



Operational Amplifiers Unit - 3

Op-amp :- It is an Analog IC (Integrated circuit)
Whose IC No is (-)

741C
 ↓ ↓ → Commercial
 TTL Logic family
 ↓
 (Transistor-Transistor Logic)

→ Op-amp is composed of 2 words *op* *amp*.

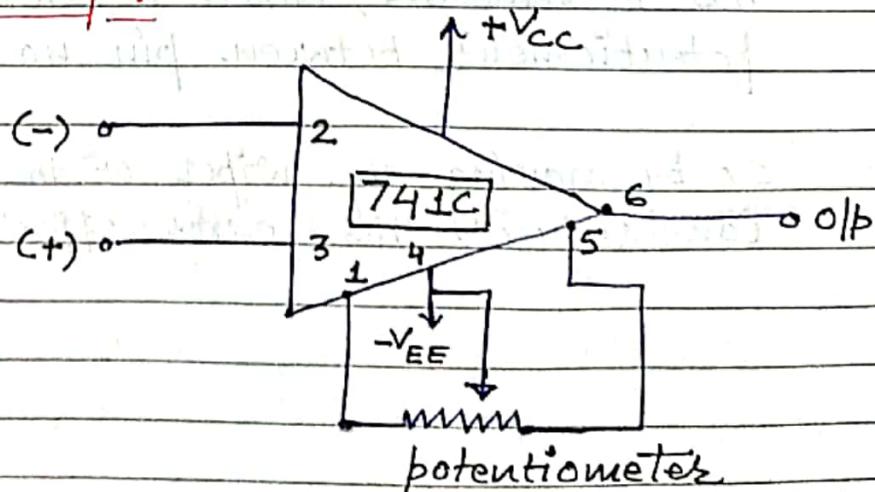
→ Op means operational ; with the help of op-amp

We can perform mathematical operations like addition, subtraction, Integration, log, antilog etc.

→ Amp means Amplifiers ; with the help of op-amp, we

can amplify the signals as well.

Symbol of op-amp :-



Pin Configuration of op-amp :-

Offset Null	1	8	NC (Not Connected)
Inverting Input	2	7	V_{CC}
Non-Inverting Input	3	1 C	Output
$-V_{EE}$	4	5	Offset Null

① Pin No : 1 & 5 :- These are known as offset null pins. Ideally when Input is zero ($V_p = 0$), output should also be zero ($V_o = 0$), but due to fluctuations or spark or short circuiting or atmospheric disturbances, some error output voltage is produced even when Input $V_p = 0$.

This error voltage is called as offset voltage and has to be removed, which is done by placing a potentiometer between pin no 1 and 5.

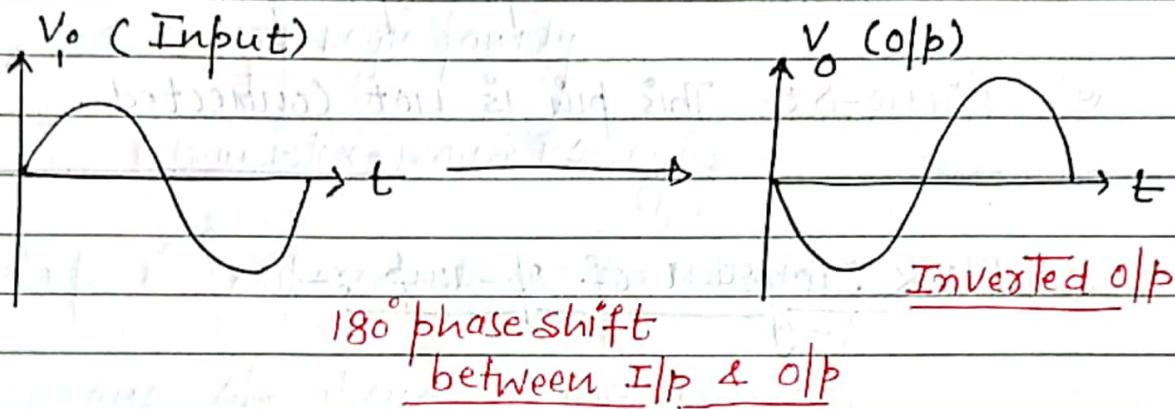
So by moving the wiper of the potentiometer, we can reduce this error offset voltage to zero.



(2) Pin no 2 :- (Inverting Input pin) :-

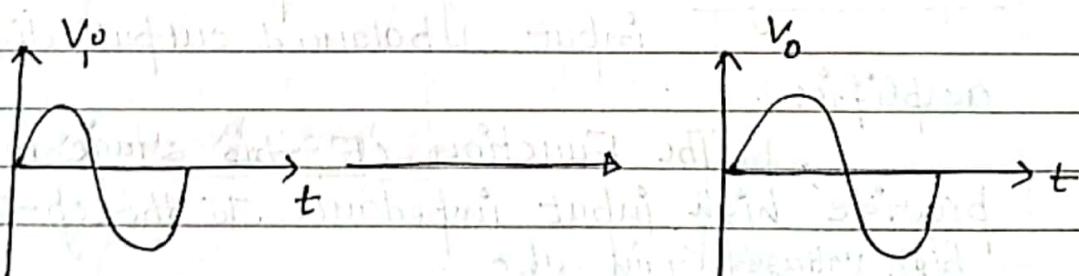
If input is applied at pin no-2, we get

amplified output at pin 6, but there is a phase shift of 180° between input and output.



(3) Pin no 3 :- (Non-Inverting pin) :-

If input is applied at pin no-3, we get amplified o/p at pin no-6 but there is no phase shift between input and o/p. means input and o/p both are in same phase.

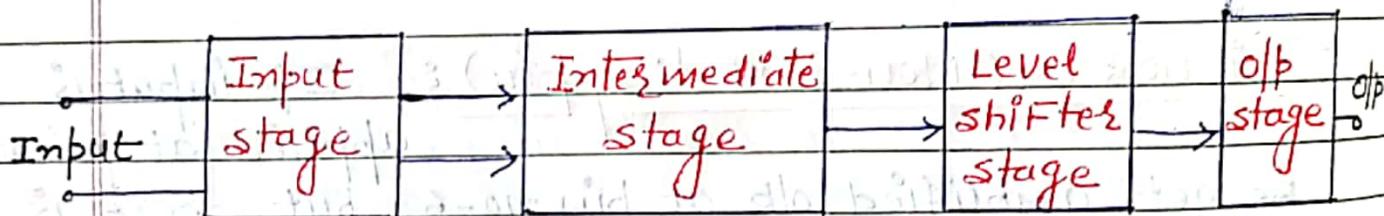


④ Pin no - 4, 7 :- These are the supply pins which are used to supply voltage to op-amp.

⑤ Pin no - 6 :- This pin is used to take the output of the op-amp.

⑥ Pin no - 8 :- This pin is not connected.

* Block Diagram of op-amp :-



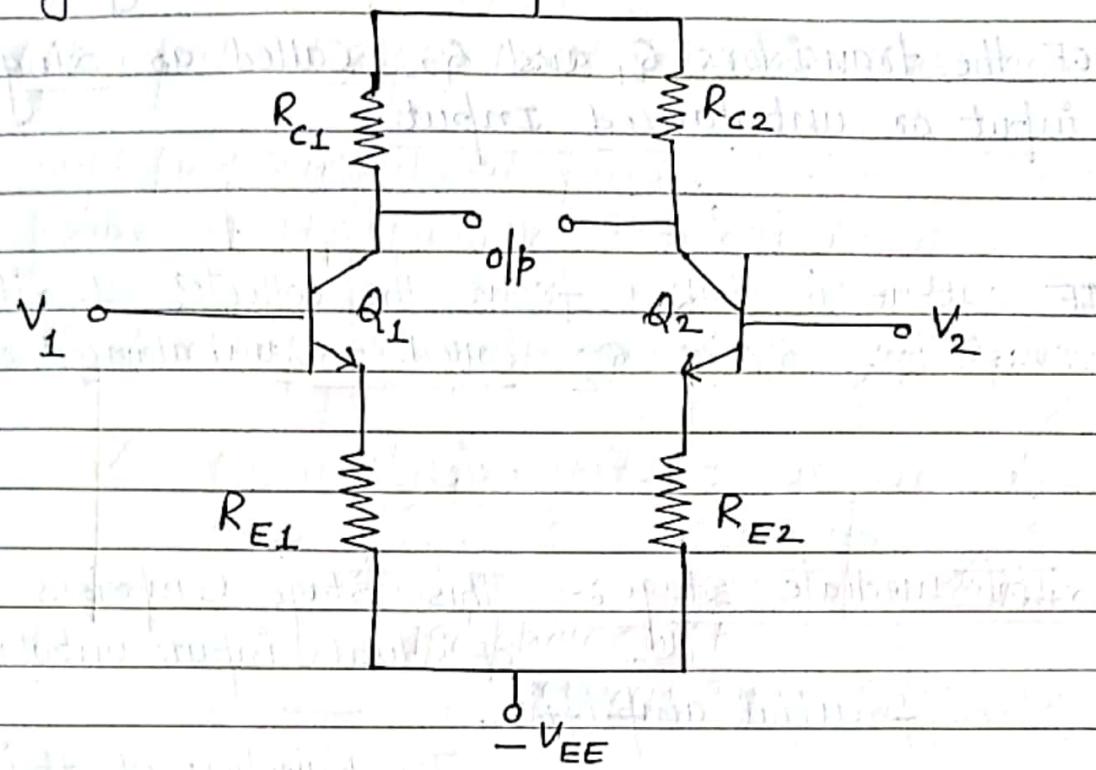
① Input stage :- This stage comprises of dual input balanced output differential amplifiers.

