

# Introduction to Kinematics of Machines

## Second Semester



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# Introduction to Machine

## Machine : -

A machine (or mechanical device) is a mechanical structure that uses power to apply forces and control movement to perform an intended action.

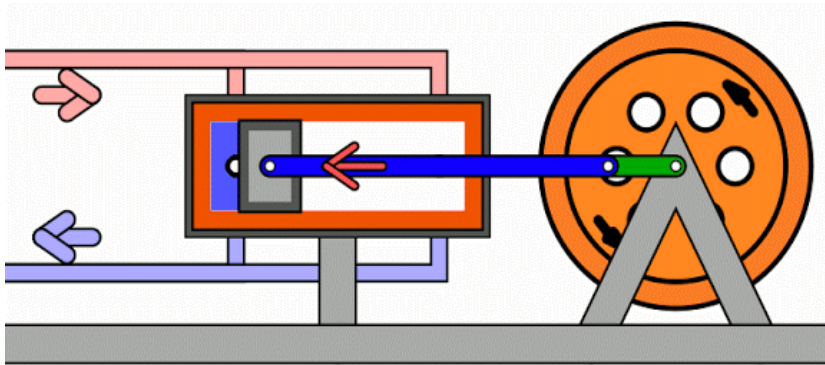


Fig 1.0 Rotary Machine

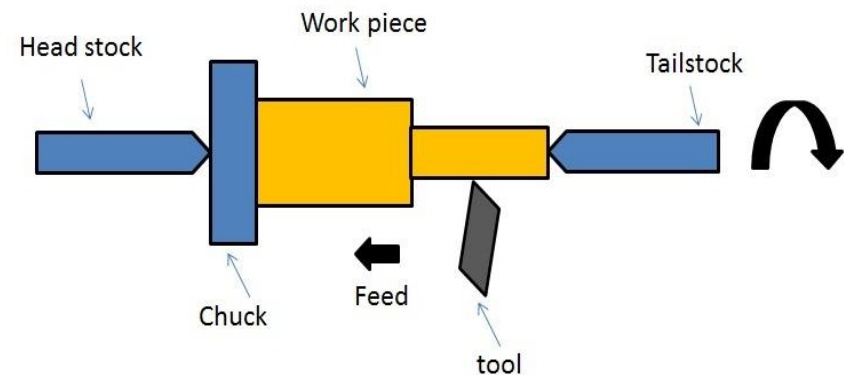


Fig 2.0 Lathe Machine

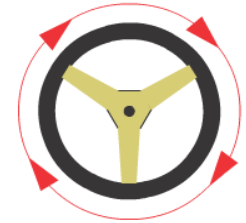
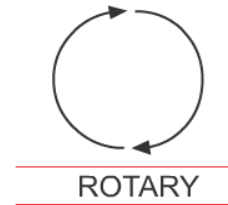
Source : <https://www.mechanicalbooster.com/>

# Difference between Machine and Structure

- The parts of a **machine** move relative to one another, whereas the members of a **structure** do not move relative to each other.
- The **machine** transforms the available energy into useful work, whereas in a **structure** no energy is transformed into useful work.
- The links of a **machine** may transmit both motion and power, while the members of a **structure** transmits forces only.
- **Machine** : - Lathe, shaper, prime mover
- **Structure** : - Bridge, Buildings

# Classification of Motion

- Continuous Rotary Motion



- Linear Motion / Rectilinear Motion



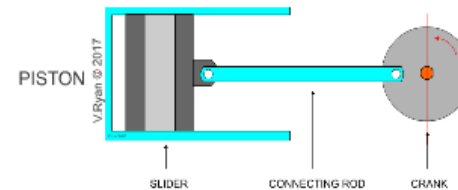
LINEAR



- Reciprocating Motion



RECIPROCATING



- Oscillating Motion



OSCILLATING

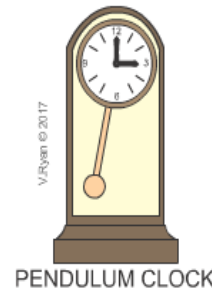


Fig 3.0 Type of motions

Source: <https://technologystudent.com/forcmom/motion1.html>

# Important Terminologies

- Link or Element
- Kinematic pair
- Kinematic chain
- Mechanism, Machine & Structure
- Degrees of Freedom (D.O.F)
- Gruber's criterion
- Inversion

# Kinematic Link

## Kinematic Link / Element : -

- I. Each part of a machine, which moves relative to some other part, is known as a kinematic link or element.
- II. A link may consist of several parts, which are rigidly fastened together, so that they do not move relative to one another.

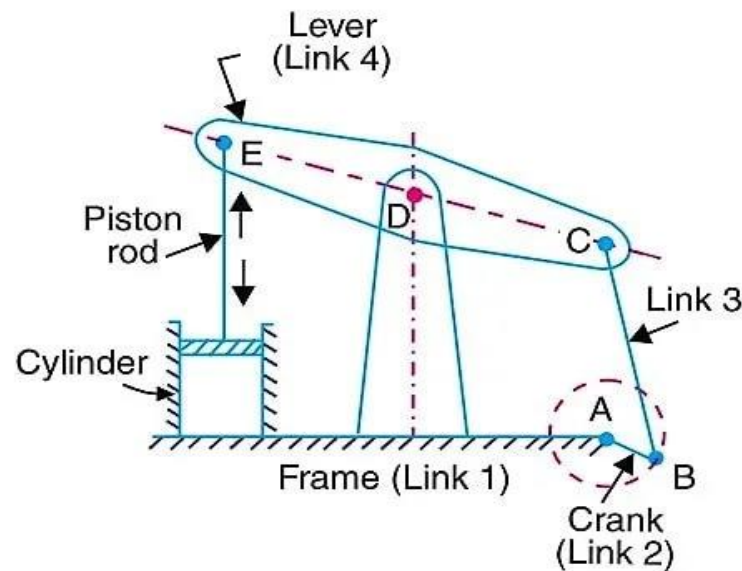


Fig 4.0 Kinematic links in a mechanism

Source: <https://technologystudent.com/forcmom/motion1.html>

# Types Link

- I. **Rigid Link** : A link which doesn't go any deformation while transmitting motion.
- II. **Flexible Link** : A link which is partly deformed in a manner not to affect the transmission of motion.  
e.g. : Belts, rope, chain drive
- III. **Fluid Link** : A link which is formed by having a fluid in a receptacle and the motion is transmitted through the fluid by pressure or compression

