1

Assignment 4

Abhishek Kumar AI21BTECH11003

Question:If A,B,C are three events associated with a random experiment,prove that

$$P(A \cup B \cup C) = P(A) + P(B) + P(C) - P(A \cap B)$$
$$-P(B \cap C) - P(C \cap A) + P(A \cap B \cap C) \quad (1)$$

Solution: Consider

$$E = B \cup C \tag{2}$$

$$P(A \cup B \cup C) = P(A \cup E) = P(A) + P(E) - P(A \cap E)$$
(3)

$$P(E) = P(B \cup C) = P(B) + P(C) - P(B \cap C)$$
 (4)

$$A \cap E = A \cap (B \cup C) = (A \cap B) \cup (A \cap C) \tag{5}$$

$$P(A \cap E) = P[(A \cap B) \cup (A \cap C)] = P(A \cap B)$$

$$+ P(A \cap C) - P[(A \cap B) \cap (A \cap C)]$$
(6)

$$P(A \cap E) = P(A \cap B) + P(A \cap C) - P(A \cap B \cap C) \quad (7)$$

using equation(3) and equation(4) and equation(7)

$$P(A \cup B \cup C) = P(A) + P(B) + P(C) - P(A \cap B)$$
(8)
- $P(B \cap C) - P(C \cap A) + P(A \cap B \cap C)$

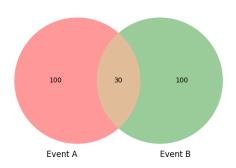


Fig. 1. By this figure generated by python code,we can verify equation (3) intutively

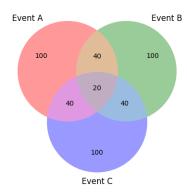


Fig. 2. By this figure generated by python code, we can verify equation (9) intutively