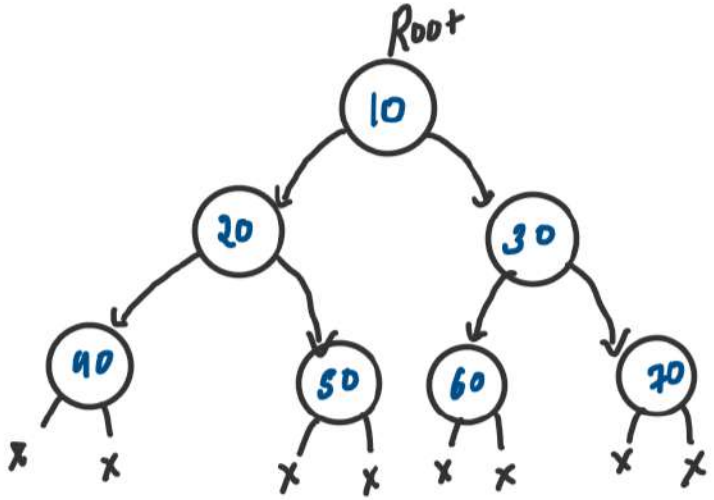
03/12/2023

BINARY TREE
CLASS - 2

1. Balanced Binary Tree (Leetcode-110)

Input



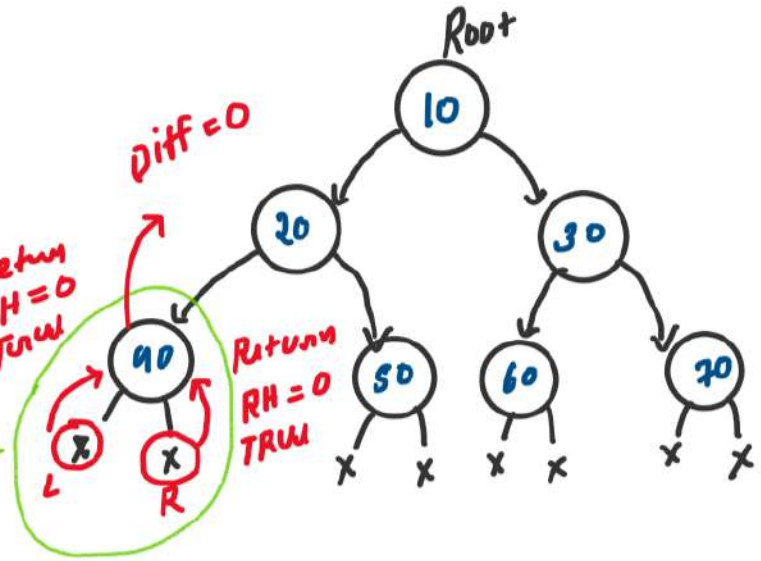
Output TRUE

What is Balanced Binary Tree?

Left and Right Sub Tree Ki height Ka diff.n at most 1 Hona chaiye.

$$LH - RH \in [0, 1]$$

Logic Building



Leaf Node

Leaf Node Ki Right and Left Node Ko Balanced Mano

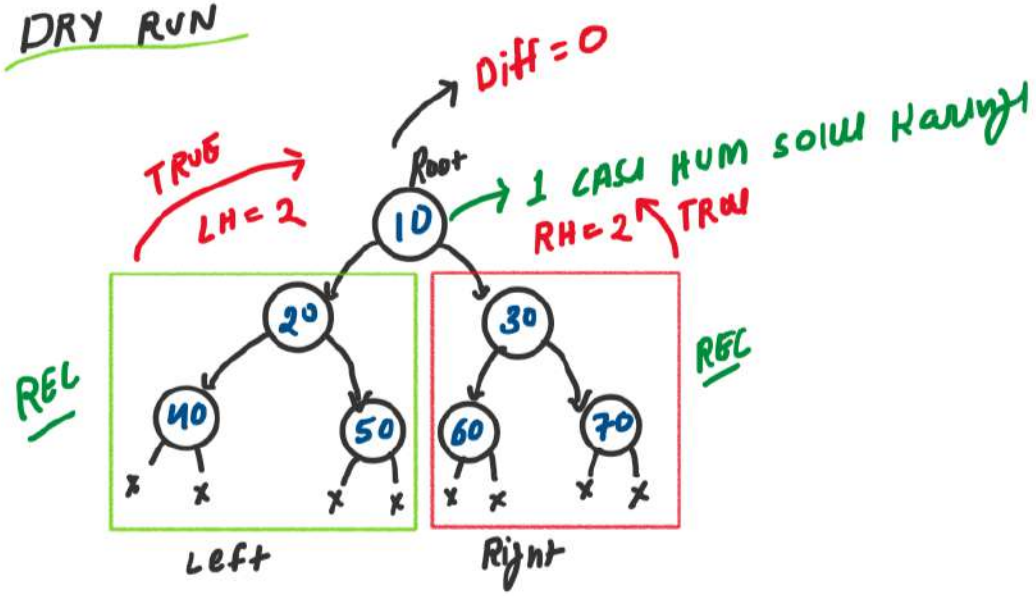
Balanced True Kab Hoga

- Left Sub Height (LH) = Balanced
- Right Sub Height (RH) = Balanced
- Diff ⇒ abs(LH - RH) <= 1

B.C.

```
if( Root == NULL)
{
  // Balanced True mano Leaf Node Ko
     return True
}
```

DRY RUN



Base case

```
if ( Root == NULL )
    return True
```

1 CASE HUM SOLVE KARNGE

LH = 2

RH = 2

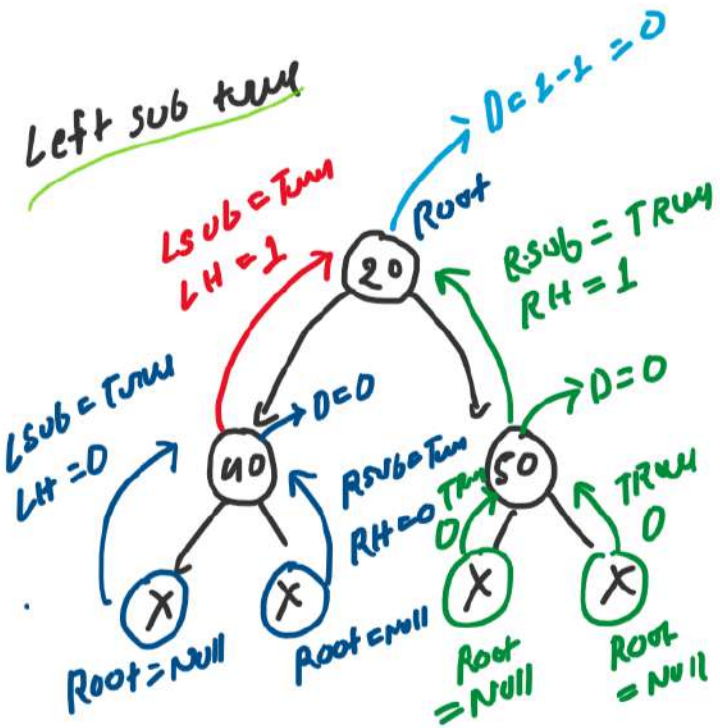
Diff = 0 ⇒ LH − RH = 2 − 2 = 0

REC

Lsub = True

Rsub = True

```
if ( Diff <= 1 && Lsub && Rsub )
{
    Return True;
}
else
{
    Return False;
}
```