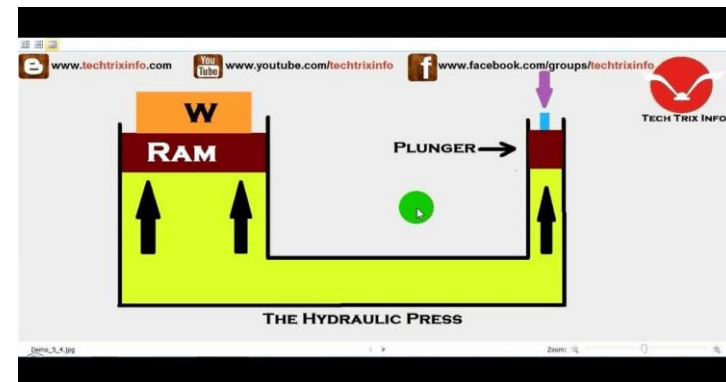
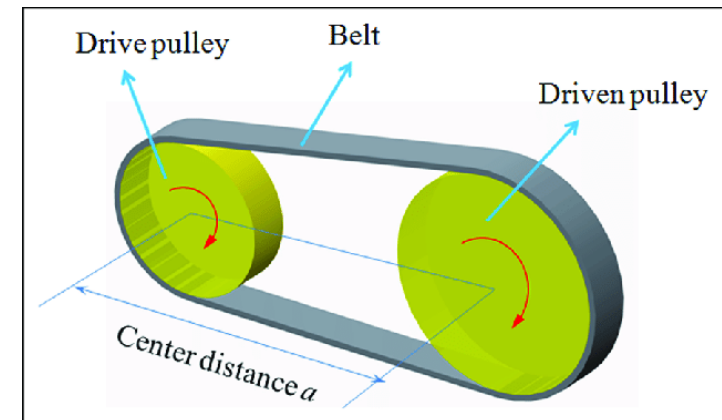


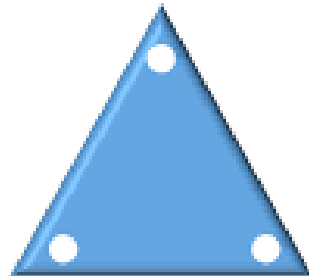
Fig 5.0 Different type of links  
Source:

# Classification of Links

- I. **Unary Link** : A link consisting of one node.
- II. **Binary Link** : A link connected to other links at two points.
- III. **Ternary Link** : A link connected to other links at three points.
- IV. **Quaternary Link** : A link connected to other links at four points.



**Binary Link**



**Ternary Link**



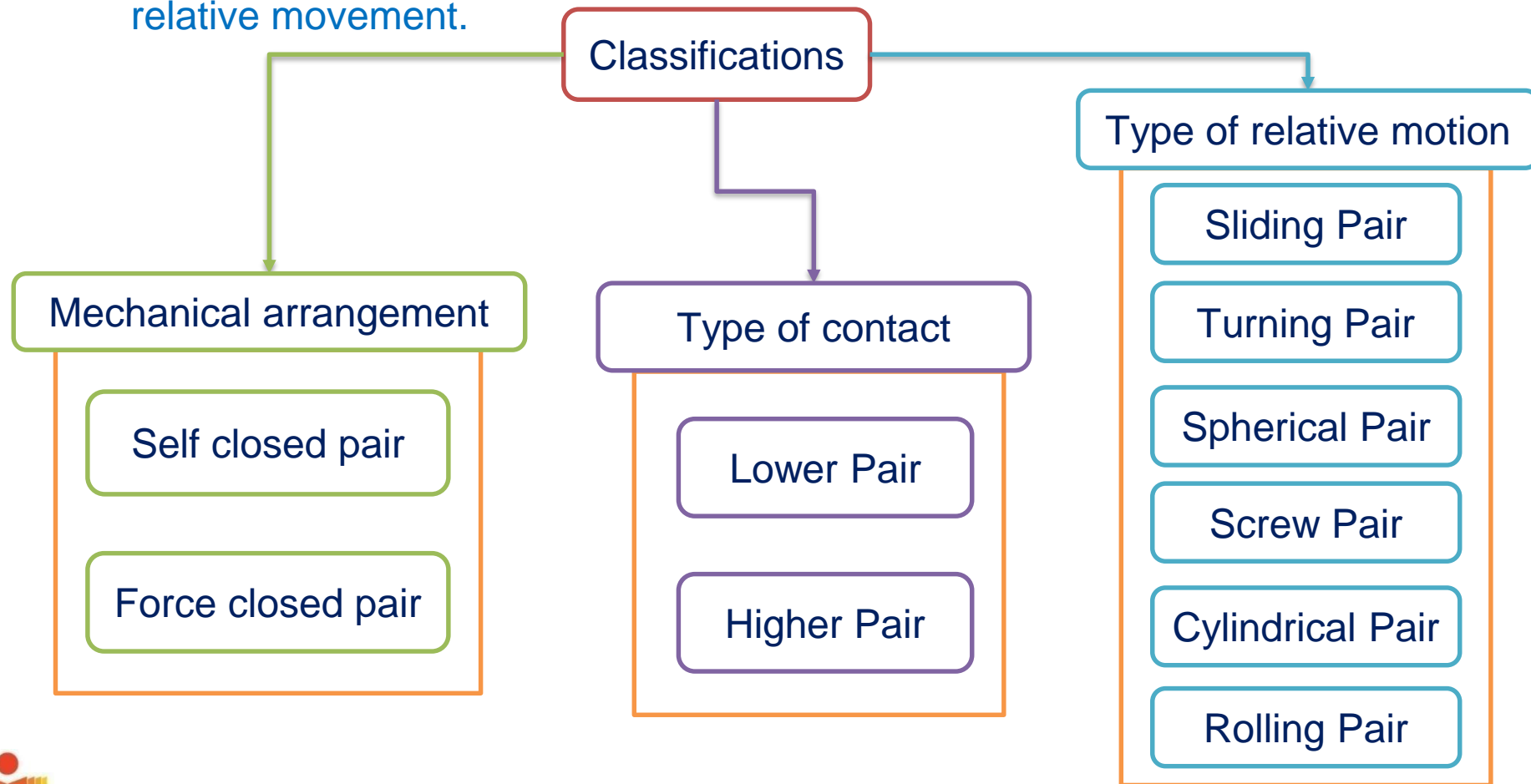
**Quaternary Link**

**Fig 6.0 Different types of link**



# Kinematic Pair

- Two links or elements of a machine connected to each other are said to form a pair, if the connection between them imposes constraints on their relative movement.



