# Can It Be Economically Rational to Restrict Big Box Retailers?

## Introduction

Conventional wisdom from committed "free market" economists would have it that moves to ban "big box" retailers such as Walmart from certain localities are rebellions against consumer sovereignty and must hurt consumer welfare. After all, if consumers did not want to shop at the big box retailer, they would simply not do so, correct? The fact that they switch their shopping to the big box and away from "mom-and-pop" stores shows they prefer the big box.

## Theoretical Considerations

This paper attempts to show that the above analysis is simplistic. We present a model in which all consumers have the following preference ordering in some retail sector:

1. Have both local shops and a big box store.
2. Have only local shops.
3. Have only a big box store.

(We can further assume they know the costs of achieving 1, 2, or 3: they want 1 even if they sometimes pay higher prices to achieve it compared to 3, i.e., we could add a monthly shopping bill to each of the above.)

We then show that, under not outrageous assumptions, it is easy for consumers, in trying to achieve their first preference, to instead wind up with their third. This is due to consumers facing a collective action problem, as well as a knowledge problem: Consumers might, if they had perfect knowledge of the exit points of the local shops and the ability to finely coordinate their own shopping with that of others, be able to achieve their first preference (a mix of big box and mom-and-pop shopping available). But, in general, consumers have little knowledge of what percentage reduction in sales will cause a small shop to exit the industry, nor do they have very much ability to coordinate their shopping with other consumers. (The latter means that even if consumers forego a certain amount of shopping at the big box stores, which they would otherwise do, simply to keep the small stores solvent, they cannot ensure their neighbors will do the same. So their rational choice is to "defect" and shop at the big box store as often as they wish, regardless of the impact on the small shops.)

Therefore, since they cannot fine tune their shopping to achieve 1), they shop at the big box store whenever it suits them for a particular purchase, without regards to the "macro" effects of their choices. (See Schelling, 2006, for extensive analysis of the potential gap between micromotives and macrobeahvior.) They shift "too" much of their shopping to the big box, with the end result is that all of the mom-and-pops are driven out of business, despite no consumer wanting that result. Thus, it *might* make sense, faced with such knowledge and game theoretic difficulties, for consumers to bind themselves in advance to 2), by banning a, or some, or all, big box stores, or to trying to achieve 1) by, say, forcing big box retailers to locate well outside the center of town, making trips to them less convenient. (All legislation has unintended consequences, which is why we make the weak claim that these types of actions *might* make sense: such legislation might also, for instance, serve the interest of an inefficient local monopolist seeking to protect its privileged position in a market.)

### Predatory Pricing

We further suggest that our model may actually capture the mechanism underlying the intuition of the existence of "predatory pricing." As has often been noted, the idea that big box stores engage in predatory pricing to drive out small competitors and then jack up the prices to achieve high profits has an obvious problem: once the prices charged by the big box stores have been raised, why don't the small competitors simply reenter the market? (See, for instance, DiLorenzo, 1992.)   
  
Our model avoids this pitfall: the big box stores do not need to set prices artificially low for a time: they can rely on their greater financial resources to ride out the period during which **all** stores will be losing money, and once their smaller competitors have exited, they can keep their prices right where they were, and now be profitable. And new smaller competitors will not enter the market, since that would merely reestablish the situation in which all stores are losing money. Furthermore, our model has the advantage that we need not posit any vicious intent on the part of big-box retailers: they need not be *intending* to drive small retailers out of business. They just know that in a year or so, their new outlet will be making plenty of money.

We note here that what we are describing, in suggesting the possibility that some restriction on big-box retailing might be rational, is an example of the general class of "constitutional constraints" described by Jon Elster in *Ulysses Unbound* (2000): we want to listen to the Sirens, but we know that if we do not tie ourselves to the mast in advance, we will not merely listen, but fall prey to their sweet song. Or, to consider more mundane circumstances, by the sober light of day, we realize that we do not want to find ourselves in a bar at 4 AM, but we also recognize that in the bar at 1 AM, we will not be thinking so clearly. So we mandate a bar closing time. Similarly, we don't want our own speech suppressed, but recognize that in power we might give in to the temptation to suppress speech we don't like, and that others in power might do so to us. So we pass the first amendment to the U.S. Constitution.

## Mathematical Analysis

In our model, if a retailer’s funding falls below zero, it is out of the game. So naturally, if the its expenses are on average higher than its income, the retailer will eventually meet this miserable fate. The situation our model seeks to create is one where the big boxes’ appearance effects the mom and pop stores to close their doors. We shall represent income and expense by *I* and *R* respectively, and abbreviate “mom-and-pop” by M; “big-box” by B. In symbols, therefore, before the B appears the M should be either making due, or making profit:

(a) *IM ≥ R*

And when the B appears,

(b) *R > IM*

where I and R respectively represent income and expense. A stronger condition is the big-boxes’ profiting even during the mom-and-pops’ competition.