The Function of this stage is to provide high input impedance to the op-amp and high voltage Gain also.

Note :- Differential Amplifiers :- A differential amplifier is a ckt which amplifies only the difference of two input



signals applied.



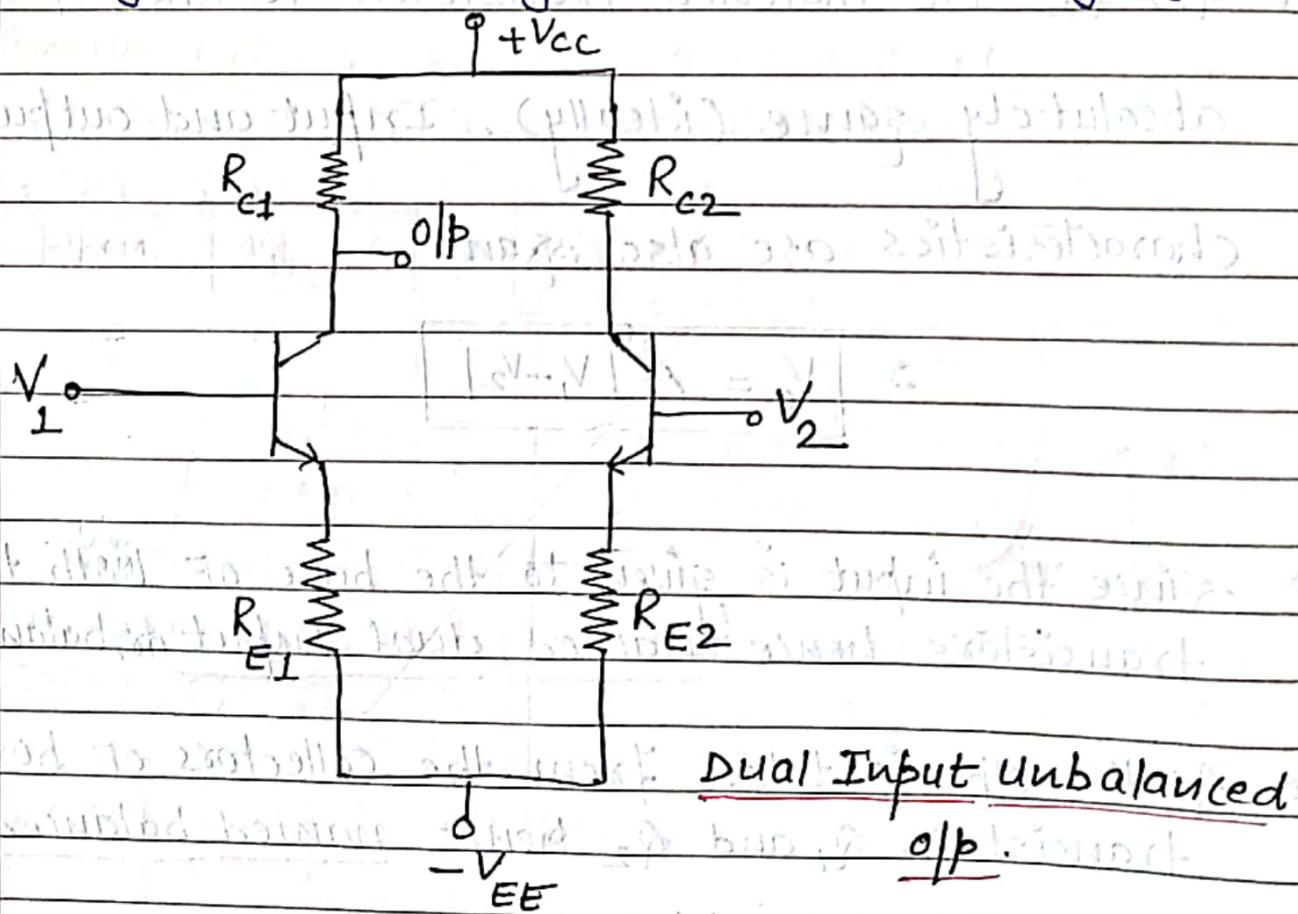
→ Q_1, Q_2 are matched transistors i.e. their β is absolutely same (ideally). Input and output characteristics are also same.

$$\therefore V_o = A |V_1 - V_2|$$

- Since the input is given to the base of both the transistors hence named dual Input or balanced I/p.
- As the o/p is taken from the collectors of both the transistors Q_1 and Q_2 hence named balanced o/p.

- If input is applied to the base of any one of the transistors Q_1 or Q_2 , called as single input or unbalanced input.
 - If output is taken from the collector of either transistors Q_1 or Q_2 , called as unbalanced o/p.
- ② Intermediate stage :- This stage Comprises of dual input unbalanced o/p differential amplifiers.

The Function of this stage for providing rest of the voltage gain.



③ Level shifter :- This stage Comprises of emitter follower. Using Constant Current Source.

IF an unwanted d.c. signal is introduced in the ckt during amplification then the Function of level shifter is to shift that d.c. level to ground either by pushing it or pulling it to ground level.

④ Output stage :- This stage Comprises of Complementary push pull Amplifiers.

The Function of this stage is to provide low output resistance.

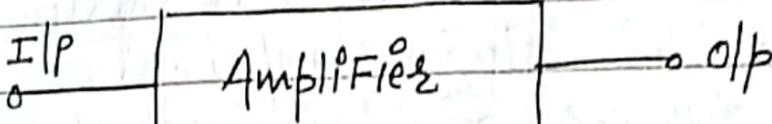
Configuration of op-amp :-

① open Loop configuration :- open Loop Configuration means there is no Feedback between input and output. Practically op-amp is not used in open loop configuration due to -

① Very high Voltage gain which leads to distortion present in amplified output signal.

② Band width is very small.

③ Gain is not Constant and varies with temp and power supply.



