

# Minimum Stack - I

9 6 5 8 2 4 -

```
public MinStack() {  
    allData = new Stack<>();  
    minData = new Stack<>();  
}
```

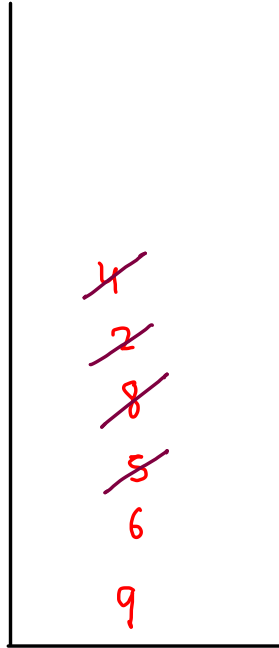
```
int size() {  
    // write your code here  
}
```

```
void push(int val) {  
    // write your code here  
}
```

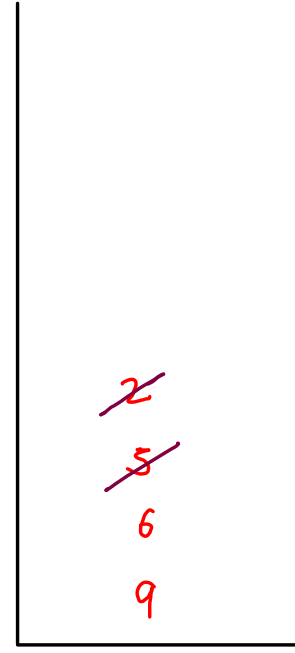
```
int pop() {  
    // write your code here  
}
```

```
int top() {  
    // write your code here  
}
```

```
int min(){  
    // write your code here  
}
```



allData



minData

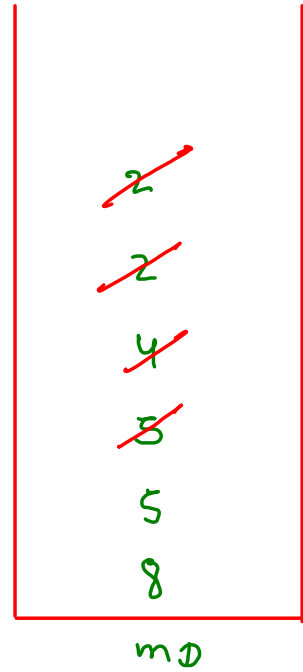
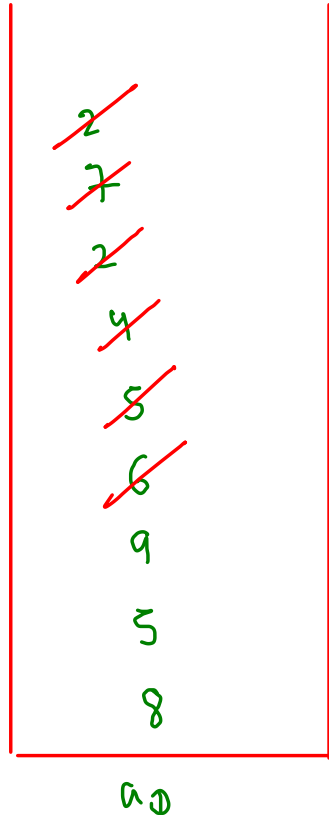
extra space

→ minData

T:  $O(1)$

S:  $O(n)$

data stream: 8 5 9 6 5 4 2 7 2



```

int pop() {
    if(allData.size() == 0) {
        System.out.println("Stack underflow");
        return -1;
    }
    else {
        int val = allData.pop();

        if(minData.peek() == val) {
            minData.pop();
        }

        return val;
    }
}

```

```

int top() {
    if(allData.size() == 0) {
        System.out.println("Stack underflow");
        return -1;
    }
    else {
        return allData.peek();
    }
}

```

```

int min(){
    if(allData.size() == 0) {
        System.out.println("Stack underflow");
        return -1;
    }
    else {
        return minData.peek();
    }
}