(c) *IB ≥ R > IM*

This stronger condition is useful to analyze for three reasons: (1) its condition is met quite often; (2) and it is illustrative of the model’s dynamics; (3) it is a way to express the incomes of our retailers against the expense they must cover.

Let’s understand how our model’s key players factor into the retailers’ incomes : We let *N* stand in place for the number of consumers who shop at retailers, *D* the dollar amount consumers give each store each turn, *G* the number of types of goods (hence the number of *M*s), and *p* the consumer preference for *M*s. The preference *p* is the probability that the consumer will choose Ms over Bs; thus it is a number between 0 and 1 inclusive.

Initially, when there is no B, the expected value for each M’s income is the money gotten from all consumers who decide to shop for their good that day. Since the total number of customers for a particular store is about *N / G*, a M’s income is expected to be

IM = D\* (*N / G*)

When the B appears, however, preference plays a role.

IM = D\* (*N / G*) \* *p*

The equation for the income of the Bs is simpler. Since they sell all goods, their income is unaffected by the number of goods sold, and the chance a customer will shop with them is the remaining probability of their shopping at the M, namely (1-p).

IB = *D* \* *N \** (1-*p*)

Therefore inequality (c) becomes

D\* *N \** (1 - *p*) *≥ R > D* \* (*N / G*) \* *p*

And this expression we may message into something easy to comprehend:

(1 - *p*) *≥ R / (N \* D) >* (1 */ G*) \* *p*

We may call the expression in the middle “S” meaning “survival threshold.”

(d) (1 - *p*) *≥ S >* (1 */ G*) \* *p*

Therefore if either (1-*p*) or (1 */ G*) \* *p* is to the right of *R*, *B* and *D* respectively are expected to fail. We may now make several interesting conclusions about our model:

(i) If (1 - p) > ( 1 / G ) \* p, Bs have higher income than Ms regardless of population size, rend, and income per visitor.

(ii) When p > 0.5, as our model conditions require than consumers have at least a slight preference for Ms, the only factor giving Bs relative success over M is the number of goods sold. For instance, a good mom-and-pop-friendly town might have shop at Ms 75% of the time. However if there are as few as four different types of good, our inequality

(1 - p) > ( 1 / G ) \* p

becomes

0.25 > 0.1875

which is bad news for the mom and pop store because there is plenty of space for S to fit between those two numbers: say, R = $4, N = 20, M = $1. With these constants, the Ms would have survived without the B, but the B puts too much pressure on the M, and the M will eventually be run out of business.

We also may conclude that even in extreme cases, where there is a high preference for Ms, Bs will win the day if too many kinds of goods exist in the economy. Let’s have p = 0.99, and G = 100. Then the B has the upper hand again!

0.01 > 0.0099

And there is still an interval where S can come in and ruin the Ms chance, leaving the big boxes with a monopoly.

## Model Design

In order to see if our notion is theoretically plausible, we create a model populated by two basic types of agents: consumers (C), and retailers (R). Retailers are further classed as mom-and-pops (M) or big-boxes (B). The mom-and-pops each supply a specific type of good, such as hardware or groceries. The big-boxes provide every sort of good. At first the environment is occupied by only Ms and Cs. Each supplies something the other needs: the consumers supply money to the mom-and-pop stores, and they supply goods to the consumers. Rs receive a periodic endowment of goods "from heaven" (which is a parameter), while Cs have the same thing happen in regards to money. Cs shop in turn at each stores selling each type of good they need. If Rs run out of money, they disappear. Without big box competitors, we discover an equilibrium can exist so that a certain number of Ms can remain in business.

At a certain point in the running of our model, the Bs appear. They have a much larger initial endowment of money then do the Ms. The Cs want to shop at both types of retailer (how much they like each is again a parameter), and split their acquisition of goods (according to that parameter) between the two types of retailers. (In order to illustrate the thesis of our paper, that consumer behavior may thwart consumer preferences, we have run our model with consumers preferring the mom-and-pops by as much as four-to-one, and have still gotten a result where the small shops disappear.) This split may cause the funds of both types of agents to dwindle. But as the Bs have a much greater initial endowment, they are able to survive this period of coexistence, while the Ms gradually disappear. We are left with an environment of only Bs and Cs, which the Cs did *not* want. Thus, given simple but not outrageous assumptions, our model shows our story above is plausible: it has what Weber would call "explanatory adequacy." Empirical work would be necessary to decide whether it has Weberian "causal adequacy." (See Callahan and Horwitz, 2010, for a brief description of the difference between the two concepts in Weber.)

## Model Implementation

### The Indra System

Indra is an agent based modeling (ABM) system built in Python. Our model runs on it, and so it would be valuable to review its [architecture](https://gcallah.github.io/Indra/index.html). Indra includes the following capabilities:

* Looping over agents randomly, in order, in reverse order, or by type.
* Automatic generation of line graphs and scatter plots.
* The ability to enter model parameters interactively, from the command line, or from a file.
* The ability to save parameters sets.
* The ability to dump the state of the system to a JSON file.
* A built-in, extensible interactive menu.
* Automatic creation of network graphs showing the relationship among objects in the system.
* Extensible Markov-matrix capabilities for easily specified, probabilistic behavior on the part of agents.
* A flexible spacial environment model that allows the composition of agent views of the environment of any desired shape, easing the creation of models exploring limited, local agent knowledge.
* In-line debugging capabilities, allowing, e.g., the screen display of all of an agent's attributes at any point during the run of a model.
* The ability to step through a model to watch it develop in real time.

