²⁹⁸A Performance Comparison of Data Mining Algorithms Based Intrusion Detection System for Smart Grid

Zakaria El Mrabet ¹, Hassan El Ghazi ², and Naima Kaabouch ¹

School of Electrical Engineering & Computer Science, University of North Dakota , USA

²National Institute of Posts and Telecommunication Rabat, Morocco

Abstract— Smart grid is an emerging and promising technology. It uses the power of information technologies to deliver intelligently the electrical power to customers, and it allows the integration of green technology to meet the environmental requirements. Unfortunately, information technologies have inherent vulnerabilities and weaknesses that expose the smart grid to a wide variety of security risks. The Intrusion detection system (IDS) plays an important role in securing smart grid networks and detecting malicious activity, yet it suffers from several limitations. Many research papers have been published to address these issues using several algorithms and techniques. Therefore, a detailed comparison between these algorithms is needed. This paper presents an overview of four data mining algorithms used by IDS in Smart Grid. A performance evaluation of these algorithms is conducted based on several metrics including the probability of detection, probability of false alarm, probability of miss detection, efficiency, and processing time. Results show that Random Forest outperforms the other three algorithms in detecting attacks with a higher probability of detection, lower probability of false alarm, lower probability of miss detection, and higher accuracy.

Keywords— Smart Grid, IDS, Data mining algorithms, probability of detection, probability of false alarm, Random Forest, Naïve Bayes

I. INTRODUCTION

Smart grid is an emerging and promising technology. It uses the power of data communication to deliver intelligently the electrical power and meet the environmental requirements. Compared to the traditional power grid, smart grid provides new functionalities such as real-time control, two-way flow of information communication, operational efficiency, and grid resilience [1]. Because of the inherent vulnerabilities of communications systems, smart grid can be subject to a wide variety of security attacks. One of the systems for detecting malicious activity and securing the networks is the intrusion detection system (IDS) [2].

IDS is based on three distinct approaches in detecting abnormalities: signature-based, specification-based, and anomaly-based. The first approach consists in detecting patterns of malicious activities using a database of well-known attack signatures. The second approach consists of identifying deviation from normal behavior profiles using logical specifications. The third approach consists in looking for deviations from normal behavior profiles using statistical measures [3]. According to Faisal et al. [4], the anomaly-based technique is more applicable and suitable approach for smart grid than signature-based and specification-based techniques.

Despite its wide use, IDS suffers from several performance limitations, including limited detection accuracy

and high rate of false positive [5]. Thus, a number of researchers tried to improve its performance. For example, Zhang et al. [6] proposed a distributed intrusion detection system for smart grid using artificial immune system and support vector machine algorithms. Ten et al. [7] proposed a substation detection algorithm that can be used to systematically extract malicious "footprints" of intrusion-based steps across substation networks. Berthier et al. [8] proposed a specification-based IDS for advanced metering infrastructure using sensors. Faisal et al. [4] proposed an anomaly based IDS for the advanced metering infrastructure (AMI) using several data stream mining techniques.

To the best of our knowledge, no previous work compared the performance of data mining algorithms used by anomaly-based IDS in smart grid networks. This paper fills this gap by evaluating the performance of four data mining algorithms which are: Naïve Bayes [9], Decision tree [10], Support Vector Machine [11], and Random Forest [12]. They have been used separately in several works with IDS, especially in the Smart Grid network, and they have produced satisfactory results. The benchmark NSL-KDD [13] dataset is selected for this evaluation. The evaluation is based on several metrics including the probability of detection, probability of false alarm, probability of miss detection, efficiency, and processing time.

The remainder of this paper is organized as follows. In section II, we describe the data mining algorithms used in this work. Section III presents the metrics used for evaluating the algorithms and discusses the results of the simulations. Some conclusions are drawn in the final section.

II. DATA MINING ALGORITHMS

In this work, we selected one algorithm from each of the four categories: Bayes model, Decision tree model, function model, and an ensemble model. These algorithms are Naïve Bayes (NB), Decision tree (DT), Support Vector Machine (SVM), and Random Forest (RF). These algorithms have been used separately with IDS, especially in the Smart Grid network. A description of each of these algorithms is given below.

A. Naive Bayes (NB)

Bayes network is a widely used graphical model to represent and handle uncertain information. NB is a simple Bayes network with the "naive" assumption of independence between child nodes. The steps for this algorithm are [9]:

1. Let *D* be a training set of a tuple and their associated class labels. In our case, a tuple is a packet and it is represented by an n-dimensional attribute vector X = (x1, x2, x3, ..., xn).

