EE 720: Introduction to Number Theory and Cryptography (Spring 2018)

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Assignment 2: 10 points

Date: January 23, 2018

Find the pdf file corresponding to your roll number in the directory https://www.ee.iitb.ac.in/~sarva/courses/EE720/2018/assignments/assignment2/. Upload the answers as a pdf file in Moodle. Use the tex file provided in the directory to fill in your answers. The upload deadline will be 11:00pm IST on Wednesday, January 31, 2018.

1. [5 points] Consider a variant of the one-time pad with message space $=\{0,1\}^l$ and keyspace \mathcal{K} restricted to all l-bit strings with an even number of 1's. Is this scheme perfectly secret? Justify your answer either with a proof or a counterexample.

Solution: Write your answer here

2. [5 points] When the one-time pad is used with the all-zeros key, i.e. $k=0^l$, we have $\operatorname{Enc}_k(m)=m\oplus k=m$. This means that the plaintext will be sent as it is. To prevent this, suppose we modify the one-time pad to use only non-zero keys, $k\neq 0^l$. The key generation algorithm Gen picks key k uniformly from the set $\{0,1\}^l\setminus\{0^l\}$ which has cardinality 2^l-1 . Is this modified scheme still perfectly secret? Justify your answer either with a proof or a counterexample.

Solution: Write your answer here