

INSERTION SORT

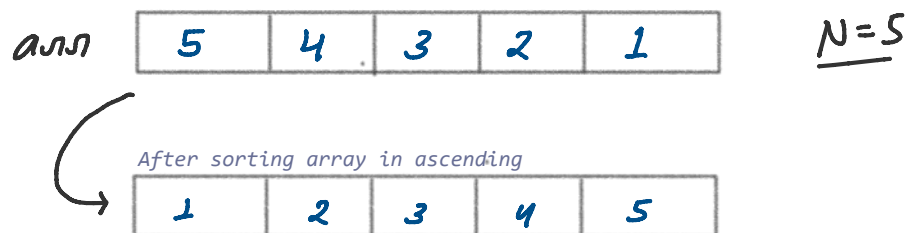
24 September 2023 09:22

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INSERTION SORT

✓ SORTINGS 03: INSERTION SORT

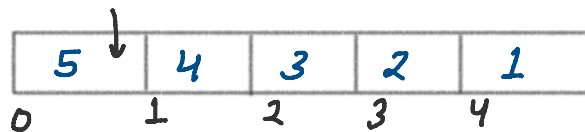
- Move element of $arr[0, i-1]$ that are greater than key to one position ahead of their current position



DRY RUN

Example: 01

Always ignore the first element



$$i=1 \quad j=i-1$$

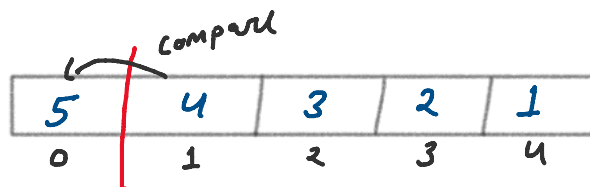
initially store the second element as a key value to Move element of $arr[0, i-1]$ that are greater than key to one position ahead of their current position