NO Feedback Present

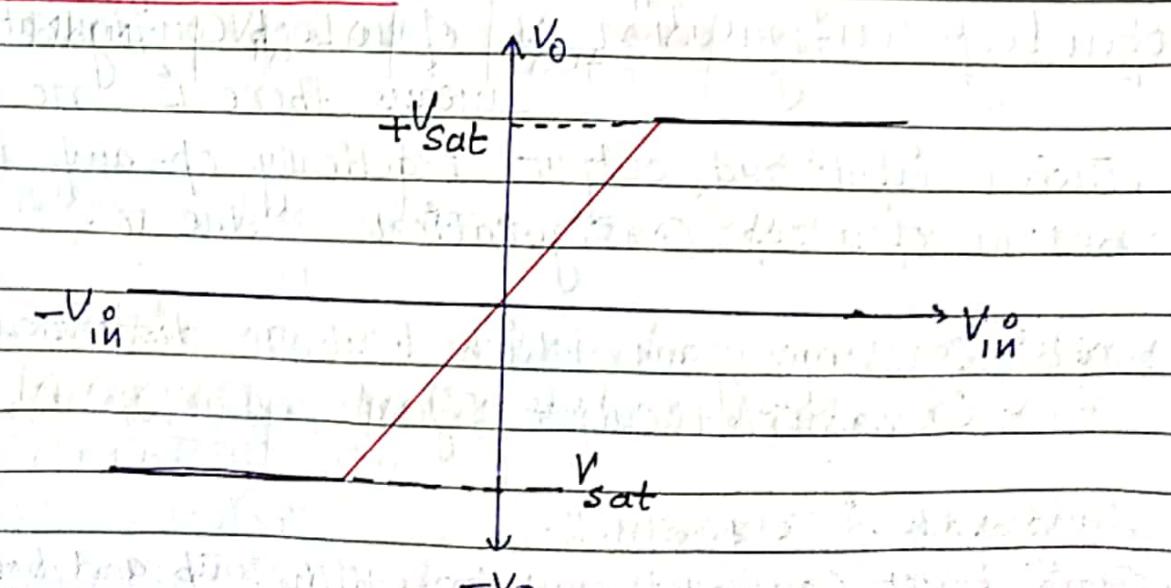
$$V_o = A |V_1 - V_2| \quad \text{where}$$

$A = \text{Open Loop Gain}$

Ideal Voltage Transfer Curve :- The maximum and minimum limit that an op-amp can amplify the input signal is $+V_{sat}$ and $-V_{sat}$.

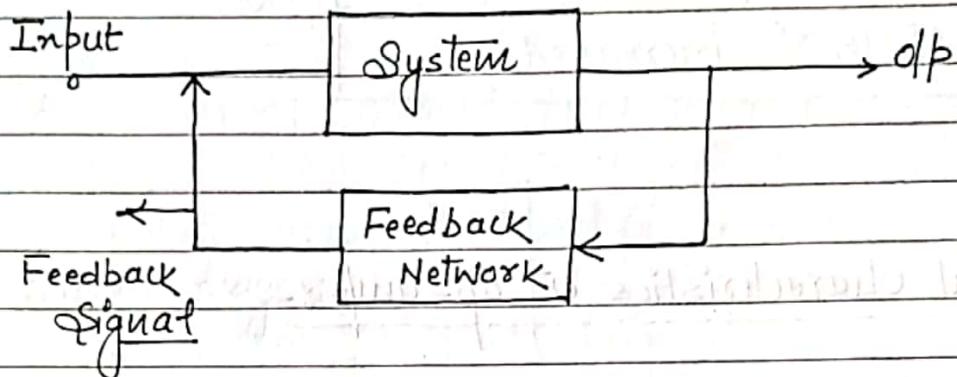
* $+V_{sat}$ & $-V_{sat}$ Values are provided by the manufacturers, which is equal to supply voltages

$+V_{cc}$ and $-V_{ee}$.





- ① Closed Loop Configuration :- In Closed Loop Configuration, Feedback is present between input and o/p.



Types of Feedback :-

- (1) (+ve) Feedback :- (Positive Feedback)

In positive Feedback, input signal and feedback signal are of same phase, this is known as Regenerative Feedback and is used in Oscillators.

- (2) Negative Feedback :- In this, there is a phase shift of 180° between input signal and feedback signal. It is also known as De-generative Feedback. It is Commonly used in Amplifiers.

Advantages of (-ve) Feedback :-

- (1) It reduces and stabilizes Voltage Gain.
- (2) It reduces distortion at op-amp signal.
- (3) Bandwidth is increased.

* Ideal characteristics of op-amp :-

① open Loop Gain $[A = \infty]$:- This characteristic tells that an infinitesimally small input signal can be amplified to such a level that it can be used for practical applications.

② When $V_{in} = 0$, $V_{out} = 0$:-

Ideally when input is zero, op-amp should also be

zero but due to sparks, Fluctuations, atmospheric disturbances, short circuiting, output appears even when Input is zero.

This error voltage is called as offset voltage which can be zero by using



pin no 1 and 5 of op-amp.

(3) Input Resistance $R_i = \infty$:-

This condition should be satisfied so that internal circuit of op-amp should not draw any amount of current from the source and all the current should flow to the output of op-amp to provide high gain and to \rightarrow avoid loading Effect.

(4) Output Resistance, $R_o = 0$:- output resistance

Should be zero so that all the amplified current should be available at the output.

(5) Bandwidth, $BW = \infty$:- Bandwidth is defined as the range of frequencies over which the device gives optimum performance.

\rightarrow This property tells that signal of least frequency to a signal of maximum freq. gets amplified.

(6) Common Mode Rejection Ratio (CMRR) = ∞ :-

It is defined as the ratio of differential gain to the common mode gain.

$$CMRR = \frac{A_d}{A_{CM}}$$

OR

$$CMRR \text{ in } db = 20 \log_{10} \frac{A_d}{A_{CM}}$$

↓
decibels

Where $A_d \rightarrow$ Differential Gain

$A_{CM} \rightarrow$ Common mode Gain

⑦ Slew Rate ; $SR = \infty$:-

Slew Rate is defined as the maximum rate of change of output voltage with respect to time.

$$S.Rate = \frac{\Delta V}{\Delta t} \text{ Volts/usec}$$

* Higher the Value of S.Rate, better will be the performance of op-amp

⑧ Power supply Rejection Ratio :- (PSRR = 0)

It is defined as the ratio of change in input offset voltage to change in supply voltage.

$$PSRR = \frac{\Delta V_o}{\Delta V_{bias}}$$

unit $\mu\text{V}/\text{volt}$

- * It is also known SVRR (Supply Voltage Rejection Ratio). Ideally PSRR should be zero but practically it should be as small as possible.

⑨ Input offset voltage V_{ios} :-

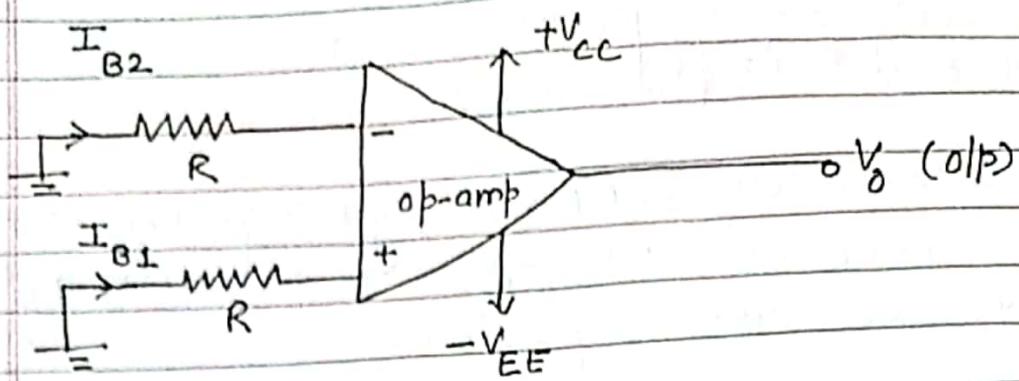
Ideally when $V_{in} = 0$, V_{out} should also be zero, but practically it is not so due to unavoidable unbalances inside the op-amp.

→ So we have to apply a small differential voltage at the input of the op-amp to make op-amp voltage zero, which is called as Input offset voltage.

It is of the order of few mV range.

⑩ Input bias current (I_B) :-

Input bias current I_B is the average of the currents flowing into the two input terminals of the op-amp ie I_{B1} and I_{B2} .



→ Input bias Current $I_B = \frac{I_{B1} + I_{B2}}{2}$

→ Ideally I_{B1} and I_{B2} must be zero but due to finite value of input resistance R , they do exist.

② Input offset Current :- (I_{ios})

The algebraic difference between the currents flowing into the inverting and non-inverting terminals of op-amp is called as Input offset current.

$$I_{ios} = | I_{B1} - I_{B2} |$$

Where I_{B1} = Current flowing into the non-inverting input

I_{B2} = Current flowing into the inverting terminal.

* Ideally, the input offset current must be zero but due to the unequal currents I_{B1} and I_{B2} flowing into the input terminals of the op-amp, input offset current exists.

