

# Assignment-3

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**Q1. If the initial and final states are as below, find the value of the Heuristic function, by taking**

- (i) Euclidean Distance**
- (ii) Manhattan Distance**
- (iii) Minkowski Distance**

**A1.**

```
import sys

import copy

import math

import numpy as

np

def find_pos(s, elem):

    for i in range(len(s)):

        for j in range(len(s[0])):

            if s[i][j] == elem:

                return [i, j]
```

```
def euclidian(s, g):  
  
    res_mat = np.zeros(len(s) * len(s[0]), dtype=float)  
  
    res_mat = res_mat.reshape(len(s), len(s))  
  
    for x1 in range(len(s)):  
        for y1 in range(len(s[0])):  
            elem = s[x1][y1]  
            pos = find_pos(g, elem)  
  
            x2 = pos[0]  
            y2 = pos[1]  
  
            res_mat[x1][y1] = math.sqrt((x2 - x1) ** 2 + (y2 - y1) ** 2)  
  
    summ = 0  
  
    for i in range(len(res_mat)):  
        summ += sum(res_mat[i])  
  
    return summ  
  
def manhattan(s, g):
```

```

res_mat = np.zeros(len(s) * len(s[0]), dtype=float)

res_mat = res_mat.reshape(len(s), len(s))


for x1 in range(len(s)):
    for y1 in range(len(s[0])):
        elem = s[x1][y1]

        pos = find_pos(g, elem)

        x2 = pos[0]
        y2 = pos[1]

        res_mat[x1][y1] = abs(x2 - x1) + abs(y2 - y1)


summ = 0


for i in range(len(res_mat)):
    summ += sum(res_mat[i])

return summ


def minkowski(s, g, p):
    res_mat = np.zeros(len(s) * len(s[0]), dtype=float)

    res_mat = res_mat.reshape(len(s), len(s))

```

```

for x1 in range(len(s)):

    for y1 in range(len(s[0])):

        elem = s[x1][y1]

        pos = find_pos(g, elem)

        x2 = pos[0]

        y2 = pos[1]

        res_mat[x1][y1] = ((abs(x2 - x1) ** p) + (abs(y2 - y1) ** p)) **
(1. / p)

    summ = 0

    for i in range(len(res_mat)):

        summ += sum(res_mat[i])

    return summ

def main():

    p_val = 3

    s0 = [[2, 0, 3], [1, 8, 4], [7, 6, 5]]

    g = [[1, 2, 3], [8, 4, 0], [7, 6, 5]]

    euc = euclidian(s0, g)

    man = manhattan(s0, g)

    mink = minkowski(s0, g, p_val)

```

```
print(euc, man, mink)

if __name__ == "__main__":
    main()
```

```
C:\Python\python.exe "D:/College Work/AI/Labs/Pycharm/lab3/q1.py"
5.414213562373095 6.0 5.259921049894873

Process finished with exit code 0
|
```

**Q2. If the initial and final states are as below and  $H(n)$ : number of misplaced tiles in the current state  $n$  as compared to the goal node need to be considered as the heuristic function. You need to use best first Search algorithm.**

