

USN: 1PV24MC032

GB Panduranga

Topic: MinMax (Searching & Sorting)

Problem

Definition: Given an array of integers, find the minimum & maximum elements using:

- ① Searching (Iterative approach)
- ② Sorting (Using a sorting algorithm)

① Using Searching (Iterative approach)

Algorithm:

- Ⓐ Initialize min & max to the first element of the array.
- Ⓑ Traverse the array from the second element to the end:
  - If the current element is smaller than min, update min,
  - If the current element is larger than max, update max.
- Ⓒ Return min & max.

Time Complexity:

- Best, Worst & Average Case:  $O(n)$  (Single pass through the array)
- Only requires one traversal making it efficient

Space Complexity:

- $O(1)$  (constant space for min & max variables)

② Using Sorting approach

Algorithm:

- Ⓐ Sort the array using a sorting algorithm (eg. Quick Sort or Merge Sort)
- Ⓑ The first element of the sorted array is the minimum element



③ The last element of the sorted array is the maximum element. ②

Time Complexity:

→ Sorting:  $O(n \log n)$

→ Fetching min & max:  $O(1)$

→ Overall:  $O(n \log n)$

Space Complexity:

→  $O(1)$  if sorting in place, otherwise  $O(n)$  for additional space in sorting algorithms

~~Code explanation:~~

① Iterative

~~Steps~~

Tracing:

For input array:  $[3, 1, 4, 1, 5, 9, 2]$

① Initialize  $\text{min} = 3, \text{max} = 3$

② Compare each element:

•  $1 < 3 \rightarrow \text{min} = 1$

•  $4 > 3 \rightarrow \text{max} = 4$

• 1 is ignored

•  $5 > 4 \rightarrow \text{max} = 5$

•  $9 > 5 \rightarrow \text{max} = 9$

• 2 is ignored

③ Final Result:  $\text{min} = 1, \text{max} = 9$ .



## Test Cases:

① Input:  $[3, 1, 4, 1, 5, 9, 2]$

Expected Output:  $\text{Min} = 1, \text{Max} = 9$

② Input:  $[7, 7, 7, 7, 7]$

Expected Output:  $\text{Min} = 7, \text{Max} = 7$

③ Input:  $[-1, -5, -3, -8, -2]$

Expected Output:  $\text{Min} = -8, \text{Max} = -1$

④ Input:  $[5]$

Expected Output:  $\text{Min} = 5, \text{Max} = 5$



G B Panduranga

Topic: Finding  $k$ th smallest element using BST (Binary Search Tree).

Problem Definition: Given a Binary Search Tree (BST) & an integer ' $k$ ', find the  $k$ th smallest element in the BST.

Algorithm (In-order Traversal):

- ① Perform in-order traversal on the BST
- ② Keep a counter to track the number of visited nodes.
- ③ When the counter equals  $k$ , the current node's value is the  $k$ th-smallest element.

Time Complexity:

→ Best, Worst and Average Case:  $O(n)$  where ' $n$ ' is the number of nodes.

→ Traverses the number of nodes.

→ Traverses the tree once.

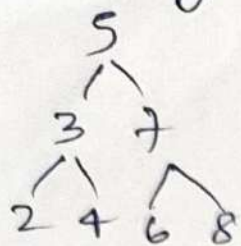
Space Complexity:

→  $O(h)$  where  $h$  is the height of the tree for recursion stack in Balanced BST.

→ In worst case (unbalanced),  $O(n)$ .



## Tracing:



Find the 3rd smallest element:

- ① Traverse left subtree of 5  $\rightarrow$  visit 2  $\rightarrow$  visit 3  $\rightarrow$  visit 4 (counter = 3)
- ② Return value 4 as the 3rd smallest element.

## Test cases:

① Input: [5, 3, 7, 2, 4, 6, 8],  $k=3$   
Expected Output: 4

② Input: [5, 3, 7, 2, 4, 6, 8],  $k=1$   
Expected Output: 2

③ Input: [5, 3, 7, 2, 4, 6, 8],  $k=7$   
Expected Output: 8

④ Input: [5],  $k=1$   
Expected Output: 5

⑤ Input: [5, 3, 7],  $k=5$   
Expected Output: Invalid  $k$  value.