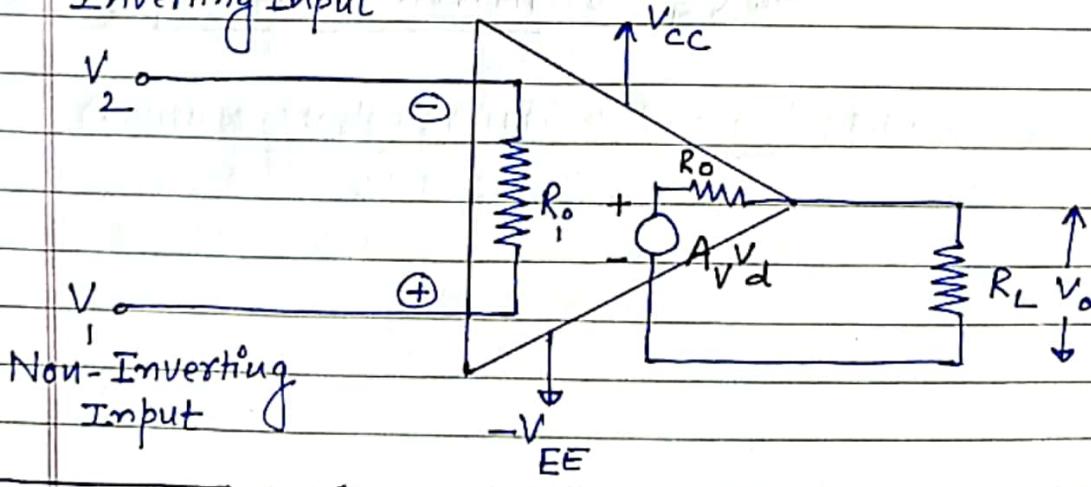
Note:- The input offset current will give rise to a finite output voltage even when the input voltage is zero; that's why input offset current should be reduced to lowest possible value.

Equivalent Ckt of op-amp:-

* R_o \rightarrow o/p Resistance

R_i \rightarrow I/p Resistance.

Inverting Input





Modes of Differential Amp :- op-amp consists

of differential amp. Differential amplifier operates in 2 modes :-

① Differential Mode

② Common mode

→ One of the common features of differential amp is its ability to cancel out or reject certain types of undesired voltage signals. Such undesired signals are referred to as 'NOISE'.

The noise signal appears equally at both inputs of the circuit means that any undesired noise signal which appear in polarity or common to both input terminals will be rejected or cancelled out at the differential amplifier output.

→ In differential Amplifiers, the common signal (noise) to both the inputs V_1 and V_2 will not effect on output.

→ The opamp depends on differential Input V_d ($|V_1 - V_2|$) and the average of two inputs called as Common mode input V_{CM} $\left[\frac{V_1 + V_2}{2} \right]$



① Differential Mode :- In Differential mode, o/p V_o depends on differential input V_d which is multiplied by differential gain A_d .

$$\therefore V_o = V_d A_d$$

Where

$$V_d = |V_1 - V_2|$$

② Common Mode :-

In Common mode, output V_o depends on Common input V_{CM} which is multiplied by A_{CM} (common mode Gain).

$$\therefore V_o = A_{CM} V_{CM}$$

Where

$$V_{CM} = \frac{|V_1 + V_2|}{2}$$

Hence Total Output

$$V_o = A_d V_d + A_{CM} V_{CM}$$

* CMRR can be defined as the ratio of differential gain to the common mode Gain.

$$CMRR = \frac{A_d}{A_{CM}}$$

→ We want to amplify the differential input V_d but don't want to amplify the common signal i.e. noise, so A_{CM} should be as small as possible (and ideally should be zero).

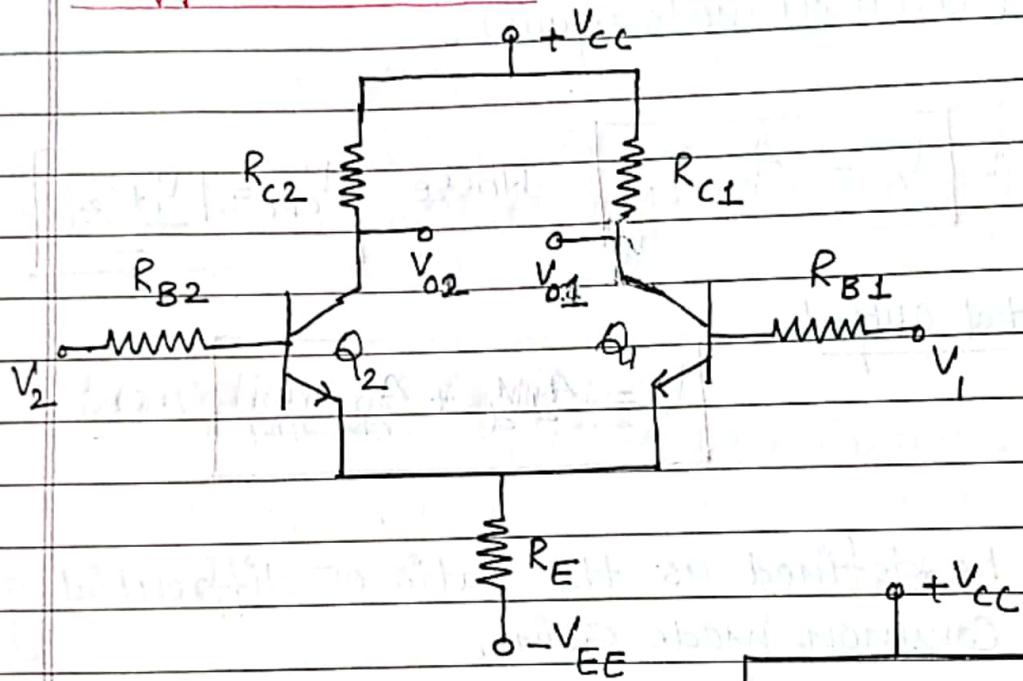
∴ $CMRR = \infty$ which is one of the ideal characteristics of op-amp.



Circuit Diagram of Differential Amp using BJT :-

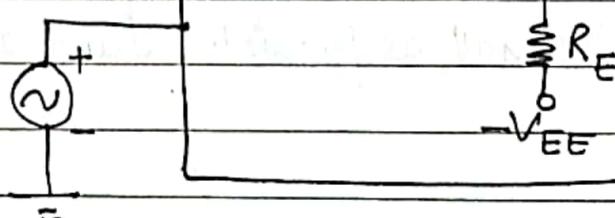
As Differential Amp operates in 2 modes so below are the ckt diagrams of differential Amp in 2 modes :- (using BJT)

① Differential Mode :-



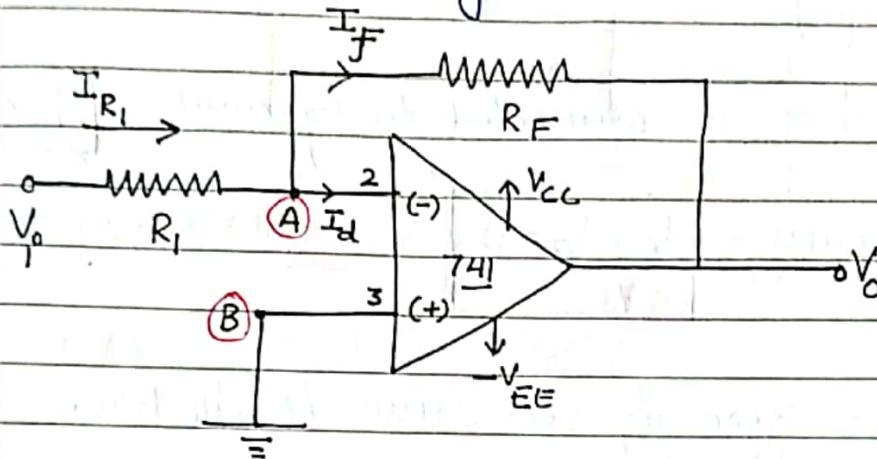
② Common Mode :-

Common Signal to both Inputs, $V_{in} = V_{CM}$



Op-amp As Inverting Amp :-

When input is applied to the inverting terminal of an op-amp, it is called as Inverting op-amp.



Concept of Virtual Ground :-

Ideally, open loop gain $A = \infty$

$$A = \frac{V_o}{|V_d|}$$

where V_d is the difference between two inputs of the op-amp.

$$\therefore A = \frac{V_o}{|V_A - V_B|}$$

V_A = Voltage At node A

V_B = Voltage At node B

For $A = \infty$

$$|V_A - V_B| = 0$$

$$V_A = V_B$$

Since Node B is connected to Ground $\therefore V_B = 0$

That means

$$V_A = V_B = 0$$

$\rightarrow V_A$ is not zero in real sense, it will have some potential but it is proven to be at ground.

