

Search 3

1. Write an efficient algorithm that searches for a value in a  $m \times n$  matrix. This matrix has the following properties:  
 a). Integers in each row are sorted from left to right.  
 b). The first integer of each row is greater than the last integer of the previous row.

pot. row

	0	1	2	3	4
0	10	19	25	38	40
1	42	49	53	56	58
2	62	64	68	72	76
3	79	82	88	92	100
4	102	110	150	190	200

key = 70

(i) to find potential row.

(ii) to find element in this potential row.

(i) row wise sorted

(ii) col wise sorted

(iii) prev row's last < next row's start

linear search  $\rightarrow n$

binary search  $\rightarrow \log_2 n$

$$n, \frac{n}{2}, \frac{n}{4}, \dots, 1$$

$$a = n$$

$$cr = \frac{1}{2}$$

$$a^{k-1} = 1$$

$$n \times \left(\frac{1}{2}\right)^{k-1} = 1$$

$$n = (2)^{k-1}$$

$$\log_2 n = (k-1)$$

$$k = \log_2 n + 1$$

$$lci = 4$$

	0	1	2	3	4
0	10	19	25	38	40
1	42	49	53	56	58
2	62	64	68	72	76
3	79	82	88	92	100
4	102	110	150	190	260

```

public static int potential_row(int[][] mat, int target) {
    int lo = 0;
    int hi = mat.length-1;
    int lci = mat[0].length-1; //last column index

    while(lo <= hi) {
        int mid = (lo + hi)/2;

        if(target >= mat[mid][0] && target <= mat[mid][lci])
            return mid;
        else if(target < mat[mid][0]) {
            hi = mid-1;
        }
        else {
            lo = mid+1;
        }
    }
}

```

$$val = 210$$

m hi

$$40 \quad 5$$

→

	0	1	2	3	4
0	10	19	25	38	40
1	42	49	53	56	58
2	62	64	68	72	76
3	79	82	88	92	100
4	102	110	150	190	200

43 , pr = 1

```

public static boolean search(int[][]matrix,int target) {
    //write your code here

    //to find potential row for this target element
    int pr = potential_row(matrix,target);

    if(pr == -1) {
        return false;
    }

    //to find whether target is actually there in potential row
    boolean ans = isElementPresent(matrix,target,pr);

    return ans;
}

public static int potential_row(int[][]mat,int target) {
    int lo = 0;
    int hi = mat.length-1;
    int lci = mat[0].length-1; //Last column index

    while(lo <= hi) {
        int mid = (lo + hi)/2;

        if(target >= mat[mid][0] && target <= mat[mid][lci]) {
            return mid;
        }
        else if(target < mat[mid][0]) {
            hi = mid-1;
        }
        else {
            lo = mid+1;
        }
    }

    return -1;
}

public static boolean isElementPresent(int[][]mat,int target,int r) {
    int lo = 0;
    int hi = mat[0].length-1;

    while(lo <= hi) {
        int mid = (lo + hi)/2;

        if(mat[r][mid] == target) {
            return true;
        }
        else if(mat[r][mid] > target){
            hi = mid-1;
        }
        else {
            lo = mid+1;
        }
    }

    return false;
}

```

1. You are given a number  $n$ , representing the number of rows and columns of a square matrix.
  2. You are given  $n * n$  numbers, representing elements of 2d array  $a$ .
- Note - Each row and column is sorted in increasing order.
3. You are given a number  $x$ .
  4. You are required to find  $x$  in the matrix and print it's location int (row, col) format as discussed in output format below.
  5. In case element is not found, print "Not Found".

	0	1	2	3	4
0	10	25	36	48	54
1	20	29	38	50	56
2	23	33	41	53	60
3	35	36	46	62	75

(i) row wise sorted  
(ii) col wise sorted

	c				
	0	1	2	3	4
0	10	25	36	48	54
1	20	29	38	50	56
2	23	33	41	53	60
3	35	36	46	62	75

r

find = 40

n+m

n → rows  
m → cols  
r = 0  
c = mat[0].length-1;

while (r < n && c >= 0) {

if (mat[r][c] == key) {

syso(r, c);

return;

else if (mat[r][c] > key) {

c--;

else {  
r++;

}

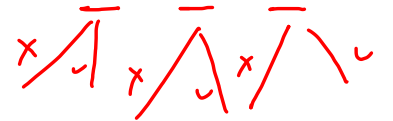
arr = [a b c]

Subarray

Subset

(i) a b c  
ab bc  
abc

- - -  
- - c  
- b -  
- b c  
a - -  
a - c  
a b -  
a b c



(ii)  $\frac{n(n+1)}{2}$

$$2 \times 2 \times 2 = 2^n$$

(iii) continuous

(iii) not continuous

arr:

a, b, c

0	→	0	0	0	→	-	-	-
1	→	0	0	1	→	-	-	c
2	→	0	1	0	→	-	b	-
3	→	0	1	1	→	-	b	c
4	→	1	0	0	→	a	-	-
5	→	1	0	1	→	a	-	c
6	→	1	1	0	→	a	b	-
7	→	1	1	1	→	a	b	c

0 → no choice

1 → yes choice

n length binary no.

$2^n$

0 to $2^n - 1$
----------------

a b c d

0  $\rightarrow$  0 0 0 0  $\rightarrow$  \_ \_ \_ \_

1  $\rightarrow$  0 0 0 1  $\rightarrow$  \_ \_ \_ \_

2  $\rightarrow$  0 0 1 0  $\rightarrow$  \_ \_ c \_

⋮

15  $\rightarrow$  1 1 1 1  $\rightarrow$  a b c d



```

public static void print_subsets(int[] arr) {
    int n = arr.length;
    int ts = (int) Math.pow(2, n); //total subsets

    for(int k = 0; k < ts; k++) {
        //we want k's binary representation of length 'n'
        int[] bin = decToBin(k, n);

        //print subset
        for(int i = 0; i < n; i++) {
            if(bin[i] == 0) {
                //ith element is excluded from this subset
                System.out.print("-\t");
            }
            else {
                //ith element is included in this subset
                System.out.print(arr[i] + "\t");
            }
        }

        System.out.println();
    }
}

public static int[] decToBin(int dec, int len) {
    int[] arr = new int[len];
    int idx = len - 1;

    while(dec > 0) {
        int d = dec % 2;
        dec = dec / 2;

        arr[idx] = d;
        idx--;
    }

    return arr;
}

```

arr :      1 0      2 0      3 0  
             0        1        2

ts =        8                n = 3

0	→	<div style="border: 1px solid black; padding: 2px; display: inline-block;">0   0   0</div>	.	—	—	—
1	→	<div style="border: 1px solid black; padding: 2px; display: inline-block;">0   0   1</div>		—	—	3 0
2	→	<div style="border: 1px solid black; padding: 2px; display: inline-block;">0   1   0</div>		—	2 0	—
3	→	<div style="border: 1px solid black; padding: 2px; display: inline-block;">0   1   1</div>		—	2 0	3 0
4	→	<div style="border: 1px solid black; padding: 2px; display: inline-block;">1   0   0</div>		1 0	—	—
5	→	<div style="border: 1px solid black; padding: 2px; display: inline-block;">1   0   1</div>		1 0	—	3 0
6	→	<div style="border: 1px solid black; padding: 2px; display: inline-block;">1   1   0</div>		1 0	2 0	—
7	→	<div style="border: 1px solid black; padding: 2px; display: inline-block;">1   1   1</div>		1 0	2 0	3 0