

(a) In best of 9 game series, First to win 5 wins the series.

$$P(CA) = 5/5! \Rightarrow 0.55$$

$$P(1-CA) \Rightarrow 1 - 0.55 \Rightarrow 0.45 \quad \left. \vphantom{P(1-CA)} \right\} \text{First frame.}$$

Assumption: A has to win only 4 more from the remaining 8 games.

$$P(A) = 0.50 \text{ (winning)}$$

$$P(1-P(A)) = 0.50 \text{ (not winning)}$$

The assumption is A is winning the games straight.

We use binomial distribution for solving this problem.

Because we have data for first frame only. Every game A has 50-50% to win or lose

$$P \cdot x = 8$$

$$n = 4$$

$$p = 0.5$$

$$1-p = 0.5$$

$$8C_4 \times (0.5)^4 \times (0.5)^{8-4}$$

\Rightarrow

$$\frac{8 \times 7 \times 6 \times 5}{4 \times 3 \times 2 \times 1} \times (0.5)^4 \times (0.5)^4$$

$$70 \times 0.0625 = 0.0625$$

$$P(n=4) = 0.27\%$$

$$\text{Overall probability} : P(\text{first game}) + P(n=4)$$

$$\Rightarrow 0.55 + 0.27$$

$$\Rightarrow 0.82$$

$$\Rightarrow 82\%$$

P(b)

Assumption: Assuming he wins the remaining 4 games with 0.55%.

$$n = 8$$

$$r = 4$$

$$p = 0.55$$

$$1 - p = 0.45$$

$$P(4) = {}^8C_4 \times (0.55)^4 \times (0.45)^4$$

$$\Rightarrow \frac{8 \times 7 \times 6 \times 5}{4 \times 3 \times 2 \times 1} \times 0.091 \times 0.04$$

$$\Rightarrow 70 \times 0.091 \times 0.04$$

$$\Rightarrow 0.26$$

$$P(\text{PCA winning the game}) = 0.55 + 0.26 \\ = 0.81 \\ \sim \boxed{81\%} //$$

(b) Atleast 8 frames

Total no. of ~~games~~ frames is 9.

$$P(\text{8 out of 9}) \Rightarrow \frac{8}{9} \Rightarrow 0.88$$

$$n = 9$$

$$r = 8, \quad r = 9$$

$$p = 0.88$$

$$q = p = 0.12$$

when 8 games are played.

$${}^9C_8 \times (0.88)^8 \times (0.12)^1$$

$$\Rightarrow 9 \times 0.35 \times 0.12$$

$$\Rightarrow 0.378$$

~~P(9 out of 9) \Rightarrow~~ w

when 9 games are played

$$\Rightarrow {}^9C_9 \times (0.88)^9 \times (0.12)^0$$

$$\Rightarrow 1 \times 0.316$$

Probability of playing at least 8 frames
 $\Rightarrow 0.694$
 $= \boxed{69.4\%}$

③ Level of odds.

1) we need to calculate B's winning probability.

Let us assume B's winning probability $\Rightarrow 0.45$

$$P(B) = 0.45$$

$$P(1 - P(B)) = 0.55$$

Player B has to win 5 matches from 8 remaining.

P

$$n = 8$$

$$x = 5$$

$$P = 0.45$$

$$1 - P = 0.55$$

$$P(5) = {}^8C_5 \times (0.45)^5 \times (0.55)^3$$

$$\Rightarrow \frac{8 \times 7 \times 6}{3 \times 2 \times 1} \times 0.018 \times 0.166$$

$$\Rightarrow 5.6 \times 0.018 \times 0.166$$

$$\Rightarrow 0.167$$

$$P(B \text{ winning}) \Rightarrow 0.45 + 0.167$$

$$\Rightarrow 0.627 //$$

converting probability to odds

$$\text{odd} \Rightarrow \frac{\text{Probability of winning}}{1 - P(\text{winning})}$$

$$\Rightarrow \frac{0.627}{1 - 0.627} \Rightarrow \frac{0.627}{0.373}$$

$$\Rightarrow 1.68 //$$

2) (a) $A \Rightarrow 1.5$

$B = 1.25$

Football has 3 ~~prob~~ outcomes \Rightarrow win, Lo

$$P(w) = \frac{1}{3} \Rightarrow 0.33$$

$$P(\text{Draw}) = \frac{1}{3} \Rightarrow 0.33$$