This is the Concept of Virtual Ground.

Derivation of Gain :-

Applying KCL at node A.

$$I_{R_1} = I_d + I_f$$

\rightarrow For an ideal op-amp, input resistance $R_i = \infty$

therefore $I_d = 0$

$$I_{R_1} = I_f$$

$$\frac{V_o - V_A}{R_1} = \frac{V_A - V_o}{R_F}$$

but $V_A = 0$, From Virtual Ground Concept

$$\frac{V_o}{R_1} = -\frac{V_o}{R_F}$$

$$A_f = \frac{V_o}{V_i} = -\frac{R_F}{R_1}$$

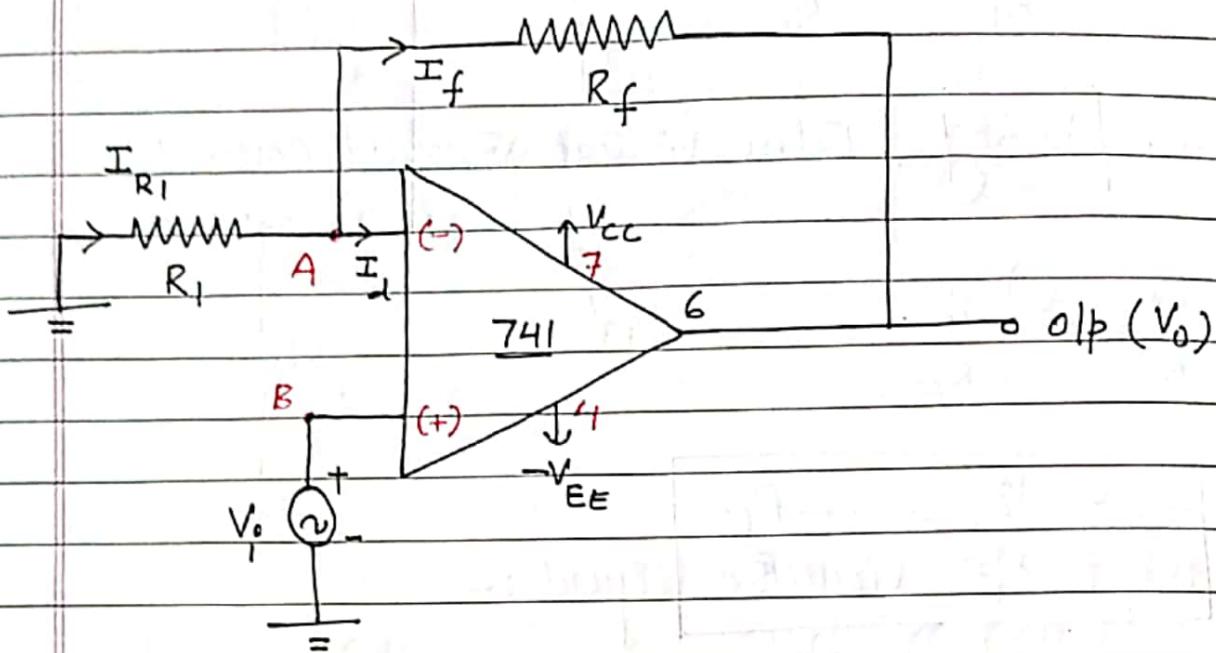
Where

A_f = closed Loop Gain / Feedback Gain

(-ve) sign indicates that there is a phase shift of 180° between input and output.

op-amp as Non-Inverting Amp

When Input is applied to Non-Inverting terminal of an op-amp, It is called as Non-Inverting op-amp.



→ Ideally, open Loop Gain $A = \infty$

$$A = \frac{V_O}{|V_A|} = \frac{V_O}{|V_A - V_B|}$$

→ Where

V_A & V_B are the 2 Inputs of op-amp.

→ For $A = \infty$, $|V_A - V_B| = 0$

$$\therefore V_A = V_B$$



But $V_B = V_I$ \therefore $V_A = V_B = V_I$ From Virtual Short Ckt Concept.

Derivation of Gain A_F :- Apply KCL at node A :-

$$I_{R_1} = I_d + I_f$$

but $I_d = 0$ b'coz $R_d = \infty$ For an ideal op-amp

$$\therefore I_{R_1} = I_f$$

$$\frac{0 - V_A}{R_1} = \frac{V_A - V_o}{R_f}$$

$$\frac{-V_A}{R_1} = \frac{V_A}{R_f} - \frac{V_o}{R_f}$$

$$\text{But } V_A = V_B = V_I$$

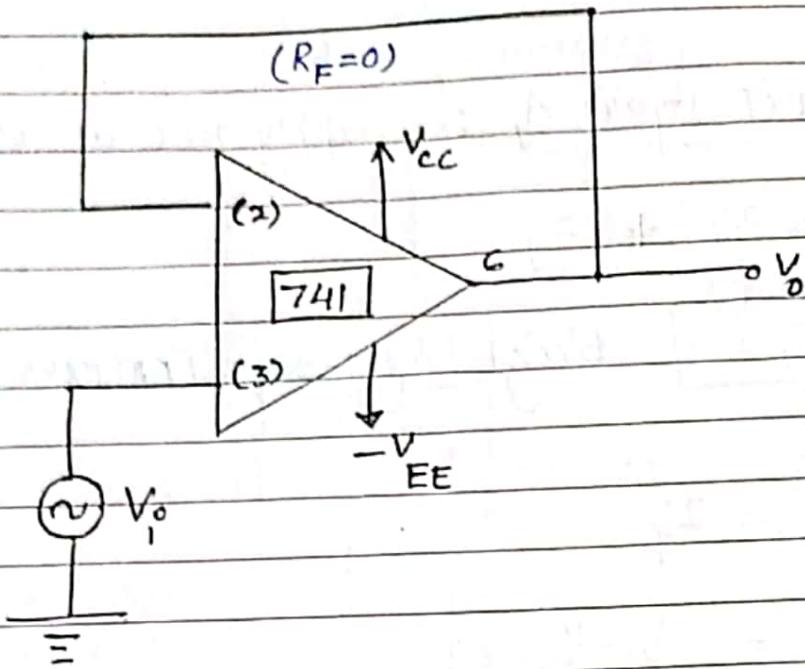
$$\therefore \frac{-V_o}{R_1} = \frac{V_I}{R_f} - \frac{V_o}{R_f}$$

$$\frac{V_o}{R_f} = \frac{V_I}{R_f} + \frac{V_o}{R_1} \Rightarrow \frac{V_o}{R_f} = V_I \left[\frac{1}{R_f} + \frac{1}{R_1} \right]$$

$$\therefore A_F = \frac{V_o}{V_I} = 1 + \frac{R_f}{R_1}$$

Proved

Op-amp As Voltage Follower & Unity Gain Buffer



→ Let us Consider Non-Inverting Configuration of op-amp.

→ If $R_i = \infty$, $R_F = 0$ in a non-inverting

op-amp then it becomes Voltage Follower, then
We know -

→ Gain $A_F = 1 + \frac{R_F}{R_i}$ of non-inverting op-amp

→ put $R_i = \infty$ & $R_F = 0$

$$A_F = 1$$

As the gain of Voltage Follower is unity \therefore It is also known as Unity Gain Buffer.

$$\rightarrow A_s A_F = 1$$

$$\frac{V_o}{V_i} = 1 \Rightarrow \boxed{V_o = V_i}$$

Since o/p voltage follows the input voltage, therefore it is also called as Voltage Follower.