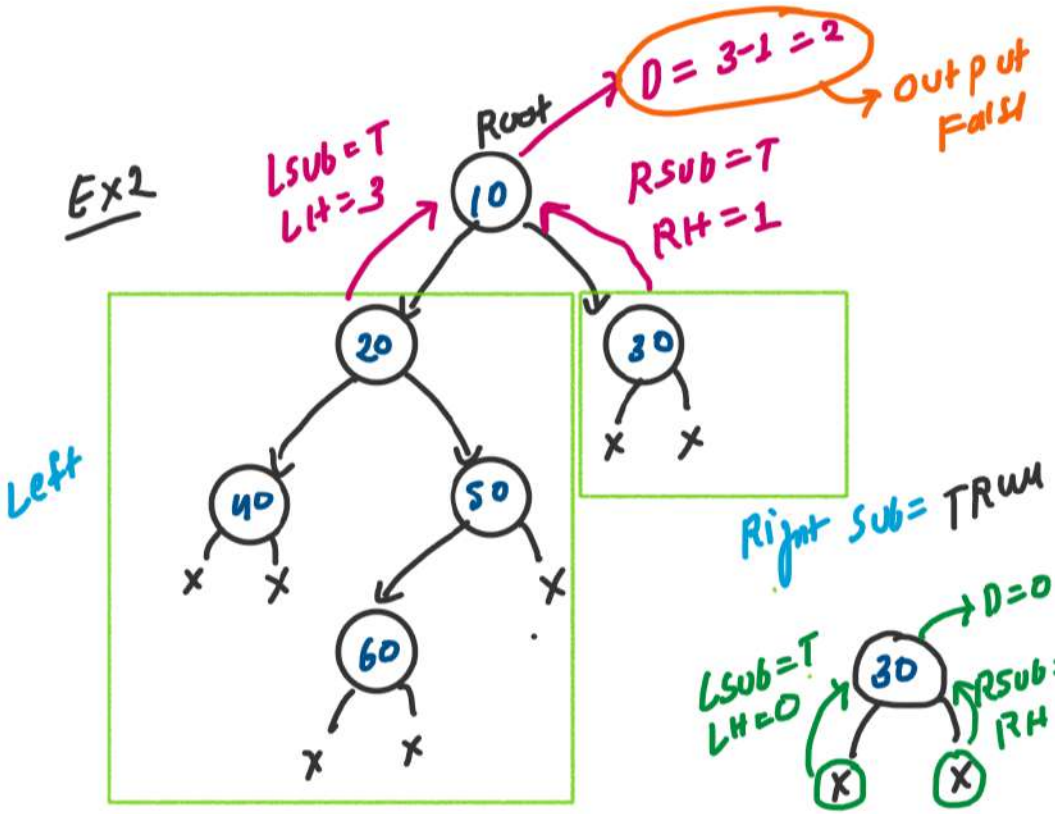
Left sub tree Balanced Hai

↳ DL = 1 and LSub = True and RSub = True

↳ Issi way me Right sub Tree check Hogi Hi wo Balanced Hai ya Nahi

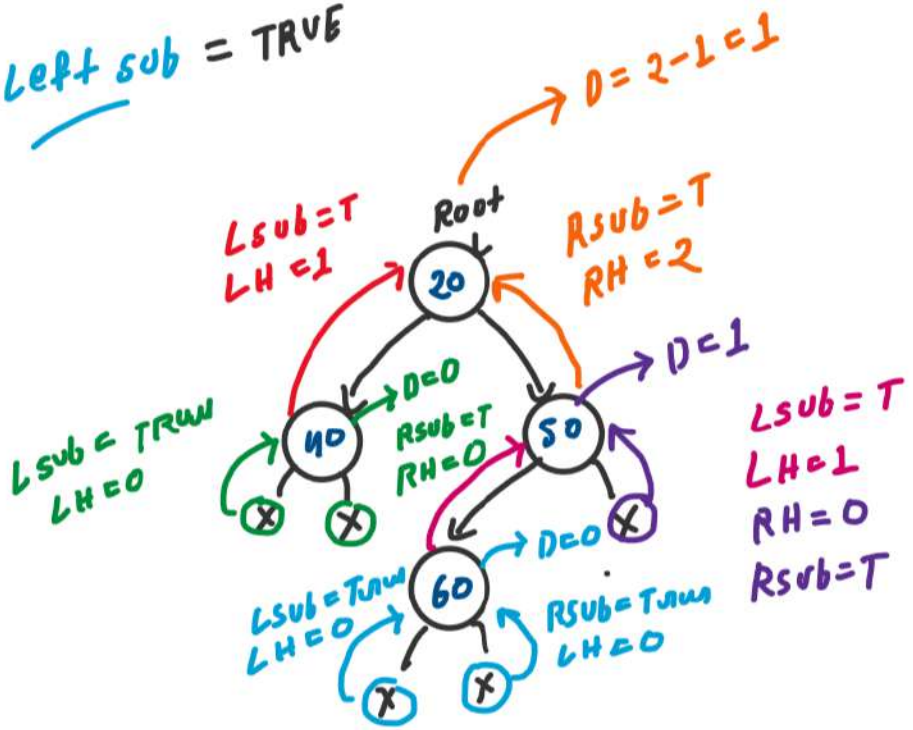
DL = 1 and LSub = True and RSub = True

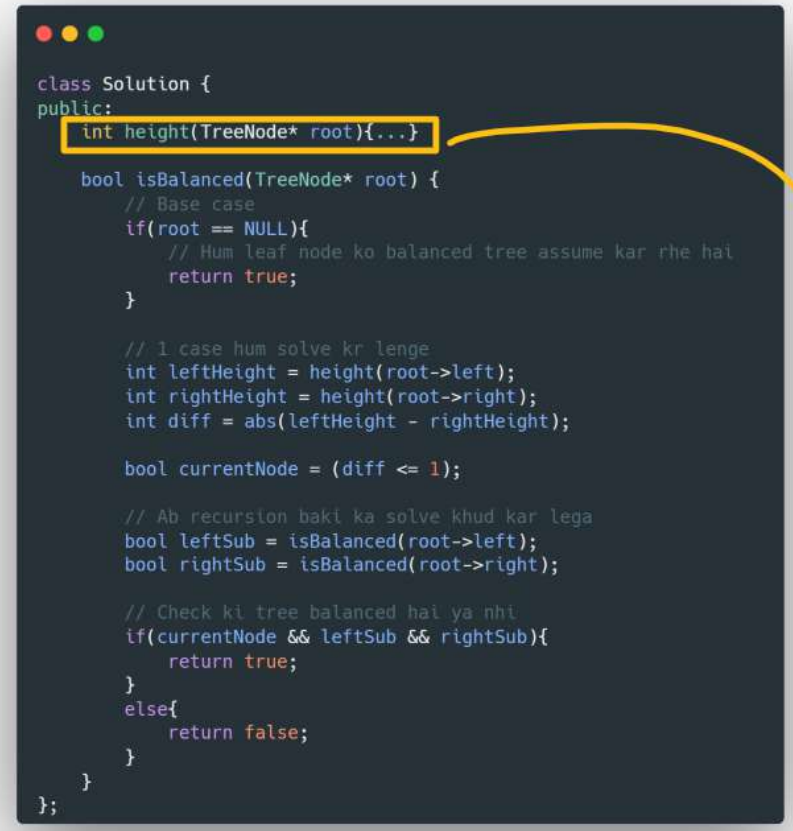
Ex2



Output = False

Left sub = TRUE





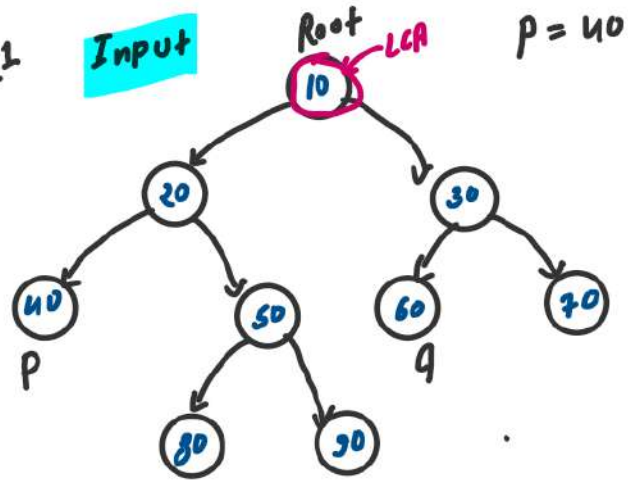
```
class Solution {
public:
    int height(TreeNode* root){...}

    bool isBalanced(TreeNode* root) {
        // Base case
        if(root == NULL){
            // Hum leaf node ko balanced tree assume kar rhe hai
            return true;
        }

        // 1 case hum solve kr lenge
        int leftHeight = height(root->left);
        int rightHeight = height(root->right);
        int diff = abs(leftHeight - rightHeight);

        bool currentNode = (diff <= 1);

        // Ab recursion baki ka solve khud kar lega
        bool leftSub = isBalanced(root->left);
        bool rightSub = isBalanced(root->right);

        // Check ki tree balanced hai ya nhi
        if(currentNode && leftSub && rightSub){
            return true;
        }
        else{
            return false;
        }
    }
};
```

```
int height(TreeNode* root){
    if(root == NULL){
        return 0;
    }

    int leftH = height(root->left);
    int rightH = height(root->right);
    int finalH = max(leftH, rightH) + 1;

    return finalH;
}
```

T.C. =? and S.C. =?

