## Assignment

## 12.7 - 8

## EE23BTECH11220 - R.V.S.S Varun

## QUESTION

A charged 30  $\mu$ F capacitor is connected to a 27 mH inductor. Suppose the initial charge on the capacitor is 6mC. What is the total energy stored in the circuit initially? What is the total energy at later time?

SOLUTION

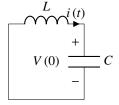


Fig. 0. Circuit diagram

Symbol	Description	Value
q(0+)	Initial charge on capacitor	6 mC
q(t)	Charge on capacitor	-
L	Value of inductance	27 mH
С	Value of capacitance	$30 \mu F$
Е	Total energy stored in circuit	-
$E_L$	Energy stored in inductor	-
$E_C$	Energy stored in capacitor	-
i(t)	current in the inductor	$\frac{dq}{dt}$
I(s)	Laplace transform of $i(t)$	-
TABLE 0		

TABLE OF PARAMETERS

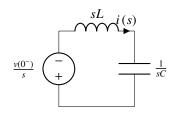


Fig. 0. Circuit diagram in laplace domain

Writing KVL in above circuit,

$$LsI(s) + \frac{v(0^{+})}{s} + \frac{1}{C}\frac{I(s)}{s} = 0$$
 (1)

$$I(s) = \frac{-v(0^+)C}{LCs^2 + 1}$$
 (2)

From initial value theorem,

$$i(0^{+}) = \lim_{s \to \infty} [sI(s)] \tag{3}$$

$$i(0^{+}) = \lim_{s \to \infty} \left[ s \frac{-v(0^{+})C}{LCs^{2} + 1} \right] = 0$$
 (4)

From final value theorem,

$$i(\infty) = \lim_{s \to 0} [sI(s)] \tag{5}$$

$$i(\infty) = \lim_{s \to 0} \left[ s \frac{-v(0^+)C}{LCs^2 + 1} \right] = 0$$
 (6)

$$i(0^+) = i(\infty) \tag{7}$$

$$=0 (8)$$

Hence,

$$q(0^+) = q(\infty) \tag{9}$$

$$= 6 mC \tag{10}$$

from (7),

$$E_L = 0 \tag{11}$$

$$E_C = \frac{q^2}{2C} \tag{12}$$

$$=0.6 J \tag{13}$$

$$E = 0.6 J \tag{15}$$

Hence , the total energy stored in the circuit initially and at a later time is  $0.6\ J.$