**WEEK:: 14** 





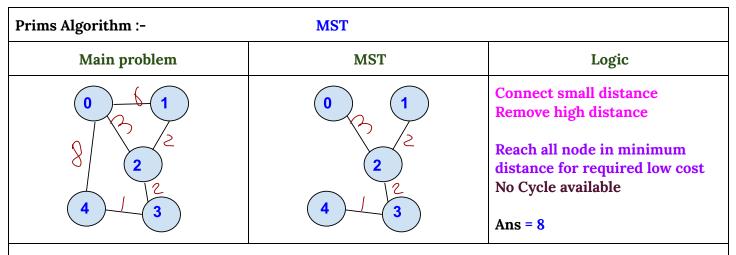
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WEEK :: 14 DAY: 01 DATE: 25-07-2023

### PRIMS AND KRUSKAL ALGORITHM



Queue = {weight,Node} q = {0, 0} = {6,1}, {3,2}, {8,4} take {3,2} = {6,1}, {2,3}, {8,4}, {2,1} take {2,3} = {6,1}, {1,4}, {8,4}, {2,1} take {1,4} = {6,1}, {8,4}, {2,1} take {2,1}

[we can stop because all node visited]

# Weight = 0 1 2 3 4

U	ı	Z	3	4
max	max	max	max	max
0	6	3	max	8
0	2	3	2	8
0	2	3	2	1

Parent:					
1	2	3	4		
-1	-1	-1	-1		
0	0	-1	0		
2	0	2	0		
2	0	2	3		
	1 -1 0 2	1 2 -1 -1 0 0 2 0	1 2 3 -1 -1 -1 0 0 -1 2 0 2		

Visited 0	a: 1	2	3	4
0	0	0	0	0
1	0	0	0	0
1	0	1	0	0
1	0	1	1	0
1	0	1	1	1
1	1	1	1	1

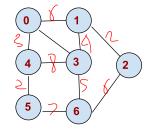
### **Minimum Spanning Tree**

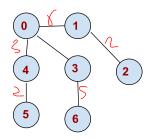
```
<< GeeksforGeeks >>
```

```
class Solution
{
public:
    int spanningTree(int V, vector<vector<int>> adj[])
    {
```

```
//weight
        vector<int> weight(V, INT MAX);
        //Parent
        vector<int> parent(V, -1);
        //visited
        vector<bool> visited(V, 0);
        int count=0, cost = 0;
        //count of vertex
        priority_queue<pair<int, int>, vector<pair<int, int>>, greater<pair<int,</pre>
int>>> q;
        q.push({0, 0}); // path , Node
        int node, path, adjNode, adjPath;
        while (!q.empty())
        {
            path = q.top().first;
            node = q.top().second;
            q.pop();
            //If node is already visited, skep the step
            if (visited[node]==1)
                continue;
            //node is not visited yet
            visited[node] = 1;
            // look at Adjacent Node
            for (int i = 0; i < adj[node].size(); i++)</pre>
                int adjNode = adj[node][i][0];
                int adjPath = adj[node][i][1];
                if (!visited[adjNode] && adjPath < weight[adjNode])</pre>
                 {
                     q.push({adjPath, adjNode});
                    parent[adjNode] = node;
                     weight[adjNode] = adjPath;
                 }
            }
        }
        for (int i = 1; i < V; i++)</pre>
            cost += weight[i];
        return cost;
    }
};
```

### KRUSKAL ALGORITHM





- 1. Connect all small edges
- 2. If there is no small edge between two nodes, then it is connected.
- 3. No Cycle create

### Create edge - Disconnected edge

### Rank

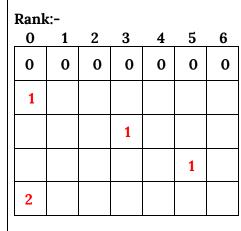
Edge :- (0,1); (1,2); (3,4); (6,5); (2,3); (1,5);

Find Parent:

Node 1 = Pv; Node2 = Pu
rank[Pv] = rank[Pu]
rank[Pv]++;
parent[Pv]=Pu;

rank[Pv] > rank[Pu]
parent[Pu] = Pv;

rank[Pv] < rank[Pu]
parent[Pv]=Pu;</pre>



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rai ciit						
0	1	2	3	4	5	6
0	1	2	3	4	5	6
	0					
		0				
				3		
						5
			0		0	

Pu=0; Pv=1; rank(0,0)



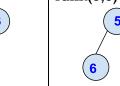
Pu=0;Pv=0 rank(0,0)



Pu=3;Pv=4 rank(0,0)



Pu=5;Pv=6 rank(0,0)