2. Lowest Common Ancestor of a Binary Tree (Leetcode-236) ****

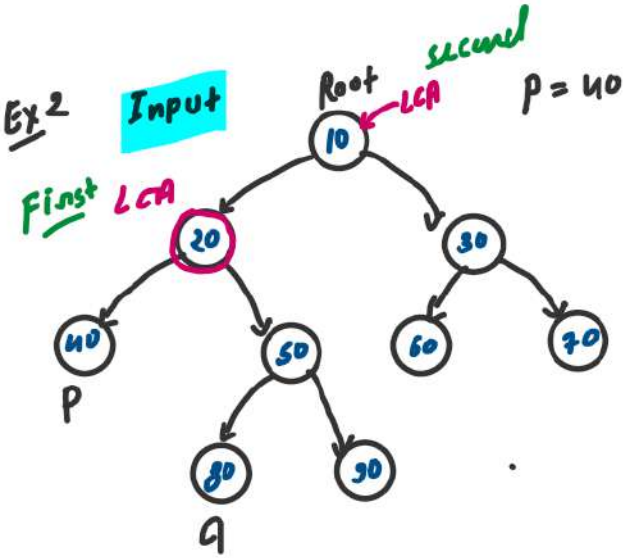
Ex 1 **Input**



p = 40 q = 60

Output 10

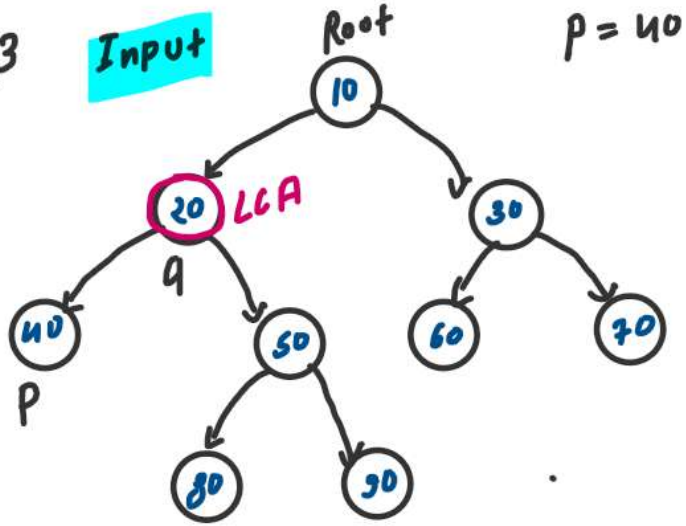
Ex 2 **Input**



p = 40 q = 80

Output 20 Always consider First LCA as output

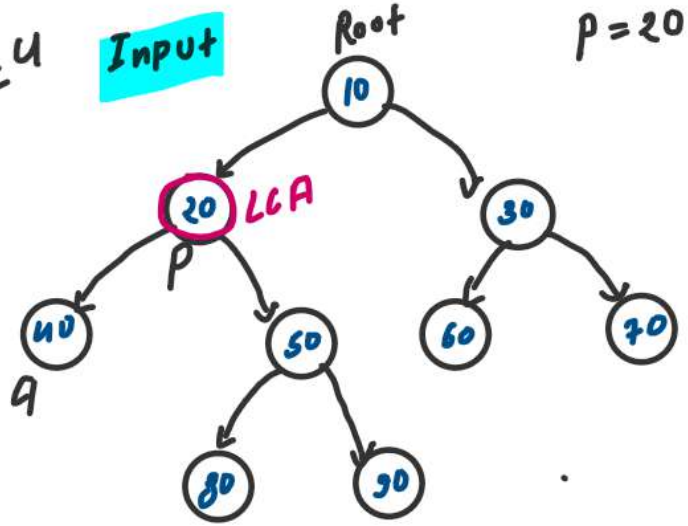
Ex 3 **Input**



p = 40 q = 20

Output 20

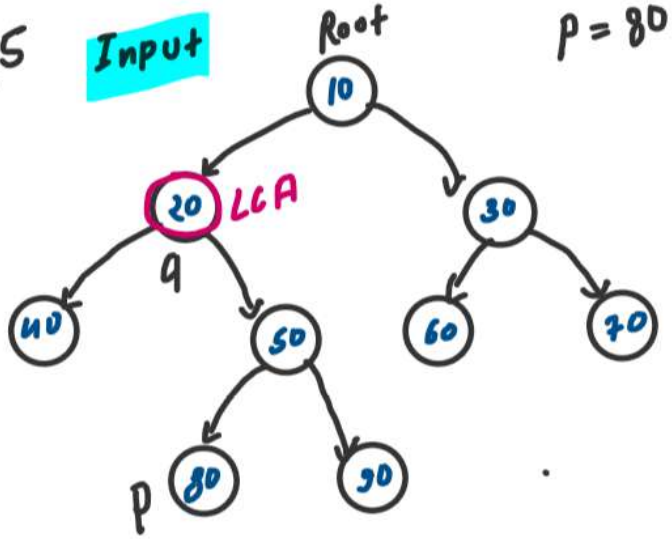
Ex 4 **Input**



p = 20 q = 40

Output 20

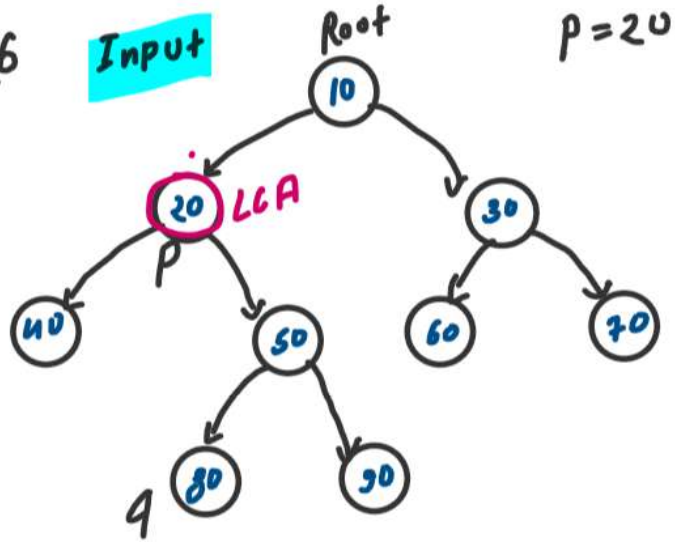
Ex 5 **Input**



p = 80 q = 20

Output 20

Ex 6 **Input**



p = 20 q = 80

Output 20

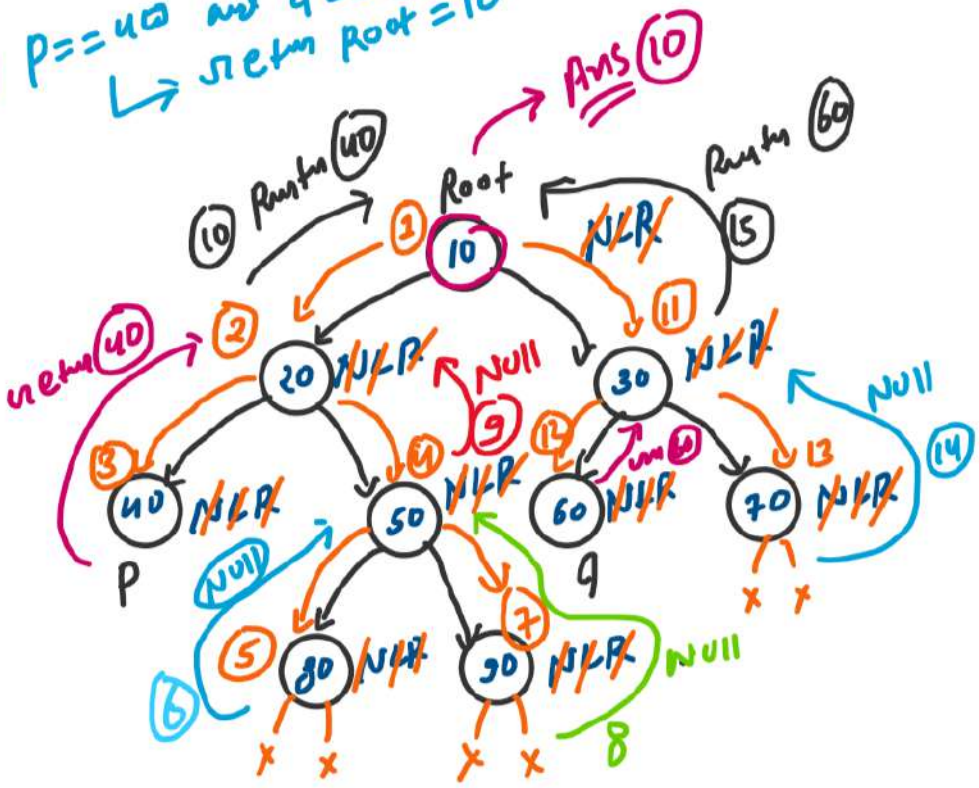
DRY RUN

EX1

P = 40

4 = 60

Output = 10



(1) First MUJHE P and 4 Ki location find Karni Hogi using Recursive Traversal

(1) 10 ≠ P & 10 ≠ 4

(2) 20 ≠ P & 20 ≠ 4

(3) 40 = P return P

(4) 50 ≠ P & 50 ≠ 4

(5) 80 ≠ P & 80 ≠ 4

(6) root == NULL return NULL

(7) 90 ≠ P & 90 ≠ 4

(8) root == NULL return NULL

(9) NULL and NULL return NULL

(10) 40 and NULL return 40

(11) 30 ≠ P & 30 ≠ 4

(12) 60 = 4 return 4

(13) 70 ≠ 4 & 70 ≠ P

(14) root == NULL return NULL

(15) 60 and NULL return 60

(16) P == 40 and 4 == 60 → return Root = 10

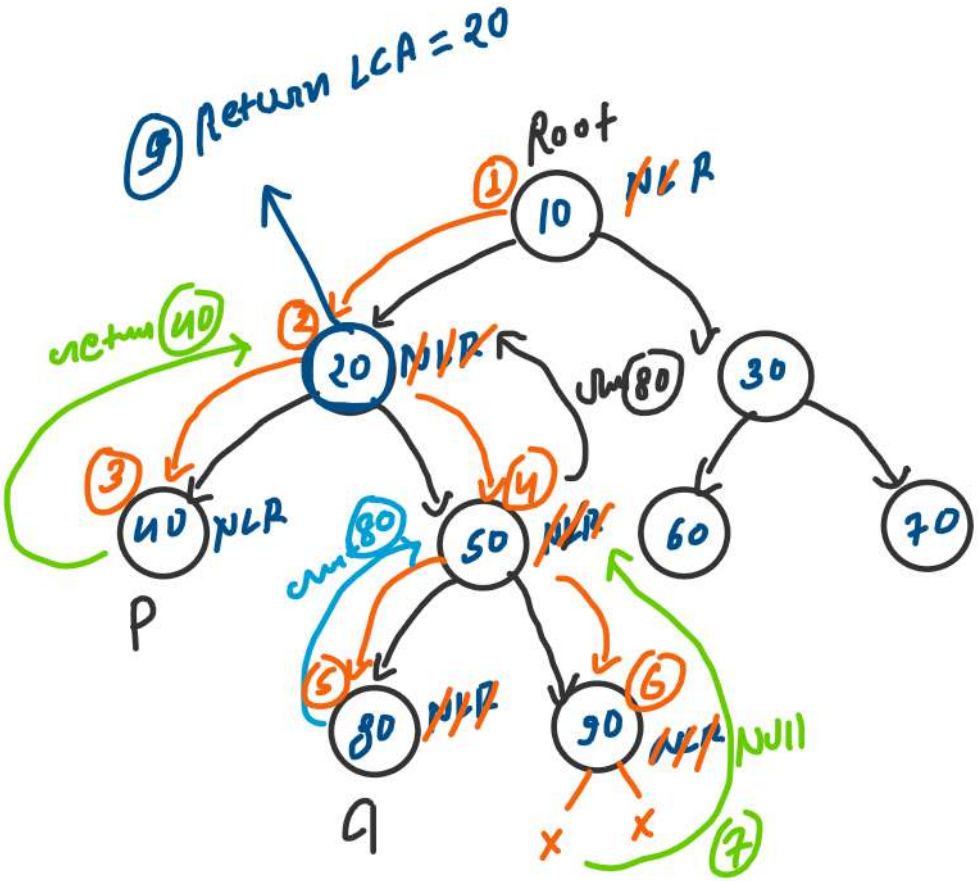
DRY RUN

GX2

p = 40

q = 80

O/P = 20



1. 10 ≠ 4 & 10 ≠ P
2. 20 ≠ 4 & 20 ≠ P
3. 40 == P Return P
4. 50 ≠ 4 & 50 ≠ P
5. 80 == 4 return q
6. 90 ≠ 4 & 90 ≠ P
7. root == NULL
   return NULL
8. 80 and NULL
   return 80
9. p == 40 and q == 80
   return root (LCA)

