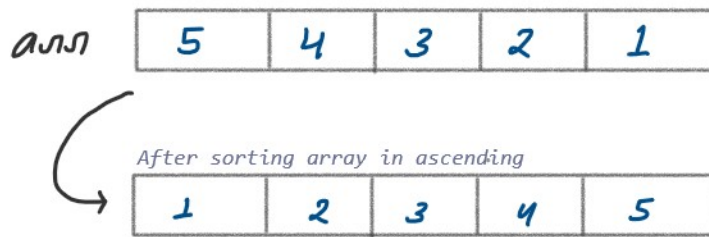


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# BUBBLE SORT

**✓ SORTINGS 01: BUBBLE SORT**

- swap the adjacent if needed till we get all the array sorted



## DRY RUN

5	4	3	2	1
0	1	2	3	4

1st largest element at it's positions

### 1st Iteration

$a$   
 $b$  } Adjacent value  
 $a > b \rightarrow \text{swap}$   
 $a < b \rightarrow \text{no swap}$

5	4	3	2	1
0	1	2	3	4

$\swarrow$   
 swap  $a > b \Rightarrow 5 > 4$

4   5   3   2   1  
 $\swarrow$   
 swap  $a > b \Rightarrow 5 > 3$

4   3   5   2   1  
 $\swarrow$   
 swap  $a > b \Rightarrow 5 > 2$

4   3   2   5   1  
 $\swarrow$   
 swap  $a > b \Rightarrow 5 > 1$

4   3   2   1   5

1st largest element = 5

## 2nd Iteration

2nd largest element at it's positions

4	3	2	1	5
0	1	2	3	4

swap  $a > b \Rightarrow 4 > 3$

3 4 2 1

swap  $a > b \Rightarrow 4 > 2$

3 2 4 1

swap  $a > b \Rightarrow 4 > 1$

3 2 1 4

2nd largest element = 4

## 3rd Iteration

3rd largest element at it's positions

3	2	1	4	5
0	1	2	3	4

swap  $a > b \Rightarrow 3 > 2$

2 3 1

swap  $a > b \Rightarrow 3 > 1$

2 1 3

3rd largest element = 3

## 4th Iteration

4th largest element at it's positions

2	1	3	4	5
0	1	2	3	4

swap  $a > b \Rightarrow 2 > 1$

1 2 3 4 5

4th largest element = 2

1	2	3	4	5
0	1	2	3	4

$N = \text{size} = 5$

$i \in [0, N-1)$   
Iteration

$j \in [0, N-i-1)$   
Comparison

Iteration

Comparison

$i \in [0, N-1)$	$j \in [0, N-i-1)$		
Iteration	Comparison		
I <sub>st</sub>	4	} GENERALIZE	1 → (N-1)
II <sub>nd</sub>	3		2 → (N-2)
III <sub>nd</sub>	2		• •
IV <sub>th</sub>	1		• •
			(N-2) → (N-1-2) = 2
			(N-1) → (N-1-1) = 1

AoP Series

$$S_n = 1 + 2 + 3 + \dots + (n-2) + (n-1)$$

$$S_n = \frac{n(n-1)}{2} = \frac{n^2 - n}{2}$$

Time complexity  $O\left(\frac{n^2}{2} - \frac{n}{2}\right) = O(n^2)$

```
// SORTINGS 01: BUBBLE SORT
#include<iostream>
#include<vector>
using namespace std;

// BUBBLE SORT Function
void bubbleSort(vector<int> &arr){
    int N=arr.size();

    // Outer Loop
    for(int i=0; i < (N-1); i++){
        // Inner Loop
        for(int j=0; j < (N-i-1); j++){
            // When a>b where a=j and b=j+1 to swap kardo
            if(arr[j] > arr[j+1]){
                swap(arr[j], arr[j+1]);
            }
        }
    }
}

int main(){
    vector<int> arr{5,4,3,1,2};

    bubbleSort(arr);
    for(auto value: arr){
        cout<<value<<" ";
    }
    return 0;
}

/*
INPUT: {5,4,3,1,2}
OUTPUT: {1,2,3,4,5}
TIME COMPLEXITY: O(N^2)
SPACE COMPLEXITY: O(1)
*/
```

*T.C. = O(N) } ⇒ O(N) (Total)*