```

```

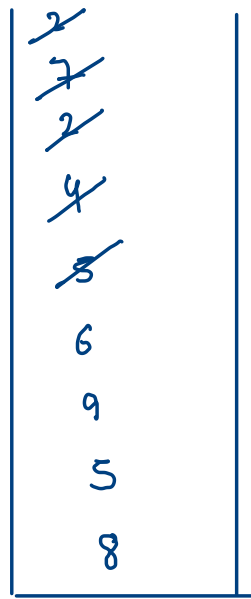
int size() {
    return allData.size();
}

void push(int val) {
    allData.push(val);

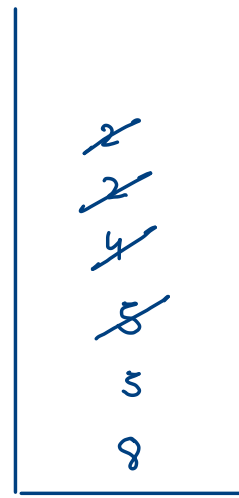
    if(minData.size() == 0 || val <= minData.peek()) {
        minData.push(val);
    }
}

```

data stream: 8 5 9 6 5 4 2 7 2



all



min

## Minimum Stack - Constant Space

data stream: 8 10 6 9 5 12 3 7 2

T :  $O(1)$

S :  $O(1)$

<del>1 (2+2-3)</del>
<del>7</del>
<del>1 (3+3-5)</del>
12
4 (5+5-6)
9
4 (6+6-8)
10
8

encode  $\rightarrow (val + val - min)$   $\swarrow (val < min)$

min = ~~8~~ ~~5~~

fake vs real

TV  $\rightarrow$  min

omin  $\rightarrow$

$val + val - omin = st.peek()$

$omin = 2 * val - st.peek()$

data stream: 8 10 6 9 5 12 3 7 2

	val	min
<del>1 (2+2-3)</del>	<del>2</del>	<del>2</del>
<del>7</del>	<del>7</del>	<del>3</del>
<del>1 (3+3-5)</del>	<del>3</del>	<del>3</del>
<del>12</del>	<del>12</del>	<del>5</del>
<del>4 (5+5-6)</del>	<del>5</del>	<del>5</del>
<del>9</del>	<del>9</del>	<del>6</del>
<del>4 (6+6-8)</del>	<del>6</del>	<del>6</del>
<del>10</del>	<del>10</del>	<del>8</del>
8	8	8

min = ~~∞~~ 8

```

if (val < min) {
    encode → (val + val - min) →
    st.push(encode);
    min = val;
}
else {
    st.push(val);
}

```

why

val > val + val - min  
 ↓  
 -ve

rv → min

rv + rv - omin = st.push()

omin = rv \* 2 - st.push()

if (val < min)

fake\_val =

$$\text{val} + \frac{\text{val} - \text{min}}{-ve}$$

identify  
decode

val

>

$$\text{val} + \frac{\text{val} - \text{min}}{\downarrow, -ve}$$

why  
not  $\nearrow$  val - min

data stream: 4 -1 3 -2

✓  
fu: val + val - min

val	
<del>-3</del>	-2
3	3
-6	-1
4	4

-1  
min = ~~4~~

✗  
fu: val - min

we can not identify val b/w fake vs real	
<div>-1</div>	-2
3	3
-5	-1
4	4

min = ~~4~~  
~~4~~  
~~-2~~

$$\begin{aligned} & -2 - (-1) \\ & = -1 \end{aligned}$$

data stream: 8 10 6 9 5 12 13 7 2

```
int pop() {
    if (data.size() == 0) {
        System.out.println("Stack underflow");
        return -1;
    } else {
        if (data.peek() < min) {
            //data.peek() is a fake value
            int rv = min;
            int omin = 2 * rv - data.pop();
            min = omin;
            return rv;
        } else {
            //data.peek() is a real value
            return data.pop();
        }
    }
}
```

```
int top() {
    if (data.size() == 0) {
        System.out.println("Stack underflow");
        return -1;
    } else {
        if (data.peek() < min) {
            //data.peek() is a fake value
            return min;
        } else {
            //data.peek() is a real value
            return data.peek();
        }
    }
}
```

```
void push(int val) {
    if (data.size() == 0) {
        data.push(val);
        min = val;
        return;
    }

    if (val < min) {
        int enc = val + (val - min);
        data.push(enc);

        min = val;
    } else {
        data.push(val);
    }
}
```

```
int min() {
    if (data.size() == 0) {
        System.out.println("Stack underflow");
        return -1;
    } else {
        return min;
    }
}
```

