

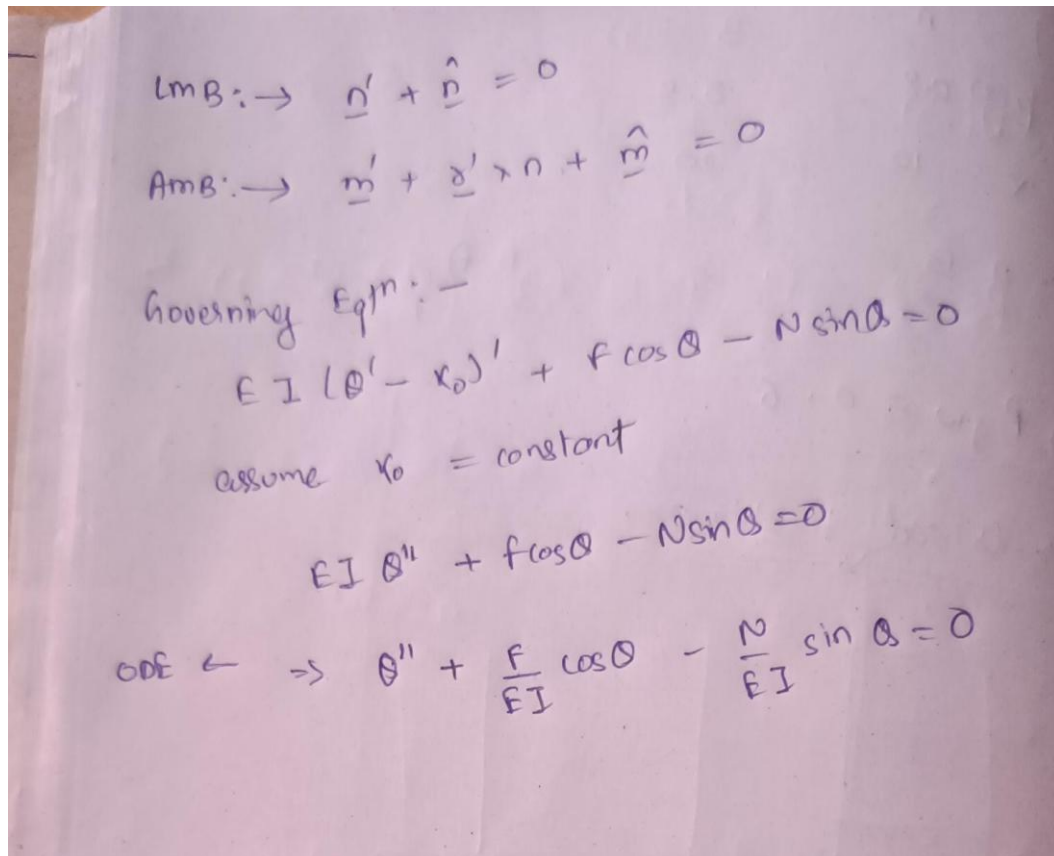
Question:

1. Plot the deformed gripper shape assuming values of F, N, EI, k_0, L
2. Find N , such that $r_3(L) = b/2$ (b : length of the workpiece).
3. Calculate maximum frictional resistance μN .

Answer:

Note: .ipynb file containing the python code for the question is attached.

1)



Handwritten mathematical derivation for the deflection of a gripper beam:

$$\text{ImB:} \rightarrow \underline{\theta}' + \hat{n} = 0$$

$$\text{AmB:} \rightarrow \underline{m}' + \underline{s}' \times n + \hat{m} = 0$$