2. The number of class m is equal to 2 as we have attack class and normal class. Given a tuple or a packet X, NB will predict that X belongs to the class with the highest posterior probability. In other words, X belongs to Ci if and only if:

$$P\left(C_{i}|X\right) > \left(P\left(C_{i}|X\right) for \ 1 \le j \le m, j \ne i \right) \tag{1}$$

So we maximize the $P(C_i|X)$ which is given by the Bayes Theorem:

$$P(C_i|X) = \frac{P(X|C_i) \cdot P(C_i)}{P(X)}$$
 (2)

3. Because P(X) is constant for all classes, we remove it then maximize only the $P(X|C_i).P(C_i)$. The prior probability $P(C_i)$ is given by:

$$P\left(C_{i}\right) = \frac{|c_{i,D}|}{|D|}\tag{3}$$

Where $|C_{i,D}|$ is the number of training tuple of class C_i in D.

4. As NB assumes that there is no relationship among child nodes or attributes, the $P(X|C_i)$ is given by:

$$P(X|C_i) = \prod_{k=1}^n P(x_k|C_i)$$
(4)

Where x_k is the value of attribute A_k for tuple X. As the attributes $A_1, A_2, ..., A_n$ in the data set are categorical, the $P(x_k|C_i)$ is the number of tuples of class C_i in D having the value x_k for A_k , divided by $|C_{i,D}|$.

B. Decision tree (DT)

The decision tree is a supervised learning algorithm that can be used for addressing the classification problem. It consists of internal nodes, branches, and leaf nodes. Each internal node represents a test on an attribute, the branch is the outcome of the test, and the leaf node is the class label to which a given object belongs. In order to classify a new object using the decision tree, two steps are required: creation and classification [14].

Several algorithms exist to create a decision tree including ID3, C4.5, and CART. In this work, we selected C4.5 (J48 in Weka) and it works as follows [10]-[14]:

Let *D* and *Attribute_list* are the inputs, where *D* is the training set and their associated class labels, in our case there are two class labels: attack and normal. *Attribute_list* is the list of attributes describing the tuples, in our case, these are the attributes describing the packets. Below is the basic algorithm for creating a decision tree using these inputs.

Algorithm 1: Create_Decision_Tree (D, attribute_list)

- 1. Create a node *N*
- 2. If packet in D are all of the same class C N = leaf node labeled with the class C return N
- 3. If the *attribute_list* is empty N = leaf node labeled with the majority class in D return N

- 4. Calculate the Gain ratio of each attribute in *attribute list*
- 5. *N.test* = attribute with the best Gain ratio // the best means the highest value
- 6. For each outcome *j* in the splitting of *D*// partition the tuple and grow a subtree for each
 //partition
- 7. if D_i is empty N = leaf node labeled with the majority class in D
- else
 N = Create_decision_tree (D_j, attribute_list)
 endFor
- 9. return *N*

C4.5 uses the Gain ratio (step 4) method for selecting the attribute that separates the given tuples according to class. It is defined as follows:

$$GainRatio(A) = \frac{Gain(A)}{SplitInfo(A)}$$
 (5)

Where Gain (A) is given by:

$$Gain(A) = Info(D) - Info_A(D)$$
 (6)

Where

$$Info(D) = -\sum_{i=1}^{m} p_i \log_2(p_i)$$
 (7)

And

$$Info_A(D) = \sum_{j=1}^{\nu} \frac{|D_j|}{D} \times info(D_j)$$
 (8)

Where, $\mathit{Info}(D)$ denotes the average amount of information needed to identify the class label of a packet in D. Pi is the probability that a tuple in D belongs to the class Ci, and it is calculated by |Ci,D| / |D|. m is the number of classes. $\mathit{Info}(A)$ is the information required to classify a tuple from D based on the partitioning by A.

The SplitInfoA(D) represents the information generated after dividing the training data set D into v partitions where each partition is the outcomes of a test on an attribute A. It is given by:

$$SplitInfo_A(D) = -\sum_{j=1}^{\nu} \frac{|D_j|}{D} \times \log_2(\frac{|D_j|}{D})$$
 (9)

After building the decision tree, the DT classifies a new tuple or packet by starting at the root node of the tree, evaluating the test, and taking the branch appropriate to the outcome. This process is continued until a leaf is encountered, at which time the new tuple is asserted to belong to the class named by the leaf [10]-[14]:

C. Support Vector Machine (SVM)

SVM is a machine learning algorithm used for classification and regression [15]. It is based on a hyper line classifier, which separates and maximizes the margin between two classes.

