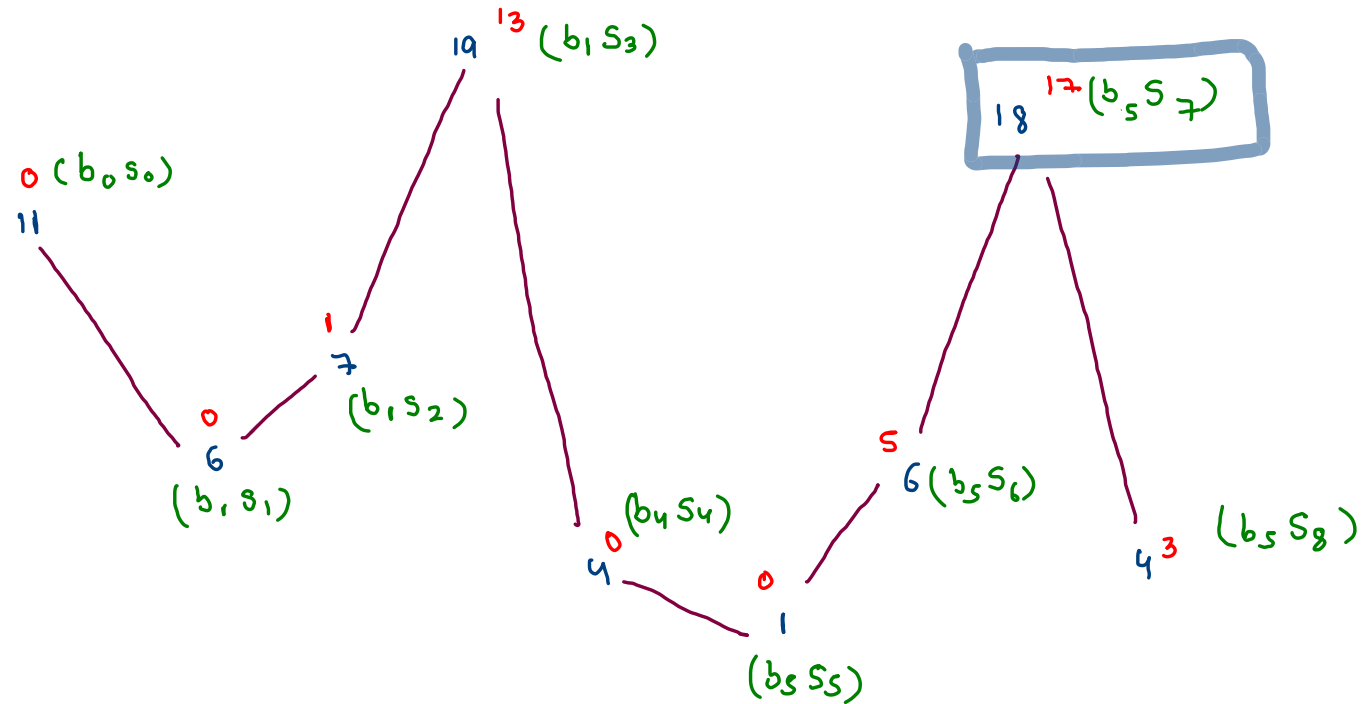
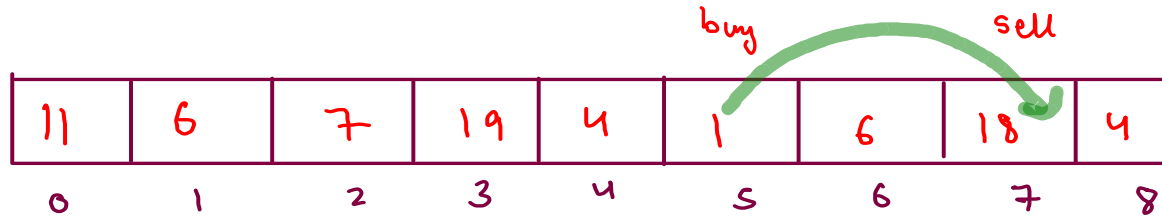


