

<b>St. Peter's Engineering College (Autonomous)</b> <b>Dullapally (P), Medchal, Hyderabad – 500100.</b> <b>I - Mid Term Examination – September 2024</b>				Dept.	:	CSM/CSC/ CSG
				Academic Year 2024-25		
Subject Code	:	AS22-00BS09	Subject	:	PROBABILITY AND STATISTICS	
Class/Section	:	B. Tech	Year	:	II	Semester : II
Duration	:	120 Min	Max. Marks	:	30	Date: : 02.09.2024

BLOOMS LEVEL					
Remember	L1	Understand	L2	Apply	L3
Analyze	L4	Evaluate	L5	Create	L6

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**PART – A (10x1M = 10M)**

Q. No	Question (s)	Marks	BL	CO								
UNIT - I												
1	<p>a) For the following the probability distribution</p> <table><tr><td>x</td><td>-3</td><td>6</td><td>9</td></tr><tr><td>P(X=x)</td><td>1/6</td><td>1/2</td><td>1/3</td></tr></table> <p>Find E(X)</p>	x	-3	6	9	P(X=x)	1/6	1/2	1/3	1M	L2	C221.1
x	-3	6	9									
P(X=x)	1/6	1/2	1/3									
1m 1c	<p>b) A random sample with replacement of size 2 is taken from <math>S = \{1, 2, 3\}</math>. Let the random variable X denote the sum of the two numbers taken, write the probability distribution.</p>	1M	L1	C221.1								
	<p>c) If the probability density of a random variable is given by <math>f(x) = \begin{cases} k(x^2 - 1), &amp; -1 \leq x \leq 3 \\ 0, &amp; \text{otherwise} \end{cases}</math> find the value of k</p>	1M	L1	C221.1								
	<p>d) Define mean and variance of continuous random variable</p>	1M	L3	C221.1								
UNIT – II												
	<p>e) Determine the probability of getting a sum of 9 exactly twice in 3 throws with a pair of dice.</p>	1M	L2	C221.2								
	<p>f) Ten coins are thrown simultaneously. Find the probability of getting atleast seven heads.</p>	1M	L1	C221.2								
	<p>g) Average number of accidents on any day on a national highway is 1.8. Determine the probability the number of accidents are atleast one.</p>	1M	L2	C221.2								
	<p>h) If X is normal variate with mean 30 and standard deviation 5. Find the probabilities that <math>26 \leq X \leq 40</math>.</p>	1M	L1	C221.2								
UNIT – III												

i) Derive critical values of Z for both two tailed and single tailed tests at 1%, 2% and 5% level of significance. 1m 1e	1M	L1	C221.3
j) Define one tailed and two tailed tests.	1M	L2	C221.3

**Note: Answer all Questions. Each Question carries equal marks.**

**PART – B (20M)**

Q. No	Question (s)	Marks	BL	CO																				
UNIT - I																								
2	a) A sample of 4 items is selected at random from a box containing 12 items of which 5 are defective. Find the expected number E of defective items. pg 18	4M	L3	C221.1																				
	b) Find the mean and variance of the uniform probability distribution given by $f(x) = \frac{1}{n}$ for $x=1,2,\dots,n$ . pg 19	4M	L2	C221.1																				
OR																								
3	a) If X is a continuous random variable and $Y = aX + b$ . Prove that $E(Y) = a E(X) + b$ and $V(Y) = a^2 V(X)$ where V stands for variance and a, b are constants.	4M	L5	C221.1																				
	b) For the continuous probability function $f(x) = kx^2 e^{-x}$ when $x \geq 0$ , find mean and variance.	4M	L3	C221.1																				
UNIT – II																								
4	a) 20% of items produced from a factory are defective. Find the probability that in a sample of 5 chosen at random (i) none is defective (ii) one is defective (iii) $p(1 < x < 4)$ 3m 2d	4M	L5	C221.2																				
	b) Seven coins are tossed and the number of heads are noted. The experiment is repeated 128 times and the following distribution is obtained. 10m 4c	4M	L4	C221.2																				
	<table><tr><td>X</td><td>0</td><td>1</td><td>2</td><td>3</td><td>4</td><td>5</td><td>6</td><td>7</td><td>Total</td></tr><tr><td>F</td><td>7</td><td>6</td><td>19</td><td>35</td><td>30</td><td>23</td><td>7</td><td>1</td><td>128</td></tr></table>				X	0	1	2	3	4	5	6	7	Total	F	7	6	19	35	30	23	7	1	128
X	0				1	2	3	4	5	6	7	Total												
F	7	6	19	35	30	23	7	1	128															
	Fit a binomial distribution assuming the coin is unbiased.																							
OR																								
5	a) In a normal distribution 31% of the items are under 45 and 8% are over 64. Find the mean and variance of distribution	4M	L3	C221.2																				
	b) Derive mean and variance of poisson distribution. 5m 3b	4M	L4	C221.2																				
UNIT – III																								
6	An ambulance service claims that it takes on the average less than 10 minutes to reach its destination in emergency calls. a sample of 36 calls has a mean of 11 minutes and the variance of 16 minutes. test the significance at 5% level of significance.	4M	L3	C221.3																				
OR																								

7	In a sample of 1000 people in Karnataka 540 are rice eaters and the rest are wheat are equally popular in this state at 1% level of significance? <a href="#">5m 3e</a>	4M	L3	C221.3
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