

Algorithm: Assignment 2:  
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### Explanation For Algorithms:

1) Dijkstra's algorithm: for calculating single source shortest path

Data set Used: Array- to store the Nodes and their adjacent node list.  
For making the Breath First Search I maintained the array list corresponding to each node. This will give the running time complexity of  $O(V+E)$ .  
Second array is for keeping the list of all node for the traversal.  
Maintained one index respective to each node to keep track which nodes have been visited.

2) Kruskal's Algorithm: Minimum Spanning Tree:

Data set used: array: to keep the record of all the edges  
Maintained union-find data structure to have minimum time complexity to check for disjoint vertex. This will give the time complexity of find() function approximately  $O(1)$ .  
Maintained one Index for Root of set to each node to check in which set it belongs, and one index.

3) Floyd Warshall's: All Pairs Shortest Paths:

Data set used: Maintained two dimensional array for keep the adjacency matrix.

4) Transitive Closure :

Data set used: Maintained two dimensional array for keep the adjacency matrix.

### Note:

- For data set generator I used the reference provided.
- User need to provide the number of vertices and edges at command line in same order.  
I maintained a two dimensional array (matrix[][]) to store the data matrix get generated and while generating the data we need to keep the sequence of each data set generated and its calculation first before the second dataset get generated.
- Below are the table for providing the CPU time taken by each algorithm for each dataset
- Each time is in milliseconds.

**Table:**

	Case 1	Case 2	Case 3
CPU Running Time For :  Dijkstra's algorithm	For connection <10 Avg CPU Time = 1	For Connections>N/2  a) =40 : Avg Time: 0 b) = 60: Avg Time: 0 C) = 100: Avg Time: 1	For Random Graph: for: 150 Nodes a)weighted, directed: 42 b) weighted,Non-directed :50 c) nonweighted, directed :26 d) nonweighted,Non-directed :18

CPU Running Time For :  Kruskal's algorithm	For connection <10 Avg CPU Time = 1	For Connections>N/2  a) =40 : Avg Time: 0 b) = 60: Avg Time: 0 C) = 100: Avg Time: 1	For Random Graph: for: 150 Nodes a)weighted, directed: 30 b) weighted, Non-directed: 25 c) nonweighted, directed :37 d) nonweighted,Non-directed :18
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CPU Running Time For :  Floyd Warshall	For connection <10 Avg CPU Time = 1	For Connections>N/2  a) =40 : Avg Time: 9 b) = 60: Avg Time: 16 C) = 100:Avg Time:126	For Random Graph: for: 150 Nodes a)weighted, directed: 210 b) weighted,Non-directed:200 c) non weighted, directed :190  d) non-weighted,Non-directed :200
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CPU Running Time For :  Transitive Clouser	For connection <10 Avg CPU Time = 1	For Connections > N/2 a) =40 : Avg Time: 11 b) = 60: Avg Time: 15 C) = 100: Avg Time: 140	For Random Graph: for: 150 Nodes a) weighted, directed: 200 b) weighted, Non-directed: 205 c) non weighted, directed : 190  d) non-weighted, Non-directed : 180
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### Example execution:

Weighted undirected graph: for nodes = 10 edge = 16

#### 1) Dijkstra's Algorithm:

The out-put representation of minimum traversal weight from source (0 ) to each other vertices :

```

Weighted undirected graph:
81 30 32 59
81 34 84 68 43
34
30 84 121
68 105 15
60
32 121 105 113 96
15 125
43 60 113 120
59 96 125 120
destination and weight :0 0
destination and weight :1 81
destination and weight :2 115
destination and weight :3 30
Time : 1 destination and weight :4 137
destination and weight :5 184
destination and weight :6 32

destination and weight :7 152
destination and weight :8 124
destination and weight :9 59

```

#### Kruskals algorithm:

The representation of out put is which all edges has been included, then its two vertices (A and B) and then the weight for that edge.

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```

Weighted undirected graph:
0 0 97 0 0 8 25 0 52 8
0 0 0 0 0 0 76 0 21 19
97 0 0 0 0 66 0 0 0 31
0 0 0 0 0 0 102 0 32
0 0 0 0 0 0 0 0 78
8 0 66 0 0 0 0 0 10
25 76 0 0 0 0 0 0 0
0 0 0 102 0 0 0 0 0
52 21 0 0 0 0 0 0 68
8 19 31 32 78 10 0 0 68 0
edge :0
A: 0B :5 weight 8
edge :1
Time : 0A: 0B :9 weight 8
edge :2

```

```

A: 1B :9 weight 19
edge :3
A: 1B :8 weight 21
edge :4
A: 0B :6 weight 25
edge :5
A: 2B :9 weight 31
edge :6
A: 3B :9 weight 32
edge :7
A: 4B :9 weight 78
edge :8
A: 3B :7 weight 102

```

Floyd Warshall Algorithm:

The out put representation is simply in form of matrix which gives the minimum weight between the two nodes.

```

Weighted directed graph:
0 99 0 0 0 0 0 0 0 0
0 0 64 36 0 1 0 14 97 128
0 118 0 0 0 0 0 0 0 0
0 0 0 0 0 0 0 0 24 0
0 0 107 0 0 0 0 0 0 0
0 0 0 0 0 0 0 0 0 0
0 0 0 111 0 0 0 42 27 0
0 16 0 0 0 0 0 0 0 0
0 0 0 117 0 0 0 0 0 0
0 0 0 0 0 0 0 19 0 0
Time : 0
final weights:
0 99 infinity infinity infinity infinity infinity infinity infinity
infinity 0 64 36 infinity 1 infinity 14 60 128
infinity 118 0 154 infinity 119 infinity 132 178 246
infinity infinity infinity 0 infinity infinity infinity infinity 24 infinity
infinity 225 107 261 0 226 infinity 239 285 353
infinity infinity infinity infinity infinity 0 infinity infinity infinity infinity
infinity 58 122 94 infinity 59 0 42 27 186
infinity 16 80 52 infinity 17 infinity 0 76 144
infinity infinity infinity 117 infinity infinity infinity infinity 0 infinity
infinity 35 99 71 infinity 36 infinity 19 95 0

```

Transitive Clouser:

In this also the out-put is the matrix describing if the there is path between any two pair of vertices.

Scanned with CamScanner

Time : 1

Weighted undirected graph:

```
0 0 0 9 15 0 11 0 0 4
0 0 81 0 0 0 0 7 0 0
0 81 0 96 0 0 121 0 11 34
9 0 96 0 0 60 0 0 76 0
15 0 0 0 0 0 0 0 0 48
0 0 0 60 0 0 0 95 85 0
11 0 121 0 0 0 0 1 0 0
0 7 0 0 0 95 1 0 0 0
0 0 11 76 0 85 0 0 0 0
4 0 34 0 48 0 0 0 0 0
```

final matrix:

```
0 0 0 1 1 0 1 0 0 1
0 0 1 1 1 1 1 1 1 1
0 1 0 1 1 1 1 1 1 1
1 1 1 0 1 1 1 1 1 1
1 1 1 1 0 1 1 1 1 1
0 1 1 1 1 0 1 1 1 1
1 1 1 1 1 1 0 1 1 1
0 1 1 1 1 1 1 0 1 1
0 1 1 1 1 1 1 1 0 1
1 1 1 1 1 1 1 1 1 0
```