\ 2x - p_M + 1, & 1 < x < 1 + p_M\\ 0, & otherwise \end{cases}$$
 (5)

And so,

$$\int_{-\infty}^{\infty} x f(x) dx \tag{6}$$

$$= \int_{p_M}^{1+p_M} 2x^2 - p_M x dx + \int_{1}^{1+p_M} 2x^2 - x p_M + x dx \tag{7}$$

$$=\frac{2}{3} - \frac{3}{2}p_M + 3p_M^2 \tag{8}$$