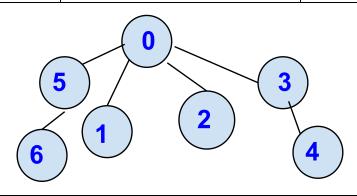


(2,3)-parent different



(0,5)-parent different





```
class Solution {
public:
    int findPar(int u, vector<int> &parent) {
        if (u == parent[u])
            return u;
        return parent[u] = findPar(parent[u], parent);
    }
   bool unionSet(int u, int v, vector<int> &rank, vector<int> &parent) {
        int pu = findPar(u, parent);
        int pv = findPar(v, parent);
        if (pu == pv)
            return true; // already connected
        if (rank[pu] == rank[pv]) {
            rank[pu]++;
            parent[pv] = pu;
        } else if (rank[pu] < rank[pv]) {</pre>
            parent[pu] = pv;
        } else {
            parent[pv] = pu;
        return false;
    }
    int spanningTree(int V, vector<vector<int>> adj[])
        vector<int> parent(V);
        vector<int> rank(V, 0);
        for (int i = 0; i < V; i++)</pre>
            parent[i] = i;
        // min heap, insert every edge
        priority_queue<pair<int, int>, int>, vector<pair<int, int>, int>>,
greater<pair<int, int>,int>>> q;
        int u, v, w;
        for (int i = 0; i < V; i++)</pre>
            for (int j = 0; j < adj[i].size(); j++) {</pre>
                u = i;
                v = adj[i][j][0];
                w = adj[i][j][1];
                q.push({ {w, u}, v });
        int count edges = 0, cost = 0;
        while (!q.empty()) {
            if (count edges == V - 1)
                break;
            w = q.top().first.first;
            u = q.top().first.second;
            v = q. top().second;
            q.pop();
```

WEEK :: 14 DAY: 02 DATE: 26-07-2023

### STRONGLY CONNECTED COMPONENT + BELLMAN FORD

```
Bridge edge in a graph
                                             << GeeksforGeeks >>
class Solution
public:
    bool DFS(int node, int target, vector<int> adj[], vector<bool> &visited)
        if (node == target)
            return 1;
        visited[node] = 1;
        for (int i = 0; i < adj[node].size(); i++)</pre>
        {
            if (!visited[adj[node][i]])
                 if (DFS(adj[node][i], target, adj, visited))
                     return 1;
        }
        return 0;
    }
    //Function to find if the given edge is a bridge in graph.
    int isBridge(int V, vector<int> adj[], int c, int d)
    {
        // Update the adjacency list to remove the edge (c, d)
        for (int i = 0; i < adj[c].size(); i++)</pre>
            if (adj[c][i] == d)
                 adj[c][i]=c;
                break;
            }
        }
        for (int i = 0; i < adj[d].size(); i++)</pre>
```

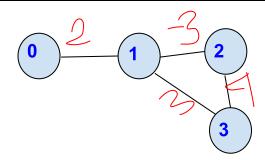
```
{
    if (adj[d][i] == c)
    {
        adj[d][i]=d;
        break;
    }
}

vector<bool> visited(V, 0);
// 0: Target node not found, the edge is a bridge
// 1: Target node found, the edge is not a bridge
return !DFS(c, d, adj, visited);
}
};
```

```
Strongly Connected Components (Kosaraju's Algo)
                                                  << GeeksforGeeks >>
class Solution
public:
    void DFS(int node, vector<vector<int>> &adj, stack<int> &s, vector<bool>
&visited)
    {
        visited[node] = 1;
        for (int i = 0; i < adj[node].size(); i++)</pre>
        {
            if (!visited[adj[node][i]])
                DFS(adj[node][i], adj, s, visited);
        s.push(node);
    }
    void SCC(int node, vector<bool> &visited, vector<vector<int>> &adj)
        visited[node] = true;
        for (int i = 0; i < adj[node].size(); i++)</pre>
            if (!visited[adj[node][i]])
                SCC(adj[node][i], visited, adj);
        }
    }
    //Function to find the number of strongly connected components in the graph.
    int kosaraju(int V, vector<vector<int>>& adj)
    {
        // Modified Topological sort
        stack<int> s;
        vector<bool> visited(V, false);
        for (int i = 0; i < V; i++)
            if (!visited[i])
                DFS(i, adj, s, visited);
        }
        // Transpose the graph, reverse the edge
        vector<vector<int>> trans(V);
        for (int i = 0; i < V; i++)
```

```
{
            for (int j = 0; j < adj[i].size(); j++)</pre>
                 trans[adj[i][j]].push_back(i);
             }
        }
        int count = 0;
        for (int i = 0; i < V; i++)</pre>
            visited[i] = 0;
        while (!s.empty())
             // stack top element is not visited, count++
            if (!visited[s.top()])
                 count++;
                 SCC(s.top(), visited, trans);
             s.pop();
        return count;
    }
};
```

