### **Design and Analysis Algorithms**

### **Assignment 3**

# Vertex k -Labeling of Non - Homogeneous Caterpillar using Algorithmic Approach

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#### Irregular Labeling of Graph Models Using Algorithmic Approach

#### 1. Find out the best data structure to represent/store the graph in memory.

The graph is represented using an adjacency list data structure.

**Adjacency List Representation:** The graph structure is stored and manipulated as an adjacency list. This data structure efficiently represents connections between nodes by mapping each node to a list of its neighboring nodes and their corresponding weights. This strategy facilitates easy access to specific connections and simplifies adding or removing edges later.

```
# Loop to create the adjacency list for the graph
while i < root_nodes:
    j = 0
    # Loop to populate the adjacency list
while j < edge_count:
    next_link = weight - root_node # Calculate the next linked node
    if weight != used_weight:
        vertex = Vertex(weight, next_link) # Create a new vertex with weight and linked node
        if root_node not in adjacency_list:
            adjacency_list[root_node] = [] # Create a new list for the root node if it doesn't exist
            adjacency_list[root_node].append(vertex) # Append the new vertex to the root node's list
            weight += 1 # Increment weight
            j += 1</pre>
```

#### 2. Devise an algorithm to assign the labels to the vertices using vertex k-labeling definition.

#### 1. Initialization:

- Create an empty adjacency\_list dictionary.
- Set weight = 3, edge\_count = 3, root\_node = 2, i = 1, and used\_weight = -1.

#### 2. Loop for Root Nodes:

```
While i < root_nodes:
```

\*Inner Loop for Edges:\*

While j < edge\_count:

Calculate next\_link = weight - root\_node.

If weight != used\_weight:

Create a Vertex(weight, next\_link).

Add the vertex to the adjacency\_list[root\_node] list (creating it if necessary).

Increment weight.

Increment edge\_count.

#### 3. Special Case for Second-to-Last Root Node (Optional):

```
If i == root_nodes - 2:

Update used_weight = max_label + root_node.

Create a vertex Vertex(max_label + root_node, root_node).

Add the vertex to adjacency_list[max_label].

Update root_node = max_label.
```

#### 4. Update Root Node (Except for Last):

```
If not in the special case above (i != root_nodes - 2):
Update root_node = weight - root_node.
```

#### **5. Increase Counter:**

Increment i.

#### 6. Return:

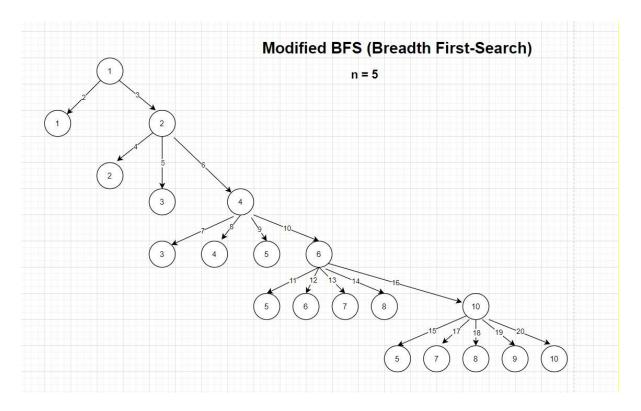
Return the final adjacency\_list.

### 3. What design strategy you adopted? And how you deduced that applied strategy is most appropriate

We used Greedy algorithm as a design strategy in this algorithm. At each level we made a locally optimize choice for labelling the vertex with the hope of finding a globally optimum solution. We assigned the next edge by incrementing the previous edge by 1 based on edge weight we are labeling the next least vertex label which satisfies the condition.

#### 4. How traversing will be applied?

The Breadth-First Search (BFS) is a graph traversal algorithm that explores a graph level by level. It starts at the root (or an arbitrary node) and explores all the neighbor nodes at the present depth before moving on to nodes at the next level of depth.



#### 5. Store the labels of vertices and weights of the edges to print as separate.

In the below output we can see the edge weights and vertices are stored

# 6. Weights must be unique, so devise a subroutine to maintain distinctive property of edge weights.

In order to guarantee that every vertex and edge in the Non-Homogenous Caterpillar graph is appropriately weighted, a careful method is used by the subroutine responsible for edge and vertex labeling maintenance. Label-1 is the first vertex that we have assigned, and the edge weight begins at 2. Edge weights can be adjusted by incrementing the previous edge weight and storing the current weight, starting with the first edge weight value. The process is repeated for each subgraph, guaranteeing that the sum of any two connected vertex weights equals the corresponding edge

weight and maintaining the mathematical integrity of the graph. For vertices, the label is subtracted from the edge weight. The result is then stored and assigned to the next vertex.

#### 7. For each value of n (length of path), compute the values of V(G) & E(G).

For different n values, these are Total nodes V(G), edges E(G) in

```
Values for different n values
                              max label
                                         total edges
     root nodes
                 total nodes
0
              1
                           2
            251
                       31877
                                  15939
                                                31876
2
            501
                      126252
                                  63126
                                              126251
3
            751
                      283127
                                 141564
                                              283126
           1001
                      502502
                                 251251
                                              502501
195
          48751
                  1188403127
                              594201564
                                          1188403126
196
          49001
                  1200622502
                              600311251
                                          1200622501
197
          49251
                  1212904377
                              606452189
                                          1212904376
198
          49501
                  1225248752
                              612624376
                                          1225248751
199
          49751 1237655627
                              618827814
                                          1237655626
[200 rows x 4 columns]
[Done] exited with code=0 in 0.498 seconds
```

## 8. Compare your results with mathematical property and tabulate the outcomes for comparison.

Total No. of Vertices V = n(n+3)/2

Total No. of Edges E = V-1

Max Vertex label k = Ceil(V/2)

Created the below table using above formulas and compared with the results generated by algorithm:

In the result output we can see the values match with the computed values.

main path $N = 1$	Total Vestices V= 2	Potal mask edges lakeling E=1 K=1
N = 2	V= 5	E=4 K=3
n= 5	V = 20	E=19 K=10

#### 9. Hardware resources supported until what maximum value of n and p.

Processor 11th Gen Intel(R) Core(TM) i7-1165G7 @ 2.80GHz 2.80 GHz

Installed RAM 12.0 GB (11.8 GB usable)

Device ID 900C14A1-B0B6-4787-A054-1A13B783B53F

Product ID 00342-21944-36780-AAOEM

System type 64-bit operating system, x64-based processor

Pen and touch Touch support with 10 touch points

For root_nodes(n)	Time(in Sec)
5	0.469
100	1.529
500	4.716
2000	26.467
5000	79.529
10000	143.446
13000	-

#### 10. Compute the Time Complexity of your algorithm T(V,E) or T(n,p).

The execution time of the valid algorithm is finite. The algorithm's time complexity is the amount of time it takes to solve a certain task. A highly helpful metric in algorithm study is time complexity.

It is the amount of time required for an algorithm to finish. We must take into account both the cost and the number of executions of each basic instruction in order to determine the temporal complexity.

Considering the dominant factor, the overall time complexity of this algorithm will be O(root\_nodes \* edge\_count)

Results(For n = 5):

n = 5,

