

left by mistake. (searching & sorting level = 2)

classmate

Date

Page

→ Binary search on 2D Array.

	0	1	2	3
0	2	4	6	8
1	10	12	14	16
2	18	20	22	24
3	28	34	40	50

→ Sorted 1D in actually,

2D → 1D

↳  $C * i + j$

1D → 2D

$$i = \frac{\text{mid}}{C} \quad j = \text{mid} \% C$$

Binary search same laggi  
But 2D to 1D ka conversion  
aana challenge.

1D → 2D

10  
6 cols = 4

$$i = \frac{\text{index}}{\text{col}} = \frac{6}{4} = 1$$

$$j = \text{index} \% \text{col}$$

$$= 6 \% 4 = 2$$

$$(i, j) = (1, 2) \rightarrow 10$$

			2
			10

# 2D → 1D

$$C * i + j$$

# 1D → 2D

$$i = \frac{\text{index}}{\text{col}}, \quad j = \text{index} \% \text{col}$$

Code ~~bool searchMatrix~~ (vector<int> &int

bool searchMatrix (vector<vector<int>> & matrix,  
int target) {

int row = matrix.size();

int col = matrix[0].size();

int total = row \* col;

int s = 0;

int e = total - 1;

while (s <= e) {

int mid = (s + e) / 2;

int rowIndex = mid / col;

int colIndex = mid % col;

int currElement = matrix[rowIndex][colIndex];

if (currElement == target) return true;

else if (currElement > target) e = mid - 1;

else s = mid + 1;

}

return false;

}.

Time Complexity :-  $O(\log n)$

Space Complexity :-  $O(1)$

## ▣ Searching & Sorting - Level 3.

Q:- find quotient of a no.

i/p :- ① Divisor  $\rightarrow a$  } Divide  
 ② Dividend  $\rightarrow b$  } Binary Search.

$$\left\lfloor \frac{a}{b} \right\rfloor \rightarrow \text{quotient}$$

$$\frac{24}{6} = 4$$

$$\frac{28}{4} = 7$$

divisor ) dividend ( Quotient.

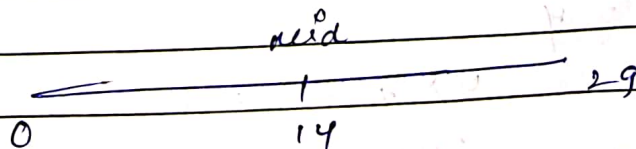
Remainder.

$\rightarrow \text{Quotient} \times \text{divisor} + \text{Remainder} = \text{Dividend}$

(  $\text{Quotient} \times \text{divisor} \leq \text{Dividend}$

let's take eg :- Divisor = 7, Dividend = 29.

$$\begin{array}{r} 29 \\ 7 \end{array}$$



$s = 0$   
 $e = 29$   $\rightarrow$  mid = 14  $\rightarrow$  It can be possible ans so let's cross check.



Quotient  $\times$  divisor  $\leq$  Dividend.

$$14 \times 7 = 98$$

$$98 > 29$$

$$e = \text{mid} - 1;$$

$$e = 14 - 1$$

$$e = 13$$

$$0 \quad \text{---} | \text{---} \quad 13$$

6

$$\text{mid} = 6$$

$$6 \times 7 = 42 > 29$$

$$e = 5$$

$$0 \quad \text{---} | \text{---} \quad 5$$

2

$$2 \times 7 = 14 < 29$$

$$\text{ans} = 2$$

$$s = \text{mid} + 1 = 2 + 1 = 3$$

store the  
range.

$$3 \quad \text{---} | \text{---} \quad 5$$

4

$$\text{mid} = 4$$

$$4 \times 7 \leq 28$$

$$\text{ans} = 4$$

$$s = 5$$

5      5

mid = 5

$5 \times 7 > 35$

$e = 6$

Here

$e > S \rightarrow$  Loop Breaks.

Code

```
int getQuotient (int divisor, int dividend) {
    int s = 0;
    int e = dividend;
    int ans = -1;
    while (s <= e) {
        int mid = s + (e - s) / 2;
        if (mid * divisor == dividend) return mid;
        else if (mid * divisor > dividend)
            e = mid - 1;
        else {
            ans = mid;
            s = mid + 1;
        }
    }
}
```

return ans;

main() {

int divisor = -7, dividend = 28;

int res = getQuotient(abs(divisor), abs(dividend));

if ((dividend < 0 && divisor > 0) || (dividend > 0 && divisor < 0))

res = 0 - res;

cout << "The quotient is : " << res << endl;



## Questions on Binary search.

- clear
- search space.
- predicate function.
- Enden → logic.

### Q. Binary search on nearly Sorted Array.

Sorted

Array. | 10 | 20 | 30 | 40 | 50 | 60 | 70 |

0 1 2 3 4 5 6

Nearly

Sorted | 20 | 10 | 30 | 50 | 40 | 70 | 60 |

Array. 0 1 2 3 4 5 6

→ value may at

↳ i

↳ i-1

↳ i+1.

Normal Sorted Array

→ if (arr[mid] == target)

return mid;

→ if (target > arr[mid])

↳ Right

else

↳ Left.

Nearly Sorted Array.

if (arr[mid-1] == target)

return mid-1;

if (arr[mid] == target)

return mid;

if (arr[mid+1] == target)

return mid+1;

if (target > arr[mid])

↳ Right

else

↳ Left.