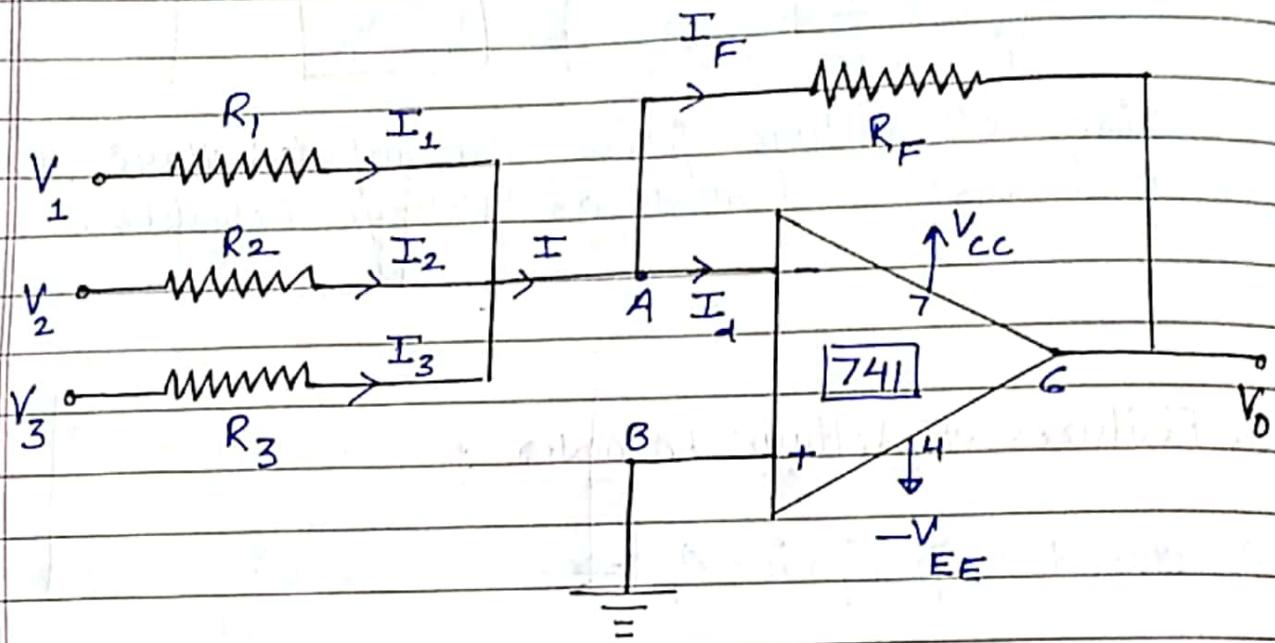
Features of Voltage Follower :-

- 1) Closed Loop Gain $A_F = 1$
- 2) Very high input resistance
- 3) Very low o/p Resistance.
- 4) Large bandwidth.

Note :- Voltage Followers are placed between two networks to reduce the loading on First network due to its high input impedance.

Applications of op-amp :-

① op-amp As Adder | Summer | Summing Amp :-



→ Ideally, open Loop Gain $A = \infty$

$$A = \frac{V_o}{V_d} = \frac{V_o}{|V_A - V_B|}$$

For $A = \infty$, $|V_A - V_B| = 0$

$$V_A = V_B$$

Since $V_B = 0$ $\therefore V_A = 0$ From Virtual Ground Concept.



Apply KCL at node A :-

$$I = I_d + I_F$$

but For ideal op-amp $k_f = \infty \therefore I_d = 0$

$$\therefore I = I_F$$

$$\rightarrow I_1 + I_2 + I_3 = I_F$$

$$\frac{V_1 - V_A}{R_1} + \frac{V_2 - V_A}{R_2} + \frac{V_3 - V_A}{R_3} = \frac{V_A - V_o}{R_F}$$

$\rightarrow V_A = 0$ From Virtual Ground Concept

$$\therefore \frac{V_1}{R_1} + \frac{V_2}{R_2} + \frac{V_3}{R_3} = -\frac{V_o}{R_F}$$

$$V_o = -R_F \left[\frac{V_1}{R_1} + \frac{V_2}{R_2} + \frac{V_3}{R_3} \right] \quad \rightarrow ①$$

IF $R_1 = R_2 = R_3 = R_F$ then

$$V_o = -(V_1 + V_2 + V_3)$$

* (-ve) sign indicates that there is 180° phase shift between input and output.

Average Amp² :- From eqⁿ ①

$$V_B = -R_F \left[\frac{V_1}{R_1} + \frac{V_2}{R_2} + \frac{V_3}{R_3} \right]$$

IF $R_1 = R_2 = R_3 = R$

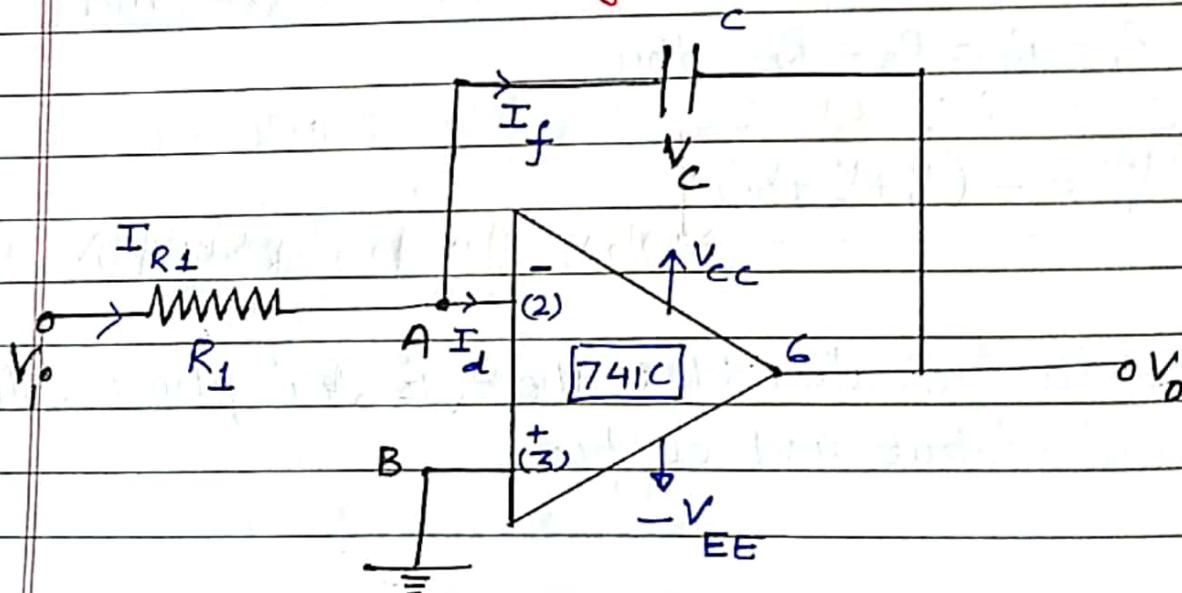
And

$$R_F = \frac{R}{3}$$

$$V_0 = - \left(\frac{V_1 + V_2 + V_3}{3} \right)$$

~~* Hence Adder behaves like an Average Amp².~~

② op-amp As an Integrator :-



Ideally, open Loop Gain $A = \infty$

$$\therefore A = \frac{V_o}{|V_A|} = \frac{V_o}{|V_A - V_B|}$$

$$\text{For } A = \infty, |V_A - V_B| = 0 \quad \therefore \boxed{V_A = V_B}$$

But $\boxed{V_B = 0}$ $\therefore \boxed{V_A = 0}$ From Virtual Ground Concept.

Now Applying KCL at node A :-

$$I_{R1} + I_d = I_f$$

but $I_d = 0$, b'coz for an ideal op-amp $\boxed{A_v = \infty}$

$$\therefore I_{R1} = I_f$$

$$\frac{V_i - V_A}{R_1} = C \frac{dV_C}{dt}$$

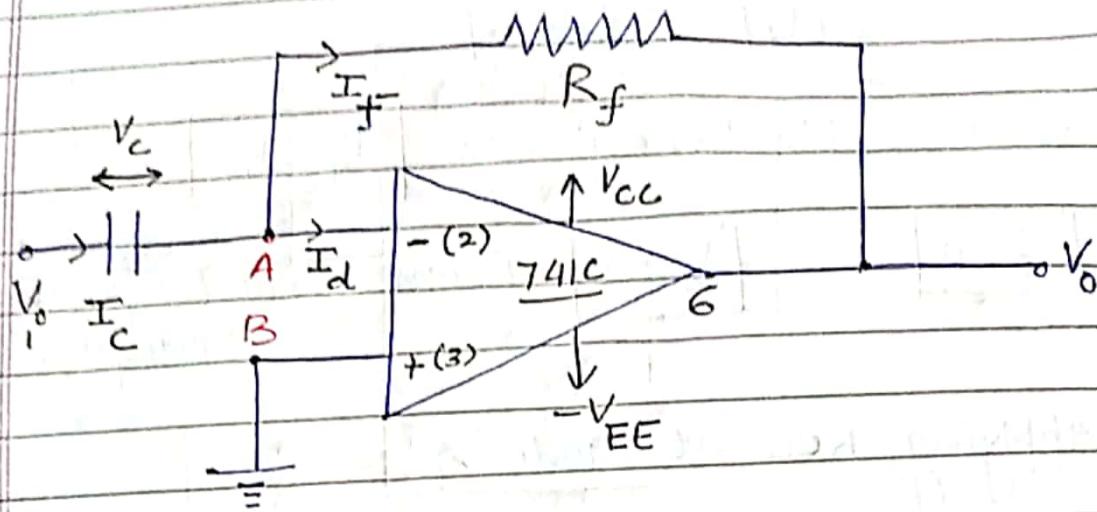
$$\text{but } \boxed{V_A = 0}, \quad \therefore \frac{V_i}{R_1} = C \frac{dV_C}{dt}$$

$$\therefore \frac{V_i}{R_1} = C \frac{d(V_A - V_o)}{dt} \Rightarrow \frac{V_i}{R_1} = C \frac{d(-V_o)}{dt}$$

$$\frac{dV_o}{dt} = -\frac{1}{R_1 C} V_i \Rightarrow \boxed{V_o = -\frac{1}{R_1 C} \int V_i dt}$$