## Buy And Sell Stocks - One Transaction Allowed

11	6	7	19	4	1	6	18	4
0	1	2	3	4	5	6	7	8





pr

0      0      1      13      0      0      5      17      3

msj (min so far)

opr (overall best profit)



$$msj = \cancel{0} / \cancel{11} / \cancel{6} / 1$$

$$opr = \cancel{0} / \cancel{13} / 17$$

```

public static int one_transaction(int[]prices) {
    int lmsf = Integer.MAX_VALUE; //left min so far
    int opr = 0; //overall best profit

    for(int i=0; i < prices.length;i++) {
        if(prices[i] < lmsf) {
            lmsf = prices[i];
        }

        int pr = prices[i] - lmsf; //ith day is selling day

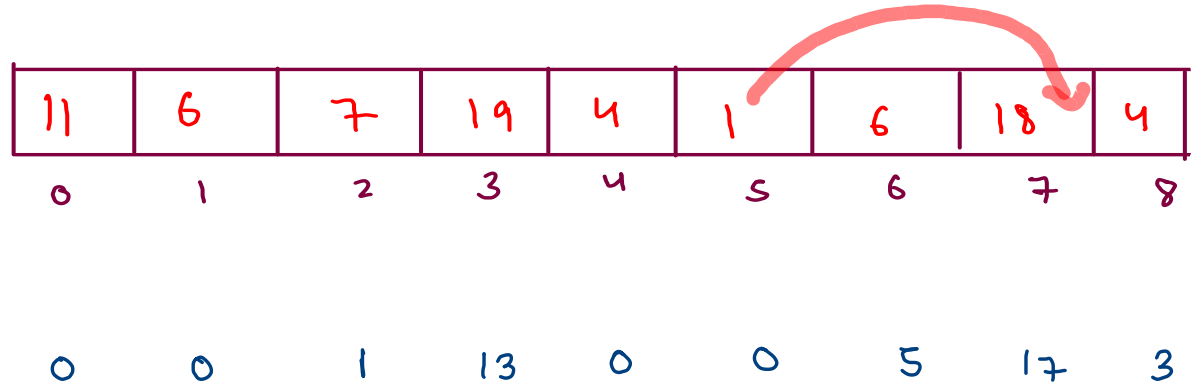
        if(pr > opr) {
            opr = pr;
        }
    }

    return opr;
}

```

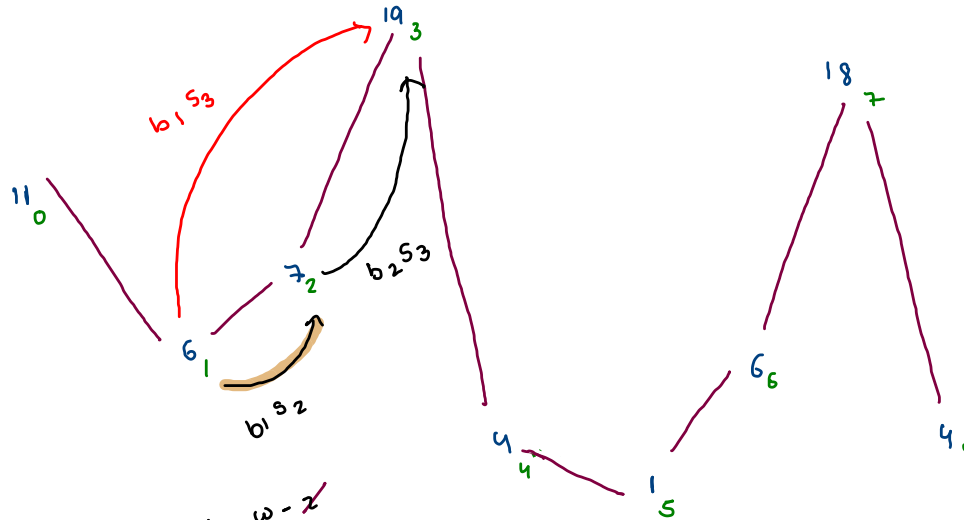
$lmsf = 1$   
~~4~~  
~~6~~  
~~11~~  
~~19~~

$opr = 0$   
~~1~~  
~~4~~  
~~13~~  
~~17~~



# Buy And Sell Stocks - Infinite Transactions Allowed

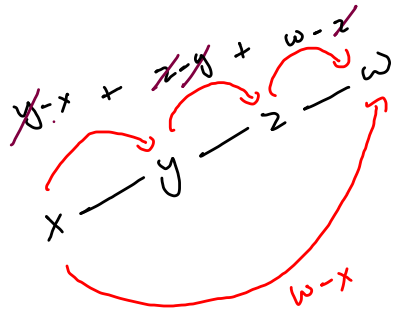
11	6	7	19	4	1	6	18	4
0	1	2	3	4	5	6	7	8



(i) overlapping transactions are not allowed.