**A2.**

```
import sys

import copy

q = []

visited = []

def compare(s, g):
```

```
if s == g:

    return (1)

else:

    return (0)


def find_pos(s):

    for i in range(3):

        for j in range(3):

            if s[i][j] == 0:

                return ([i, j])


def up(s, pos):

    i = pos[0]

    j = pos[1]

    if i > 0:

        temp = copy.deepcopy(s)

        temp[i][j] = temp[i - 1][j]

        temp[i - 1][j] = 0

        return (temp)

    else:

        return (s)
```

```
def down(s, pos):  
  
    i = pos[0]  
  
    j = pos[1]  
  
    if i < 2:  
  
        temp = copy.deepcopy(s)  
  
        temp[i][j] = temp[i + 1][j]  
  
        temp[i + 1][j] = 0  
  
        return (temp)  
  
    else:  
  
        return (s)
```

```
def right(s, pos):  
  
    i = pos[0]  
  
    j = pos[1]  
  
    if j < 2:  
  
        temp = copy.deepcopy(s)  
  
        temp[i][j] = temp[i][j + 1]  
  
        temp[i][j + 1] = 0  
  
        return (temp)
```

```
    else:
        return (s)

def left(s, pos):
    i = pos[0]
    j = pos[1]

    if j > 0:
        temp = copy.deepcopy(s)
        temp[i][j] = temp[i][j - 1]
        temp[i][j - 1] = 0
        return (temp)
    else:
        return (s)

def enqueue(s, val):
    global q
    q = q + [(val, s)]

def heuristic(s, g):
    d = 0
```



```
for i in range(3):  
    for j in range(3):  
        if s[i][j] != g[i][j]:  
            d += 1  
  
print(d)  
  
return d
```

```
def dequeue(g):  
    global q  
    global visited  
  
    q.sort()  
  
    visited = visited + [q[0][1]]  
  
    elem = q[0][1]  
    del q[0]  
  
    return (elem)
```

```
def search(s, g):  
    curr_state = copy.deepcopy(s)  
  
    if s == g:  
  
        return
```

```
global visited

while (1):

    pos = find_pos(curr_state)

    new = up(curr_state, pos)

    if new != curr_state:

        if new == g:

            print("found!! The intermediate states are:")

            print(visited + [g])

            return

        else:

            if new not in visited:

                enqueue(new, heuristic(new, g))

    new = down(curr_state, pos)

    if new != curr_state:

        if new == g:

            print("found!! The intermediate states are:")

            print(visited + [g])

            return

        else:
```

```
        if new not in visited:

            enqueue(new, heuristic(new, g))

    new = right(curr_state, pos)

    if new != curr_state:

        if new == g:

            print("found!! The intermediate states are:")

            print(visited + [g])

            return

        else:

            if new not in visited:

                enqueue(new, heuristic(new, g))

    new = left(curr_state, pos)

    if new != curr_state:

        if new == g:

            print("found!! The intermediate states are:")

            print(visited + [g])

            return

        else:

            if new not in visited:

                enqueue(new, heuristic(new, g))
```

```
        if len(q) > 0:

            curr_state = dequeue(g)

        else:

            print("not found")

            return

def main():

    s = [[2, 0, 3], [1, 8, 4], [7, 6, 5]]

    g = [[1, 2, 3], [8, 0, 4], [7, 6, 5]]

    global q

    global visited

    q = q

    visited = visited + [s]

    search(s, g)

if __name__ == "__main__":

    main()
```

```

C:\Python\python.exe "D:/College Work/AI/Labs/Pycharm/Lab3/q2.py"
3
5
3
2
3
Found!! The intermediate states are:
[[[2, 0, 3], [1, 0, 4], [7, 6, 5]], [[0, 2, 3], [1, 8, 4], [7, 6, 5]], [[1, 2, 3], [0, 8, 4], [7, 6, 5]], [[1, 2, 3], [8, 0, 4], [7, 6, 5]]]

Process finished with exit code 0

```

**Q3.If the initial and final states are as below and  $H(n)$ : number of misplaced tiles in the current state  $n$  as compared to the goal node need to be considered as the heuristic function. You need to use Hill Climbing algorithm.**

**A3.**

```

import sys

import copy

curr_min = sys.maxsize

q = []

visited = []

def compare(s, g):

    if s == g:

        return (1)

    else:

        return (0)

```

```
def find_pos(s):  
    for i in range(len(s)):  
        for j in range(len(s[0])):  
            if s[i][j] == 0:  
                return ([i, j])  
  
def up(s, pos):  
    i = pos[0]  
    j = pos[1]  
  
    if i > 0:  
        temp = copy.deepcopy(s)  
        temp[i][j] = temp[i - 1][j]  
        temp[i - 1][j] = 0  
        return (temp)  
    else:  
        return (s)  
  
def down(s, pos):  
    i = pos[0]
```

```
j = pos[1]

if i < 2:

    temp = copy.deepcopy(s)

    temp[i][j] = temp[i + 1][j]

    temp[i + 1][j] = 0

    return (temp)

else:

    return (s)


def right(s, pos):

    i = pos[0]

    j = pos[1]

    if j < 2:

        temp = copy.deepcopy(s)

        temp[i][j] = temp[i][j + 1]

        temp[i][j + 1] = 0

        return (temp)

    else:

        return (s)
```

```
def left(s, pos):  
  
    i = pos[0]  
  
    j = pos[1]  
  
    if j > 0:  
  
        temp = copy.deepcopy(s)  
  
        temp[i][j] = temp[i][j - 1]  
  
        temp[i][j - 1] = 0  
  
        return (temp)  
  
    else:  
  
        return (s)
```

```
def enqueue(s):
```

```
    global q  
  
    q = q + [s]
```

```
def heuristic(s, g):
```

```
    d = 0  
  
    for i in range(len(s)):  
  
        for j in range(len(s[0])):  
  
            if s[i][j] != g[i][j]:  
  
                d += 1
```



```
    return d

def dequeue(g):

    h = []

    global q

    global visited

    global curr_min

    for i in range(len(q)):

        h = h + [heuristic(q[i], g)]

    if min(h) < curr_min:

        curr_min = min(h)

        index = h.index(min(h))

        visited = visited + [q[index]]

    else:

        print("optimal solution found !! The intermediate states are: ")

        print(visited)

        exit()

    elem = q[index]

    q = []

    return (elem)
```

```
def search(s, g):  
    curr_state = copy.deepcopy(s)  
  
    if s == g:  
        return  
  
    global visited  
  
    while (1):  
  
        pos = find_pos(curr_state)  
  
        new = up(curr_state, pos)  
  
        if new != curr_state:  
            if new == g:  
                print("Goal State found !! The intermediate States are :")  
                print(visited + [g])  
                return  
            else:  
                if new not in visited:  
                    enqueue(new)  
  
        new = down(curr_state, pos)
```

```
if new != curr_state:

    if new == g:

        print("Goal State found !! The intermediate States are :")

        print(visited + [g])

        return

    else:

        if new not in visited:

            enqueue(new)

new = right(curr_state, pos)

if new != curr_state:

    if new == g:

        print("Goal State found !! The intermediate States are :")

        print(visited + [g])

        return

    else:

        if new not in visited:

            enqueue(new)

new = left(curr_state, pos)

if new != curr_state:

    if new == g:
```

```

        print("Goal State found !! The intermediate States are :")

        print(visited + [g])

        return

    else:

        if new not in visited:

            enqueue(new)

        if len(q) > 0:

            curr_state = dequeue(g)

        else:

            print("not found")

            return

def main():

    s = [[2, 8, 3], [1, 5, 4], [7, 6, 0]]

    g = [[1, 2, 7], [8, 0, 5], [3, 4, 6]]

    global q

    global visited

    q = q + [s]

    visited = visited + [s]

    search(s, g)