* $R_1 C$ is called as time Constant of the Integrator.

③ Op-amp as Differentiator



Ideally, open loop Gain $A = \infty$

$$A = \frac{V_o}{|V_d|} = \frac{V_o}{|V_A - V_B|}$$

For $A = \infty$, $|V_A - V_B| = 0$

$$\therefore V_A = V_B$$

but $V_B = 0$ $\therefore V_A = V_B = 0$, as node B is grounded

↳ From Virtual Ground concept.

→ Applying KCL at node A:-

$$I_c = I_d + I_f$$

but $I_d = 0$, (For an ideal op-amp $R_i = \infty$)

$$\therefore I_c = I_f$$

$$C \frac{dV_c}{dt} = \frac{V_A - V_o}{R_f}$$

$$C \frac{d(V_o - V_A)}{dt} = \frac{V_A - V_o}{R_f}$$

But $V_A = 0$

$$\therefore C \frac{dV_o}{dt} = - \frac{V_o}{R_f}$$

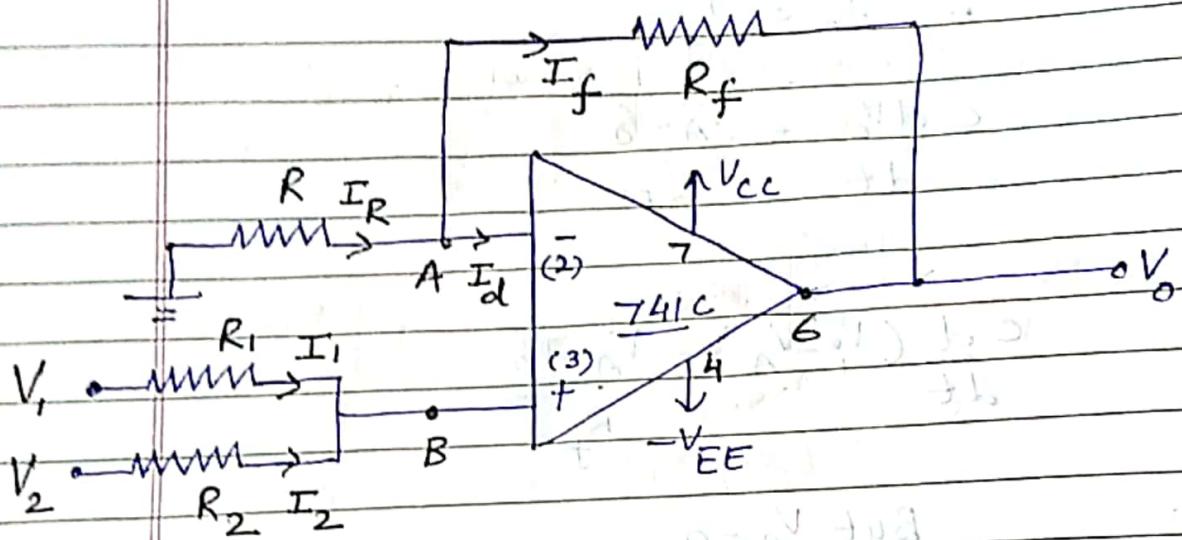
Hence

$$V_o = - R_f C \frac{dV_o}{dt}$$

Hence it produces the differentiation of the input voltage at its output, is called as differentiator.

* $-R_f C$ is called as time constant of the differentiator.

Non-Inverting Summing Amplifiers / Adder :-



→ Ideally, open Loop Gain $A = \infty$

$$A = \frac{V_o}{V_d} = \frac{V_o}{V_A - V_B}$$

$$\text{For } A = \infty, |V_A - V_B| = 0$$

$$\boxed{V_A = V_B}$$

* As Input Current of op-amp is zero, b'coz $R_i = \infty$

$$I_1 + I_2 = 0$$

$$\frac{V_1 - V_B}{R_1} + \frac{V_2 - V_B}{R_2} = 0$$

$$\frac{V_1}{R_1} + \frac{V_2}{R_2} = V_B \left[\frac{1}{R_1} + \frac{1}{R_2} \right]$$

$$V_B = \frac{V_1 R_2 + V_2 R_1}{R_1 + R_2}$$

But $V_A = V_B$, From Virtual Ground Concept

$$\therefore V_A = V_B = \frac{V_1 R_2 + V_2 R_1}{R_1 + R_2}$$

* Applying KCL at node A:

$$I_R = I_d + I_f$$

but $I_d = 0$ (For ideal op-amp, $R_i = \infty$
 $\therefore I_d = 0$)

$$\therefore I_R = I_f$$

$$\frac{0 - V_A}{R} = \frac{V_A - V_o}{R_f}$$

$$\frac{-V_A}{R} = \frac{V_A - V_o}{R_f}$$

$$V_o = R_f \left[\frac{V_A}{R_f} + \frac{V_A}{R} \right]$$

$$V_o = V_A \left[1 + \frac{R_f}{R} \right] \rightarrow ①$$

put the value of V_A in eqⁿ ① :-

$$V_o = \left[1 + R_F \right] \left(\frac{V_1 R_2 + V_2 R_1}{R_1 + R_2} \right)$$

∴ If $R_1 = R_2 = R_f = R$:- we get

$$V_o = 2 \times \frac{V_1 + V_2}{2}$$

$$V_o = V_1 + V_2$$

As there is no phase difference between Input and output, it is called as Non-Inverting summing Amplifier.

~~Q No 3~~ Draw a neat ckt diagram of 3 input Non-Inverting summing Amplifier and obtain the expression for its output voltage.

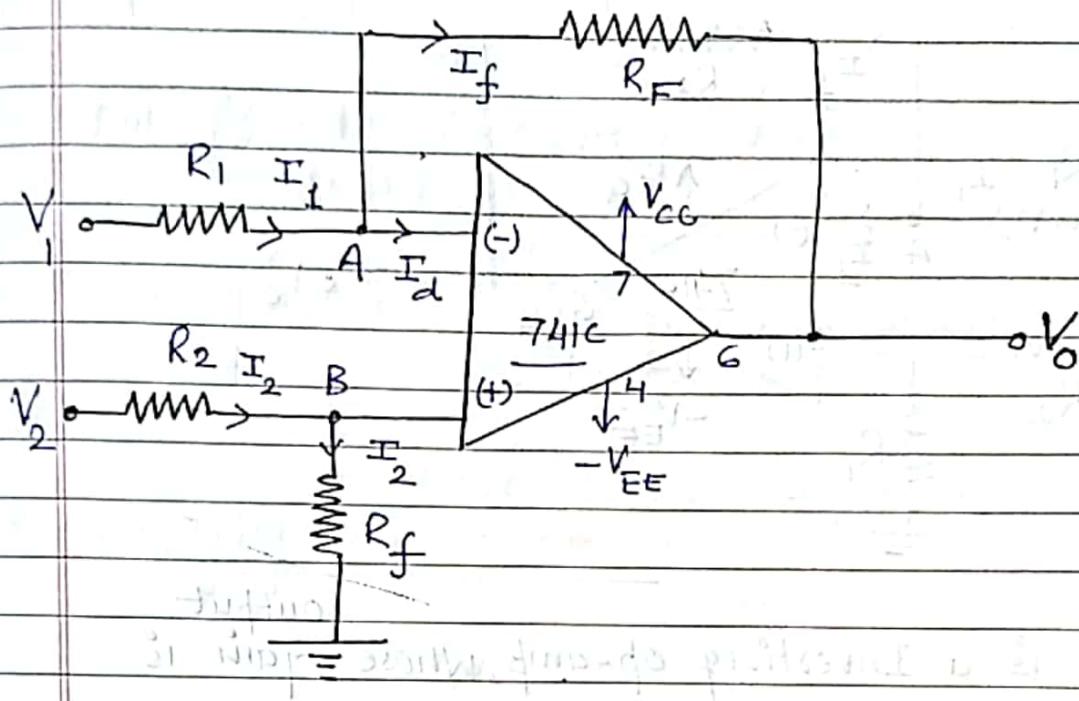
Hint :- same as above, but in last step, Assume

$$R_1 = R_2 = R_3 = R \text{ and } R_F = 2R$$

Ans :-

$$V_o = V_1 + V_2 + V_3$$

Op-amp As Subtractor or Difference Amplifiers :-



→ To Find relation between Input and output, Apply Superposition theorem.

