Decision Trees

Nipun Batra and teaching staff

January 5, 2024

IIT Gandhinagar

Discrete Input Discrete Output

The need for interpretability

How to maintain trust in AI

Beyond developing initial trust, however, creators of AI also must work to maintain that trust. Siau and Wang suggest seven ways of "developing continuous trust" beyond the initial phases of product development:

- Usability and reliability. Al "should be designed to operate easily and intuitively,"
 Siau and Wang write. "There should be no unexpected downtime or crashes."
- Collaboration and communication. Al developers want to create systems that
 perform autonomously, without human involvement. Developers must focus on
 creating Al applications that smoothly and easily collaborate and communicate
 with humans.
- Sociability and bonding. Building social activities into AI applications is one way to strengthen trust. A robotic dog that can recognize its owner and show affection is one example, Siau and Wang write.
- Security and privacy protection. Al applications rely on large data sets, so
 ensuring privacy and security will be crucial to establishing trust in the
 applications.
- Interpretability. Just as transparency is instrumental in building initial trust, interpretability – or the ability for a machine to explain its conclusions or actions – will help sustain trust.

Training Data

Day	Outlook	Temp	Humidity	Windy	Play
D1	Sunny	Hot	High	Weak	No
D2	Sunny	Hot	High	Strong	No
D3	Overcast	Hot	High	Weak	Yes
D4	Rain	Mild	High	Weak	Yes
D5	Rain	Cool	Normal	Weak	Yes
D6	Rain	Cool	Normal	Strong	No
D7	Overcast	Cool	Normal	Strong	Yes
D8	Sunny	Mild	High	Weak	No
D9	Sunny	Cool	Normal	Weak	Yes
D10	Rain	Mild	Normal	Weak	Yes
D11	Sunny	Mild	Normal	Strong	Yes
D12	Overcast	Mild	High	Strong	Yes
D13	Overcast	Hot	Normal	Weak	Yes
D14	Rain	Mild	High	Strong	No

Learning a Complicated Neural Network



Learnt Decision Tree



Medical Diagnosis using Decision Trees



Source: Improving medical decision trees by combining relevant health-care criteria

Leo Brieman



Leo Breiman 1928-2005

Professor of Statistics, <u>UC Berkeley</u>
Verified email at stat.berkeley.edu - <u>Homepage</u>
Data Analysis Statistics Machine Learning



Cited by		VIEW AL
	All	Since 201
Citations	142857	6873
h-index	51	3
1401 1		





Optimal Decision Tree

Volume 5, number 1

INFORMATION PROCESSING LETTERS

May 1976

CONSTRUCTING OPTIMAL BINARY DECISION TREES IS NP-COMPLETE*

Laurent HYAFII.

IRIA - Laboria, 78150 Rocquencourt, France

and

Ronald L. RIVEST

Dept. of Electrical Engineering and Computer Science, M.I.T., Cambridge, Massachusetts 02139, USA

Received 7 November 1975, revised version received 26 January 1976

Binary decision trees, computational complexity, NP-complete

Greedy Algorithm

Core idea: At each level, choose an attribute that gives **biggest estimated** performance gain!



 ${\sf Greedy!} {=} {\sf Optimal}$

Day	Outlook	Temp	Humidity	Windy	Play
D1	Sunny	Hot	High	Weak	No
D2	Sunny	Hot	High	Strong	No
D3	Overcast	Hot	High	Weak	Yes
D4	Rain	Mild	High	Weak	Yes
D5	Rain	Cool	Normal	Weak	Yes
D6	Rain	Cool	Normal	Strong	No
D7	Overcast	Cool	Normal	Strong	Yes
D8	Sunny	Mild	High	Weak	No
D9	Sunny	Cool	Normal	Weak	Yes
D10	Rain	Mild	Normal	Weak	Yes
D11	Sunny	Mild	Normal	Strong	Yes
D12	Overcast	Mild	High	Strong	Yes
D13	Overcast	Hot	Normal	Weak	Yes
D14	Rain	Mild	High	Strong	No