$$key = arr[i] \quad \boxed{4}$$

1st Iteration

$$key = 4$$

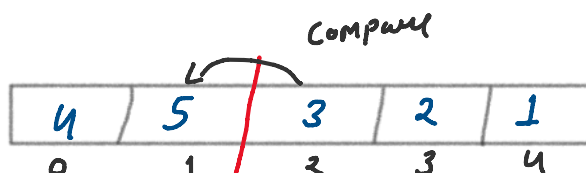
$$i=1, j=0$$



$5 > 4 \checkmark \rightarrow 4 \ 5 \ 3 \ 2 \ 1$

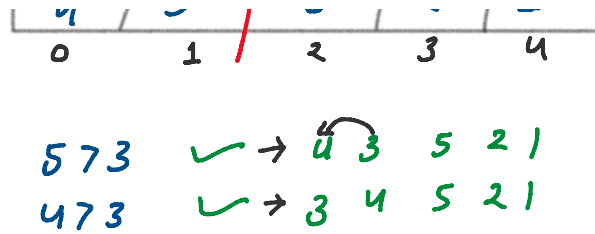
2nd Iteration

$$key = 3$$



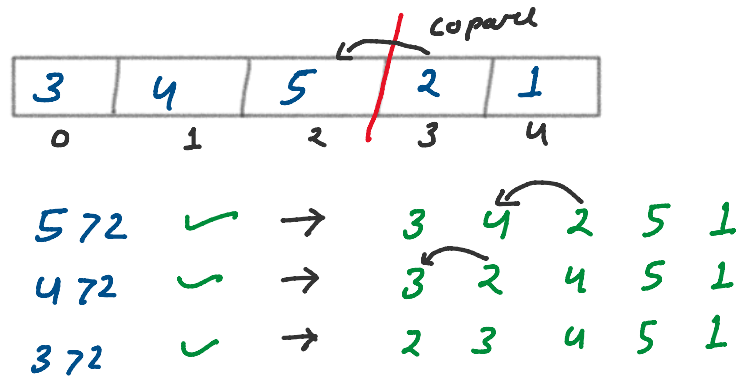
2nd Iteration

key = 3
 $i = 2, j = 1$
 $i = 2, j = 0$



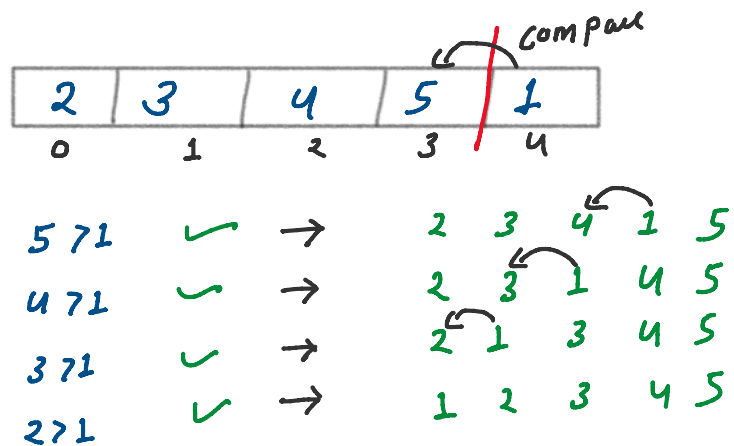
3rd Iteration

key = 2
 $i = 3, j = 2$
 $i = 3, j = 1$
 $i = 3, j = 0$



4th Iteration

key = 1
 $i = 4, j = 3$
 $i = 4, j = 2$
 $i = 4, j = 1$
 $i = 4, j = 0$



$i = 5$ { ROK jaaaao... (i < 5) END }

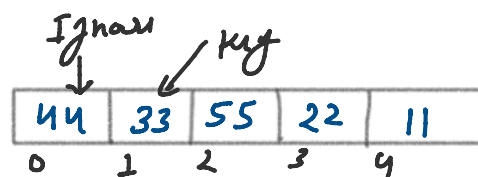
Final Output



DRY RUN

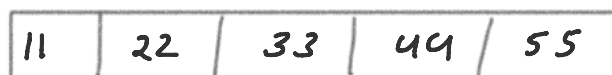
Example: 02

ans



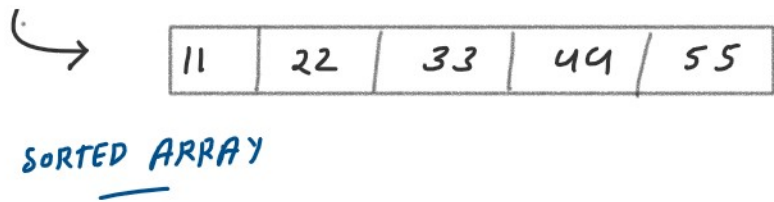
N = 5

$i = 1, j = i - 1$
 and = arr[i]



$$i=1, j=i-1$$

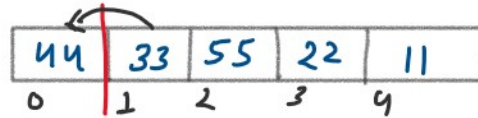
$$key = arr[i]$$



Iteration: 01

$$key = 33$$

$$i=1, j=0$$

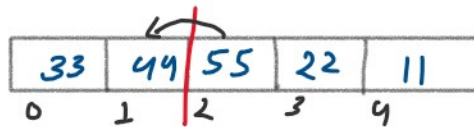


$$44 > 33 \checkmark \rightarrow 33 \ 44 \ 55 \ 22 \ 11$$

Iteration: 02

$$key = 55$$

$$i=2, j=1$$



$$44 > 55 \times \rightarrow \text{SAME} \Rightarrow 33 \ 44 \ 55 \ 22 \ 11$$

BREAK inner loop

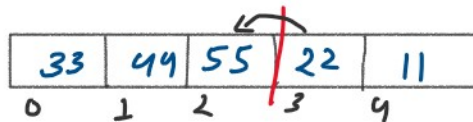
Iteration: 03

$$key = 22$$

$$i=3, j=2$$

$$i=3, j=1$$

$$i=3, j=0$$



$$55 > 22 \checkmark \rightarrow 33 \ 44 \ 22 \ 55 \ 11$$

$$44 > 22 \checkmark \rightarrow 33 \ 22 \ 44 \ 55 \ 11$$

$$33 > 22 \checkmark \rightarrow 22 \ 33 \ 44 \ 55 \ 11$$

Iteration: 04

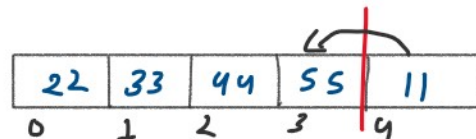
$$key = 11$$

$$i=4, j=3$$

$$i=4, j=2$$

$$i=4, j=1$$

$$i=4, j=0$$



$$55 > 11 \checkmark \rightarrow 22 \ 33 \ 44 \ 11 \ 55$$

$$44 > 11 \checkmark \rightarrow 22 \ 33 \ 11 \ 44 \ 55$$

$$33 > 11 \checkmark \rightarrow 22 \ 11 \ 33 \ 44 \ 55$$

$$22 > 11 \checkmark \rightarrow 11 \ 22 \ 33 \ 44 \ 55$$

$i = -1$, END inner loop

$$i = 4, j = 0$$

$$22 > 11 \quad \checkmark$$

$j = -1 \times$ END Inner loop

$i = 5 \{$ RUK $j = 0, 0, 0, \dots (i < 5)$

\rightarrow Final output

11	22	33	44	55
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$i \in [1, N]$		$j \in [i-1, 0]$		$N = 5$	
Iteration		Comparison		Iteration	Comparison
Outer Loop \rightarrow	I st	Inner Loop \rightarrow	1	1	\rightarrow 1
	II nd		2	2	\rightarrow 2
	III rd		3	0	0
	IV th		4	0	0
				0	0
		GENERALIZE		n-1	\rightarrow n-1
				n	\rightarrow n

$$S_n = 1 + 2 + 3 + \dots + n$$

$$= O\left(\frac{n^2 - n}{2}\right) \Rightarrow O(n^2)$$

$$T.O.C. = O(N^2)$$

$$S.O.C. = O(1)$$

```

// ✅ SORTINGS 03: INSERTION SORT

#include<iostream>
#include<vector>
using namespace std;

// INSERTION SORT Function
void insertionSort(vector<int> &arr){
    int N=arr.size();
    for(int i=1; i<N; i++){
        // Key value = key value se pahle ki all values ko hum compare karte hai key value se hi
        // taki key value ko hum uske right position par rakh paye
        int key = arr[i];
        int j = i-1;

        // Move element of arr[0,i-1] that are greater than key to one position ahead of there current position
        while(j>=0 && arr[j]>key){
            arr[j+1]=arr[j];
            j--;
        }
        // Insert key at right index/position (Insertion)
        arr[j+1]=key;
    }
}

int main(){
    vector<int> arr{5,4,3,1,2};

    insertionSort(arr);
    for(auto value: arr){
        cout<<value<<" ";
    }
    return 0;
}

/*
INPUT: {5,4,3,1,2}
OUTPUT: {1,2,3,4,5}
TIME COMPLEXITY: O(N^2)
SPACE COMPLEXITY: O(1)
*/

```