# Type of Constrained Motions

## I. Completely constrained motion :

When the motion between a pair is limited to a definite direction irrespective of the directions of force applied, then the motion is called completely constrained motion

- Example :

- i) Motion of square bar in a square hole.

- ii) Motion of a shaft with collars at each end of the hole.

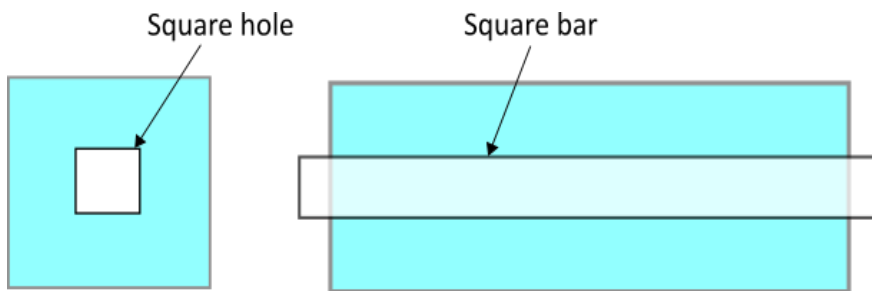


Fig 7.0 Square bar

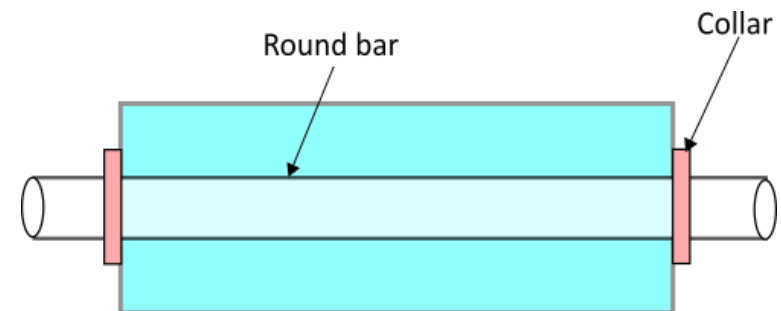


Fig 8.0 Circular bar

## II. Incompletely constrained motion :

When the motion between a pair can take place in **more than one direction**, then it is termed as incompletely constrained motion

- **Example :**

- i) Motion of circular bar or shaft in a circular hole. It can freely rotate or translate.

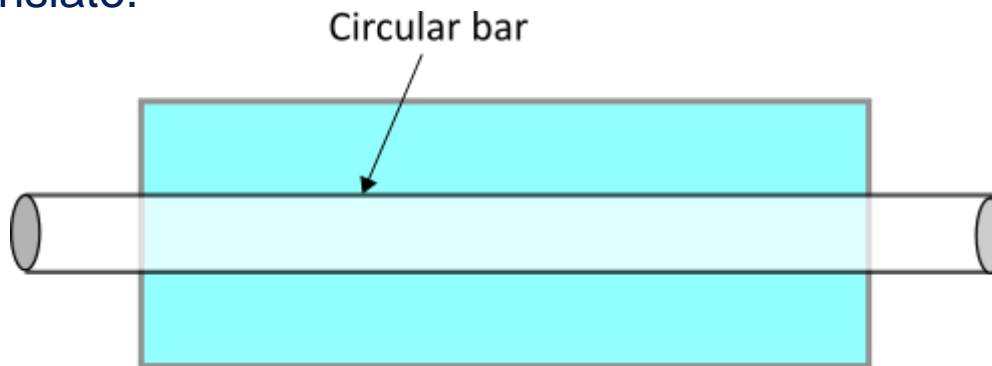


Fig 9.0 Circular bar in circular hole

## III. Successfully constrained motion :

When the motion between the elements, forming a pair, is such that the constrained motion is not completed by itself but by some other means.

- Example :
  - i) Shaft in foot-step bearing
  - ii) Piston inside the cylinder

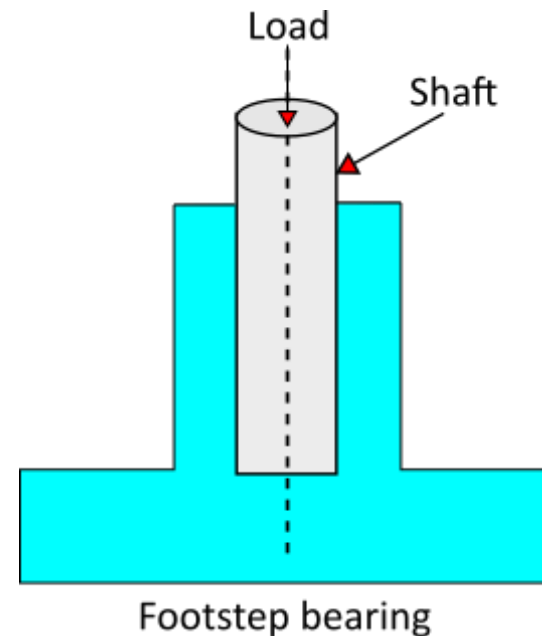


Fig 10.0 Footstep Bearing

# Classification of Kinematic pair - I

## 1. Sliding pair :

When two elements of pair are connected in such a way that one can **only slide relatively to other**, having completely constrained motion.

- **Example :** (D.O.F = 1)

Piston cylinder arrangement, ram and its guide in shaper

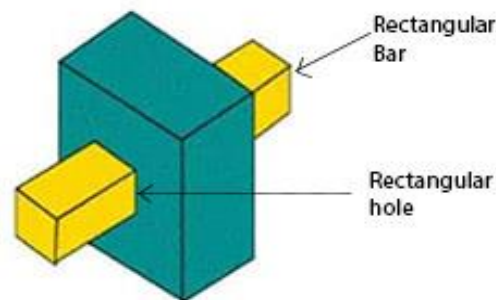


Fig 11.0 Sliding pair

## 2. Turning pair / Revolute pair :

When two elements of pair are connected in such a way that one can only turn or revolve about a fixed axis of another link.

- Example : (D.O.F = 1)

Lathe spindle supported in head stock.

Cycle wheels turning over their axles.