Let the data set D be given as $\{(x_1, y_1), (x_2, y_2), (x_3, y_3), ..., (x_N, y_N)\}$ where x_i is the set of training tuples with associated class label y_i . Each y_i can take one of two values, either +1 or -1, corresponding to the class 'attack' and class 'normal'.

SVM finds the best decision boundary to separate two classes by searching for the maximum margin hyper line [11]. A separating hyper line can be written as:

$$h(x) = w.x + b = \sum_{i=1}^{N} \alpha_i y_i(x_i, x) + b$$
 (10)

Where w is a weight vector W, N is the number of attributes, and b is a bias.

In the case of non-linear data, we can first transform the data through non-linear mapping to another higher dimension space and then use a linear model to separate the data. The mapping function is done by a kernel function K, and this time we will use the following formula [11]:

$$h(x) = w. x + b = \sum_{i=1}^{N} \alpha_i y_i K(x_i, x) + b$$
 (11)

Where $K(x_i,x)$ is the kernel function.

After finding and drawing the separating hyper line, SVM classifies a new tuple or packet based on its position with respect to this hyper line. For example, if a tuple lies on or above the hyper line, it will belong to the class +1 (in our case the class 'attack'), and if it falls on or below the hyper line, it will belong to the class -1 (the class 'normal').

D. Random Forest (RF)

RF is a classifier which induces an ensemble of unpruned and randomized decision trees for classification and prediction [12]. Randomness is achieved either by selecting a bootstrap sample from the training data set or by selecting randomly a subset of attribute at each node of each decision tree. The pseudo-code of the RF algorithm is described in Fig. 1.

After building the learner, RF classifies a new object x by aggregating the decisions (votes) over all the decision trees Ti in the forest. The predicted class Ti(x) of x determined by the tree Ti is the class that occurs often in the random forest and has the majority of the votes [12]. In our experiment, we used the default value of $Number_of_features$ and $Number_of_trees$ in Weka. $Number_of_feature$ is given by log2M+1, where M is the number of attributes in the data set, and $Number_of_feature$ is equal to 10.

Building a bootstrapped sample D_i from the data set D. Creating a decision tree T_i using the training data set D_i For each node in the decision tree

Define the number of attributes and select a random subset $(x_1, x_2,..., x_n)$, where n is the *Number of features*.

For i = 1 to $Number_of_trees$ Create a forest of trees T_i .

Fig. 1. Pseudo-code of the Random Forest classifier

III. RESULTS AND DISCUSSION

In this paper, we use an improved version of the KDD cup 99 data set called NSL KDD. KDD cup 99 is a data set gathered at the MIT Lincoln Laboratory. It contains 5 209 460

network connections divided into two subsets: training subset with 4 898 431 connections and testing subset with 311 029 connections [13], [16].

Each connection represents a packet that has 41 features, 34 are numerical and 7 are symbolic. Each packet is classified either as normal traffic or as an attack. Attacks fall into the four categories: Remote to Local (R2L), User to Root (U2R), Denial of service (DOS), and Probing [13]. Description of each attack's category along with some attack's examples is given in Table I.

TABLE I. ATTACK'S CATEGORIES IN KDD CUP 99 AND NSL KDD

Attack's category	Description	Attack's Examples	
Remote to Local (R2L)	Unauthorized access from a remote machine	Password guessing	
User to Root (U2R)	Unauthorized access to local root privileges from a local unprivileged user	Rootkits, buffer overflow attack	
DOS	Denial of service	Teardrop attack and Smurf attack	
Probing	Surveillance and scanning	Scanning attack	

Although KDD Cup 99 is considered as a benchmark data set for assessing anomaly detection algorithms, it has a large number of redundant connections, especially a repeating record of DOS category. In addition, there is a bias distribution of the four categories which makes an accurate classification of the U2R and R2L difficult. These issues have been addressed in the NSL-KDD data set [16]-[19]. In this new version, many redundant and repeated records were removed, so the number of training and testing data were reduced 125 937 records and 22 544 records, respectively. In our experiment, we randomly selected 20% of this data set, which consists of 25 191 connections. Table II presents some statistics about NSL KDD.

