

## HW 02: Find K-Closest Element (Leetcode-658)

### Example 1:

Input: arr = [1,2,3,4,5], k = 4, x = 3

Output: [1,2,3,4]

### Example 2:

Input: arr = [1,2,3,4,5], k = 4, x = -1

Output: [1,2,3,4]

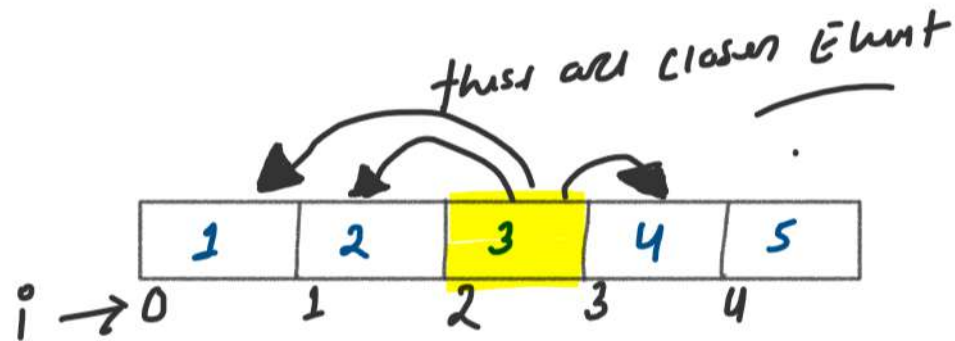
$\left\{ \begin{array}{l} \text{An integer } a \text{ is closer to } x \text{ than an integer } b \text{ if:} \\ - |a - x| < |b - x|, \text{ or} \\ - |a - x| == |b - x| \text{ and } a < b \end{array} \right\} \text{Note}$

What is closer  
Element to X?

Example 1:

Input: arr = [1,2,3,4,5], k = 4, x = 3

Output: [1,2,3,4]

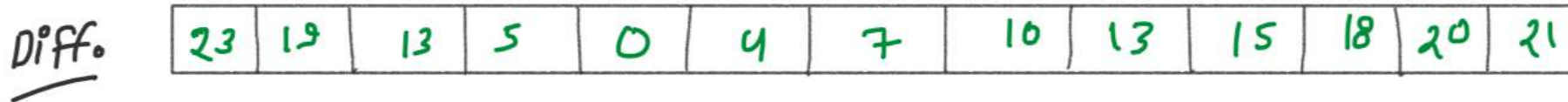
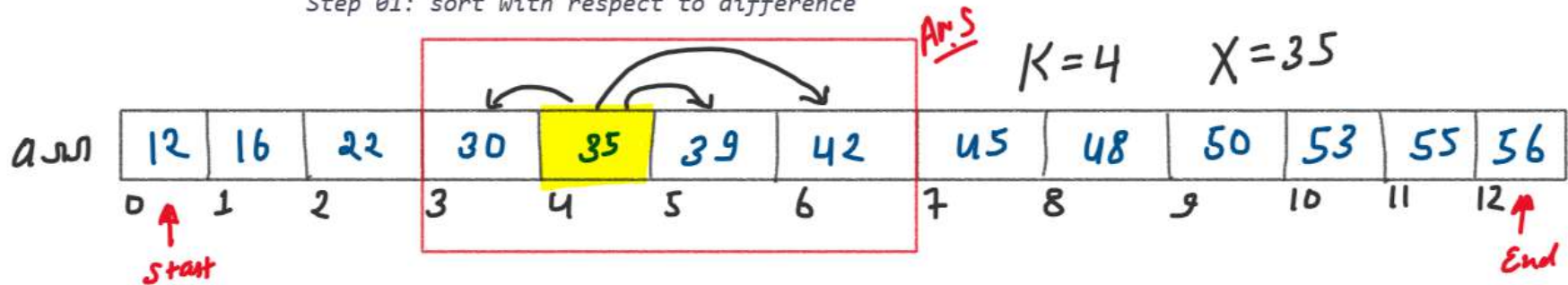


$\text{diff}\{x - \text{arr}[i]\} \Rightarrow$  2    1    0    1    2

WHAT IS CLOSER ELEMENTS OF X?

