

# Introduction to NLP (CS7.401)

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## Smoothing (contd.)

### Interpolation and Backoff

Discounting algorithms help solve the problem of zero-frequency  $N$ -grams, but they do not use the knowledge we have of smaller  $N$ -grams. For example, if we are working with a zero-frequency 4-gram, we could consider the frequency of the 3-grams and 2-grams that make it up.

Interpolation mixes estimates from all smaller  $N$ -grams. For example, we have linear interpolation, in which we use the formula

$$\begin{aligned} P(w_n \mid w_{n-1}w_{n-2}) &= \lambda_1 P(w_n \mid w_{n-1}w_{n-2}) \\ &\quad + \lambda_2 P(w_n \mid w_{n-1}) \\ &\quad + \lambda_3 P(w_n), \end{aligned}$$

where

$$\sum_i \lambda_i = 1.$$

A slightly more sophisticated model would use context-dependent weights:

$$\begin{aligned} P(w_n \mid w_{n-1}w_{n-2}) &= \lambda_1(w_{n-2}^{n-1})P(w_n \mid w_{n-1}w_{n-2}) \\ &\quad + \lambda_2(w_{n-2}^{n-1})P(w_n \mid w_{n-1}) \\ &\quad + \lambda_3(w_{n-2}^{n-1})P(w_n), \end{aligned}$$

where

$$\sum_i \lambda_i(w_{n-2}^{n-1}) = 1.$$

To compute the  $\lambda_i$ , we use the held-out corpus (an additional training corpus used to set parameters of the model like these).

In backoff, we check each smaller  $N$ -gram at a time: first we check the 3-gram, and if it has zero frequency, then we check the 2-gram, and then the 1-gram. It

can work better than interpolation, which is relatively simple.

One model is called Katz backoff, which calculates the probabilities as:

$$P_{\text{katz}}(w_n | w_{n-N+1}^{n-1}) = \begin{cases} P^*(w_n | w_{n-N+1}^{n-1}) & C(w_{n-N+1}^n) > 0 \\ \alpha(w_{n-N+1}^{n-1}) P_{\text{katz}}(w_n | w_{n-N+2}^{n-1}) & \text{otherwise.} \end{cases}$$

Here the discounted probability  $P^*$  is defined as

$$P^*(w_n | w_{n-N+1}^{n-1}) = \frac{c^*(w_{n-N+1}^n)}{c(w_{n-N+1}^{n-1})}$$

and the function  $\alpha$  as

$$\begin{aligned} \alpha(w_{n-N+1}^{n-1}) &= \frac{\beta(w_{n-N+1}^{n-1})}{\sum_{w_n: c(w_{n-N+2}^{n-1}) > 0} P_{\text{katz}}(w_n | w_{n-N+2}^{n-1})} \\ &= \frac{1 - \sum_{w_n: c(w_{n-N+2}^{n-1}) > 0} P^*(w_n | w_{n-N+1}^{n-1})}{1 - \sum_{w_n: c(w_{n-N+2}^{n-1}) > 0} P^*(w_n | w_{n-N+2}^{n-1})} \end{aligned}$$

If  $x(w_{n-N+1}^{n-1}) = 0$ , then

$$\begin{aligned} P_{\text{katz}}(w_n | w_{n-N+1}^{n-1}) &= P_{\text{katz}}(w_n | w_{n-N+2}^{n-1}) \\ P^*(w_n | w_{n-N+1}^{n-1}) &= 0 \\ \beta(w_n | w_{n-N+1}^{n-1}) &= 1. \end{aligned}$$

Discounting tells us how much probability mass to set aside from nonzero-frequency counts, and backoff allows us to distribute it in a more informed manner.

## Kneser-Ney Smoothing

Kneser-Ney smoothing is an algorithm that counts the *number of histories* a word has occurred with, and uses it to estimate the probability of the current context. Kneser-Ney backoff is formalised as follows (assuming  $\alpha$  is defined so as to make everything sum to 1):

$$\begin{aligned} P_{\text{continuation}}(w_i) &= \frac{|\{w_{i-1} : c(w_{i-1}w_i) > 0\}|}{\sum_{w_i} |\{w_{i-1} : c(w_{i-1}w_i) > 0\}|} \\ P_{\text{KN}}(w_i | w_{i-1}) &= \begin{cases} \frac{c(w_{i-1}w_i) - D}{c(w_{i-1})} & c(w_{i-1}w_i) > 0 \\ \alpha(w_i) P_{\text{continuation}}(w_i) & \text{otherwise.} \end{cases} \end{aligned}$$

Kneser-Ney interpolation, however, has been shown to be superior to the backoff algorithm. It is calculated as

$$P_{\text{KN}}(w_i | w_{i-1}) = \frac{c(w_{i-1}w_i) - D}{c(w_{i-1})} + \beta(w_i) P_{\text{continuation}}(w_i).$$