### Implementing the Big Box Model in Indra

#### Overview

In addition to running on the base framework of agents and environments, our model includes Indra's Markov classes. These allow our Consumers to display psuedorandom shopping behavior according to the logic of [Markov chains](https://en.wikipedia.org/wiki/Markov_chain). These Consumers choose to either buy from a MomAndPop Retailer or a BigBox retailer; their preference is decided by use of a [transition matrix](https://en.wikipedia.org/wiki/https://en.wikipedia.org/wiki/Stochastic_matrix). When an agent sees a collection of stores he could possibly go to, he needs some way to choose. Let's say we define his preferences so that when there are multiple places to go, he goes to a mom and pop about 70% of the time and to a big box 30% of the time. An option to simulate this is to generate random numbers: If a random number between 0.0 and 1.0 is less than 0.7, the agent goes to the mom and pop; otherwise he goes to the big box. We can do this by use of Indra's Markov classes, which provide the capability to work with a large array of phenomena that are, or, at least, look like, Markov processes.

The way we read the transition matrix is as follows. Our Consumer sees that there are both MomAndPop and BigBox retailers who sell his desired good. Further, he has a predilection for the MomAndPops such that he goes to them about 70% of the time; leaving the remaining 30% of shopping for the BigBox stores.

#### Model Details

Let us look, first, at the behavior of consumers, and then, briefly, at the simpler behavior of retailers.

When a **consumer** acts, he surveys the world around him, evaluates his world on the basis of this survey, and he responds according to his evaluation. Naturally, therefore, we call these methods survey\_env, eval\_env, and respond\_to\_cond.

def act(self):

env\_vars = self.survey\_env()

eval\_vars = self.eval\_env(env\_vars)

if eval\_vars:

self.respond\_to\_cond(eval\_vars)

The way the consumer surveys his environment goes like this: he finds all the stores he can view (a view which happens to be the whole environment this model) and he only remembers the stores which sell the good he wants.

def survey\_env(self):

view = self.env.get\_square\_view(

center=self.pos,

distance=math.sqrt(

self.env.width\*\*2 +

self.env.height\*\*2))

n\_census = []

n\_census.extend(self.neighbor\_iter(view=view,

filt\_func=lambda x:

x.sells(self.goal)))

return n\_census

Here is how a Consumer decides where to go shopping:

def eval\_env(self, n\_census):

self.state\_pre = self.env.get\_pre(self, n\_census)

self.state\_vec = markov.probvec\_to\_state(

self.state\_pre.matrix)

self.state = markov.get\_state(self.state\_vec)

if(self.state == 0):

self.preference = MomAndPop

if(self.state == 1):

self.preference = BigBox

for store in n\_census:

if type(store) is self.preference:

return store

Consumers obtain their prehension from the Environment. We build a 2x1 matrix. The (1,1) entry represents the agent's chance of going to a mom\_and\_pop, and the (1,2) entry is that of the big\_box. If a type is not in the agents neighborhood, we cannot go there. Since this means there may be a zero entry, we must normalize the vector. For the column must sum to 1, according to the idea of a transition matrix.

def get\_pre(self, agent, n\_census):

trans\_str = ""

if(self.there\_is(n\_census, MomAndPop)):

trans\_str += "0.7 "

else:

trans\_str += "0.0 "

if(self.there\_is(n\_census, BigBox)):

trans\_str += "0.3"

else:

trans\_str += "0.0"

state\_pre = markov.from\_matrix(np.matrix(trans\_str))

state\_pre.matrix = vs.normalize(state\_pre.matrix)

return state\_pre

After choosing where to go, he goes there and buys his long sought after good.

def respond\_to\_cond(self, store):

self.move(store)

store.buy\_from(self.allowance)

After this action, the consumer now decides his goal is to aquire a new good. This goal is to be acted out during the next cycle of interactions.

def postact(self):

"""

We cycle through the goods the agent might want

turn-by-turn.

"""

self.goal = (self.goal + 1) % NUM\_GOODS

The **retailer**'s action is much simpler. It merely pays its bills. If its funds go below zero, it goes bankrupt, and it disappears from the environment never to reappear.

def act(self):

self.pay\_bills(self.rent)

if(self.funds <= 0):

self.declare\_bankruptcy()

## Appendix: Source Code and Mathematics

* [Big Box Model](https://github.com/gcallah/Indra/blob/master/bigbox/big_box_model.py)
* [Big Box Run](https://github.com/gcallah/Indra/blob/master/bigbox/big_box_run.py)

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