## EE 720: Introduction to Number Theory and Cryptography (Spring 2018) Instructor: Saravanan Vijayakumaran

Indian Institute of Technology Bombay

Date: January 23, 2018

Assignment 2: 10 points

Find the pdf file corresponding to your roll number in the directory https://www.ee.iitb.ac.in/~sarva/courses/EE720/2018/assignments/assignment2/. Upload the answers as a pdf file in Moodle. Use the tex file provided in the directory to fill in your answers. The upload deadline will be 11:00pm IST on Wednesday, January 31, 2018.

1. [5 points] Prove that the Vigenére cipher using period t is perfectly indistinguishable when used to encrypt messages of length t. Prove this directly without proving the perfect secrecy of the scheme and then using the equivalence of perfect secrecy and perfect indistinguishability.

Solution: Write your answer here

2. [5 points] State whether the following encryption scheme is perfectly secret or not. Justify your answer either with a proof or a counterexample.

The message space is  $\mathcal{M} = \{m \in \{0,1\}^l \mid \text{the last bit of } m \text{ is } 0\}$ . Algorith Gen chooses a uniform key from the keyspace  $\{0,1\}^{l-1}$ .  $\operatorname{Enc}_k(m) = m \oplus (k\|0)$  and  $\operatorname{Dec}_k(c) = c \oplus (k\|0)$ .

Solution: Write your answer here