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GATE 2023-EE Q49

EE23BTECH11052 - Abhilash Rapolu

Question 49: The period of the discrete-time signal x[n] described by the equation below is N = (Round off to the nearest integer).

$$x[n] = 1 + 3\sin\left(\frac{15\pi}{8}n + \frac{3\pi}{4}\right) - 5\sin\left(\frac{\pi}{3}n - \frac{\pi}{4}\right)$$

Solution:

Parameter	Description	Value
f_1	Sinusoid1 Frequency	15/16
f_2	Sinusoid2 Frequency	6
TABLE I		

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The time period must be an integer for a discretetime signal.

$$T_1 = \frac{1}{f_1} = \frac{16}{15} \tag{1}$$

$$T_2 = \frac{1}{f_2} = 6 \tag{2}$$

$$N = LCM(T_1, T_2) = 48$$
 (3)

The Time Period of the signal is N=48. Let's find the Discrete Fourier Transform (X[k]):

$$X[k] = \sum_{n=0}^{N-1} x[n]e^{-j\frac{2\pi}{N}kn}$$
 (4)

$$X[k] = \begin{cases} 48 & \text{if } k = 0\\ 50.9117 - 50.9117j & \text{if } k = 3\\ 0 & \text{otherwise} \end{cases}$$
 (5)

