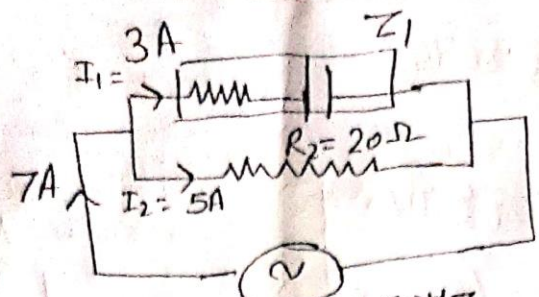


## Electrical Engineering (KEE-101)

### Assignment- Parallel Series parallel & Three phase AC Circuit

Q1. A series combination of R and C is in parallel with  $20\ \Omega$  resistance across  $50\text{ Hz}$  supply. If the total current is  $7\text{ A}$ , Current through  $20\ \Omega$  resistor is  $5\text{ A}$  and current in R-C branch is  $3\text{ A}$ . Find values of R & C.

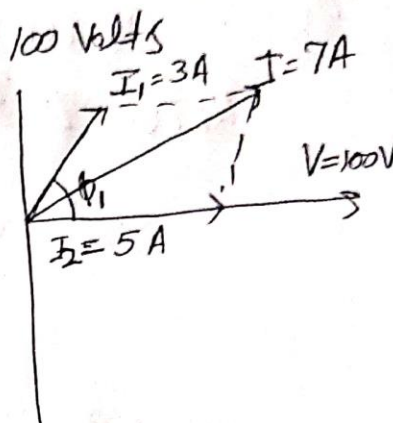
Q1-1



Now Current in Resistive Branch =  $5\text{ A}$ .  
 So Voltage. =  $I_2 \times R_2 = 5 \times 20 = 100\text{ Volts}$

Now As phasor diagram

Now As Net Current is  $7\text{ A}$ . So



$$7 = \sqrt{(5)^2 + (3)^2 + 2 \times 5 \times 3 \cos \phi_1}$$

$$\Rightarrow 49 = 25 + 9 + 30 \cos \phi_1$$

$$\Rightarrow \cos \phi_1 = \frac{15}{30} = 0.5 \Rightarrow \phi_1 = 60^\circ$$

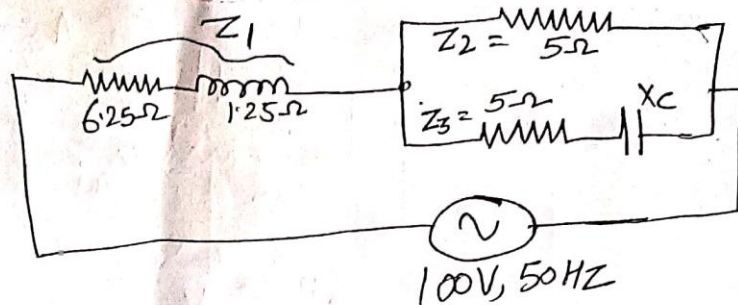
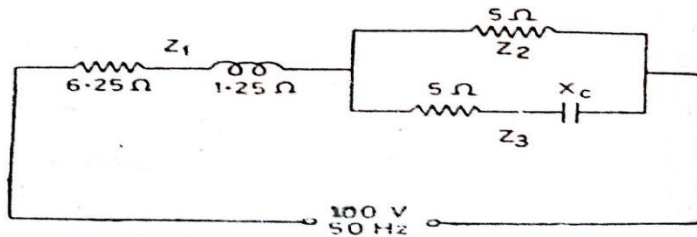
Now  $Z_1 = \frac{V}{I_1} = \frac{100}{3} = 33.33\ \Omega$

Now  $R_1 = Z_1 \cos \phi_1$   
 $= 33.33 \times 0.5$   
 $= 16.666\ \Omega$

$X_C = Z_1 \sin \phi_1$   
 $= 33.33 \times 0.866$   
 $X_C = 28.8674\ \Omega$

$\Rightarrow C = \frac{1}{314 \times 28.8674}$   
 $= \underline{\underline{110.322\ \mu\text{F}}}$

