1.1.8.25

EE24BTECH11024 - G.Abhimanyu Koushik

Question:

Find a point on the Y axis which is equidistant from the points $A \begin{pmatrix} 6 \\ 5 \end{pmatrix}$ and $B \begin{pmatrix} -4 \\ 3 \end{pmatrix}$. **Solution:**

Symbol	Value	Description
A	$\binom{6}{5}$	First point
В	$\begin{pmatrix} -4 \\ 3 \end{pmatrix}$	Second point
Y	$\begin{pmatrix} 0 \\ y \end{pmatrix}$	Point on Y-Axis equidistant from A and B

TABLE 0: Variables Used

$$\|\mathbf{A} - \mathbf{Y}\|^2 = \|\mathbf{B} - \mathbf{Y}\|^2 \tag{0.1}$$

$$(\mathbf{A} - \mathbf{Y})^{\top} (\mathbf{A} - \mathbf{Y}) = (\mathbf{B} - \mathbf{Y})^{\top} (\mathbf{B} - \mathbf{Y})$$
(0.2)

$$\left(\mathbf{A}^{\mathsf{T}}\right)(\mathbf{A}) + \left(\mathbf{Y}^{\mathsf{T}}\right)(\mathbf{Y}) - 2\left(\mathbf{A}^{\mathsf{T}}\right)(\mathbf{Y}) = \left(\mathbf{B}^{\mathsf{T}}\right)(\mathbf{B}) + \left(\mathbf{Y}^{\mathsf{T}}\right)(\mathbf{Y}) - 2\left(\mathbf{B}^{\mathsf{T}}\right)(\mathbf{Y}) \tag{0.3}$$

$$\mathbf{A}^{\mathsf{T}}\mathbf{A} - \mathbf{B}^{\mathsf{T}}\mathbf{B} = 2\left(\mathbf{A}^{\mathsf{T}} - \mathbf{B}^{\mathsf{T}}\right)(\mathbf{Y}) \tag{0.4}$$

$$36 + 25 - (16 + 9) = 2 \begin{pmatrix} 10 & 2 \end{pmatrix} \begin{pmatrix} 0 \\ y \end{pmatrix}$$
 (0.6)

$$y = 9 \tag{0.7}$$

The point on the Y axis which is equidistant to **A** and **B** is $\begin{pmatrix} 0 \\ 9 \end{pmatrix}$

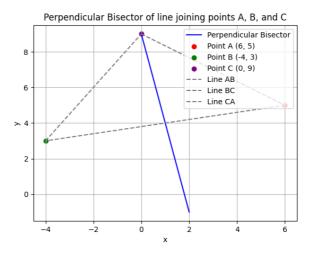


Fig. 0.1: Plot of the given points and the bisector