Day	Outlook	Temp	Humidity	Windy	Play
D1	Sunny	Hot	High	Weak	No
D2	Sunny	Hot	High	Strong	No
D3	Overcast	Hot	High	Weak	Yes
D4	Rain	Mild	High	Weak	Yes
D5	Rain	Cool	Normal	Weak	Yes
D6	Rain	Cool	Normal	Strong	No
D7	Overcast	Cool	Normal	Strong	Yes
D8	Sunny	Mild	High	Weak	No
D9	Sunny	Cool	Normal	Weak	Yes
D10	Rain	Mild	Normal	Weak	Yes
D11	Sunny	Mild	Normal	Strong	Yes
D12	Overcast	Mild	High	Strong	Yes
D13	Overcast	Hot	Normal	Weak	Yes
D14	Rain	Mild	High	Strong	No

• For examples, we have 9 Yes, 5 No

Day	Outlook	Temp	Humidity	Windy	Play
D1	Sunny	Hot	High	Weak	No
D2	Sunny	Hot	High	Strong	No
D3	Overcast	Hot	High	Weak	Yes
D4	Rain	Mild	High	Weak	Yes
D5	Rain	Cool	Normal	Weak	Yes
D6	Rain	Cool	Normal	Strong	No
D7	Overcast	Cool	Normal	Strong	Yes
D8	Sunny	Mild	High	Weak	No
D9	Sunny	Cool	Normal	Weak	Yes
D10	Rain	Mild	Normal	Weak	Yes
D11	Sunny	Mild	Normal	Strong	Yes
D12	Overcast	Mild	High	Strong	Yes
D13	Overcast	Hot	Normal	Weak	Yes
D14	Rain	Mild	High	Strong	No

- For examples, we have 9 Yes, 5 No
- Would it be trivial if we had 14 Yes or 14 No?

Day	Outlook	Temp	Humidity	Windy	Play
D1	Sunny	Hot	High	Weak	No
D2	Sunny	Hot	High	Strong	No
D3	Overcast	Hot	High	Weak	Yes
D4	Rain	Mild	High	Weak	Yes
D5	Rain	Cool	Normal	Weak	Yes
D6	Rain	Cool	Normal	Strong	No
D7	Overcast	Cool	Normal	Strong	Yes
D8	Sunny	Mild	High	Weak	No
D9	Sunny	Cool	Normal	Weak	Yes
D10	Rain	Mild	Normal	Weak	Yes
D11	Sunny	Mild	Normal	Strong	Yes
D12	Overcast	Mild	High	Strong	Yes
D13	Overcast	Hot	Normal	Weak	Yes
D14	Rain	Mild	High	Strong	No

- For examples, we have 9 Yes, 5 No
- Would it be trivial if we had 14 Yes or 14 No?
- Yes!

Day	Outlook	Temp	Humidity	Windy	Play
D1	Sunny	Hot	High	Weak	No
D2	Sunny	Hot	High	Strong	No
D3	Overcast	Hot	High	Weak	Yes
D4	Rain	Mild	High	Weak	Yes
D5	Rain	Cool	Normal	Weak	Yes
D6	Rain	Cool	Normal	Strong	No
D7	Overcast	Cool	Normal	Strong	Yes
D8	Sunny	Mild	High	Weak	No
D9	Sunny	Cool	Normal	Weak	Yes
D10	Rain	Mild	Normal	Weak	Yes
D11	Sunny	Mild	Normal	Strong	Yes
D12	Overcast	Mild	High	Strong	Yes
D13	Overcast	Hot	Normal	Weak	Yes
D14	Rain	Mild	High	Strong	No

- For examples, we have 9 Yes, 5 No
- Would it be trivial if we had 14 Yes or 14 No?
- Yes!
- Key insights: Problem is "easier" when there is lesser disagreement