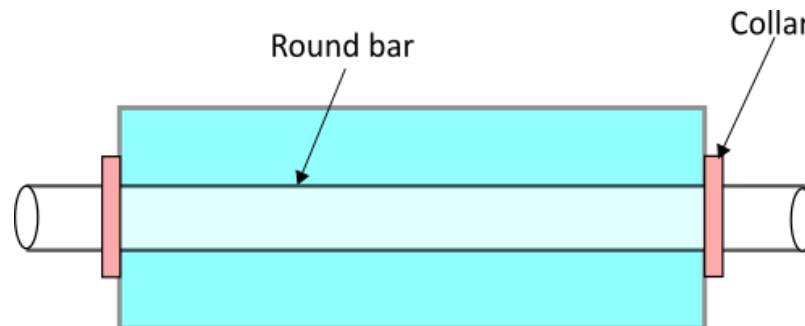


Fig 12.0 Turning pair

## 3. Spherical pair:

When two elements of pair are connected in such a way that one element turns or swivels about the other fixed element.

- Example : (D.O.F = 3)

Ball and socket joint.

Car mirror attachment.

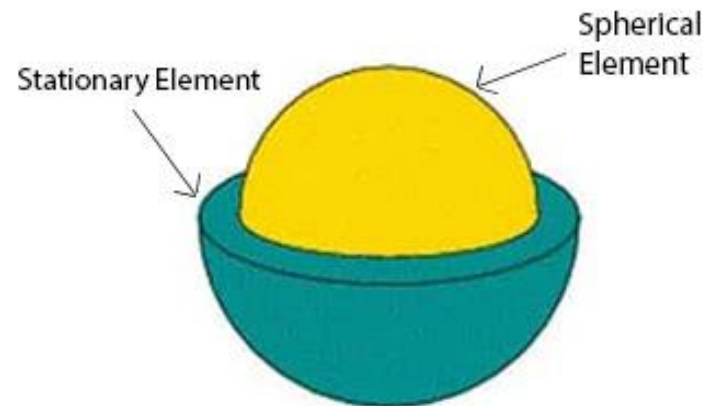


Fig 13.0 Spherical pair

## 4. Screw pair:

When two elements of pair are connected in such a way that one element can turn about the other by screw threads.

- Example : (D.O.F = 1)

Lead screw of a lathe with nut.

Bolt with nut.

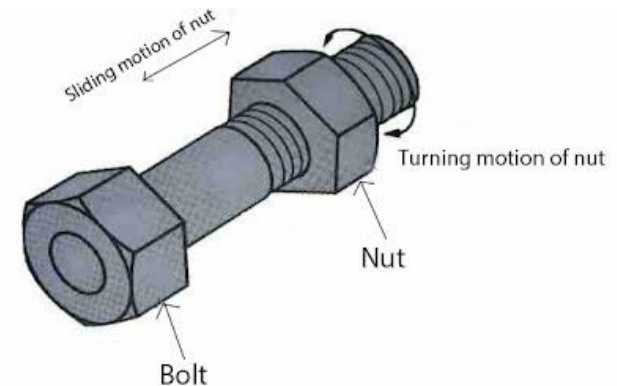


Fig 14.0 Screw pair



## 5. Cylindrical pair:

If the relative motion between the pairing elements is the combination of turning and sliding, then it is called as cylindrical pair.

- Example : (D.O.F = 2)

Lead screw of a lathe with nut.

Bolt with nut.

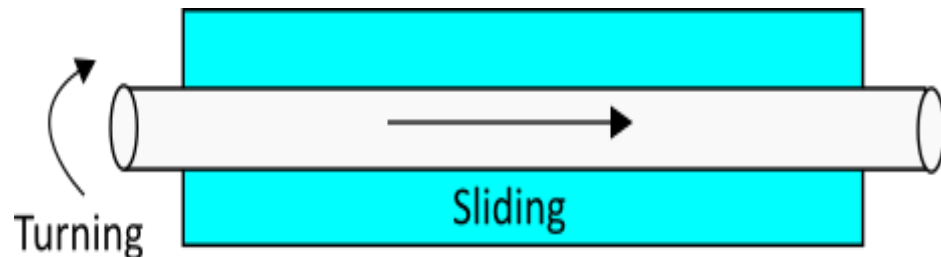


Fig 15.0 Cylindrical pair

## 6. Rolling pair:

When two elements of a pair are connected in such a way that one rolls over another fixed link.

- **Example :** (D.O.F = 1)

Ball and roller bearing.

Railway wheel rolling over a fixed rail.

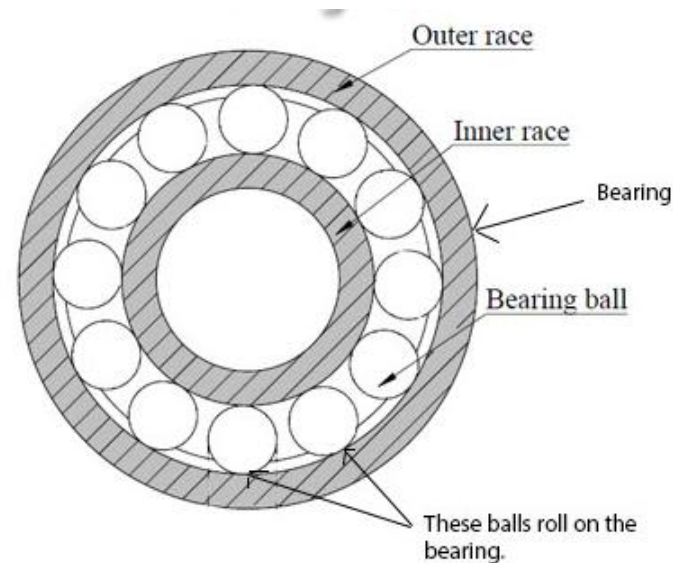


Fig 16.0 Rolling pair

# Classification of Kinematic pair - II

## 1. Lower pair :

When two elements of pair have a **surface contact**, and the surface of one element slides or rolls over the surface of the other.

- **Example :**

Sliding pairs, turning pair, & screw pair

## 2. Higher pair :

When two elements of a pair have a **line or point contact**, and the motion between the two elements is partly turning and sliding.

- **Example:**

Toothed gear, ball and roller bearing, cam and follower mechanism

# Classification of Kinematic pair - III

## 1. Self closed pair :

When two elements of pair are connected together mechanically in such a way that only required relative motion occurs.

- Example :

All Lower pairs

## 2. Force closed pair :

When two elements of a pair are kept in contact by the action of external forces, the pair is called force closed pair.