1. X ka sabse jyada closer element konsa hoga jo uske sabse jyada nearly ya uske barabar hoga
2. I need only number of K elements jo X ke nearly hai Like: 1 2 3 and 4

Two Pointer Approach  
Step 01: sort with respect to difference



Iteration: 1       $X=35$        $start = 0$        $End = 12$        $a = arr[start] = 12$        $b = arr[End] = 56$

①  $End - start + 1 = K$   
 $12 - 0 + 1 = 4$   
 TRUE

②  $(|X - a| > |X - b|)$   
 $|35 - 12| > |35 - 56|$   
 $23 > 21$   
 start++

arr

12	16	22	30	35	39	42	45	48	50	53	55	56
0	1	2	3	4	5	6	7	8	9	10	11	12

start

End

Diff.

23	19	13	5	0	4	7	10	13	15	18	20	21
----	----	----	---	---	---	---	----	----	----	----	----	----

[illegible]

End - start + 1 = K  
12 - 1 + 1 = 4  
TRUE

(2)  $|x - a| < |x - b|$   
 $|35 - 16| < |35 - 56|$   
 $19 < 21$   
 End--

arr

12	16	22	30	35	39	42	45	48	50	53	55	56
0	1	2	3	4	5	6	7	8	9	10	11	12

↑  
start
↑  
End

Diff.

23	19	13	5	0	4	7	10	13	15	18	20	21
----	----	----	---	---	---	---	----	----	----	----	----	----

iteration: 3     $x = 35$     start = 1    End = 11   
  $a = arr[start] = 16$      $b = arr[End] = 55$

①  $End - start + 1 = K$   
 $11 - 1 + 1 = 11$   
 $11 \neq 4$   
 TRUE

②  $(|x - a| < |x - b|)$   
 $|35 - 16| < |35 - 55|$   
 $19 < 20$   
 End--

arr

12	16	22	30	35	39	42	45	48	50	53	55	56
0	1	2	3	4	5	6	7	8	9	10	11	12

↑ start
↑ End

Diff.

23	19	13	5	0	4	7	10	13	15	18	20	21
----	----	----	---	---	---	---	----	----	----	----	----	----

Iteration: 4     $x = 35$      $start = 1$      $End = 10$      $a = arr[start] = 16$      $b = arr[End] = 53$

①  $End - start + 1 = K$   
 $10 - 1 + 1 = 10$   
 $10 > 7$   
 TRUE

②  $(|x - a| > |x - b|)$   
 $|35 - 16| > |35 - 53|$   
 $19 > 18$   
 Start++

ans

12	16	22	30	35	39	42	45	48	50	53	55	56
0	1	2	3	4	5	6	7	8	9	10	11	12

Start

End

Diff.

23	19	13	5	0	4	7	10	13	15	18	20	21
----	----	----	---	---	---	---	----	----	----	----	----	----

Iteration: 5     X=35     start = 2     End = 10     a = arr[start] = 22     b = arr[End] = 53

①  $End - start + 1 = K$   
 $10 - 2 + 1 = 9$   
 TRUE

(2)  $|x - a| < |x - b|$   
 $|35 - 22| < |35 - 53|$   
 $13 < 18$   
 End--



arr

12	16	22	30	35	39	42	45	48	50	53	55	56
0	1	2	3	4	5	6	7	8	9	10	11	12

↑  
Start

↑  
End

Diff.

23	19	13	5	0	4	7	10	13	15	18	20	21
----	----	----	---	---	---	---	----	----	----	----	----	----

Iteration: 6    X=35   start = 2   End = 9    a = arr[start] = 22    b = arr[End] = 50

$x_{c35}$  Start = 2

End = 9

$$a = a_{in} [start]$$

$$= 22$$

$$b = \text{arr}[\text{End}]$$
$$= 50$$

①  $End - start + 1 = K$   
 $9 - 2 + 1 = 8$   
 TRUE

$$End - Start + 1 = K$$

$$9 - 2 = 7 = 4$$

TRUE

(2)  $|x - a| < |x - b|$   
 $|35 - 24| < |35 - 50|$   
 $13 < 15$   
 End--

$$(|x-a| < |x-b|)$$

$$|35-22| < |35-50|$$

$13 < 15$

End--



arr

12	16	22	30	35	39	42	45	48	50	53	55	56
0	1	2	3	4	5	6	7	8	9	10	11	12

↑  
Start
↑  
End

Diff.