```

```
if __name__ == "__main__":

    main()
```

```
C:\Python\python.exe "D:/College Work/AI/Labs/Pycharm/lab3/q3.py"
optimal solution found !! The intermediate states are:
[[[2, 8, 3], [1, 5, 4], [7, 6, 0]], [[2, 8, 3], [1, 5, 4], [7, 0, 6]], [[2, 8, 3], [1, 0, 4], [7, 5, 6]]]

Process finished with exit code 0
```

**Q4. If the initial and final states are as below and  $H(n)$ : Manhattan distance as the heuristic function. You need to use Best First Search algorithm.**

**A4.**

```
import copy

from heuristic import *

q = []

visited = []

def compare(s, g):

    if s == g:

        return (1)

    else:

        return (0)
```

```
def find_pos(s):  
    for i in range(3):  
        for j in range(3):  
            if s[i][j] == 0:  
                return ([i, j])  
  
def up(s, pos):  
    i = pos[0]  
    j = pos[1]  
  
    if i > 0:  
        temp = copy.deepcopy(s)  
        temp[i][j] = temp[i - 1][j]  
        temp[i - 1][j] = 0  
        return (temp)  
    else:  
        return (s)  
  
def down(s, pos):  
    i = pos[0]
```

```
j = pos[1]

if i < 2:

    temp = copy.deepcopy(s)

    temp[i][j] = temp[i + 1][j]

    temp[i + 1][j] = 0

    return (temp)

else:

    return (s)


def right(s, pos):

    i = pos[0]

    j = pos[1]

    if j < 2:

        temp = copy.deepcopy(s)

        temp[i][j] = temp[i][j + 1]

        temp[i][j + 1] = 0

        return (temp)

    else:

        return (s)
```

```
def left(s, pos):  
  
    i = pos[0]  
  
    j = pos[1]  
  
    if j > 0:  
  
        temp = copy.deepcopy(s)  
  
        temp[i][j] = temp[i][j - 1]  
  
        temp[i][j - 1] = 0  
  
        return (temp)  
  
    else:  
  
        return (s)
```

```
def enqueue(s, val):  
  
    global q  
  
    q = q + [(val, s)]
```

```
def heuristic(s, g):  
  
    d = (s, g)  
  
    print  
  
    d  
  
    # d = 0  
  
    # for i in range(3):
```



```
#         for j in range(3):  
  
#             if s[i][j] != g[i][j]:  
  
#                 d += 1  
  
return d
```

```
def dequeue(g):  
  
    global q  
  
    global visited  
  
    q.sort()  
  
    visited = visited + [q[0][1]]  
  
    elem = q[0][1]  
  
    del q[0]  
  
    return (elem)
```

```
def search(s, g):  
  
    curr_state = copy.deepcopy(s)  
  
    if s == g:  
  
        return  
  
    global visited
```

```
while (1):

    pos = find_pos(curr_state)

    new = up(curr_state, pos)

    if new != curr_state:

        if new == g:

            print("found!! The intermediate states are:")

            print(visited + [g])

            return

        else:

            if new not in visited:

                enqueue(new, heuristic(new, g))

    new = down(curr_state, pos)

    if new != curr_state:

        if new == g:

            print("found!! The intermediate states are:")

            print(visited + [g])

            return

        else:

            if new not in visited:

                enqueue(new, heuristic(new, g))
```

```
new = right(curr_state, pos)

if new != curr_state:

    if new == g:

        print("found!! The intermediate states are:")

        print(visited + [g])

        return

    else:

        if new not in visited:

            enqueue(new, heuristic(new, g))

new = left(curr_state, pos)

if new != curr_state:

    if new == g:

        print("found!! The intermediate states are:")

        print(visited + [g])

        return

    else:

        if new not in visited:

            enqueue(new, heuristic(new, g))

if len(q) > 0:
```

```
        curr_state = dequeue(g)

    else:

        print("not found")

    return


def main():

    s = [[2, 0, 3], [1, 8, 4], [7, 6, 5]]

    g = [[1, 2, 3], [8, 0, 4], [7, 6, 5]]

    global q

    global visited

    q = q

    visited = visited + [s]

    search(s, g)


if __name__ == "__main__":

    main()
```

```
C:\Python\python.exe "D:/College Work/AI/Labs/Pycharm/lab3/q5.py"
found!! The intermediate states are:
[[[2, 0, 3], [1, 8, 4], [7, 6, 5]], [[0, 2, 3], [1, 8, 4], [7, 6, 5]], [[1, 2, 3], [0, 8, 4], [7, 6, 5]], [[1, 2, 3], [8, 0, 4], [7, 6, 5]]]

Process finished with exit code 0
```