- Example:

cam and follower mechanism

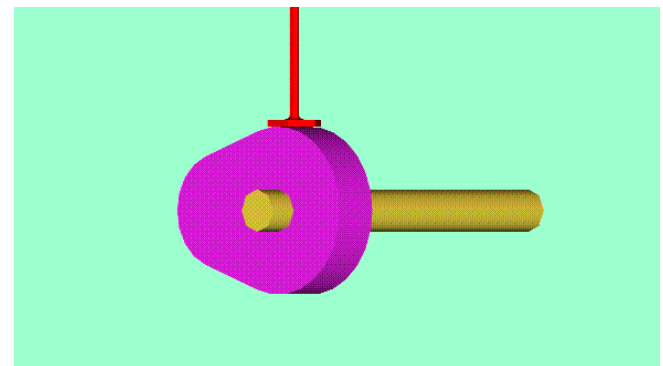


Fig 17.0 Cam and follower mechanism  
source : <https://www.pinterest.com>

# Kinematic Chain

- Kinematic chain is an assembly of rigid bodies connected by joints to provide constrained or desired motion for a mechanical system.

Or

- When the kinematic pairs are coupled in such a way that the last link is connected to the first link to transmit definite motion (completely or successfully constrained), it is called a kinematic chain.

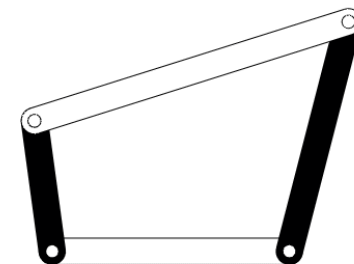


Fig 18.0 Kinematic chain

Source : <https://extrudesign.com/kinematic-chain-types/>

# Types of Kinematic Chain

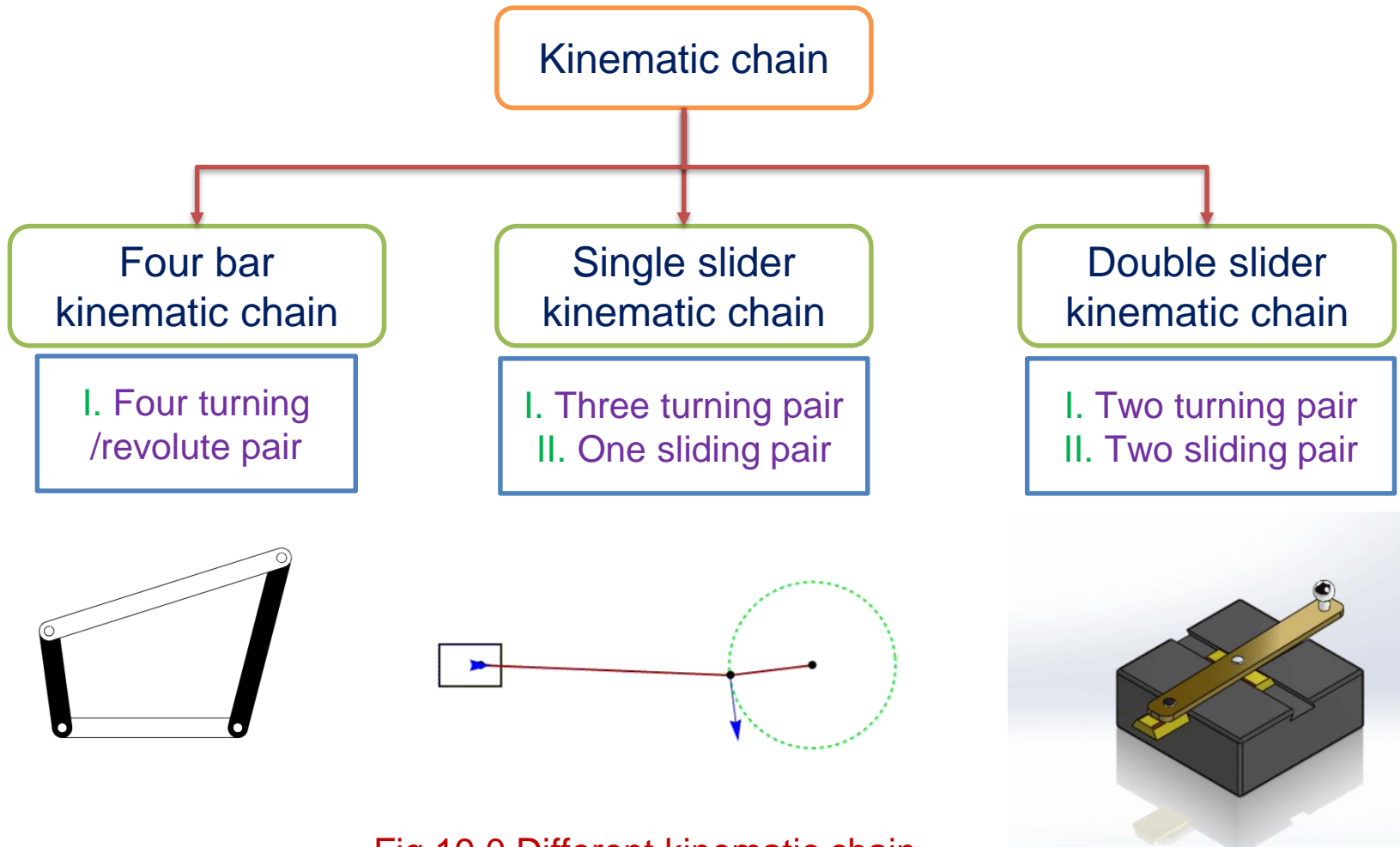


Fig 19.0 Different kinematic chain

Source : <https://extrudesign.com/kinematic-chain>

# Mechanism

- When one of the links of a **kinematic chain is fixed**, the chain is termed as mechanisms.
- It is used for transmitting or transforming motion.

**Example :** Printing machine, robot arms

- A mechanism may be regarded as a **machine** in which each part is reduced to the simplest form to **transmit the required motion**.