23	19	13	5	0	4	7	10	13	15	18	20	21
----	----	----	---	---	---	---	----	----	----	----	----	----

iteration: 7     $x=35$     start = 2    End = 8

$$a = \text{arr}[\text{start}]$$

$$= 22$$

$$b = \text{arr}[\text{End}]$$

$$= 48$$

①

$$\text{End} - \text{start} > K$$

$$8 - 2 \quad 7 = 4$$

TRUE

②

$$(|x - a| == |x - b|)$$

$$|35 - 22| == |35 - 48|$$

$$13 == 13$$

End--     $\rightarrow (a < b)$

arr

12	16	22	30	35	39	42	45	48	50	53	55	56
0	1	2	3	4	5	6	7	8	9	10	11	12

↑  
Start
↑  
End

Diff.

23	19	13	5	0	4	7	10	13	15	18	20	21
----	----	----	---	---	---	---	----	----	----	----	----	----

iteration: 8     $x=35$      $start=2$      $End=7$      $a = arr[start] = 22$      $b = arr[End] = 45$

①  $End - start + 1 = K$   
 $7 - 2 + 1 = 4$   
 TRUE

②  $(|x - a| > |x - b|)$   
 $|35 - 22| > |35 - 45|$   
 $13 > 10$   
 $start++$

ans

12	16	22	30	35	39	42	45	48	50	53	55	56
0	1	2	3	4	5	6	7	8	9	10	11	12

↑  
start
↑  
end

Diff.

23	19	13	5	0	4	7	10	13	15	18	20	21
----	----	----	---	---	---	---	----	----	----	----	----	----

iteration-9     $x=35$     start = 3    end = 7    
  $a = \text{arr}[\text{start}] = 30$     
  $b = \text{arr}[\text{end}] = 45$

①  $\text{end} - \text{start} > K$   
 $7 - 3 \quad 7 = 4$   
 TRUE

②  $(|x - a| < |x - b|)$   
 $|35 - 30| < |35 - 45|$   
 $5 < 10$   
 End--

arr

12	16	22	30	35	39	42	45	48	50	53	55	56
0	1	2	3	4	5	6	7	8	9	10	11	12

↑ start

↑ end

Diff.

23	19	13	5	0	4	7	10	13	15	18	20	21
----	----	----	---	---	---	---	----	----	----	----	----	----

Iteration-10  $X=35$  start = 3 end = 6

 $x = 35$ 
$$\text{start} = 3$$
$$End = 6$$
$$a = a_0 [st + nt] = 30$$
$$b = \text{sum}[\text{End}]$$
$$= 42$$

①

$$End - Start + 1 = K$$
$$6 - 3 = 3$$

FAISE

30	35	39	42
----	----	----	----

Output

```

// HW 02: Find K-Closest Element (Leetcode-658)
class Solution {
public:
    // APPROACH 01: Two Pointer Approach (Maximum/Top to Minimum/Bottom)
    vector<int> twoPointerApp(vector<int>& arr, int k, int x){
        vector<int> ans;
        int n = arr.size();
        int start = 0;
        int end = n-1;

        // Step 01: Sorting with respect to diff of a and b
        while(end-start >= k){
            int a = arr[start];
            int b = arr[end];

            if(abs(x-a)<abs(x-b)){
                end--;
            }
            else if(abs(x-a)>abs(x-b)){
                start++;
            }
            else{
                end--;
            }
        }

        // Step 02: find nearly element of x
        for(int i=start;i<=end;i++){
            ans.push_back(arr[i]);
        }
        // return ans; or
        return vector<int>(arr.begin()+start,arr.begin()+end+1);
    }
    vector<int> findClosestElements(vector<int>& arr, int k, int x) {
        return twoPointerApp(arr,k,x);
    }
};

/*
Time complexity: O(N-K), where N is length of arr and K is length of ans
Space complexity: O(1), no extra space used
*/

/*
Example 1:
Input: arr = [1,2,3,4,5], k = 4, x = 3
Output: [1,2,3,4]

Example 2:
Input: arr = [1,2,3,4,5], k = 4, x = -1
Output: [1,2,3,4]

Example 3:
Input: arr = [1,2,3,4,5], k = 4, x = 6
Output: [1,2,3,4]

Example 4:
Input: arr = [12,16,22,30,35,39,42,45,48,50,53,55,56], k = 4, x = 35
Output: [30,35,39,42]
*/