### **BELLMAN FORD ALGORITHM**



# dist [V] = min(dist[v], dist[v]+w) u v w 2 -> 3 4 Edges = 4 1 -> 3 3 operation = (4-1)=3 0 -> 1 2 1 -> 2 -3

### Distance from 0 to node

0	1	2	3
0	max	max	max
	2	-1	
			3
0	2	-1	3

# 1st:2 ->3 =4; 0 -> 2 -> 3 = max, max +4; 1 ->3 =3; 0 -> 1 -> 3 = max, max +3; 0 ->1 =2; 0 -> 0 -> 1 = 0, 2; 1 ->2 =-3; 0 -> 1 -> 2 = 2, -1; 2nd:2 ->3 =4; 0 -> 2 -> 3 = -1, 3; 1 ->3 =3; 0 -> 1 -> 3 = 2, 5; 0 ->1 =2; 0 -> 0 -> 1 = 0, 2;

```
1->2=-3; 0->1-> 2=2, -1;

3rd-

2->3=4; 0->2->3=-1, 3;

1->3=3; 0->1->3=2, 5;

0->1=2; 0->0->1=0, 2;

1->2=-3; 0->1->2=2, -1;
```

### **Limitation of BELLMAN FORD**

- 1. Not work in negative cycle
- 2. Not work in negative edge of undirected graph

# LEARN DSA WITH C++

WEEK :: 14 DAY: 03 DATE: 27-07-2023

### **BELLMAN FORD + FLOYD WARSHAL**

### Distance from the Source (Bellman-Ford Algorithm) << <u>GeeksforGeeks</u> >>

```
class Solution {
 public:
    /* Function to implement Bellman Ford
      edges: vector of vectors which represents the graph
      S: source vertex to start traversing graph with
      V: number of vertices
    */
    void Bellmon(vector<vector<int>> &edges, vector<int> &dist)
        for(int i=0; i<edges.size(); i++)</pre>
            dist[edges[i][1]] = min(dist[edges[i][1]], dist[edges[i][0]] +
edges[i][2]);
        }
    vector<int> bellman ford(int V, vector<vector<int>>& edges, int S) {
        // Code here
        vector<int>dist(V,1e8);
        dist[S]=0;
        for(int i=0; i<V-1; i++)</pre>
            Bellmon(edges, dist);
        // Nagetive Cycle
```

```
vector<int>ans(V);
        for(int i =0; i<V; i++)</pre>
        ans[i]=dist[i];
        Bellmon (edges, dist);
        for(int i=0; i<V; i++)</pre>
            if(ans[i] != dist[i])
                vector<int>temp;
                temp.push back(-1);
                return temp;
        }
        return dist;
    }
};
class Solution {
public:
    /* Function to implement Bellman Ford
        edges: vector of vectors which represents the graph
        dist: vector to store the shortest distances from the source vertex
    */
    bool Bellman(vector<vector<int>>& edges, vector<int>& dist)
        bool count = false;
        for (int i = 0; i < edges.size(); i++)</pre>
            if (dist[edges[i][1]] > dist[edges[i][0]] + edges[i][2])
                dist[edges[i][1]] = dist[edges[i][0]] + edges[i][2];
                count = true; // Set 'count' to true when a relaxation is made
            }
        return count;
    vector<int> bellman ford(int V, vector<vector<int>>& edges, int S)
        vector<int> dist(V, 1e8);
        dist[S] = 0;
        // Relax edges (V-1) times to find the shortest paths
        for (int i = 0; i < V - 1; i++)
            if (!Bellman(edges, dist))
                return dist; // No relaxation in this iteration, return early
        }
        // Check for negative cycles after (V-1) iterations
        if (Bellman(edges, dist))
            vector < int > temp = \{-1\};
            return temp; // Negative cycle detected
        return dist;
    }
};
```

WEEK :: 14 DAY: 04 DATE: 28-07-2023

### **GRAPH ADVANCE EULER**

```
Floyd Warshall
                                 << GeeksforGeeks >>
class Solution {
  public:
      void shortest distance(vector<vector<int>>&matrix) {
           // Code here
           int n= matrix.size();
           for(int i=0; i<n; i++)</pre>
           for(int j=0; j<n; j++)</pre>
           if (matrix[i][j] ==-1)
          matrix[i][j] = 1e9;
           for (int k=0; k<n; k++)</pre>
           for(int i=0; i<n; i++)</pre>
           for(int j=0;j<n; j++)</pre>
               matrix[i][j] = min(matrix[i][j], matrix[i][k] + matrix[k][j]);
           for(int i=0; i<n; i++)</pre>
           for(int j=0; j<n; j++)</pre>
           if (matrix[i][j] ==1e9)
           matrix[i][j] =-1;
      }
};
```