TABLE II. NUMBER OF NETWORK CONNECTIONS IN KDD CUP 99 AND NSL_KDD

Attack's category	Number of network connections				
	KDD Cup 99		NSL KDD		
	Training	Testing	Training	Testing	
DOS	3 883 370	299 853	45 927	7 458	
R2L	1 073	11 980	942	1 656	
U2R	105	4 437	105	1 298	
Probing	41 102	4 166	11 656	2 421	
Normal	972 781	60 593	67 343	9 711	
Total	4 898 431	311 029	125 973	22 544	

To evaluate and compare the efficiencies of the four algorithms, metrics used are [20]-[22]:

- Probability of detection or true positive rate (TPR)
- Probability of false alarm or false positive rate (FPR)
- Probability of miss detection or false negative rate (FNR)

- Efficiency or accuracy
- Processing time.

The probability of detection or true positive rate (*TPR*) corresponds to the number of attack connections (packets) detected divided by the total number of attack packets. It is given by:

Probability of detection =
$$\frac{TP}{TP+FN} * 100$$
 (12)

Where true positive (TP) corresponds to the number of attack connections (packets) correctly classified as attacks and false negative (FN) is the number of attack connections that are classified normal packets by the algorithm.

The probability of false alarm or false positive rate (*FPR*) is the percentage of connections that are incorrectly classified as attacks, while in fact, they are normal. This probability is given by:

Probability of false alarm =
$$\frac{FP}{FP+TN} * 100$$
 (13)

Where false positive (FP) is the number of normal connections classified as attacks and true negative (TN) is the number of normal connections classified as normal connections.

The probability of miss detection or false negative rate (FNR) is the percentage of connections that are incorrectly classified as normal, while in fact, they are attacks. It is given by:

Probability of miss Detection =
$$\frac{FN}{TP+FN} * 100 (14)$$

The efficiency or accuracy is the percentage of correct classified connection by the algorithm over the total number of connections. This efficiency is given by:

$$Efficiency = \frac{TP + TN}{TP + TN + FP + FN} * 100$$
 (15)

Where false positive (FP) is the number of normal connections classified as attacks. False negative (FN) refers to the number of attack connections wrongly classified as normal.

Finally, the processing time is defined as the time taken to process a certain number of connections and classify them as normal or attack packets.

Fig. 2 shows the probability of detection or true positive rate (*TPR*) with respect to the number of connections. It is apparent from this figure that Random Forest has the highest probability of detection, followed by Decision Tree, SVM, and then Naïve Bayes. For instance, with 2000 instances, the *TPR* of Random Forest is 98.7%, Decision Tree is 98%, SVM is 97.5%, and then Naïve Bayes is 90.2%. It is noticeable also that *TPR* is almost independent of the number of connections, except for Naïve Bayes which decreases.

Fig. 3 illustrates the probability of false alarm, false positive rate (*FPR*), as a function of the number of connections. As observed, the *FPR* decreases as the number

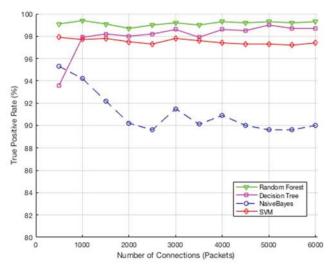


Fig. 2. True positive rate with respect to the number of connections

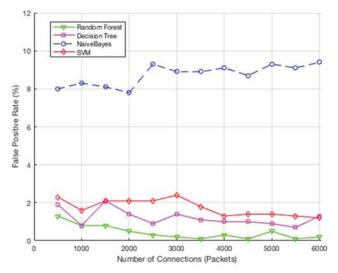


Fig. 3. False positive rate with respect to the number of connections

of connections increases for all the algorithms except Naïve Bayes. It can also be seen that the Random Forest has the lowest *FPR* value while Naïve Bayes has the highest value. For example, with 5000 connections, the *FPR* of Random Forest is 0.5% while it is 9.3% for the Naïve Bayes.

Fig. 4 presents the probability of miss detection or false negative rate (FNR) with respect to the number of connections. It is apparent from this figure that FNR remains almost the same for connections over 1000 for all algorithms except Naïve Bayes. The FNR of this algorithm increases sharply for connections under 2500 then slightly after. This figure also shows that Random Forest has the lowest FNR value, followed by Decision Tree, SVM, and then Naïve Bayes.