Day	Outlook	Temp	Humidity	Windy	Play
D1	Sunny	Hot	High	Weak	No
D2	Sunny	Hot	High	Strong	No
D3	Overcast	Hot	High	Weak	Yes
D4	Rain	Mild	High	Weak	Yes
D5	Rain	Cool	Normal	Weak	Yes
D6	Rain	Cool	Normal	Strong	No
D7	Overcast	Cool	Normal	Strong	Yes
D8	Sunny	Mild	High	Weak	No
D9	Sunny	Cool	Normal	Weak	Yes
D10	Rain	Mild	Normal	Weak	Yes
D11	Sunny	Mild	Normal	Strong	Yes
D12	Overcast	Mild	High	Strong	Yes
D13	Overcast	Hot	Normal	Weak	Yes
D14	Rain	Mild	High	Strong	No

- For examples, we have 9 Yes, 5 No
- Would it be trivial if we had 14 Yes or 14 No?
- Yes!
- Key insights: Problem is "easier" when there is lesser disagreement
- Need some statistical measure of "disagreement"

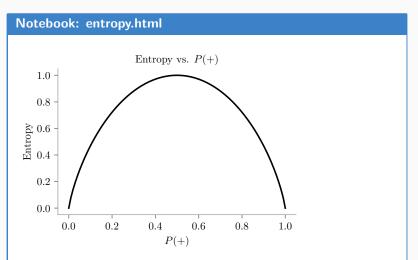
Entropy

Statistical measure to characterize the (im)purity of examples

Entropy

Statistical measure to characterize the (im)purity of examples

$$H(X) = -\sum_{i=1}^{n} p(x_i) \log p(x_i)$$



Day	Outlook	Temp	Humidity	Windy	Play
D1	Sunny	Hot	High	Weak	No
D2	Sunny	Hot	High	Strong	No
D3	Overcast	Hot	High	Weak	Yes
D4	Rain	Mild	High	Weak	Yes
D5	Rain	Cool	Normal	Weak	Yes
D6	Rain	Cool	Normal	Strong	No
D7	Overcast	Cool	Normal	Strong	Yes
D8	Sunny	Mild	High	Weak	No
D9	Sunny	Cool	Normal	Weak	Yes
D10	Rain	Mild	Normal	Weak	Yes
D11	Sunny	Mild	Normal	Strong	Yes
D12	Overcast	Mild	High	Strong	Yes
D13	Overcast	Hot	Normal	Weak	Yes
D14	Rain	Mild	High	Strong	No

Day	Outlook	Temp	Humidity	Windy	Play
D1	Sunny	Hot	High	Weak	No
D2	Sunny	Hot	High	Strong	No
D3	Overcast	Hot	High	Weak	Yes
D4	Rain	Mild	High	Weak	Yes
D5	Rain	Cool	Normal	Weak	Yes
D6	Rain	Cool	Normal	Strong	No
D7	Overcast	Cool	Normal	Strong	Yes
D8	Sunny	Mild	High	Weak	No
D9	Sunny	Cool	Normal	Weak	Yes
D10	Rain	Mild	Normal	Weak	Yes
D11	Sunny	Mild	Normal	Strong	Yes
D12	Overcast	Mild	High	Strong	Yes
D13	Overcast	Hot	Normal	Weak	Yes
D14	Rain	Mild	High	Strong	No

 Can we use Outlook as the root node?

Day	Outlook	Temp	Humidity	Windy	Play
D1	Sunny	Hot	High	Weak	No
D2	Sunny	Hot	High	Strong	No
D3	Overcast	Hot	High	Weak	Yes
D4	Rain	Mild	High	Weak	Yes
D5	Rain	Cool	Normal	Weak	Yes
D6	Rain	Cool	Normal	Strong	No
D7	Overcast	Cool	Normal	Strong	Yes
D8	Sunny	Mild	High	Weak	No
D9	Sunny	Cool	Normal	Weak	Yes
D10	Rain	Mild	Normal	Weak	Yes
D11	Sunny	Mild	Normal	Strong	Yes
D12	Overcast	Mild	High	Strong	Yes
D13	Overcast	Hot	Normal	Weak	Yes
D14	Rain	Mild	High	Strong	No

- Can we use Outlook as the root node?
- When Outlook is overcast, we always Play and thus no "disagreement"