Q2. Find The value of  $X_c$  (Fig. 1) so that total circuit current is in phase with the applied voltage. Also Find the value of circuit current and power consumption



$$Z_1 = 6.25 + 1.25j$$

$$Z_2 = 5 \Omega$$

$$Z_3 = 5 - jX_c$$

Parallel Combination of  $Z_2$  &  $Z_3$  i.e.  $Z_{23} = \frac{5(5 - jX_c)}{10 - jX_c}$

$$Z_{23} = \frac{5(5 - jX_c)}{(10 - jX_c)} \times \frac{(10 + jX_c)}{(10 + jX_c)} = \frac{250 + 5X_c^2 - 25X_cj}{100 + X_c^2} \Omega$$

Total Impedance  $Z_{Total} = Z_1 + Z_{23} =$

$$Z_{Total} = \left[ 6.25 + \frac{250 + 5X_c^2}{100 + X_c^2} \right] + \left[ 1.25 - \frac{25X_c}{100 + X_c^2} \right] j$$

For Current to be in phase with Voltage Reactance should be Zero.

$$\text{i.e. } 1.25 = \frac{25X_c}{100 + X_c^2} \Rightarrow 1.25X_c^2 - 25X_c + 125 = 0$$

$$\text{So } X_c = \frac{25 \pm \sqrt{(-25)^2 - 4 \times 1.25 \times 125}}{2 \times 1.25} = \frac{25 \pm \sqrt{625 - 625}}{2.5}$$

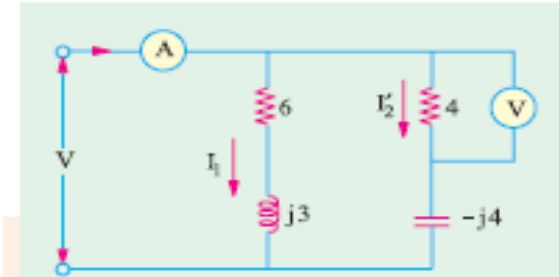
$$\Rightarrow X_c = 10 \Omega$$

When  $X_c = 10 \Omega$  Then  $Z_{Total} = \left[ 6.25 + \frac{250 + 5(10)^2}{100 + (10)^2} \right]$

$$\Rightarrow Z_{Total} = 10 \Omega$$

$$\text{Net Current} = \frac{V}{Z_{Total}} = \frac{100}{10} = 10 \text{ A}$$

Q3. If in fig.2 given values are in ohms and the voltmeter reads 60 V find the reading of ammeter. (Ans- 22.47 A)



**Solution.**  $I_2 = 60/4 = 15$  A. Taking it as reference quantity

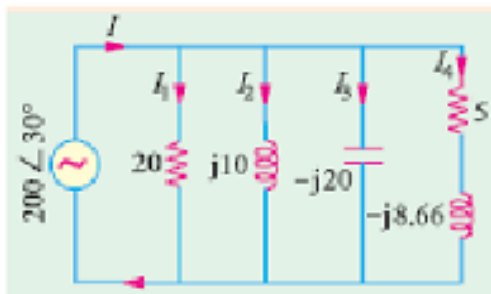
Obviously, the applied voltage is

$$V = 15 \angle 0^\circ \times (4 - j4) = 84.8 \angle 45^\circ$$

$$I_1 = 84.8 \angle 45^\circ / (6 + j3) = 84.8 \angle 45^\circ / 6.7 \angle 26.6^\circ = 12.6 \angle 18.4^\circ = (4 - j12)$$

$$I = I_1 + I_2 = (15 + j0) + (4 - j12) = 19 - j12 = 22.47 \angle 32.3^\circ$$

Q4. Calculate total current and impedance of given four branched circuit.