### **Euler Circuit in an Undirected Graph**

<< GeeksforGeeks >>

```
class Solution {
public:
void DFS(int node, vector<int>adj[], vector<bool> &visited)
   visited[node] = 1;
        for (int i = 0; i < adj[node].size(); i++)</pre>
        {
            if (!visited[adj[node][i]])
                DFS(adj[node][i], adj, visited);
        }
}
     bool isEularCircuitExist(int V, vector<int>adj[])
          // Code here
          vector<int> degree(V, 0);
        for (int i = 0; i < V; i++)</pre>
            degree[i] = adj[i].size();
        int node = -1;
```

```
for (int i = 0; i < V; i++) {</pre>
             if (degree[i]) {
                 node = i;
                 break;
             }
        }
        if (node == -1)
             return 1;
        // Check if degree is even or odd
        for (int i = 0; i < V; i++) {</pre>
             if (degree[i] % 2)
                 return 0;
        }
        // Traverse the whole circuit
        vector<bool> visited(V, 0);
        DFS(node, adj, visited);
        // Node is not visited and degree of node is exist
        for (int i = 0; i < V; i++) {</pre>
            if (!visited[i] && degree[i])
                 return 0;
        }
        return 1;
    }
};
```

### Circle of strings

### << <u>Geeksforgeeks</u> >>

```
class Solution
    public:
    void DFS(int node, vector<int>adj[], vector<bool> &visited)
        visited[node]=1;
        for(int i=0; i<adj[node].size(); i++)</pre>
            if(!visited[adj[node][i]])
            DFS(adj[node][i], adj, visited);
        }
    int isCircle(int N, vector<string> A)
        // code here
        vector<int>adj[26];
        vector<int>in(26,0);
        vector<int>out(26, 0);
        string s;
        for(int i=0; i<N; i++)</pre>
            s = A[i];
            adj[s[0]-'a'].push back(s[s.size()-1]-'a');
            out[s[s.size()-1] -'a']++;
            in[s[0]-'a']++;
```

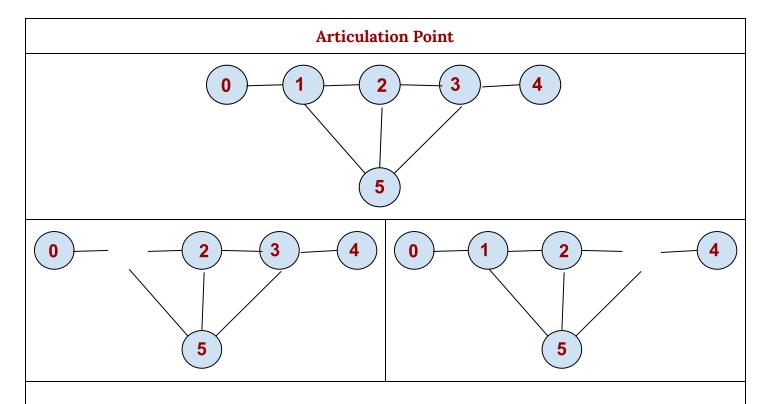
```
}
         int node =-1;
         for(int i=0; i<26; i++)</pre>
             if(in[i] != out[i])
             return 0;
             if(in[i])
             node = i;
         }
        vector<bool>visited(26,0);
        DFS(node, adj, visited);
         for(int i=0; i<26; i++)</pre>
             if(in[i] && !visited[i])
             return 0;
        return 1;
    }
};
```

WEEK :: 14 DAY: 05 DATE: 31-07-2023

### **ARTICULATION POINT**

```
Critical Connections
                                  << GeeksforGeeks >>
class Solution {
public:
int DFS(int node, vector<int> adj[], vector<int> &disc, vector<int> &low,
vector<vector<int>>> &bridge, int timer, int parent)
{
    if(disc[node] != -1)
    return disc[node];
    timer++;
    disc[node] = low[node] = timer;
    for(int i=0; i<adj[node].size(); i++)</pre>
        int neighbour = adj[node][i];
        if(neighbour == parent)
        continue;
        low[node] = min(low[node], DFS(neighbour, adj, disc, low, bridge, timer,
node));
```

```
// Bridge condition
        if(low[neighbour] > disc[node])
            if(node > neighbour)
            bridge.push_back({neighbour, node});
            bridge.push back({node, neighbour});
        }
    }
    return low[node];
};
     vector<vector<int>>criticalConnections(int V, vector<int> adj[]) {
         // Code here
         vector<vector<int>>bridge;
         vector<int>disc(V, -1);
         vector<int>low(V, -1);
         int timer =-1, parent =-1;
         DFS(0, adj, disc, low, bridge, timer, parent);
          sort(bridge.begin(), bridge.end());
         return bridge;
      }
};
```



Node 1 & 3 is an Articulation Point because if we remove them, the tree is disconnected.