Information Gain

Reduction in entropy by partitioning examples (S) on attribute A

$$Gain(S, A) \equiv Entropy(S) - \sum_{v \in Values(A)} \frac{|S_v|}{|S|} Entropy(S_v)$$

• Create a root node for tree

- Create a root node for tree
- If all examples are +/-, return root with label =+/-

- Create a root node for tree
- If all examples are +/-, return root with label =+/-
- If attributes = empty, return root with most common value of Target Attribute in Examples

- Create a root node for tree
- If all examples are +/-, return root with label =+/-
- If attributes = empty, return root with most common value of Target Attribute in Examples
- Begin

- Create a root node for tree
- ullet If all examples are +/-, return root with label =+/-
- If attributes = empty, return root with most common value of Target Attribute in Examples
- Begin
 - ullet A \leftarrow attribute from Attributes which best classifies Examples

- Create a root node for tree
- If all examples are +/-, return root with label =+/-
- If attributes = empty, return root with most common value of Target Attribute in Examples
- Begin
 - A ← attribute from Attributes which best classifies Examples
 - Root \leftarrow A

- Create a root node for tree
- If all examples are +/-, return root with label =+/-
- If attributes = empty, return root with most common value of Target Attribute in Examples
- Begin
 - A ← attribute from Attributes which best classifies Examples
 - Root \leftarrow A
 - For each value (v) of A

- Create a root node for tree
- If all examples are +/-, return root with label =+/-
- If attributes = empty, return root with most common value of Target Attribute in Examples
- Begin
 - A ← attribute from Attributes which best classifies Examples
 - Root \leftarrow A
 - For each value (v) of A
 - Add new tree branch : A = v

- Create a root node for tree
- If all examples are +/-, return root with label =+/-
- If attributes = empty, return root with most common value of Target Attribute in Examples
- Begin
 - A ← attribute from Attributes which best classifies Examples
 - Root \leftarrow A
 - For each value (v) of A
 - Add new tree branch : A = v
 - Examples_v: subset of examples that A = v

- Create a root node for tree
- If all examples are +/-, return root with label =+/-
- If attributes = empty, return root with most common value of Target Attribute in Examples
- Begin
 - A ← attribute from Attributes which best classifies Examples
 - Root \leftarrow A
 - For each value (v) of A
 - Add new tree branch : A = v
 - Examples_v: subset of examples that A = v
 - If Examples_vis empty: add leaf with label = most common value of Target Attribute

- Create a root node for tree
- If all examples are +/-, return root with label =+/-
- If attributes = empty, return root with most common value of Target Attribute in Examples
- Begin
 - A ← attribute from Attributes which best classifies Examples
 - Root \leftarrow A
 - For each value (v) of A
 - Add new tree branch : A = v
 - ullet Examples_v: subset of examples that A = v
 - If Examples_vis empty: add leaf with label = most common value of Target Attribute
 - Else: ID3 (Examples_v, Target attribute, Attributes A)

Learnt Decision Tree

Root Node (empty)

Training Data

Day	Outlook	Temp	Humidity	Windy	Play
D1	Sunny	Hot	High	Weak	No
D2	Sunny	Hot	High	Strong	No
D3	Overcast	Hot	High	Weak	Yes
D4	Rain	Mild	High	Weak	Yes
D5	Rain	Cool	Normal	Weak	Yes
D6	Rain	Cool	Normal	Strong	No
D7	Overcast	Cool	Normal	Strong	Yes
D8	Sunny	Mild	High	Weak	No
D9	Sunny	Cool	Normal	Weak	Yes
D10	Rain	Mild	Normal	Weak	Yes
D11	Sunny	Mild	Normal	Strong	Yes
D12	Overcast	Mild	High	Strong	Yes
D13	Overcast	Hot	Normal	Weak	Yes
D14	Rain	Mild	High	Strong	No

Entropy calculated

We have 14 examples in S: 5 No, 9 Yes

$$\begin{split} &\text{Entropy(S)} = -\,p_{\textit{No}}\log_2 p_{\textit{No}} - p_{\textit{Yes}}\log_2 p_{\textit{Yes}} \\ &= -(5/14)\log_2(5/14) - (9/14)\log_2(9/14) = 0.94 \end{split}$$