→ Let V_{01} be the output, When Input V_1 is acting.

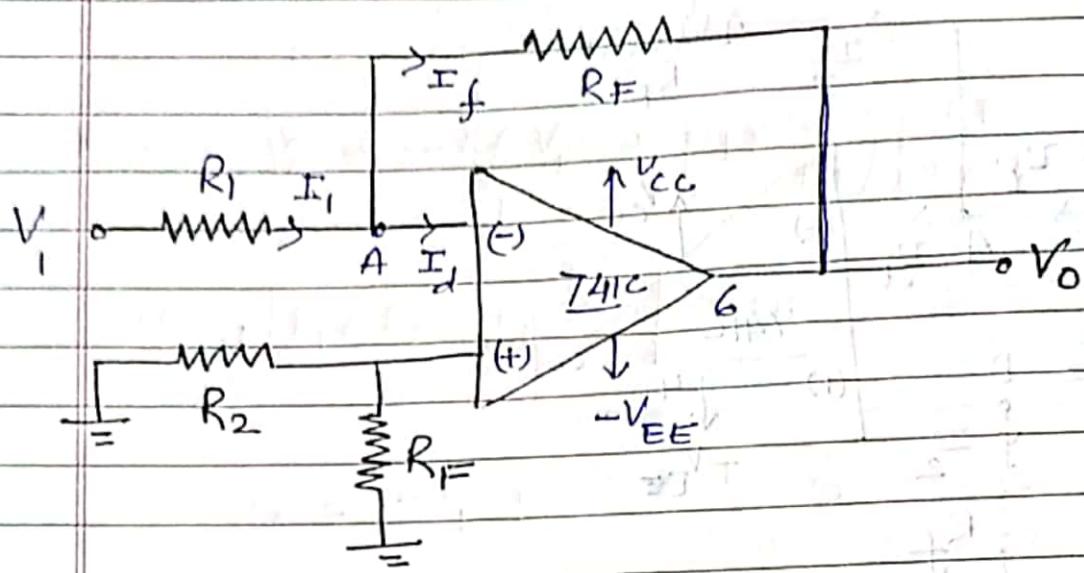
Assuming V_2 to be zero.

→ Let V_{02} be the output, When Input V_2 is acting

Assuming V_1 to be zero.

P.T.O

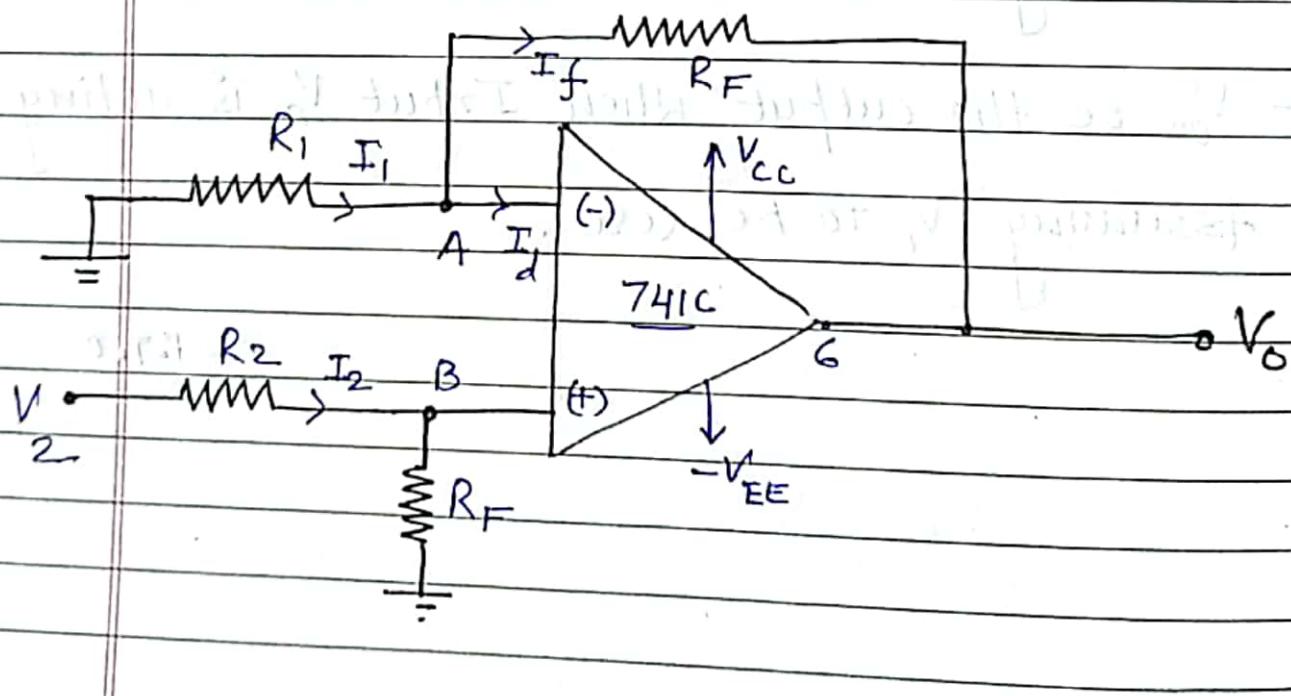
Considering Input V_1 and V_2 zero :-



→ This is a Inverting op-amp, Whose output is given by -

$$V_{O1} = -\frac{R_F}{R_1} V_1$$

Considering Input V_2 and V_1 zero :-



* Now we need to find V_B . Apply Voltage Divider Rule:-

$$V_B = \frac{R_F}{R_2 + R_F} V_2$$

→ Now Apply KCL at node 1 :-

$$I_1 = I_d + I_f$$

But $I_d = 0$, b'coz For an ideal op-amp $I_o = 0$
 $\therefore I_d = 0$

$$I_1 = I_f$$

$$\frac{V_A - V_A}{R_1} = \frac{V_A - V_{O2}}{R_f}$$

$$-\frac{V_A}{R_1} = \frac{V_A}{R_f} - \frac{V_{O2}}{R_f} \Rightarrow V_{O2} = \left[1 + \frac{R_f}{R_1} \right] V_A$$

but $V_A = V_B$, From Virtual Ground Concept

$$\therefore \boxed{V_{O2} = \left[1 + \frac{R_F}{R_1} \right] V_B}, \text{ but the value of } V_B.$$

$$\Rightarrow \boxed{V_{O2} = \left(1 + \frac{R_F}{R_1} \right) \left(\frac{R_F}{R_2 + R_F} \right) V_2}$$

Hence using superposition theorem :-

$$V_0 = V_{01} + V_{02}$$

$$V_0 = -\frac{R_F}{R_1} V_1 + \left(1 + \frac{R_F}{R_1}\right) \left(\frac{R_E}{R_F + R_2}\right) V_2$$

if $R_1 = R_2 = R_F = R$ then

$$V_0 = -V_1 + 2 \times \frac{1}{2} V_2$$

$$V_0 = V_2 - V_1$$

Thus o/p voltage is equal to the difference

of two input voltages, thus it acts as Subtractor.

$$V_0 = V_2 - V_1$$

$$V_0 = V_2 - V_1$$

input

$$V_0 = V_2 - V_1$$