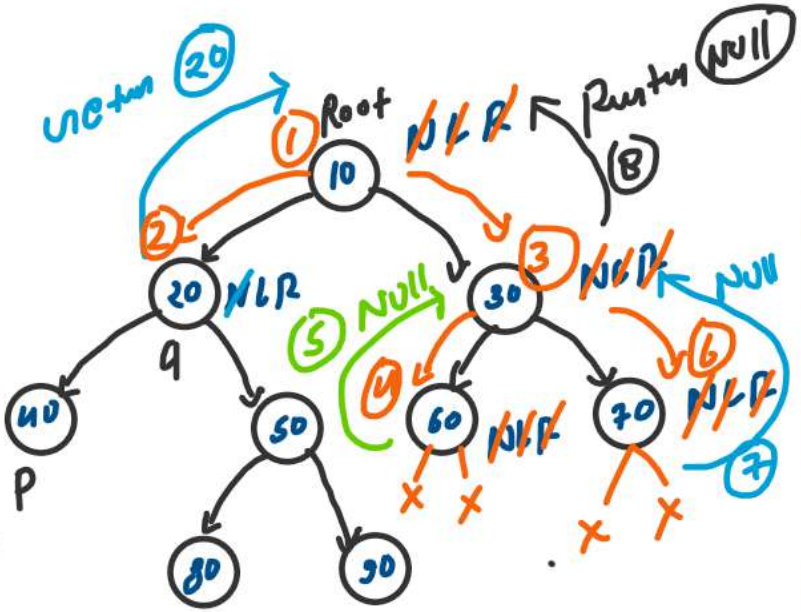
DRY RUN

EX 3

p = 40

q = 20

o/p = 20



(1) 10 ≠ p & 10 ≠ q

(2) 20 == q return q

(3) 30 ≠ p and q

(4) 60 ≠ p and q

(5) Root == NULL
return NULL

(6) 70 ≠ p and q

(7) root == NULL
return NULL

(8) NULL and NULL
return NULL

(9) q == 20 and NULL
↳ Return q as LCA

Ans = q

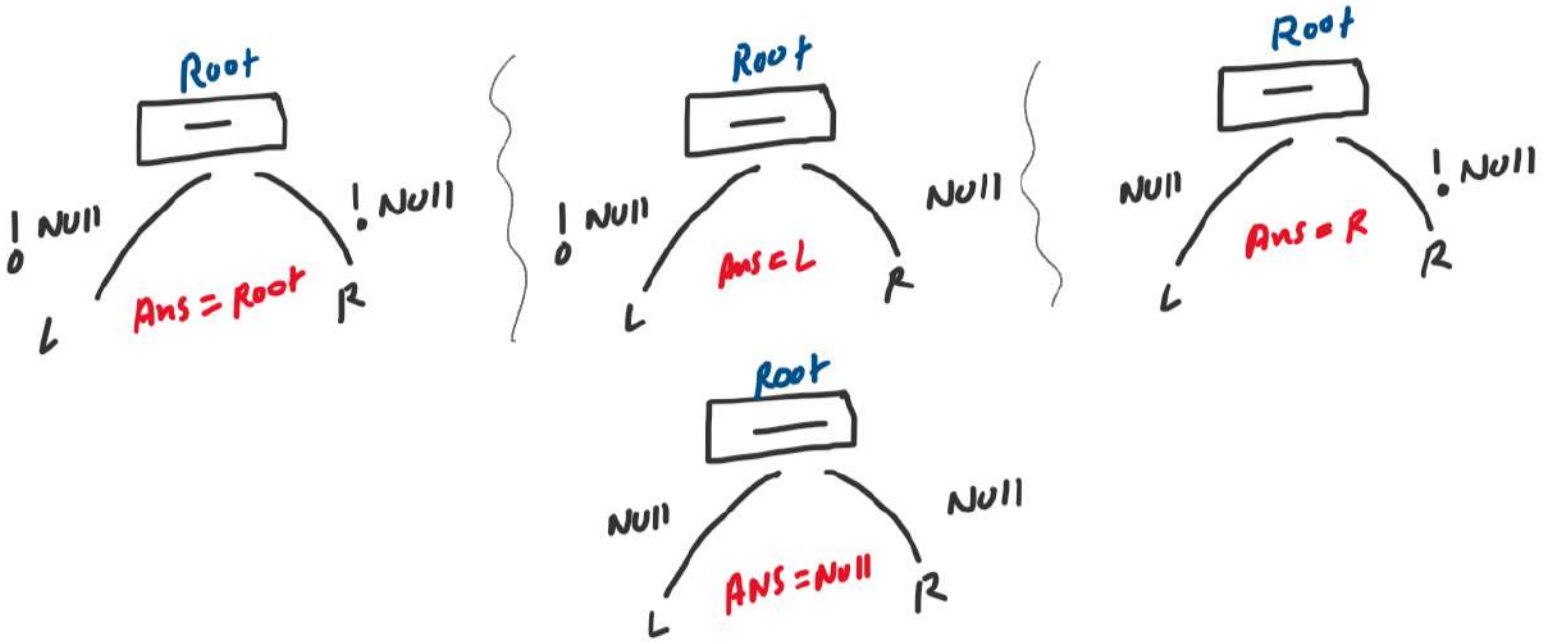
3 Base Cases

if(Root == NULL)
↳ return NULL

if(Root -> val == p->val)
↳ Return p

if (Root->val == q->val)
↳ Return q

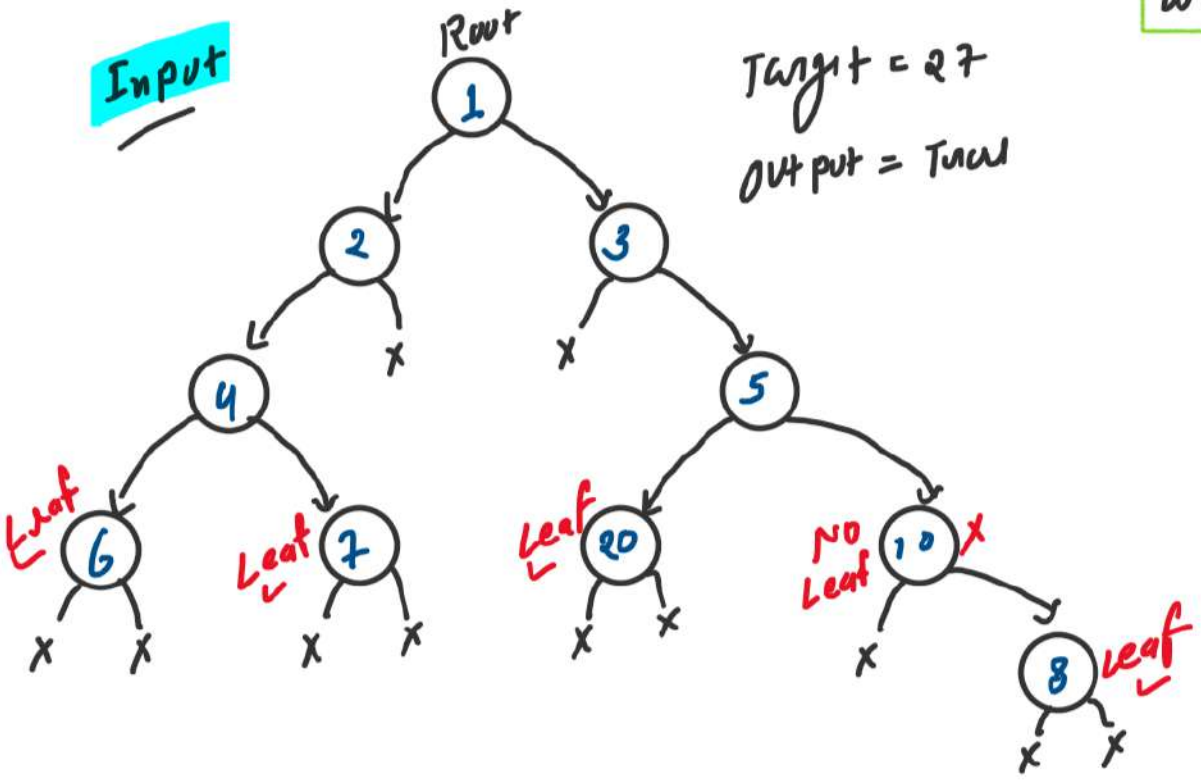
4 Condition to LCA



```cpp
// PROBLEM 02: Lowest Common Ancestor of a Binary Tree (Leetcode-236)

/**
 * Definition for a binary tree node.
 * struct TreeNode {
 *     int val;
 *     TreeNode *left;
 *     TreeNode *right;
 *     TreeNode(int x) : val(x), left(NULL), right(NULL) {}
 * };
 */
class Solution {
public:
    TreeNode* lowestCommonAncestor(TreeNode* root, TreeNode* p, TreeNode* q) {
        // Base case
        if(root == NULL){
            return NULL;
        }
        if(root->val == p->val){
            return p;
        }
        if(root->val == q->val){
            return q;
        }

        // Preoder traversal (NLR)