Outlook	Play	
Sunny	No	
Sunny	No	
Overcast	Yes	
Rain	Yes	
Rain	Yes	
Rain	No	
Overcast	Yes	
Sunny	No	
Sunny	Yes	
Rain	Yes	
Sunny	Yes	
Overcast	Yes	
Overcast	Yes	
Rain	No	

Outlook Play				
Sunny	No			
Sunny	No			
Sunny	No			
Sunny	Yes			
Sunny	Yes			
We have 2 Y	es, 3 No			
Entropy	/ =			
$(-3/5)\log_2(3/5)$ -				
$(-2/5)\log_2(2/5) =$				
0.971				

Outlook	Play
Sunny	No
Sunny	No
Sunny	No
Sunny	Yes
Sunny	Yes
We have 2 Y	es, 3 No
Entropy	y =
$(-3/5)\log_2$	(3/5) -
$(-2/5)\log_2($	2/5) =
0.97	1

Outlook	Play
Overcast	Yes
We have 4 Y	es, 0 No
Entropy	= 0

Play

Sunny	No
Sunny	No
Sunny	No
Sunny	Yes
Sunny	Yes
We have 2 Y	es, 3 No
Entropy	/ =
$(-3/5)\log_2($	(3/5) -
$(-2/5)\log_2($	2/5) =
0.97	1

Outlook

Outlook	Play
Overcast	Yes
We have 4 Y	es, 0 No
Entropy	= 0

Outlook	Play
Rain	Yes
Rain	Yes
Rain	No
Rain	Yes
Rain	No
We have 3 Y	és, 2 No
Entropy	/ =
$(-3/5)\log_2($	(3/5) -
$(-2/5)\log_2($	2/5) =
0.97	1

18

Information Gain

= 0.246

$$\begin{aligned} & \mathsf{Gain}(S,\mathit{Outlook}) = \; \mathsf{Entropy}\;(S) - \sum_{v \in \{\mathit{Rain},\mathit{Sunny},\mathit{Windy}\}} \frac{|S_v|}{|S|} \mathsf{Entropy}\,(S_v) \\ & \mathsf{Gain}\;(\mathsf{S},\;\mathsf{Outlook}) = \mathsf{Entropy}\;(\mathsf{S})\;\text{-}(5/14)^*\;\mathsf{Entropy}(\mathsf{S}_{\mathsf{Sunny}}) \text{-}\\ & (4/14)^*\;\mathsf{Entropy}\;(\mathsf{S}_{\mathsf{overcast}}) - (5/14)^*\;\mathsf{Entropy}(\mathsf{S}_{\mathsf{Rain}}) \\ & = 0.940\;\text{-}\;0.347\;\text{-}\;0.347 \end{aligned}$$

Information Gain



Learnt Decision Tree



Day	Temp	Humidity	Windy	Play
D1	Hot	High	Weak	No
D2	Hot	High	Strong	No
D8	Mild	High	Weak	No
D9	Cool	Normal	Weak	Yes
D11	Mild	Normal	Strong	Yes

Day	Temp	Humidity	Windy	Play
D1	Hot	High	Weak	No
D2	Hot	High	Strong	No
D8	Mild	High	Weak	No
D9	Cool	Normal	Weak	Yes
D11	Mild	Normal	Strong	Yes

• $Gain(S_{Outlook=Sunny}, Temp) = Entropy(3 Yes, 2 No) - (2/5)*Entropy(2 No, 0 Yes) - (2/5)*Entropy(1 No, 1 Yes) - (1/5)*Entropy(1 Yes)$

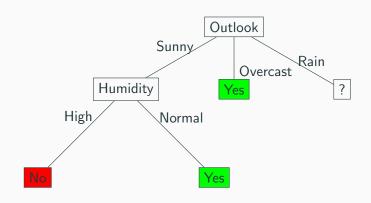
Day	Temp	Humidity	Windy	Play
D1	Hot	High	Weak	No
D2	Hot	High	Strong	No
D8	Mild	High	Weak	No
D9	Cool	Normal	Weak	Yes
D11	Mild	Normal	Strong	Yes