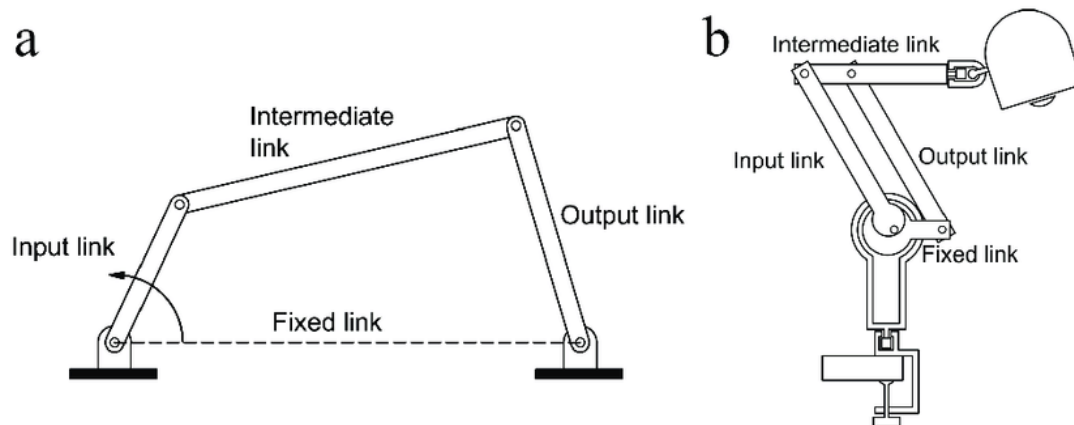


Fig 20.0 Different mechanisms

Source : <https://www.researchgate.net/figure/Four-bar-Mechanism>

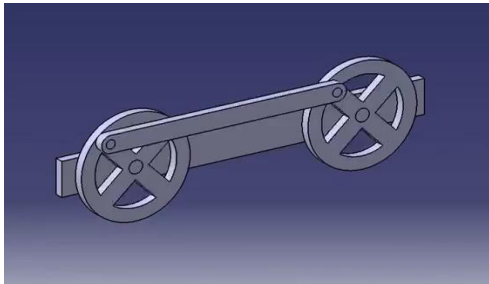
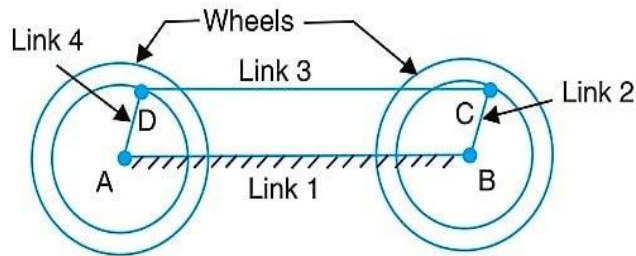
# Inversion of Mechanism - 1

- Different mechanisms can be obtained by fixing different links of the same kinematic chain.

## Inversion of Four bar chain

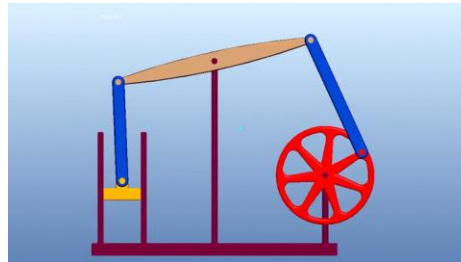
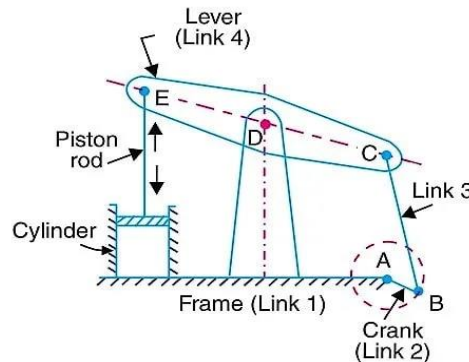
Double crank mechanism

Coupling rod of a locomotive



Crank and lever mechanism

Beam engine



Double lever mechanism

Watt's indicator

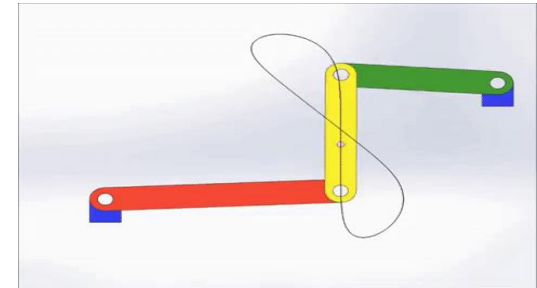
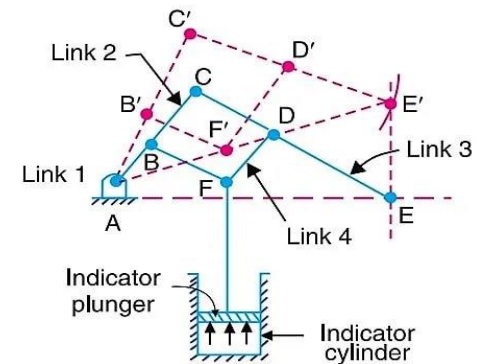