        TreeNode* leftAns = lowestCommonAncestor(root->left, p, q);
        TreeNode* rightAns = lowestCommonAncestor(root->right, p, q);

        // Return LCA
        if(leftAns == NULL && rightAns == NULL) return NULL;
        else if(leftAns != NULL && rightAns == NULL) return leftAns;
        else if(leftAns == NULL && rightAns != NULL) return rightAns;
        else return root; // else if(leftAns != NULL && rightAns != NULL)
    }
};
```

Time and space complexity = ?

3. Path Sum (Leetcode-112)



Target = 27

Output = True

What is path? Root → Leaf Node

Explaination

① 1 + 2 + 4 + 6 = 13

② 1 + 2 + 4 + 7 = 14

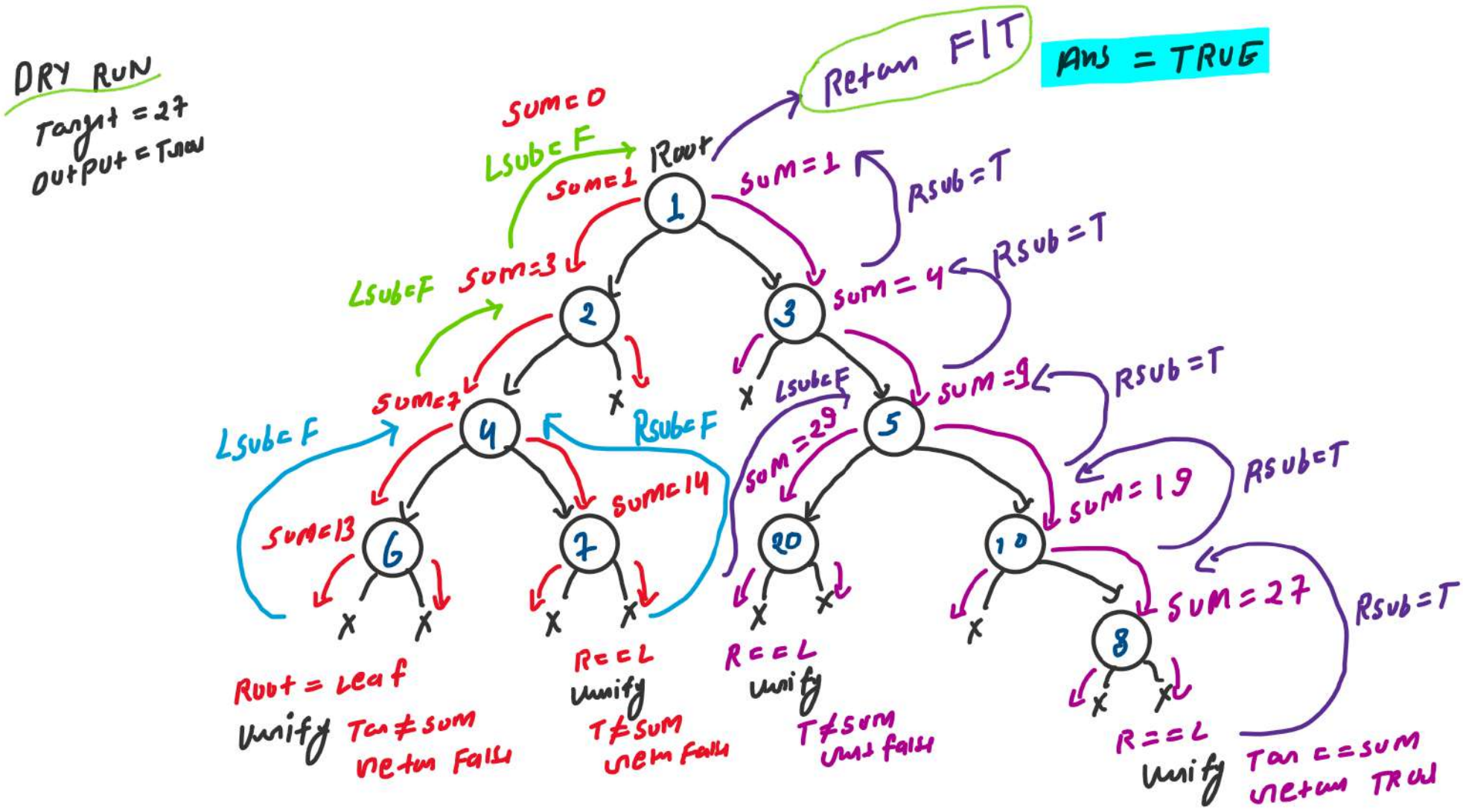
③ 1 + 3 + 5 + 20 = 29

~~④~~ 1 + 3 + 5 + 10 = 18 X Not a path

⑤ 1 + 3 + 5 + 10 + 8 = 27

Target == path ⑤

↳ Ans = TRUE


DRY RUN
Target = 27
Output = True
Sum = 0
LSub = F
Root
Return F|T
Ans = TRUE
Sum = 1
1
RSub = T
Sum = 1
LSub = F
Sum = 3
2
3
Sum = 4
RSub = T
Sum = 7
LSub = F
X
X
LSub = F
Sum = 9
RSub = T
4
RSub = F
5
Sum = 29
Sum = 19
RSub = T
Sum = 13
Sum = 14
6
7
20
10
Sum = 27
RSub = T
8
Root = Leaf
Unify
Tar ≠ sum
return False
R == L
Unify
T ≠ sum
return False
R == L
Unify
T ≠ sum
Ans False
R == L
Unify
Tar == sum
return TRUE