$$b_1s_k + b_k s_j \rightarrow b_1s_j$$

$$= -p[i] + p[k] - p[k] + p[j]$$



$$b_1s_3 \rightarrow -6 + 19$$

$$b_1s_2 + b_2s_3 \rightarrow -6 + 7 - 7 + 19$$

$$b_1s_3 = b_1s_2 + b_2s_3$$

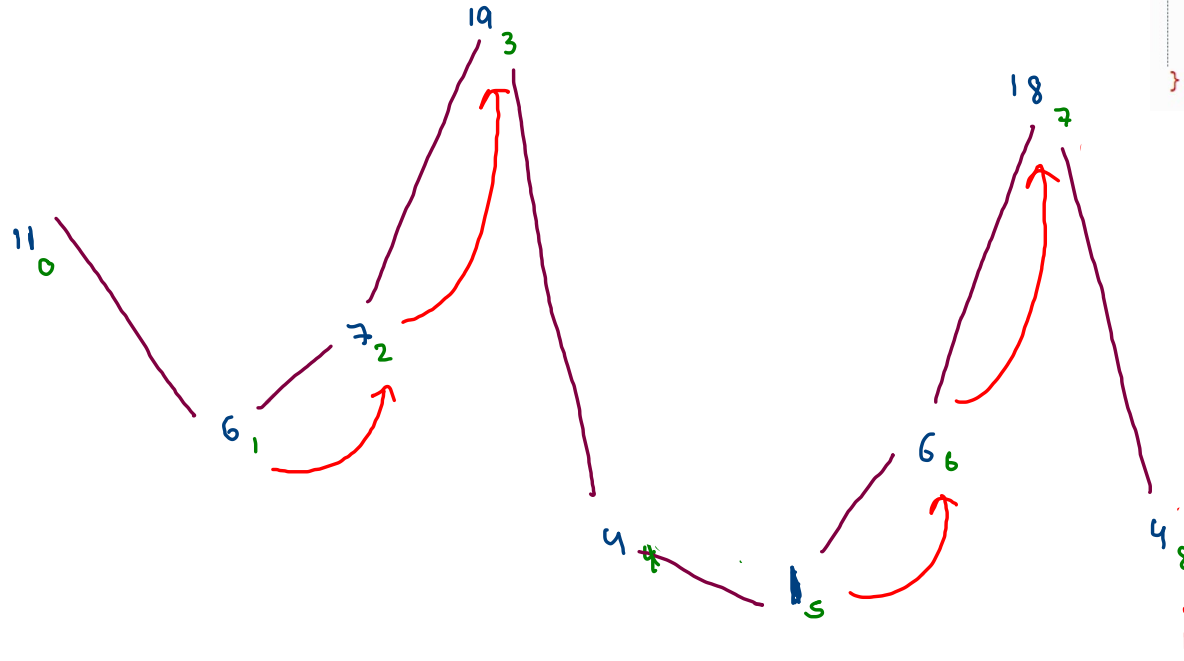
```

public static int infinite_transaction(int[] prices) {
    int acc = 0; //overall profit accumulator

    for(int i=0; i < prices.length - 1; i++) {
        if(prices[i] < prices[i+1]) {
            acc += (prices[i+1] - prices[i]);
        }
    }

    return acc;
}