~~-1 (2+2-5)~~  
~~7~~  
~~13~~  
~~12~~  
~~4 (5+5-6)~~  
~~9~~  
~~4 (6+6-8)~~  
10  
8

min = 8



```
TwoStack st = new TwoStack(n);
```

```
public static class TwoStack {  
    int[] data;  
    int tos1;  
    int tos2;  
  
    public TwoStack(int cap) {  
        // write your code here  
    }  
  
    int size1() {  
        // write your code here  
    }  
  
    int size2() {  
        // write your code here  
    }  
  
    void push1(int val) {  
        // write your code here  
    }  
  
    void push2(int val) {  
        // write your code here  
    }  
  
    int pop1() {  
        // write your code here  
    }  
  
    int pop2() {  
        // write your code here  
    }  
  
    int top1() {  
        // write your code here  
    }  
  
    int top2() {  
        // write your code here  
    }  
}
```

tos2 6

5

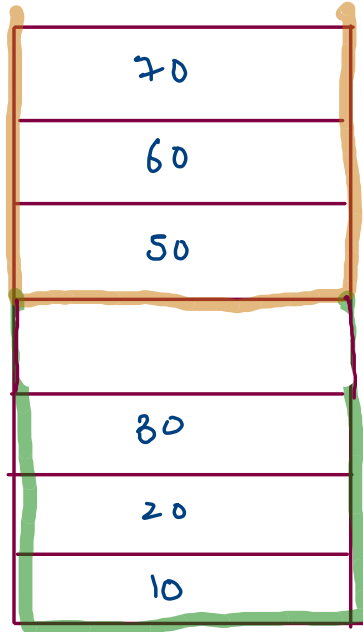
4

3

tos1 2

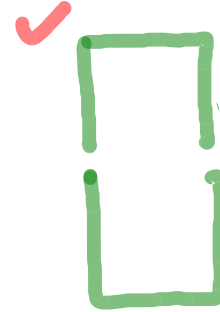
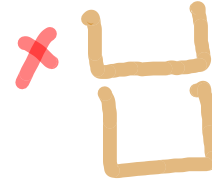
1

0



data

not able to manage  
space efficiently



space  
efficient

push1(10)

push1(20)

push1(30)

push1(40)

push2(50)

push2(60)

push2(70)

pop1() -> 40

push2() X

$$n = 7$$

```

public static class TwoStack {
    int[] data;
    int tos1;
    int tos2;

    public TwoStack(int cap) {
        // write your code here
    }

    int size1() {
        // write your code here
    }

    int size2() {
        // write your code here
    }

    void push1(int val) {
        // write your code here
    }

    void push2(int val) {
        // write your code here
    }

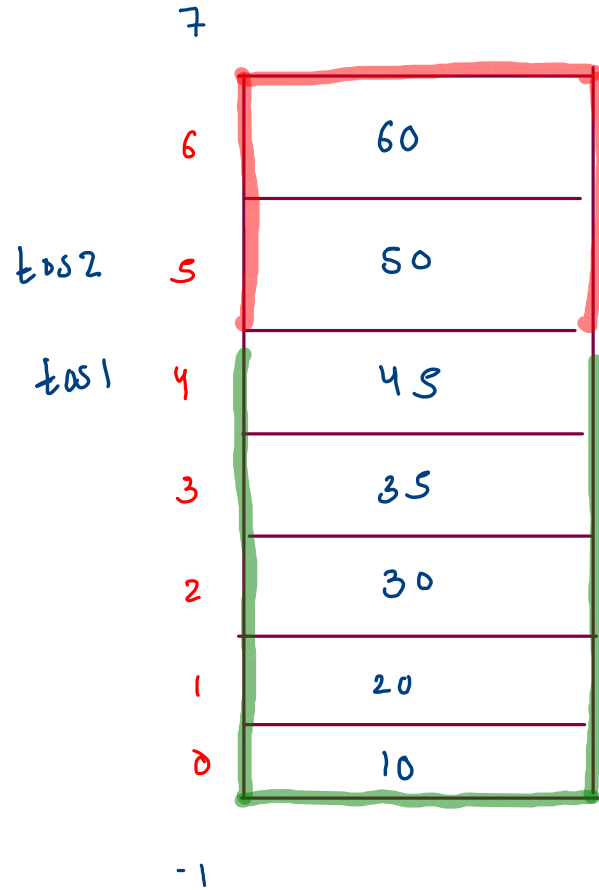
    int pop1() {
        // write your code here
    }

    int pop2() {
        // write your code here
    }

    int top1() {
        // write your code here
    }

    int top2() {
        // write your code here
    }
}

```



push1(10)

push1(20)

push2(60)

push2(50)

push2(40)

push1(30)

push1(35)

push2(38) → of

pop2 →  
push1(45)