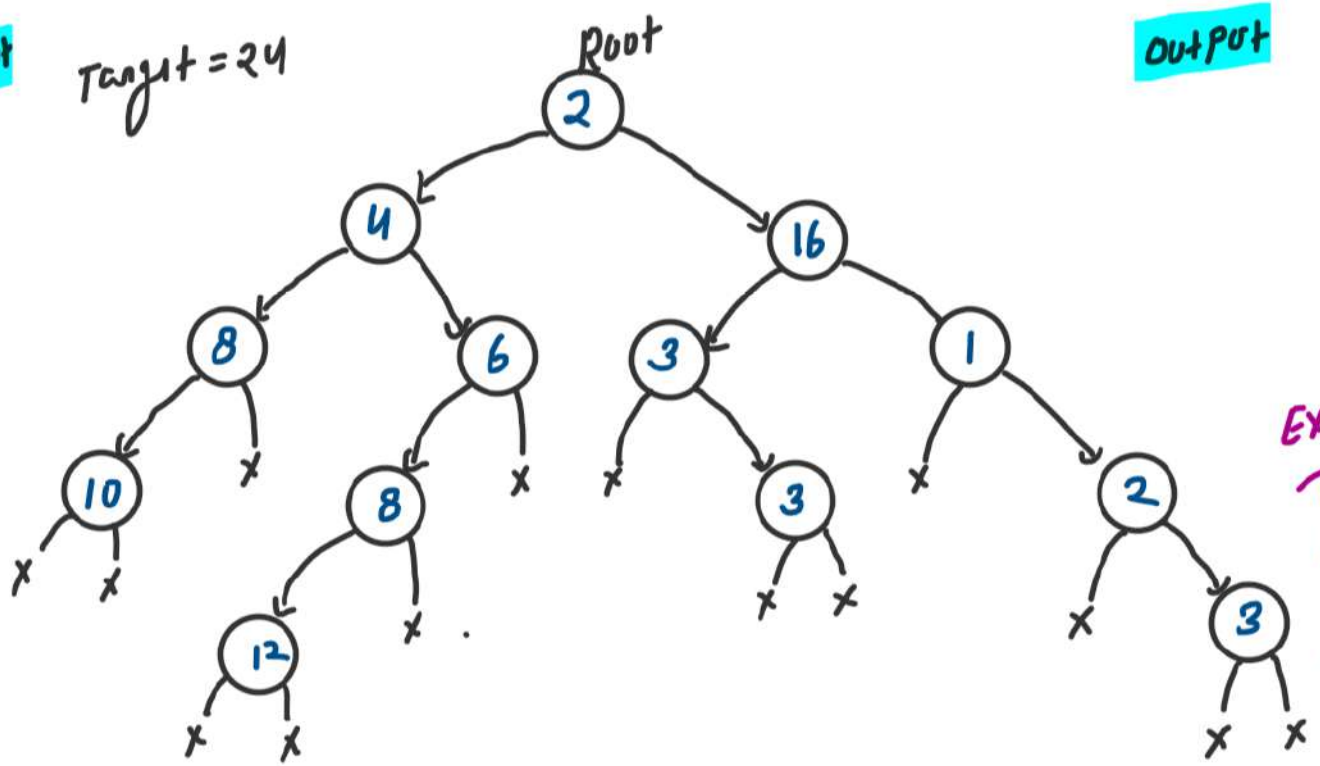
```cpp
// PROBLEM 03: Path Sum (Leetcode-112)
class Solution {
public:
    bool solve(TreeNode* root, int targetSum, int sum){
        // Base case
        if(root == NULL){
            return false;
        }

        // 1 case hum solve kar lenge
        sum += root->val;
        // Check krlo --> current root node leaf node par to nhi hai
        if(root->left == NULL && root->right == NULL){
            // Verify
            if(targetSum == sum){
                return true;
            }
            else{
                return false;
            }
        }

        // Ab recursion solve kr lega
        bool leftSub = solve(root->left, targetSum, sum);
        bool rightSub = solve(root->right, targetSum, sum);
        // Yeh important line hai --> return kaise karna hai
        return leftSub || rightSub;
    }


    bool hasPathSum(TreeNode* root, int targetSum) {
        int sum = 0;
        bool ans = solve(root, targetSum, sum);
        return ans;
    }
};
```

T.C. = ? and S.C. = ?

4. Path Sum (Leetcode-113)

Input

Target = 24



Output

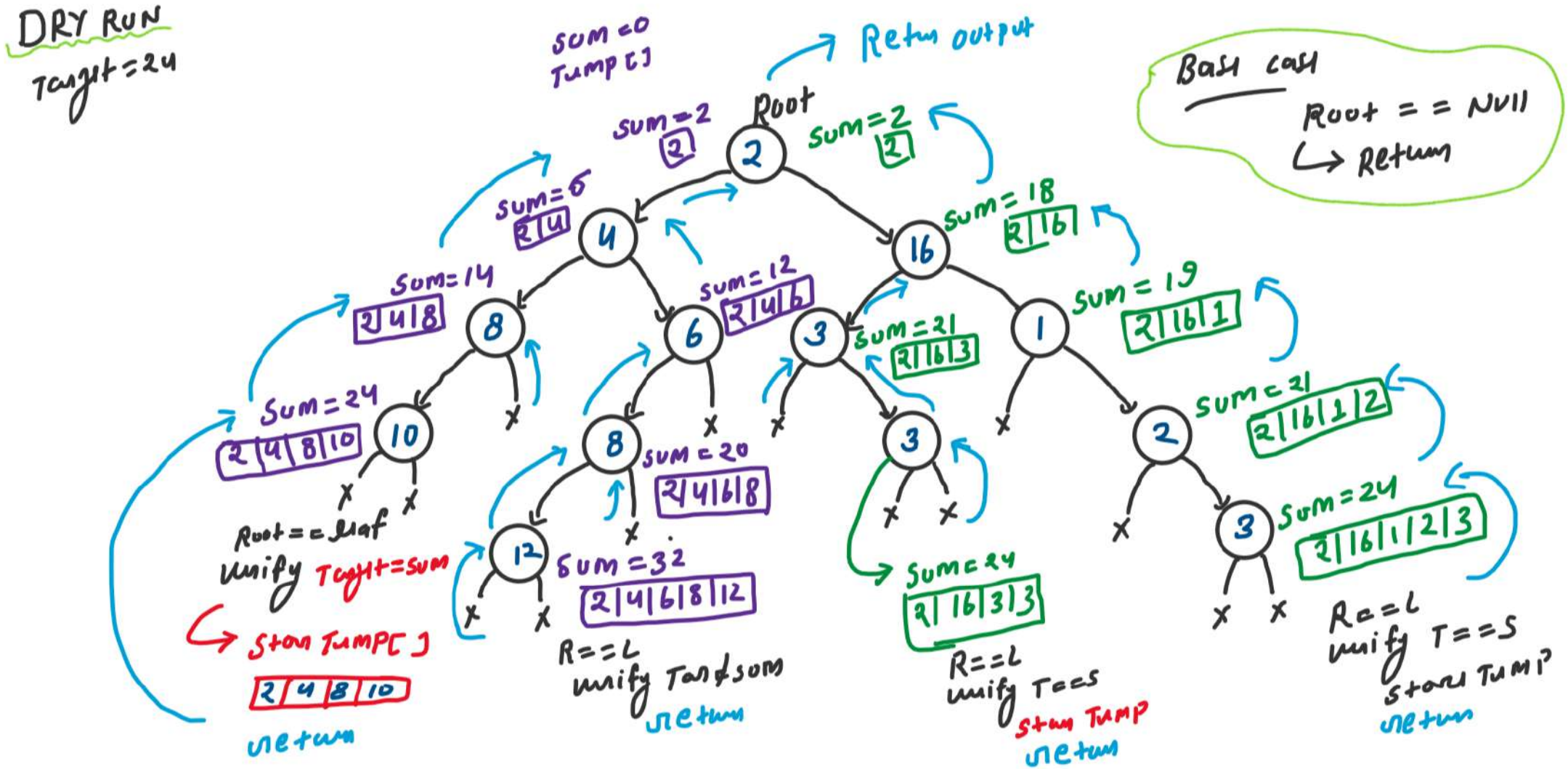
2D-ARRAY

2	4	8	10	
2	16	3	3	
2	16	1	2	3

vector < vector < int > > ans

Explanation

1. 2 → 4 → 8 → 10 = 24
2. ✗ 2 → 4 → 6 → 8 → 12 = 32
3. 2 → 16 → 3 → 3 = 24
4. 2 → 16 → 1 → 2 → 3 = 24


DRY RUN
Target = 24
sum = 0
Temp []
Return output
Base case
Root == NULL
↳ Return
Root
sum = 2
2
sum = 2
2
sum = 6
2 | 4
4
sum = 18
2 | 16
16
sum = 14
2 | 4 | 8
8
sum = 12
2 | 4 | 6
6
sum = 21
2 | 16 | 3
3
sum = 19
2 | 16 | 1
1
Sum = 24
2 | 4 | 8 | 10
10
sum = 20
2 | 4 | 6 | 8
8
sum = 21
2 | 16 | 1 | 2
2
3
sum = 24
2 | 16 | 3 | 3
3
Sum = 24
2 | 16 | 1 | 2 | 3
3
12
Sum = 32
2 | 4 | 6 | 8 | 12
X
Root == Leaf
Unify Target == sum
Store Temp[ ]
2 | 4 | 8 | 10
return
R == L
Unify Target == sum
return
R == L
Unify T == S
Store Temp
return
R == L
Unify T == S
Store Temp
return

```cpp
//PROBLEM 04: Path Sum II (Leetcode-113)
class Solution {
public:
    void solve(TreeNode* root, int targetSum, int sum, vector<int>
temp, vector<vector<int>> &ans){
        // Base case
        if(root == NULL){
            return;
        }

        // 1 case hum solve kar lenge
        sum += root->val;
        temp.push_back(root->val);
        // Check krlo --> current root node leaf node par to nhi hai
        if(root->left == NULL && root->right == NULL){
            // Verify
            if(targetSum == sum){
                ans.push_back(temp);
            }
            else{
                return;
            }
        }

        // Ab recursion solve kar lega
        solve(root->left, targetSum, sum, temp, ans);
        solve(root->right, targetSum, sum, temp, ans);
    }

    vector<vector<int>> pathSum(TreeNode* root, int targetSum) {
        vector<vector<int>> ans;
        vector<int> temp;
        int sum = 0;
        solve(root, targetSum, sum, temp, ans);
        return ans;
    }
};
```

T.C. and S.C. = ?