```

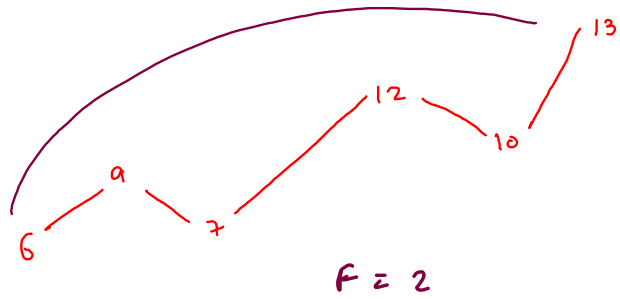


$$acc = 1 + 12 + 5$$

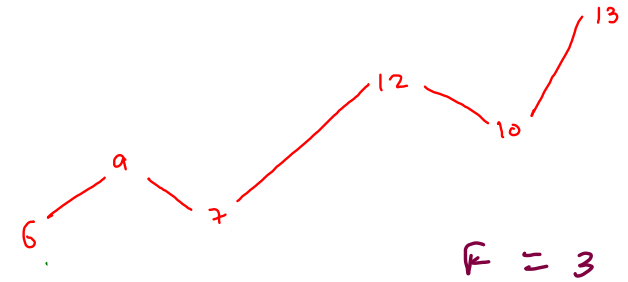
$$12$$

$$acc = \underline{30}$$

# Buy And Sell Stocks With Transaction Fee - Infinite Transactions Allowed



	bs	ss
6 <sub>0</sub>	-6 b <sub>0</sub>	0 .
9 <sub>1</sub>	-6 b <sub>0</sub>	1 b <sub>0</sub> s <sub>1</sub>
7 <sub>2</sub>	-6 b <sub>0</sub>	1 b <sub>0</sub> s <sub>1</sub>
12 <sub>3</sub>	-6 b <sub>0</sub>	4 b <sub>0</sub> s <sub>3</sub>
10 <sub>4</sub>	-6 b <sub>0</sub>	4 b <sub>0</sub> s <sub>3</sub>
13 <sub>5</sub>	-6 b <sub>0</sub>	5 b <sub>0</sub> s <sub>5</sub>



	bs	ss
6 <sub>0</sub>	-6 b <sub>0</sub>	0 .
9 <sub>1</sub>	-6 b <sub>0</sub>	0 .
7 <sub>2</sub>	-6 b <sub>0</sub>	0 .
12 <sub>3</sub>	-6 b <sub>0</sub>	3 b <sub>0</sub> s <sub>3</sub>
10 <sub>4</sub>	-6 b <sub>0</sub>	3 b <sub>0</sub> s <sub>3</sub>
13 <sub>5</sub>	-6 b <sub>0</sub>	4 b <sub>0</sub> s <sub>5</sub>

12 10 15 17 20  
16 18 22 20 22  
20 23 25 3

	buy state	sell state
10 <sub>0</sub>	-10 b <sub>0</sub>	0
15 <sub>1</sub>	-10 b <sub>0</sub>	2 b <sub>0</sub> s <sub>1</sub>
17 <sub>2</sub>	-10 b <sub>0</sub>	4 b <sub>0</sub> s <sub>2</sub>
20 <sub>3</sub>	-10 b <sub>0</sub>	2 b <sub>0</sub> s <sub>3</sub>
16 <sub>4</sub>	-9 b <sub>0</sub> s <sub>3</sub> b <sub>4</sub>	7 b <sub>0</sub> s <sub>3</sub>
18 <sub>5</sub>	-9 b <sub>0</sub> s <sub>3</sub> b <sub>4</sub>	7 b <sub>0</sub> s <sub>3</sub>
22 <sub>6</sub>	-9 b <sub>0</sub> s <sub>3</sub> b <sub>4</sub>	10 b <sub>0</sub> s <sub>3</sub> b <sub>4</sub> s <sub>6</sub>
20 <sub>7</sub>	-9 b <sub>0</sub> s <sub>3</sub> b <sub>4</sub>	10 b <sub>0</sub> s <sub>3</sub> b <sub>4</sub> s <sub>6</sub>
22 <sub>8</sub>	-9 b <sub>0</sub> s <sub>3</sub> b <sub>4</sub>	10 b <sub>0</sub> s <sub>3</sub> b <sub>4</sub> s <sub>6</sub>
20 <sub>9</sub>	-9 b <sub>0</sub> s <sub>3</sub> b <sub>4</sub>	10 b <sub>0</sub> s <sub>3</sub> b <sub>4</sub> s <sub>6</sub>
23 <sub>10</sub>	-9 b <sub>0</sub> s <sub>3</sub> b <sub>4</sub>	11 b <sub>0</sub> s <sub>3</sub> b <sub>4</sub> s <sub>10</sub>
25 <sub>11</sub>	-9 b <sub>0</sub> s <sub>3</sub> b <sub>4</sub>	13 b <sub>0</sub> s <sub>3</sub> b <sub>4</sub> s <sub>11</sub>

fee = 3

buy state:

→ one extra 'b'  
→ end at b

sell state:

→ no. of b =  
no. of s.

obsp, ossp

$$i \begin{cases} \text{nbsp} = \max(\text{obsp}, \text{ossp} - p[i]) ; \\ \text{hssp} = \max(\text{ossp}, \text{obsp} + p[i] - \text{fee}) ; \end{cases}$$

```

public static int infinite_transactions_with_fee(int[] prices, int fee) {
    int obsp = -prices[0]; //old buy state profit
    int ossp = 0; //old sell state profit

    for(int i=1; i < prices.length; i++) {
        int nbsp = Math.max(osp, ossp - prices[i]); //new buy state profit
        int nssp = Math.max(osp, obsp + prices[i] - fee); //new sell state profit

        obsp = nbsp;
        ossp = nssp;
    }

    return ossp;
}