Governing Eqⁿ: -

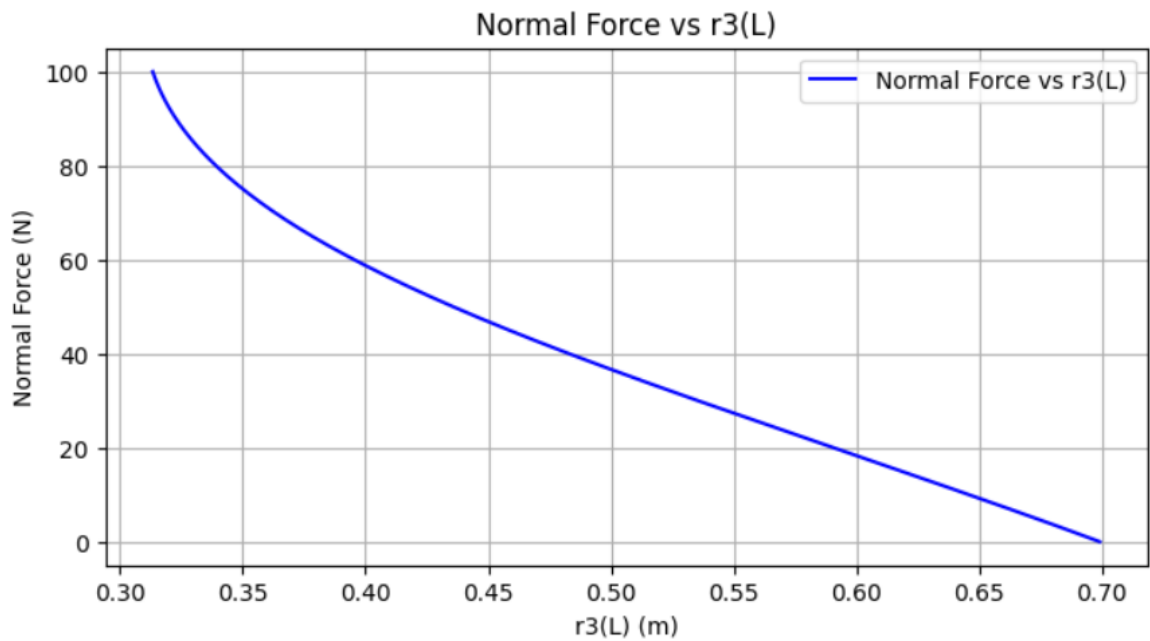
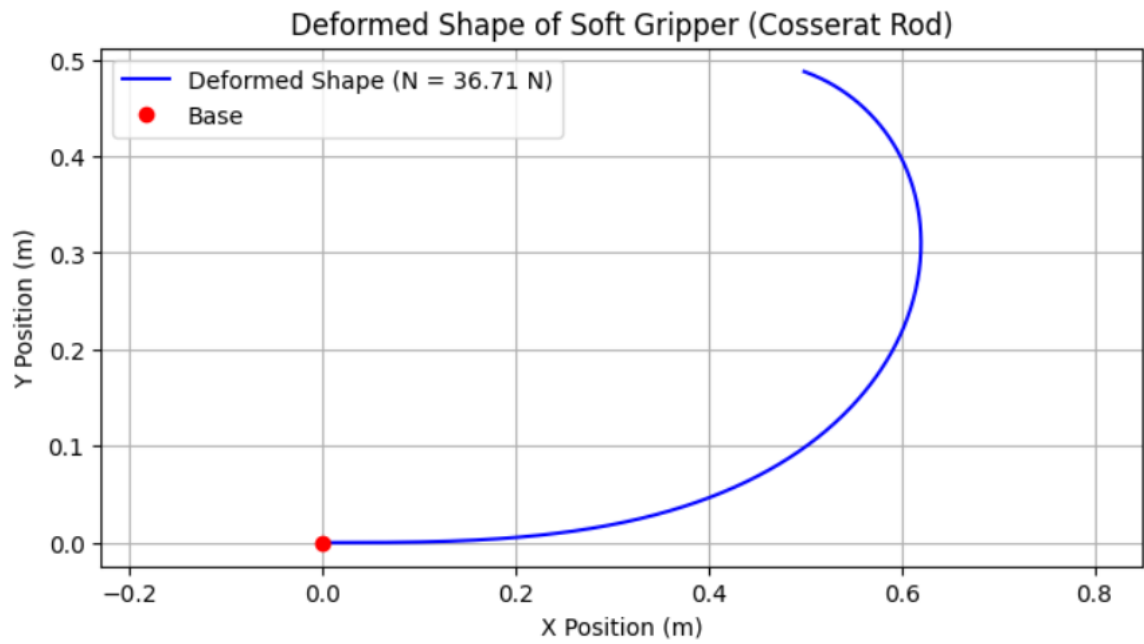
$$EI (\theta' - \kappa_0)' + F \cos \theta - N \sin \theta = 0$$

assume $\kappa_0 = \text{constant}$

$$EI \theta'' + F \cos \theta - N \sin \theta = 0$$

ODE $\leftrightarrow \theta'' + \frac{F}{EI} \cos \theta - \frac{N}{EI} \sin \theta = 0$

Required Normal Force (N) using Newton-Raphson: 36.7140 N



Maximum Frictional Resistance: 18.3570 N

The Cosserat rod equation for a soft robotic gripper

$$EI(\theta' - k_0)' + F\cos\theta - N\sin\theta = 0$$

Where:

- E is the Young's modulus,
- I is the moment of area,
- θ is the bending angle,
- k is the initial curvature,
- F and N are force components along the rod.

Assuming the unknown values

2) Maximum Normal Force = 36.714 N.

To determine the internal normal force N that ensures the gripper's end position $r_3(L)$ aligns with half the workpiece length $b/2$, we follow these steps:

1. Define the Objective Function

- Solve the governing differential equation for a given N .
- Compute $r_3(L)$ using numerical integration.
- Define an equation where the difference between $r_3(L)$ and $b/2$ is minimized.

2. Use the Newton-Raphson Method to Find N

- Iteratively adjust N using Newton-Raphson's formula.
- Converge to a solution where the objective function approaches zero.

This process ensures that the normal force N is accurately determined to match the specified boundary condition for the gripper's deformation.

3) Maximum Frictional Force = 18.35 N.

The maximum frictional resistance is given by:

$$F_{\max} = \mu N.$$

Where:

- μ is the coefficient of friction.
- N is the normal force calculated in Part (b).

This frictional resistance determines the maximum force the gripper can apply without slipping.