Fig. 5 illustrates the efficiency, the accuracy, of the four algorithms as a function of the number of connections. As one can see, Random Forest has the highest accuracy level, followed by Decision Tree, SVM, and then Naïve Bayes. For example, with 3500 connections, Random Forest reaches an accuracy of 99.48%, followed by Decision Tree with 98.41%, SVM with 97.89%, and then Naïve Bayes with 90.64%. Another noticeable thing is that the efficiency of Naïve Bayes decreases as the number of connections increases, whereas it is almost constant for the three other algorithms.

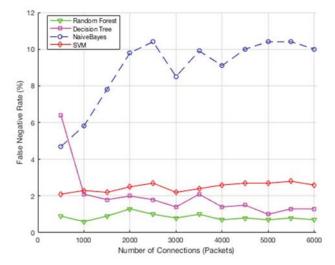


Fig. 4. False negative rate with respect to the number of connections

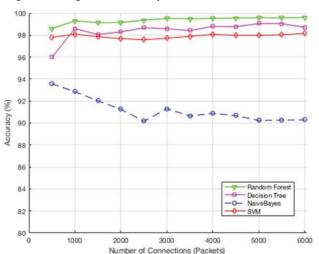


Fig. 5. Accuracy against the number of connections

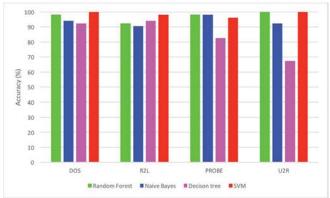


Fig. 6. Accuracy of four algorithms for each attack category

Fig. 6 shows the efficiency of the four algorithms for each attack category. Due to the bias distribution of the four attack categories in the NSL_KDD, we selected 208 instances for training and testing the algorithms, 52 instances of each category. As one can see, Random Forest detects efficiently (near to 100%) PROBE, U2R, and DOS attacks, while R2L attacks are better detected by SVM.

Fig. 7 shows the processing time as a function of the number of connections. As expected Random Forest and SVM require high processing time, followed by Decision Tree, and

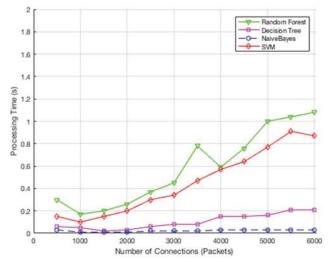


Fig. 7. Processing time against the number of connections

then Naïve Bayes. For instance, Random Forest takes 1.04s for processing 5500 connections, followed by SVM with 0.91s, Decision Tree with 0.21s, and then Naïve Bayes with 0.03s.

From these results, we can conclude that Random Forest is better than the other three algorithms in classifying attacks with a higher probability of detection, lower probability of false alarm, lower probability of miss detection, and higher accuracy. It detects most of the attack including DOS, PROBE, and U2R attacks. However, its main drawback is that it is time-consuming. On the other hand, Naïve Bayes shows the lowest probability of detection, highest probability of false alarm, the highest probability of miss detection, and lowest accuracy; but, it requires less processing time than the three other algorithms.

IV. CONCLUSION

In this paper, we have evaluated the performance of four algorithms used by IDS in smart grid namely Random Forest, SVM, Decision Tree, and Naïve Bayes. For this assessment, we have selected several metrics, including the probability of detection, probability of false alarm, probability of miss detection, efficiency, and processing time. The results show that some algorithms offer high accuracy with longer processing time, while others exhibit moderate accuracy but require less processing time. As future work, we aim to develop algorithms that satisfy the tradeoff between processing time and accuracy.

V. REFERENCES

- N. Framework, "Roadmap for Smart Grid Interoperability Standards, Release 2.0 (2012)," NIST Spec. Publ., vol. 1108.
- [2] Z. El Mrabet, N. Kaabouch, H. El Ghazi, and H. El Ghazi, "Cyber-security in smart grid: Survey and challenges," Comput. Electr. Eng., vol. 67, pp. 469–482, 2018.
- [3] R. Berthier, W. H. Sanders, and H. Khurana, "Intrusion Detection for Advanced Metering Infrastructures: Requirements and Architectural Directions," in 2010 First IEEE International Conference on Smart Grid Communications, 2010, pp. 350–355.
- [4] M. A. Faisal, Z. Aung, J. R. Williams, and A. Sanchez, "Data-stream-based intrusion detection system for advanced metering infrastructure in smart grid: A feasibility study," IEEE Syst. J., vol. 9, no. 1, pp. 31–44, 2015.
- [5] E. D. Knapp and J. T. Langill, "Industrial Network Security: Securing critical infrastructure networks for smart grid, SCADA, and other Industrial Control Systems," Syngress, 2014.