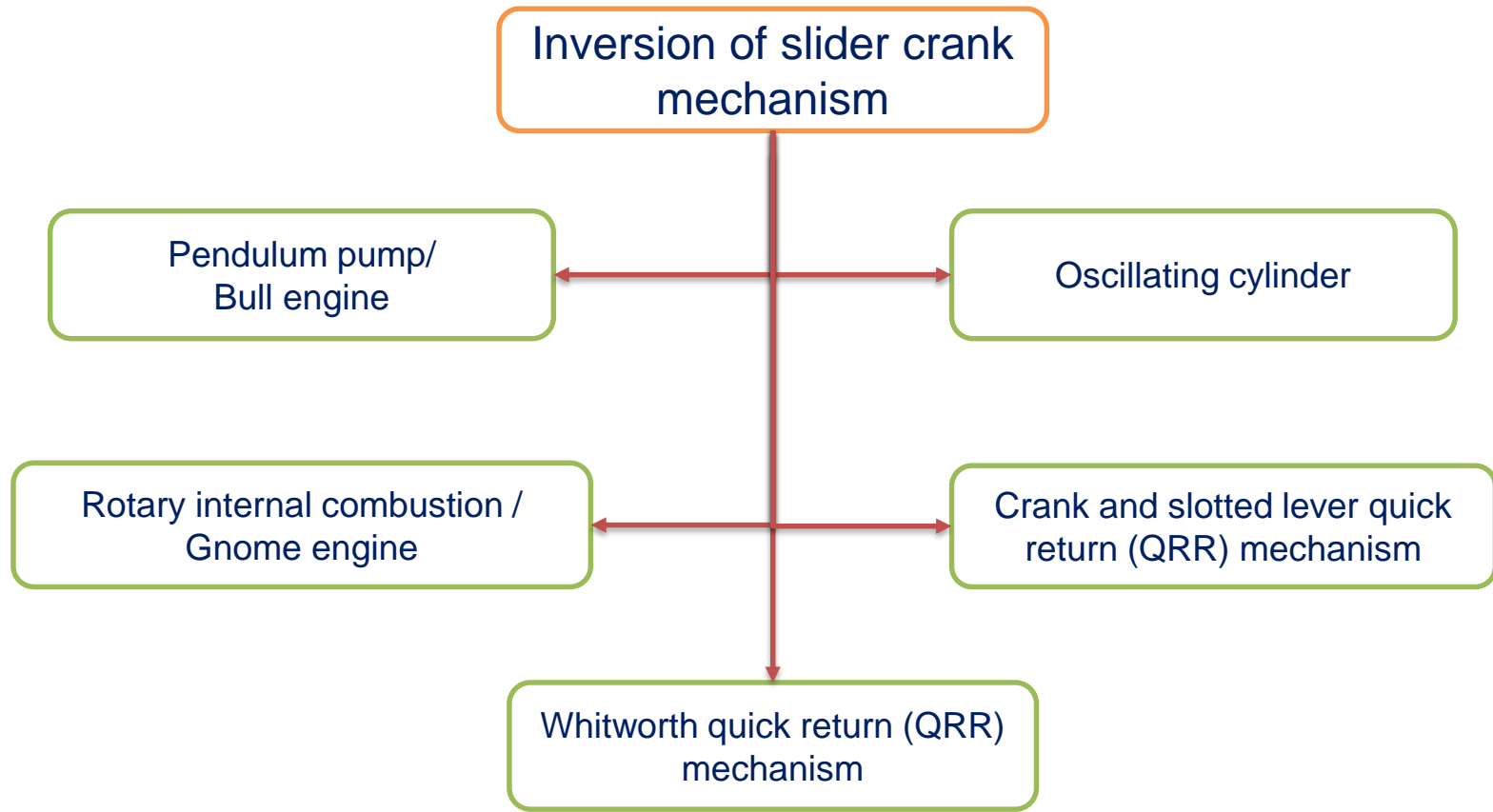
Fig 21.0 Inversion mechanisms

Source : <https://extrudesign.com/four-bar-mechanism-inversions/>



# Inversion of Mechanism - 2

- Different mechanisms can be obtained by fixing different links of the same kinematic chain.



# Cont...

## 1. Pendulum pump / Bull engine :

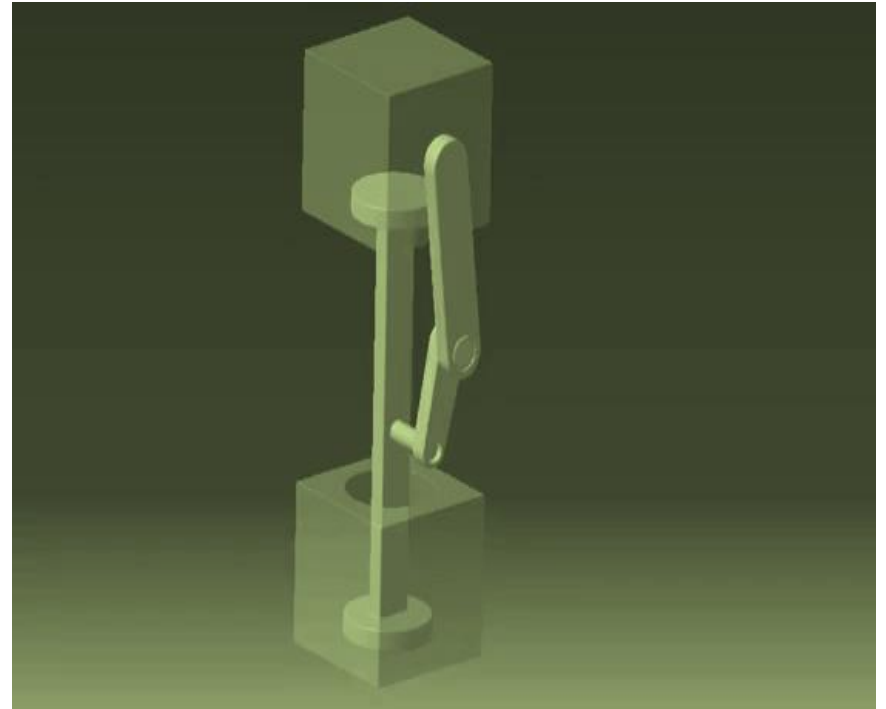
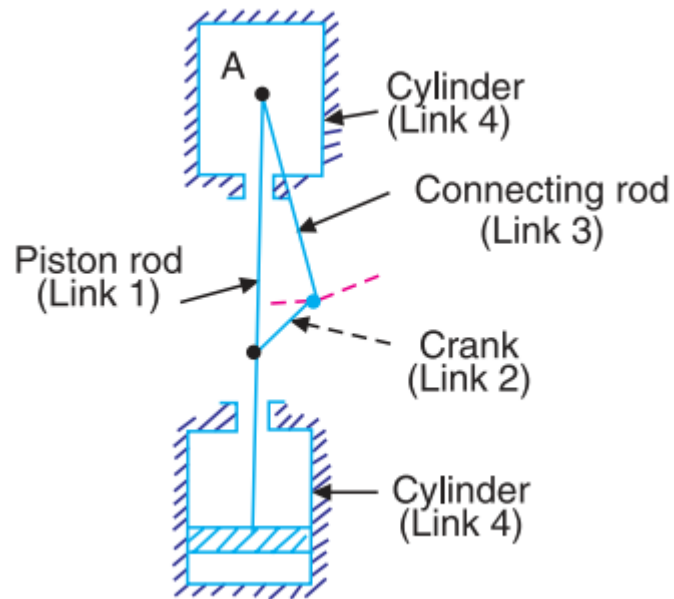
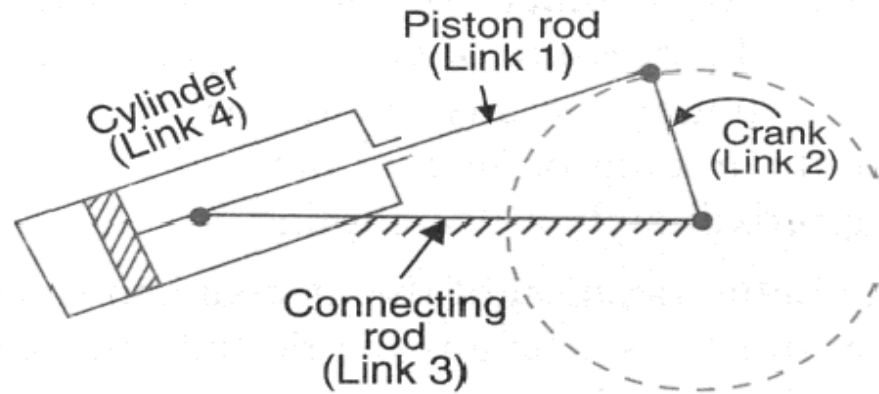