```

## HW 02: Find K-Closest Element (Leetcode-658)

Ex:ol

$K=4$      $X=35$

12	16	22	30	35	39	42	45	48	50	53	55	56
----	----	----	----	----	----	----	----	----	----	----	----	----

Output

12	16	22	30	35	39	42	45	48	50	53	55	56
0	1	2	3	4	5	6	7	8	9	10	11	12

$|X - \text{arr}[i]| \rightarrow$     23    19    13    5    0    4    7    10    13    15    18    20    21



Binary search and two pointer (Minimum/Bottom to Maximum/Top approach)

Step 01: Find lower bound value using Binary Search

Step 02: High => this is closest value of x

Low => High - 1

Step 03: Expand the window from [Low, High] to K

If arr[Low]-X > arr[High]-X then High++

Else arr[Low]-X < arr[High]-X then Low-- till K==0

Step 04: Return ans



```

// HW 02: Find K-Closest Element (Leetcode-658)
/*
APPROACH: 02
Binary search and two pointer (Minimum/Bottom to Maximum/Top approach)
Step 01: Find lower bound value using Binary Search
Step 02: High => this is closest value of x
        Low => High - 1
Step 03: Expand the window from [Low, High] to K
        If arr[Low]-X > arr[High]-X then High++
        Else arr[Low]-X < arr[High]-X then Low-- till K==0
Step 04: Return ans
*/
class Solution {
public:
    // Step 01: Lower bound value using binary search
    int lowerBound(vector<int>& arr, int x){
        int start = 0;
        int end = arr.size()-1;
        int ans = end; // -1 index bound error de skta hai when x=-1 ho ya x=invalid value

        while(start<=end){
            int mid = (start + end)/2;
            if(arr[mid]>=x){
                ans = mid;
                end = mid-1;
            }
            else if(arr[mid]<x){
                start = mid + 1;
            }
            else{
                end = mid-1;
            }
        }
        return ans;
    }

    // Two Pointer Approach + binary search
    vector<int> bs_method(vector<int>& arr, int k, int x){
        int h = lowerBound(arr,x);
        int l = h-1;

        // Sorting with respect to diff of a and b
        while(k--){
            if(l < 0){
                h++;
            }
            else if(h >= arr.size()){
                l--;
            }
            else if(abs(x-arr[l])>abs(x-arr[h])){
                h++;
            }
            else{
                l--;
            }
        }
        return vector<int>(arr.begin()+l+1,arr.begin()+h);
    }

    vector<int> findClosestElements(vector<int>& arr, int k, int x) {
        return bs_method(arr,x);
    }
};

/*
Time complexity: O(NlogN), where N is length of arr
Space complexity: O(1), no extra space used
*/

/*
Example 1:
Input: arr = [1,2,3,4,5], k = 4, x = 3
Output: [1,2,3,4]

Example 2:
Input: arr = [1,2,3,4,5], k = 4, x = -1
Output: [1,2,3,4]

Example 3:
Input: arr = [1,2,3,4,5], k = 4, x = 6
Output: [1,2,3,4]

Example 4:
Input: arr = [12,16,22,30,35,39,42,45,48,50,53,55,56], k = 4, x = 35
Output: [30,35,39,42]
*/

```