- [6] Y. Zhang, L. Wang, W. Sun, R. C. Green II, and M. Alam, "Distributed intrusion detection system in a multi-layer network architecture of smart grids," IEEE Trans. Smart Grid, vol. 2, no. 4, pp. 796–808, 2011.
- [7] C.-W. Ten, J. Hong, and C.-C. Liu, "Anomaly Detection for Cybersecurity of the Substations," IEEE Trans. Smart Grid, vol. 2, no. 4, pp. 865–873, Dec. 2011.
- [8] R. Berthier and W. H. Sanders, "Specification-based intrusion detection for advanced metering infrastructures," in 2011 IEEE 17th Pacific Rim International Symposium on Dependable Computing, 2011, pp. 184–193.
- [9] S. Aljawarneh, M. Aldwairi, and M. B. Yassein, "Anomaly-based intrusion detection system through feature selection analysis and building hybrid efficient model," J. Comput. Sci., vol. 25, pp. 152– 160, Mar. 2018.
- [10] S. Aljawarneh, M. B. Yassein, and M. Aljundi, "An enhanced J48 classification algorithm for the anomaly intrusion detection systems," Clust. Comput., Sep. 2017.
- [11] W. L. Al-Yaseen, Z. A. Othman, and M. Z. A. Nazri, "Multi-level hybrid support vector machine and extreme learning machine based on modified K-means for intrusion detection system," Expert Syst. Appl., vol. 67, pp. 296–303, Jan. 2017.
- [12] N. Farnaaz and M. A. Jabbar, "Random Forest Modeling for Network Intrusion Detection System," Procedia Comput. Sci., vol. 89, pp. 213– 217, Jan. 2016.
- [13] L. Dhanabal and S. P. Shantharajah, "A study on NSL-KDD dataset for intrusion detection system based on classification algorithms," Int. J. Adv. Res. Comput. Commun. Eng., vol. 4, no. 6, pp. 446–452, 2015.
- [14] Y. K. Jain, "An efficient intrusion detection based on decision tree classifier using feature reduction," Int. J. Sci. Res. Publ., vol. 2, no. 1, pp. 1–6, 2012.
- [15] N. Guenther and M. Schonlau, "Support Vector Machines," Stata J., vol. 16, no. 4, pp. 917–937, Dec. 2016.
- [16] M. Tavallaee, E. Bagheri, W. Lu, and A. A. Ghorbani, "A detailed analysis of the KDD CUP 99 data set," 2009, pp. 1–6.
- [17] "The KDD99 dataset available at https://kdd.ics.uci.edu/databases/kddcup99/task.html." .
- [18] Z. Elmrabet, H. Elghazi, T. Sadiki, and H. Elghazi, "A New Secure Network Architecture to Increase Security Among Virtual Machines in Cloud Computing," in Advances in Ubiquitous Networking, E. Sabir, H. Medromi, and M. Sadik, Eds. Springer Singapore, 2016, pp. 105–116.
- [19] W. F. Fihri, Y. Arjoune, H. El Ghazi, N. Kaabouch, and B. A. El Majd, "A particle swarm optimization based algorithm for primary user emulation attack detection," in Computing and Communication Workshop and Conference (CCWC), 2018 IEEE 8th Annual, 2018, pp. 823–827.
- [20] Z. El Mrabet, Y. Arjoune, H. El Ghazi, B. Abou Al Majd, and N. Kaabouch, "Primary User Emulation Attacks: A Detection Technique Based on Kalman Filter," J. Sens. Actuator Netw., vol. 7, no. 3, p. 26, Sep.2018.
- [21] Y. Arjoune, Z. El Mrabet, H. El Ghazi, and A. Tamtaoui, "Spectrum sensing: Enhanced energy detection technique based on noise measurement," in 2018 IEEE 8th Annual Computing and Communication Workshop and Conference (CCWC), 2018, pp. 828– 834.
- [22] Y. Arjoune, Z. Mrabet, and N. Kaabouch, "Multi-Attributes, Utility-Based, Channel Quality Ranking Mechanism for Cognitive Radio Networks," Appl. Sci., vol. 8, no. 4, p. 628, 2018.