```

jees = 3

days	buy state	sell state
15 <sub>0</sub>	-15	0
10 <sub>1</sub>	-10	0
17 <sub>2</sub>	-10	4
20 <sub>3</sub>	-10	7
16 <sub>4</sub>	-9	7
18 <sub>5</sub>	-9	7
22 <sub>6</sub>	-9	10
20 <sub>7</sub>	-9	10
23 <sub>8</sub>	-9	11
25 <sub>9</sub>	-9	13



12 10 15 17 20  
16 18 22 20 22  
20 23 25

	buy state	sell state	cooldown
10 <sub>0</sub>	-10 b <sub>0</sub>	0 .	0 .
15 <sub>1</sub>	-10 b <sub>0</sub>	5 b <sub>0</sub> s <sub>1</sub>	0 .
17 <sub>2</sub>	-10 b <sub>0</sub>	7 b <sub>0</sub> s <sub>2</sub>	5 b <sub>0</sub> s <sub>1</sub> c <sub>2</sub>
20 <sub>3</sub>	-10 b <sub>0</sub>	10 b <sub>0</sub> s <sub>3</sub>	7 b <sub>0</sub> s <sub>2</sub> c <sub>3</sub>
16 <sub>4</sub>	-9 b <sub>0</sub> s <sub>2</sub> c <sub>3</sub> b <sub>4</sub>	10 b <sub>0</sub> s <sub>3</sub>	10 b <sub>0</sub> s <sub>3</sub> c <sub>4</sub>
18 <sub>5</sub>	-8 b <sub>0</sub> s <sub>3</sub> c <sub>4</sub> b <sub>5</sub>	10 b <sub>0</sub> s <sub>3</sub>	10 b <sub>0</sub> s <sub>3</sub> c <sub>4</sub>
22 <sub>6</sub>	-8 b <sub>0</sub> s <sub>3</sub> c <sub>4</sub> b <sub>5</sub>	14 b <sub>0</sub> s <sub>3</sub> c <sub>4</sub> b <sub>5</sub> s <sub>6</sub>	10 b <sub>0</sub> s <sub>3</sub> c <sub>4</sub>
20 <sub>7</sub>	-8 b <sub>0</sub> s <sub>3</sub> c <sub>4</sub> b <sub>5</sub>	14 b <sub>0</sub> s <sub>3</sub> c <sub>4</sub> b <sub>5</sub> s <sub>6</sub>	14 b <sub>0</sub> s <sub>3</sub> c <sub>4</sub> b <sub>5</sub> s <sub>6</sub> c <sub>7</sub>
22 <sub>8</sub>	-8 b <sub>0</sub> s <sub>3</sub> c <sub>4</sub> b <sub>5</sub>	14 b <sub>0</sub> s <sub>3</sub> c <sub>4</sub> b <sub>5</sub> s <sub>6</sub>	14 b <sub>0</sub> s <sub>3</sub> c <sub>4</sub> b <sub>5</sub> s <sub>6</sub> c <sub>7</sub>
20 <sub>9</sub>	-6 b <sub>0</sub> s <sub>3</sub> c <sub>4</sub> b <sub>5</sub> s <sub>6</sub> c <sub>7</sub> b <sub>9</sub>	14 b <sub>0</sub> s <sub>3</sub> c <sub>4</sub> b <sub>5</sub> s <sub>6</sub>	14 b <sub>0</sub> s <sub>3</sub> c <sub>4</sub> b <sub>5</sub> s <sub>6</sub> c <sub>7</sub>
23 <sub>10</sub>	-6 b <sub>0</sub> s <sub>3</sub> c <sub>4</sub> b <sub>5</sub> s <sub>6</sub> c <sub>7</sub> b <sub>9</sub>	17 <u>b<sub>0</sub>s<sub>3</sub>c<sub>4</sub>b<sub>5</sub>s<sub>6</sub>c<sub>7</sub>b<sub>9</sub>s<sub>10</sub></u>	14 b <sub>0</sub> s <sub>3</sub> c <sub>4</sub> b <sub>5</sub> s <sub>6</sub> c <sub>7</sub>

→ buy state

extra b

→ sell state

no. of s = no. of b

→ coolstate

extra c

ob, os, oc

$$nb = \max(ob, oc - p[i]);$$

$$ns = \max(os, ob + p[i]);$$

$$nc = \max(oc, os + 0);$$