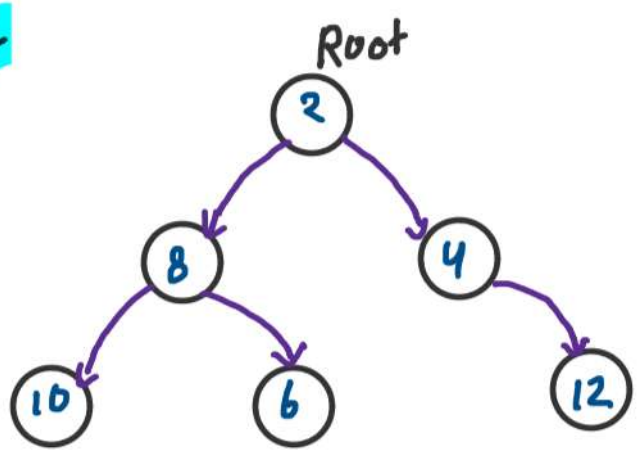
6. Construct Binary Tree from In-Order and Pre-Order Traversal (Leetcode-105)

Input

Pre-order: | 2 | 8 | 10 | 6 | 4 | 12 |

In-order: | 10 | 8 | 6 | 2 | 4 | 12 |

Output



Logic building ...

Input

(NLR)
Pre-order

Index →	0	1	2	3	4	5
	2	8	10	6	4	12

Always Root node at zero Index

(LNR)
In-order

	0	1	2	3	4	5
	10	8	6	2	4	12

Root

InStart Index = 0

InEnd Index = 5

Left RE SubTREE

Position

Right RE SubTREE

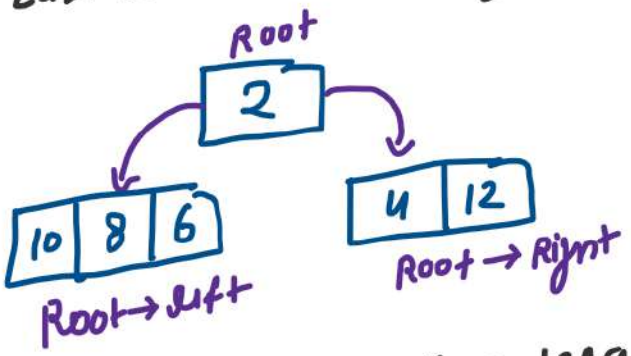
Base case

Index >= size || InStartIndex > InENDIndex

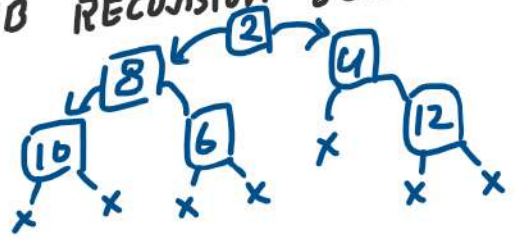
↳ Return NULL

STEP 01 Find position index of Root Node in In-order Array

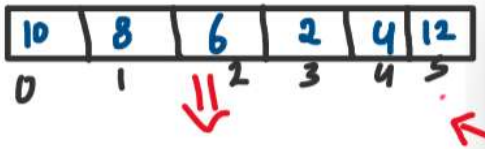
1 case hum solve karenge



AB Recursion solve kar lega



In-order



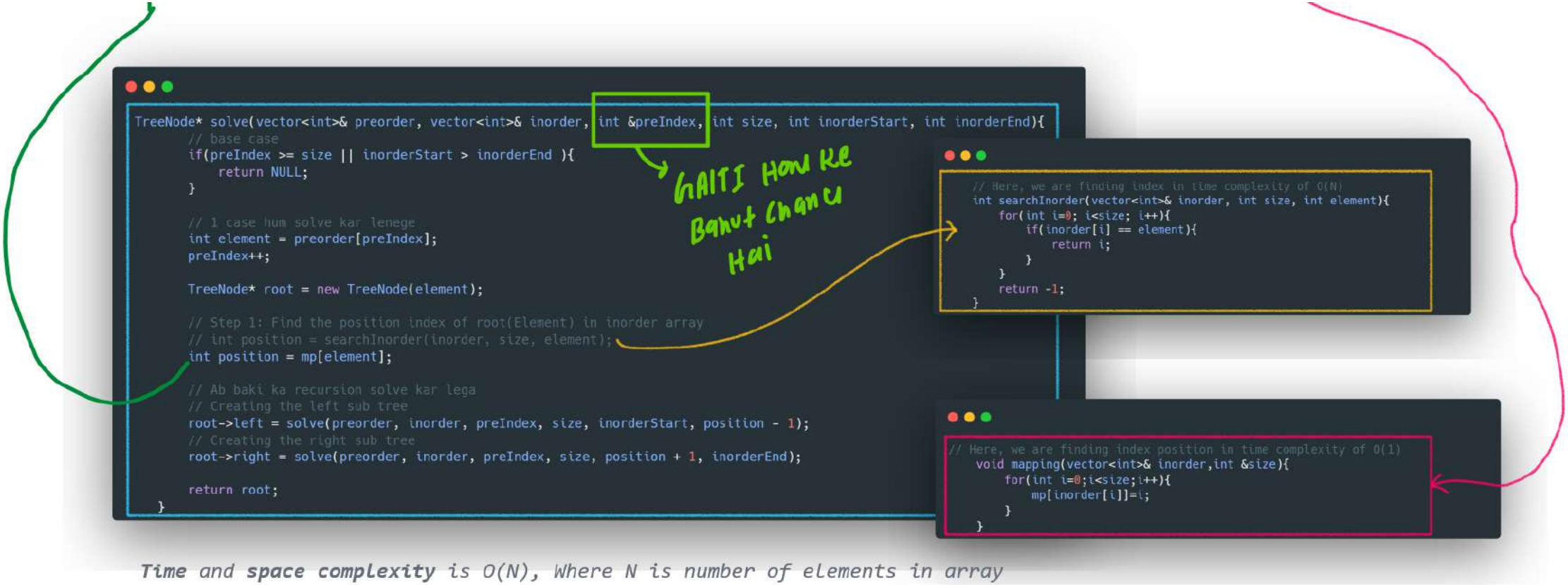
Map

Element	Index
10	0
8	1
6	2
2	3
4	4
12	5

```cpp
// PROBLEM 06: Construct Binary Tree from Inorder and Preorder Traversal (Leetcode-105)
class Solution {

private:

    map<int,int> mp; // Global mapping variable

public:

    // Here, we are finding index in time complexity of O(N)
    int searchInorder(vector<int>& inorder, int size, int element){...}

    // Here, we are finding index position in time complexity of O(1)
    void mapping(vector<int>& inorder,int &size){...}

    TreeNode* solve(vector<int>& preorder, vector<int>& inorder, int &preIndex, int size, int inorderStart, int inorderEnd){...}

    TreeNode* buildTree(vector<int>& preorder, vector<int>& inorder) {
        int preIndex = 0;
        int size = inorder.size();
        int inorderStart = 0;
        int inorderEnd = size - 1;
        mapping(inorder, size);
        TreeNode* binaryTreeRoot = solve(preorder, inorder, preIndex, size, inorderStart, inorderEnd);

        return binaryTreeRoot;
    }
};
```

** GALTI KE YAHI PAR HUI THI preIndex KO with Reference Hi Send Karna Hoga Otherwise preIndex = 0 Rahega Always

To Find the position Index of Element => map is best due to T.C. = O(1) Rather than O(N).