- $Gain(S_{Outlook=Sunny}, Temp) = Entropy(3 Yes, 2 No) (2/5)*Entropy(2 No, 0 Yes) (2/5)*Entropy(1 No, 1 Yes) (1/5)*Entropy(1 Yes)$
- Gain($S_{Outlook=Sunny}$, Humidity) = Entropy(3 Yes, 2 No) (2/5)*Entropy(2 Yes) -(3/5)*Entropy(3 No) \Longrightarrow maximum possible for the set

Day	Temp	Humidity	Windy	Play
D1	Hot	High	Weak	No
D2	Hot	High	Strong	No
D8	Mild	High	Weak	No
D9	Cool	Normal	Weak	Yes
D11	Mild	Normal	Strong	Yes

- Gain(S_{Outlook=Sunny}, Temp) = Entropy(3 Yes, 2 No) -(2/5)*Entropy(2 No, 0 Yes) -(2/5)*Entropy(1 No, 1 Yes) -(1/5)*Entropy(1 Yes)
- $Gain(S_{Outlook=Sunny}, Humidity) = Entropy(3 Yes, 2 No) (2/5)*Entropy(2 Yes) (3/5)*Entropy(3 No) <math>\Longrightarrow$ maximum possible for the set
- Gain(S_{Outlook=Sunny}, Windy) = Entropy(3 Yes, 2 No) -(3/5)*Entropy(2 No, 1 Yes) -(2/5)*Entropy(1 No, 1 Yes)

Learnt Decision Tree



Calling ID3 on (Outlook=Rain)

Day	Temp	Humidity	Windy	Play
D4	Mild	High	Weak	Yes
D5	Cool	Normal	Weak	Yes
D6	Cool	Normal	Strong	No
D10	Mild	Normal	Weak	Yes
D14	Mild	High	Strong	No

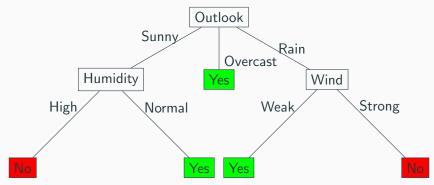
• The attribute Windy gives the highest information gain

Learnt Decision Tree



Prediction for Decision Tree

Just walk down the tree!



Prediction for Decision Tree

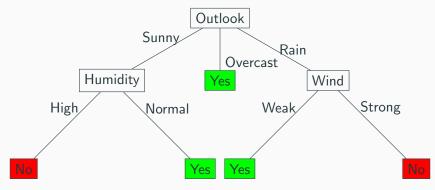
Just walk down the tree!



Prediction for <High Humidity, Strong Wind, Sunny Outlook, Hot Temp> is ?

Prediction for Decision Tree

Just walk down the tree!



Prediction for <High Humidity, Strong Wind, Sunny Outlook, Hot Temp> is ?

Assuming if you were only allowed depth-1 trees, how would it look for the current dataset?

Assuming if you were only allowed depth-1 trees, how would it look for the current dataset?

Apply the same rules, except when depth limit reached, the leaf node is assigned the "most" common occuring value in that path.

Assuming if you were only allowed depth-1 trees, how would it look for the current dataset?

Apply the same rules, except when depth limit reached, the leaf node is assigned the "most" common occuring value in that path.

What is depth-0 tree (no decision) for the examples?

Assuming if you were only allowed depth-1 trees, how would it look for the current dataset?

Apply the same rules, except when depth limit reached, the leaf node is assigned the "most" common occuring value in that path.

What is depth-0 tree (no decision) for the examples? Always predicting Yes

Assuming if you were only allowed depth-1 trees, how would it look for the current dataset?

Apply the same rules, except when depth limit reached, the leaf node is assigned the "most" common occuring value in that path.

What is depth-0 tree (no decision) for the examples? Always predicting Yes

What is depth-1 tree (no decision) for the examples?

Assuming if you were only allowed depth-1 trees, how would it look for the current dataset?

Apply the same rules, except when depth limit reached, the leaf node is assigned the "most" common occuring value in that path.