Fig 22.0 Pendulum pump

Source : <https://extrudesign.com/four-bar-mechanism-inversions/>

# Cont...

## 2. Oscillating cylinder :



Application : Steam engine

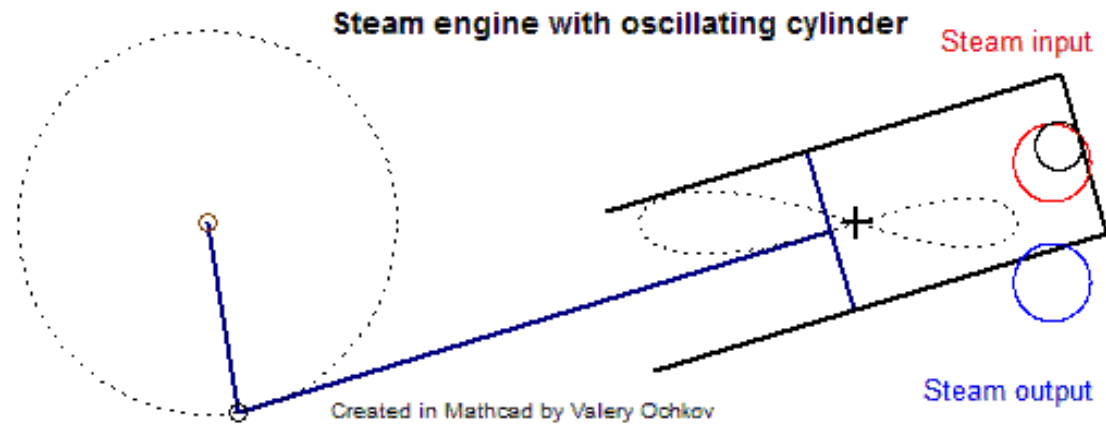
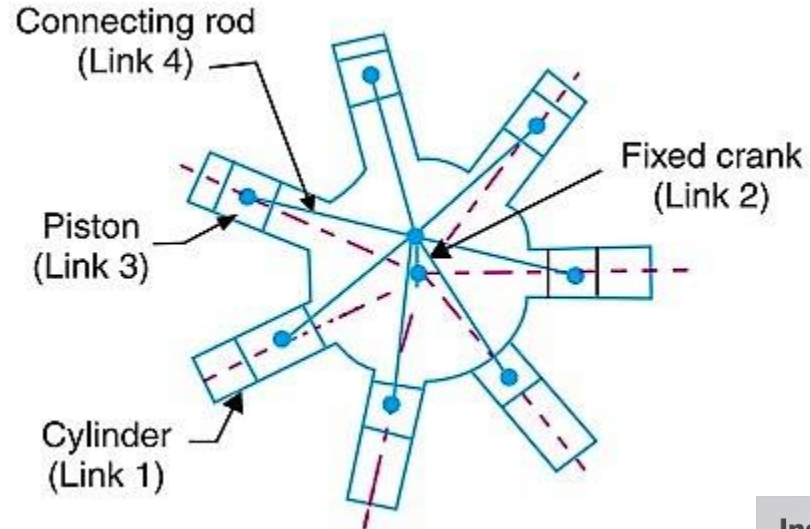


Fig 23.0 Oscillating cylinder

Source : <https://extrudesign.com/four-bar-mechanism-inversions/>

# Cont...

## 3. Gnome engine :



Application : Radial engine

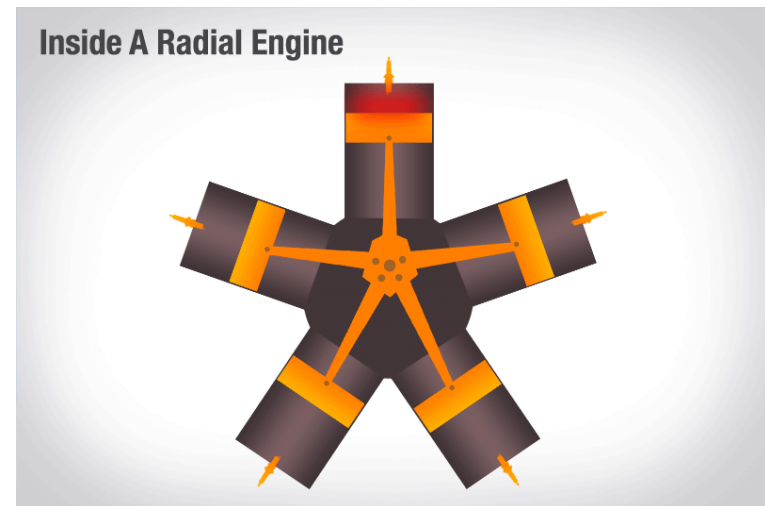


Fig 24.0 Gnome engine

Source : <https://extrudesign.com/four-bar-mechanism-inversions/>

# Cont...

## 4. Crank and slotted QRR:



Application : Shaper machine,  
Cutting machines

## 5. Whitworth QRR:

Application : High velocity impact  
press, slotting machines

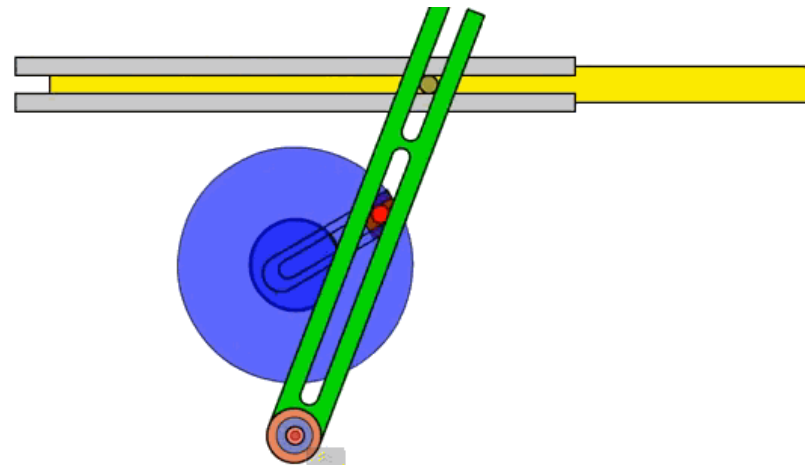


Fig 25.0 QRR mechanism  
Source : <https://skill-lync.com/>