**Q5. Solve this given problem using Uniform Cost search. A is the initial state and G is the goal state**

**A5.**

```
def uniform_cost_search(goal, start):

    # minimum cost upto

    # goal state from starting

    global graph, cost

    answer = []

    # create a priority queue

    queue = []

    # set the answer vector to max value

    for i in range(len(goal)):

        answer.append(10 ** 8)

    # insert the starting index

    queue.append([0, start])

    # map to store visited node
```

```
visited = {}

# count

count = 0

# while the queue is not empty
while (len(queue) > 0):

    # get the top element of the
    queue = sorted(queue)

    p = queue[-1]

    # pop the element
    del queue[-1]

    # get the original value
    p[0] *= -1

    # check if the element is part of
    # the goal list
    if (p[1] in goal):

        # get the position
        index = goal.index(p[1])
```

```

        # if a new goal is reached

        if (answer[index] == 10 ** 8):

            count += 1

        # if the cost is less

        if (answer[index] > p[0]):

            answer[index] = p[0]

        # pop the element

        del queue[-1]

        queue = sorted(queue)

        if (count == len(goal)):

            return answer

        # check for the non visited nodes

        # which are adjacent to present node

        if (p[1] not in visited):

            for i in range(len(graph[p[1]])):

                # value is multiplied by -1 so that

                # least priority is at the top

                queue.append([(p[0] + cost[(p[1], graph[p[1]][i])]) * -1,
graph[p[1]][i]])

```

```
        # mark as visited

        visited[p[1]] = 1

    return answer

# main function
if __name__ == '__main__':

    # create the graph

    graph, cost = [[] for i in range(8)], {}

    # add edge

    graph[0].append(1)

    graph[0].append(3)

    graph[3].append(1)

    graph[3].append(6)

    graph[3].append(4)

    graph[1].append(6)

    graph[4].append(2)

    graph[4].append(5)

    graph[2].append(1)

    graph[5].append(2)

    graph[5].append(6)

    graph[6].append(4)
```



```
# add the cost

cost[(0, 1)] = 2

cost[(0, 3)] = 5

cost[(1, 6)] = 1

cost[(3, 1)] = 5

cost[(3, 6)] = 6

cost[(3, 4)] = 2

cost[(2, 1)] = 4

cost[(4, 2)] = 4

cost[(4, 5)] = 3

cost[(5, 2)] = 6

cost[(5, 6)] = 3

cost[(6, 4)] = 7


# goal state

goal = []


# set the goal

# there can be m

goal.append(6)


# get the answer

answer = uniform
```

```
# print the answer
```

```
print("Minimum cost from 0 to 6 is = ", answer[0])
```

```
C:\Python\python.exe "D:/College Work/AI/Labs/Pycharm/lab3/q5.py"
```

```
Minimum cost from 0 to 6 is = 3
```

```
Process finished with exit code 0
```