What is depth-0 tree (no decision) for the examples? Always predicting Yes

What is depth-1 tree (no decision) for the examples?



Discrete Input, Real Output

Modified Dataset

Day	Outlook	Temp	Humidity	Wind	Minutes Played
D1	Sunny	Hot	High	Weak	20
D2	Sunny	Hot	High	Strong	24
D3	Overcast	Hot	High	Weak	40
D4	Rain	Mild	High	Weak	50
D5	Rain	Cool	Normal	Weak	60
D6	Rain	Cool	Normal	Strong	10
D7	Overcast	Cool	Normal	Strong	4
D8	Sunny	Mild	High	Weak	10
D9	Sunny	Cool	Normal	Weak	60
D10	Rain	Mild	Normal	Weak	40
D11	Sunny	Mild	High	Strong	45
D12	Overcast	Mild	High	Strong	40
D13	Overcast	Hot	Normal	Weak	35
D14	Rain	Mild	High	Strong	20

• Any guesses?

- Any guesses?
- Mean Squared Error

- Any guesses?
- Mean Squared Error
- MSE(S) = 311.34

- Any guesses?
- Mean Squared Error
- MSE(S) = 311.34
- Information Gain analogoue?

- Any guesses?
- Mean Squared Error
- MSE(S) = 311.34
- Information Gain analogoue?
- Reduction in MSE (weighted)

Gain by splitting on Wind

Wind	Minutes Played
Weak	20
Strong	24
Weak	40
Weak	50
Weak	60
Strong	10
Strong	4
Weak	10
Weak	60
Weak	40
Strong	45
Strong	40
Weak	35
Strong	20

$$MSE(S)=311.34$$

Wind	Minutes Played
Weak	20
Weak	40
Weak	50
Weak	60
Weak	10
Weak	60
Weak	40
Weak	35

Weighted

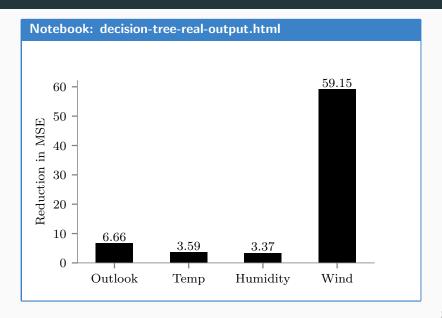
$$MSE(S_{Wind=Weak} = (8/14)*277 = 159)$$