**Solution.**  $Y_1 = 1/20 = 0.05$  S,  $Y_2 = 1/j10 = -j0.1$  S;

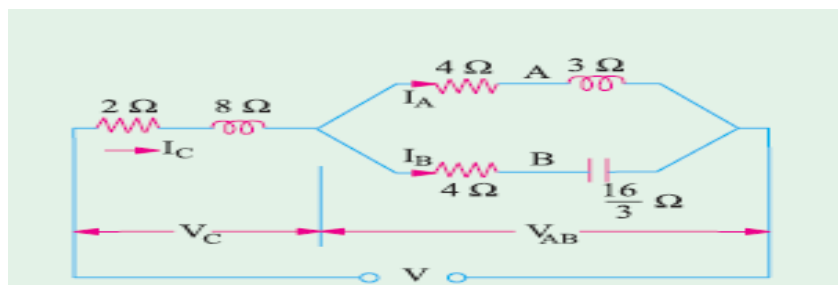
$$Y_3 = 1/-j20 = j0.05 \text{ S}; Y_4 = 1/5 - j8.66 = 1/10 \angle 60^\circ = 0.1 \angle 60^\circ = (0.05 - j0.0866) \text{ S}$$

$$Y = Y_1 + Y_2 + Y_3 + Y_4 = (0.1 - j0.1366) \text{ S} = 0.169 \angle 53.8^\circ \text{ S}$$

$$(i) I = VY = 200 \angle 30^\circ \times 0.169 \angle 53.8^\circ = 33.8 \angle 23.8^\circ \text{ A}$$

$$(ii) Z = 1/Y = 1/0.169 \angle 53.8^\circ = 5.9 \angle 53.8^\circ \Omega$$

Q5. In given series parallel circuit if current  $I_C = 25$ , determine branch currents and power consumption in each branch.





$$Z_A = 4 + 3j = 5 \angle 36.86^\circ, \quad Z_B = 4 - \frac{16}{3}j = 6.664 \angle -53.13^\circ \Omega$$

Parallel Combination.  $Z_A || Z_B$

$$Z_{AB} = \frac{5 \angle 36.86^\circ \times 6.664 \angle -53.13^\circ}{8 - 2.333j} = \frac{5 \angle 36.86^\circ \times 6.664 \angle -53.13^\circ}{8.333 \angle -16.26^\circ}$$

$$Z_{AB} = 3.998 \angle 0.01^\circ \approx 4 \angle 0^\circ \Omega$$

Now Voltage.  $V_{AB} = I_C \cdot Z_{AB} = 100 \angle 0^\circ$

$$\text{Current } I_A = \frac{V_{AB}}{Z_A} = \frac{100 \angle 0^\circ}{5 \angle 36.86^\circ} = 20 \angle -36.86^\circ \text{ A} \quad I_B = \frac{100 \angle 0^\circ}{6.664 \angle -53.13^\circ} = 15 \angle 53.13^\circ$$

$$\text{Power in Branch A} = (20)^2 \times 4 = 1600 \text{ Watt} \quad \text{Power in Branch B} = (15)^2 \times 4 = 900 \text{ Watt}$$

$$\text{Total Impedance of Circuit} = Z_{\text{Total}} = (2 + 8j) + Z_{AB}$$

$$Z_{\text{Total}} = 2 + 8j + 4 + 0j = 6 + 8j = 10 \angle 53.13^\circ \Omega$$

$$\text{Total Voltage } V_{\text{Total}} = I_C \cdot Z_{\text{Total}} = 25 \angle 0^\circ \times 10 \angle 53.13^\circ = 250 \angle 53.13^\circ \text{ Volts}$$

$$Z_C = 2 + 8j = \cancel{8.246 \angle 75.96^\circ} = 8.246 \angle 75.96^\circ \Omega$$

$$\text{So Voltage } V_C = I_C \cdot Z_C = 20.615 \angle 75.96^\circ \text{ Volts}$$

$$\text{Total Power in } Z_C = (25)^2 \times 2 = 1250 \text{ Watt}$$

$$\text{Total Power } P_{\text{Total}} = VI \cos \phi = 250 \times 25 \times \cos 53.13^\circ = 3750 \text{ Watts}$$

$$\text{Also } P_{\text{Total}} = P_A + P_B + P_C = 1600 + 900 + 1250 = 3750 \text{ watt}$$