## 1.1.8.25

## EE24BTECH11024 - G.Abhimanyu Koushik

## Question:

Find a point on the Y axis which is equidistant from the points  $A \begin{pmatrix} 6 \\ 5 \end{pmatrix}$  and  $B \begin{pmatrix} -4 \\ 3 \end{pmatrix}$ . **Solution:** 

Symbol	Value	Description
A	$\binom{6}{5}$	First point
В	$\begin{pmatrix} -4 \\ 3 \end{pmatrix}$	Second point
Y	$\begin{pmatrix} 0 \\ y \end{pmatrix}$	Point on Y-Axis equidistant from A and B

TABLE 0: Variables Used

$$\|\mathbf{A} - \mathbf{Y}\|^2 = \|\mathbf{B} - \mathbf{Y}\|^2 \tag{0.1}$$

$$\|\mathbf{A}\|^2 + \|\mathbf{Y}\|^2 - 2(\mathbf{A}^\top)(\mathbf{Y}) = \|\mathbf{B}\|^2 + \|\mathbf{Y}\|^2 - 2(\mathbf{B}^\top)(\mathbf{Y})$$
 (0.2)

$$\|\mathbf{A}\|^2 - \|\mathbf{B}\|^2 = 2\left(\mathbf{A}^{\mathsf{T}} - \mathbf{B}^{\mathsf{T}}\right)(\mathbf{Y}) \tag{0.3}$$

$$\mathbf{A}^{\mathsf{T}}\mathbf{A} - \mathbf{B}^{\mathsf{T}}\mathbf{B} = 2(\mathbf{A}^{\mathsf{T}} - \mathbf{B}^{\mathsf{T}})(\mathbf{Y}) \tag{0.4}$$

$$\begin{pmatrix} 6 & 5 \end{pmatrix} \begin{pmatrix} 6 \\ 5 \end{pmatrix} - \begin{pmatrix} -4 & 3 \end{pmatrix} \begin{pmatrix} -4 \\ 3 \end{pmatrix} = 2 \begin{pmatrix} 6 & 5 \end{pmatrix} - \begin{pmatrix} -4 & 3 \end{pmatrix} \begin{pmatrix} 0 \\ y \end{pmatrix} \tag{0.5}$$

$$36 + 25 - (16 + 9) = 2 \begin{pmatrix} 10 & 2 \end{pmatrix} \begin{pmatrix} 0 \\ y \end{pmatrix}$$
 (0.6)

$$y = 9 \tag{0.7}$$

The point on the Y axis which is equidistant to **A** and **B** is  $\begin{pmatrix} 0 \\ 9 \end{pmatrix}$ 

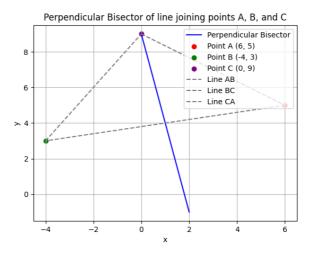


Fig. 0.1: Plot of the given points and the bisector