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Discrete

EE1205: Signals and Systems Indian Institute of Technology Hyderabad

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I. Question 11.9.5 (18)

If a and b are the roots of $x^2 - 3x + p = 0$ and c, d are roots of $x^2 - 12x + q = 0$ where a, b, c, dform a G.P. Prove that (q + p) : (q - p) = 17:15.

II. SOLUTION

Value	Description
-	G.P. Sequence
а	First term of G.P.
b	Second term of G.P.
c	Third term of G.P.
d	Fourth term of G.P.
$\frac{b}{a}$	Common ratio
	- a b c

GIVEN PARAMETERS

On dividing eq. ?? and eq. ??, we get

$$\frac{ar^2(1+r)}{a(1+r)} = \frac{12}{3} \tag{7}$$

$$r^2 = 4 \tag{8}$$

$$r = \pm 2 \tag{9}$$

When r = 2, a = 1When r = -2, a = -3

Case 1: When r = 2 and a = 1

$$p = ab \tag{10}$$

$$p = 2 \tag{11}$$

$$q = cd \tag{12}$$

$$q = 32 \tag{13}$$

$$\frac{q+p}{q-p} = \frac{32+2}{32-2} \tag{14}$$

$$=\frac{17}{15}$$
 (15)

Case 2: When r = -2 and a = -3

Given $x_1(0)$ and $x_1(1)$ are the roots of $x^2-3x+p=$ 0 So, we have:

$$a + b = 3 \tag{1}$$

$$ab = p \tag{2}$$

Also, $x_1(2)$ and $x_1(3)$ are the roots of $x^2-12x+q=$ 0 , so,

$$c + d = 12 \tag{3}$$

$$cd = q$$

(4) Hence, case 1 satisfies the condition.

From ?? and ??, we get,

$$a(1+r) = 3 \tag{5}$$

$$ar^n u(n) \longleftrightarrow \frac{a}{1 - rz^{-1}} \; ; \; |z| > |r|$$
 (22)

And,

$$p = 2 \tag{11}$$

$$q = ca$$
 (12)

$$q = 32 \tag{13}$$

$$\frac{d+p}{d-p} = \frac{32+2}{32-2} \tag{14}$$

$$=\frac{17}{15}$$
 (15)

(16)

(17)

(18)

(19)

(20)

(21)

p = ab

p = -18

q = cd

q = 288

 $\frac{q+p}{q-p} = \frac{288-18}{288+18}$

 $x_1(n) \longleftrightarrow X(z)$