Wind	Minutes Played
Strong	24
Strong	10
Strong	4
Strong	45
Strong	40
Strong	20

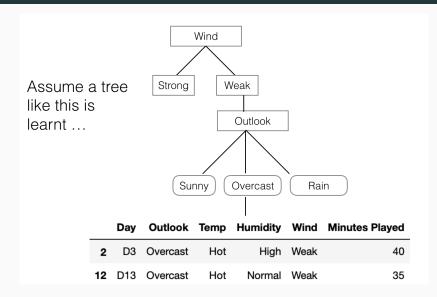
Weighted

$$\mathsf{MSE}(\mathsf{S}_{\mathsf{Wind}=\mathsf{Strong}}{=}(6/14)^*218{=}93)$$

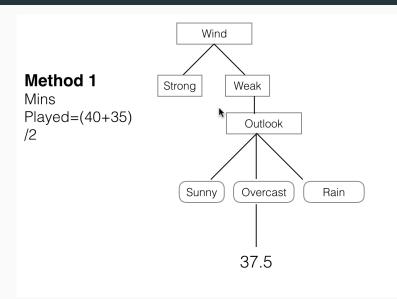
Information Gain



Learnt Tree



Learnt Tree



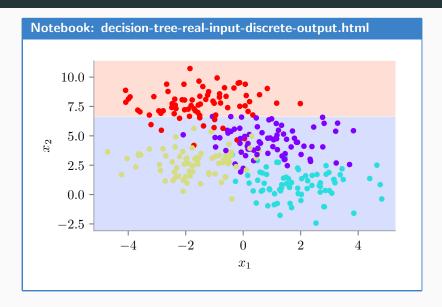
Real Input Discrete Output

Finding splits

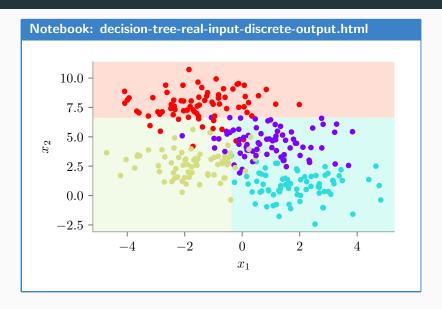
Day	Temperature	PlayTennis
D1	40	No
D2	48	No
D3	60	Yes
D4	72	Yes
D5	80	Yes
D6	90	No

- How do you find splits?
- Sort by attribute
- Find attribute values where changes happen
- \bullet For example, splits are: Temp > (48+60)/2 and Temp > (80+90)/2

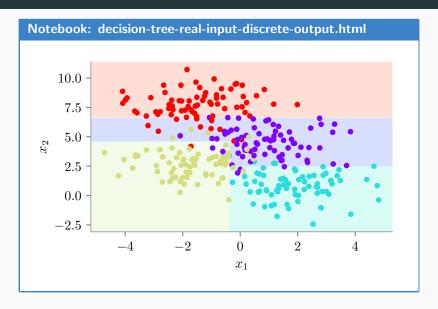
Example (DT of depth 1)



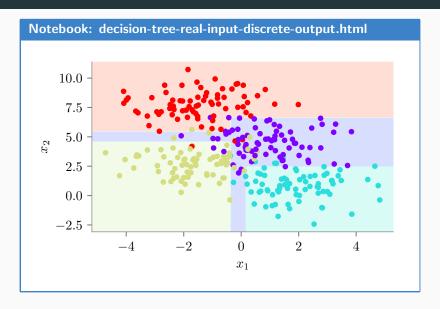
Example (DT of depth 2)



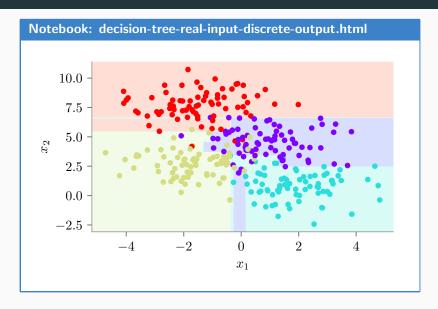
Example (DT of depth 3)



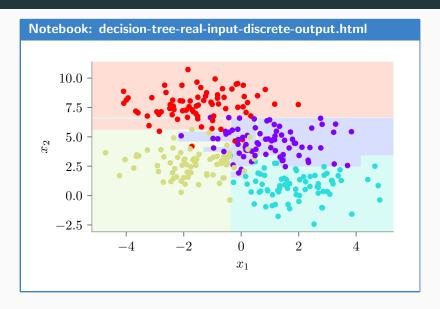
Example (DT of depth 4)



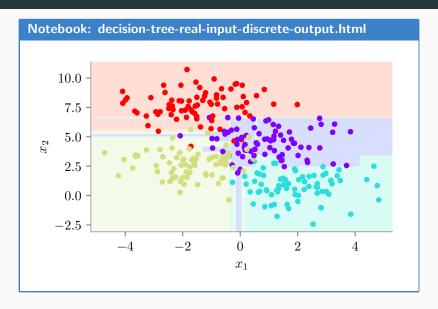
Example (DT of depth 5)



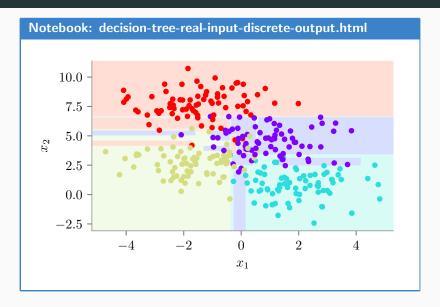
Example (DT of depth 6)



Example (DT of depth 7)



Example (DT of depth 8)



Example (DT of depth 9)

