

## Topics: Confidence Intervals

1. For each of the following statements, indicate whether it is True/False. If false, explain why.

I. The sample size of the survey should at least be a fixed percentage of the population size in order to produce representative results.

**Ans: True**

II. The sampling frame is a list of every item that appears in a survey sample, including those that did not respond to questions.

**Ans: False, including that will not make respond to question.**

III. Larger surveys convey a more accurate impression of the population than smaller surveys.

**Ans: True**

2. *PC Magazine* asked all of its readers to participate in a survey of their satisfaction with different brands of electronics. In the 2004 survey, which was included in an issue of the magazine that year, more than 9000 readers rated the products on a scale from 1 to 10. The magazine reported that the average rating assigned by 225 readers to a Kodak compact digital camera was 7.5. For this product, identify the following:

A. The population

**Ans:** Readers of the Magazine.

B. The parameter of interest

**Ans:** Satisfaction with the product.

C. The sampling frame

**Ans:** An issue of Magazine in 2004.

D. The sample size

**Ans:** 9000

E. The sampling design

**Ans:** Rating the product on a scale from 1 to 10

F. Any potential sources of bias or other problems with the survey or sample

**Ans:** Many of the readers may not have used the product.

3. For each of the following statements, indicate whether it is True/False. If false, explain why.

I. If the 95% confidence interval for the average purchase of customers at a department store is \$50 to \$110, then \$100 is a plausible value for the population mean at this level of confidence.

**Ans:** True

- II. If the 95% confidence interval for the number of moviegoers who purchase concessions is 30% to 45%, this means that fewer than half of all moviegoers purchase concessions.

Ans: True

- III. The 95% Confidence-Interval for  $\mu$  only applies if the sample data are nearly normally distributed.

Ans: False

4. What are the chances that  $\bar{X} > \mu$  ?

- A.  $\frac{1}{4}$
- B.  $\frac{1}{2}$
- C.  $\frac{3}{4}$
- D. 1

Ans: B

5. In January 2005, a company that monitors Internet traffic (WebSideStory) reported that its sampling revealed that the Mozilla Firefox browser launched in 2004 had grabbed a 4.6% share of the market.

- I. If the sample were based on 2,000 users, could Microsoft conclude that Mozilla has a less than 5% share of the market?

Ans:

$$\sqrt{\frac{(0.046)(1 - 0.046)}{2000}}$$
$$= 0.006$$

So Now we find the lower and upper bounds looking like this.

If we are using 95% confidence Intervals, The Z – Score is 1.96

$$= 0.046 \pm (1.96)(0.006)$$

**Lower Bound** = 0.0362 or 3.62 %

**Upper Bound** = 0.0558 or 5.58 %

**Final Answer :** Yes, Microsoft could conclude that Mozilla has a less than 5% share of the market using 95% Confidence Interval and Actual Share could range from 3.62 % - 5.58 %

- II. WebSideStory claims that its sample includes all the daily Internet users. If that's the case, then can Microsoft conclude that Mozilla has a less than 5% share of the market?

**Ans:** Suppose the daily internet users = 30,000, 000

So calculate the standard error using a population of 30,000,000

$$SE = \sqrt{\frac{(0.046)(1 - 0.046)}{30,000,000}}$$

$$SE = 0.000038$$

$$CI = 0.046 \pm (1.96)(0.000038)$$

$$\text{Lower Bound} = 0.04592 \text{ or } 4.59 \%$$

$$\text{Upper Bound} = 0.04607 \text{ or } 4.60 \%$$

**Final Answer:** In this case Microsoft can only conclude that they are 95% certain that Mozilla share of the Market is between 4.59% - 4.60% of the Market

6. A book publisher monitors the size of shipments of its textbooks to university bookstores. For a sample of texts used at various schools, the 95% confidence interval for the size of the shipment was  $250 \pm 45$  books. Which, if any, of the following interpretations of this interval are correct?
- A. All shipments are between 205 and 295 books.
  - B. 95% of shipments are between 205 and 295 books.
  - C. The procedure that produced this interval generates ranges that hold the population mean for 95% of samples.
  - D. If we get another sample, then we can be 95% sure that the mean of this second sample is between 205 and 295.
  - E. We can be 95% confident that the range 160 to 340 holds the population mean.

**Ans:** Choice **B & D** are Correct

7. Which is shorter: a 95% z-interval or a 95% t-interval for  $\mu$  if we know that  $\sigma = s$ ?
- A. The z-interval is shorter
  - B. The t-interval is shorter
  - C. Both are equal
  - D. We cannot say

**Ans:** C

Questions 8 and 9 are based on the following: To prepare a report on the economy, analysts need to estimate the percentage of businesses that plan to hire additional employees in the next 60 days.

8. How many randomly selected employers (minimum number) must we contact in order to guarantee a margin of error of no more than 4% (at 95% confidence)?
- A. 600
  - B. 400
  - C. 550
  - D. 1000

**Ans: B**

9. Suppose we want the above margin of error to be based on a 98% confidence level. What sample size (minimum) must we now use?
- A. 1000
  - B. 757
  - C. 848
  - D. 543

**Ans: D**