EE 720: Introduction to Number Theory and Cryptography (Spring 2018)
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Assignment 2: 10 points Date: January 23, 2018

Find the pdf file corresponding to your roll number in the directory `https://www.ee.iitb.ac.in/~sarva/courses/EE720/2018/assignments/assignment2/`. Upload the answers as a **pdf** file in Moodle. Use the tex file provided in the directory to fill in your answers. The **upload deadline** will be 11:00pm IST on Wednesday, January 31, 2018.

1. [5 points] State whether the following encryption scheme is perfectly secret or not. Justify your answer either with a proof or a counterexample.

   The message space is $\mathcal{M} = \left\{m \in \{0,1\}^l \mid \text{the last bit of } m \text{ is } 0\right\}$. Algorith `Gen` chooses a uniform key from the keyspace $\{0,1\}^{l-1}$. $\texttt{Enc}_k(m) = m \oplus (k \| 0)$ and $\texttt{Dec}_k(c) = c \oplus (k \| 0)$.

   Solution: Write your answer here

2. [5 points] State whether the following encryption scheme is perfectly secret or not. Justify your answer either with a proof or a counterexample.

   The message space is $\mathcal{M} = \{0, \ldots, 4\}$. Algorithm `Gen` chooses a uniform key from the keyspace $\{0, \ldots, 5\}$. $\texttt{Enc}_k(m) = (k + m) \bmod 5$ and $\texttt{Dec}_k(c) = (c - k) \bmod 5$.

   Solution: Write your answer here