Dry Run

0	1	2	3	4	5	6
20	10	30	50	40	70	60
↑			↓			↑
s			mid.			e

s = 0

e = 6

target = 30.

arr[mid-1] → 30 == 70 X

arr[mid] → 50 == 70 X

arr[mid+1] → 40 == 70 X

if (target &gt; arr[mid])

right-jana hai

s = mid + 2 → catch.

	s		e
	↓		↓
{	40   70   60		
	4	5	6
	s = 4		
	e = 6		

→ Agar hum  
s = mid + 1 kote  
for.

s	e
↓	↓
70	60
5	6
mid	

s = 5  
e = 6

arr[mid] == target ✓

return mid

→ Any



another target = 20

s			mid				e
↓			↓				↓
	20	10	30	50	40	70	60
	0	1	2	3	4	5	6

s = 0  
e = 6 → mid = 3

arr[mid-1] == target X

arr[mid] == target X

arr[mid+1] == target X

if (target > arr[mid])

s = mid + 2;

else

e = mid - 2 → catch

s		e
↓		↓
	20	10
	0	1

mid =  $\frac{s+e}{2} = 0 \rightarrow arr[0] = 20$  target ✓

found.

return mid

0 → Any



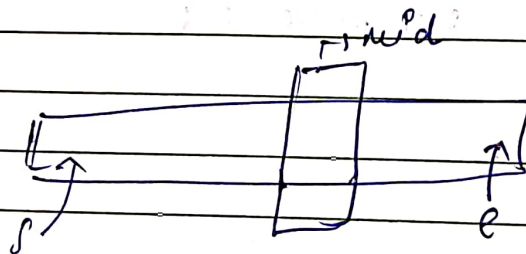
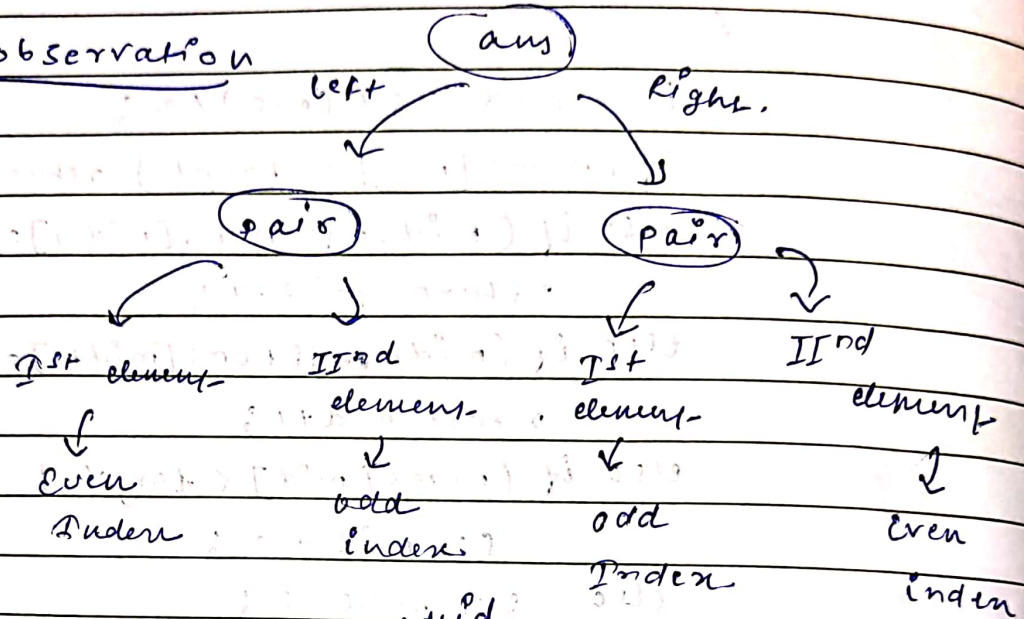
```
Code Search Nearly Sorted Array (vector<int> &nums,  
int &target)  
{  
    int n = nums.size() - 1;  
    int s = 0;  
    int e = n;  
    while (s <= e)  
    {  
        int mid = s + (e - s) / 2;  
        if (nums[mid] == target) return mid;  
        else if (mid > 0 && nums[mid - 1] == target)  
            return mid - 1;  
        else if (mid < n && nums[mid + 1] == target)  
            return mid + 1;  
        else if (nums[mid] < target)  
            s = mid + 2;  
        else e = mid - 2;  
    }  
    return -1;  
}
```

Time complexity  $\rightarrow O(\log n)$   
Space complexity  $\rightarrow O(1)$

Q. find the odd occurring element.

| 1 | 1 | 5 | 5 | 2 | 2 | 3 | 3 | 2 | 4 | 4 |  
0 1 2 3 4 5 6 7 8 9 10

observation



if (mid % 2 == 0)

if (arr[mid] == arr[mid+1])

s = mid + 2  
else e = mid

else.

if (arr[mid] == arr[mid-1])

s = mid + 1

else e = mid - 1



Code Odd occurring Element (vector<int> nums)

```

{
    int n = nums.size();
    int s = 0;
    int e = nums.size() - 1;
    while (s <= e) {
        if (s == e) return s;
        int mid = s + (e - s) / 2;
        if (mid & 1)
        {
            if (mid > 0 && nums[mid] == nums[mid - 1])
                s = mid + 1;
            else e = mid - 1;
        }
        else
        {
            if (mid + 1 < n && nums[mid] == nums[mid + 1])
                s = mid + 2;
            else e = mid;
        }
    }
}

```

Time complexity :-  $O(\log n)$   
 Space complexity :-  $O(1)$