***Time** and **space complexity** is O(N), Where N is number of elements in array*

7. Construct Binary Tree from In-Order and Post-Order Traversal (Leetcode-106)

Input

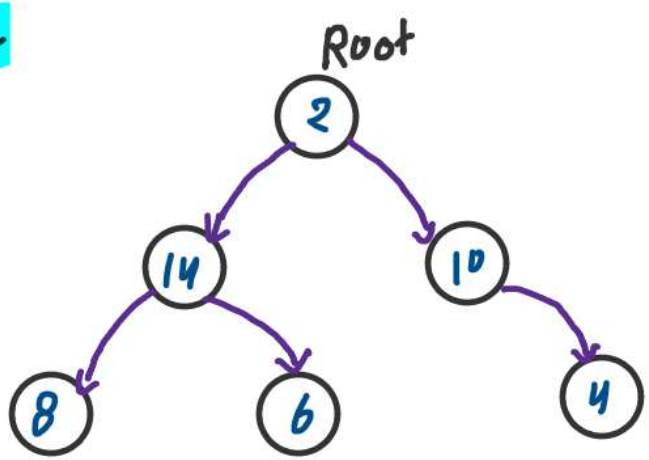
Post-order (LRN)

8	6	14	4	10	2

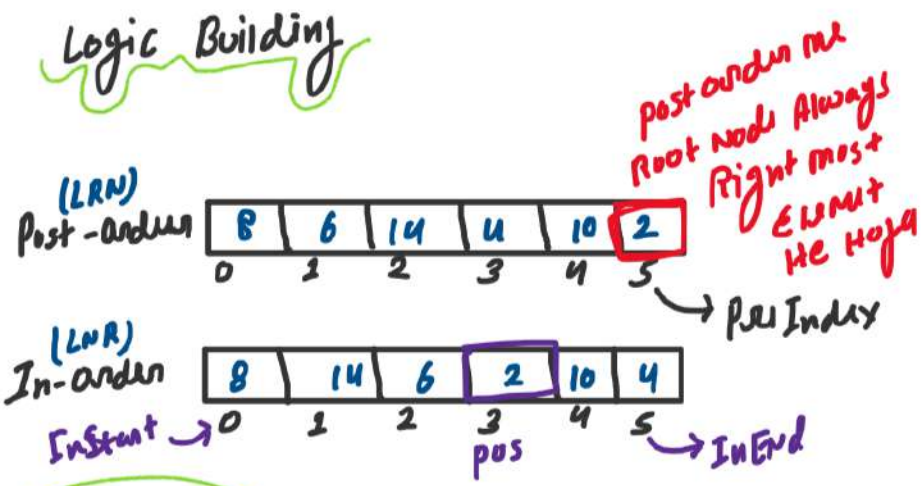
In-order (LNR)

8	14	6	2	10	4

Output



Logic Building



Post order me Root Node Always Right most Element he hoga

Base Case

(PostIndex < 0 || InStart > InEnd)

→ Return NULL

Yani Important Hai

→ Right call 1st

Left call 2nd

1 Case HUM solve karenge

Element = 2

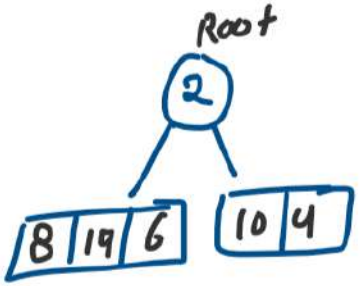
PostIndex--;

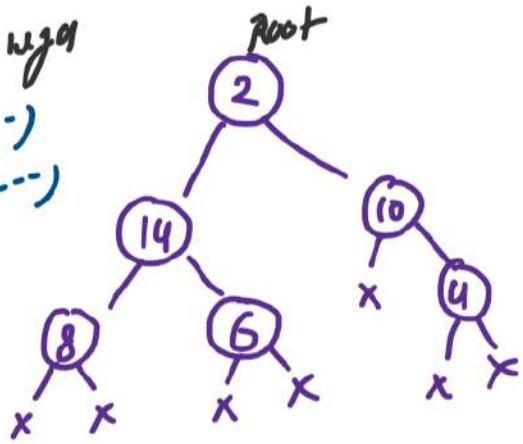
Node* Root = new Node(Element);

AB Recursion solve kar lenge

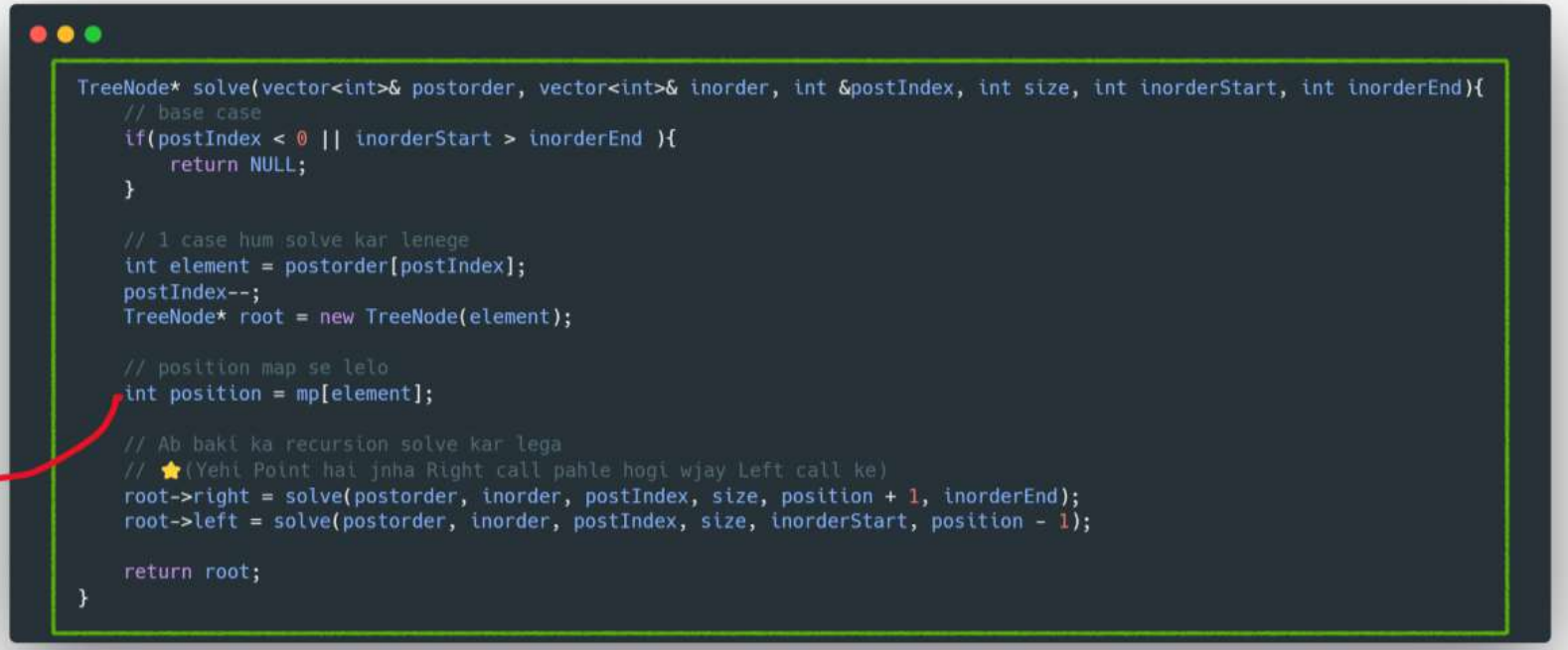
Root → Right = solve(...)

Root → Left = solve(...)






// PROBLEM 07: Construct Binary Tree from Inorder and POSTorder Traversal (Leetcode-106)
class Solution {
private:
map<int,int> mp;
public:
// Here, we are finding index position in time complexity of O(1)
void mapping(vector<int>& inorder,int &size){
for(int i=0;i<size;i++){
mp[inorder[i]]=i;
}
}
TreeNode* solve(vector<int>& postorder, vector<int>& inorder, int &postIndex, int size, int inorderStart, int inorderEnd){...}
TreeNode* buildTree(vector<int>& inorder, vector<int>& postorder) {
int size = inorder.size();
int postIndex = size - 1;
int inorderStart = 0;
int inorderEnd = size - 1;
mapping(inorder, size);
TreeNode* binaryTreeRoot = solve(postorder, inorder, postIndex, size, inorderStart, inorderEnd);
return binaryTreeRoot;
}
};
GALTI HONE
COMMON HAI YAAR



```
TreeNode* solve(vector<int>& postorder, vector<int>& inorder, int &postIndex, int size, int inorderStart, int inorderEnd){
    // base case
    if(postIndex < 0 || inorderStart > inorderEnd ){
        return NULL;
    }

    // 1 case hum solve kar lenege
    int element = postorder[postIndex];
    postIndex--;
    TreeNode* root = new TreeNode(element);

    // position map se lelo
    int position = mp[element];

    // Ab baki ka recursion solve kar lega
    // ⭐(Yehi Point hai jnha Right call pahle hogi wjay Left call ke)
    root->right = solve(postorder, inorder, postIndex, size, position + 1, inorderEnd);
    root->left = solve(postorder, inorder, postIndex, size, inorderStart, position - 1);

    return root;
}
```

Time *and* ***space complexity*** *is O(N), Where N is number of elements in array*