ME3030 Assignment 3

ME21BTECH11001
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Damping force, $f_c = -c(\tilde{r}_i - \tilde{s}_i)$ for m_i ,

 $m = \{ \frac{1}{3} \} = R \frac{(182-31)-1}{(182-31)} = R \frac{(182-3$

where 182-811 = 1 (4,-41)2+ (2-21)2

Let $Y = [n_1, y_1, v_3], v_3y_1, n_2, y_2, v_{n_2}, v_{g_2}]$ By RK4 method ?- $Y_{n+1} = Y_n + \frac{h}{6}(k_1 + 2k_2 + 2k_3 + k_4)$

 $t_{n+1} = t_n + h \qquad h = 0,1 - \dots$

where
$$k_1 = \int (t_n, y_n)$$
 $R_2 = \int (t_n + \frac{h}{2}, y_n + h \frac{k_1}{2})$
 $R_3 = \int (t_n + \frac{h}{2}, y_n + h \frac{k_2}{2})$
 $R_4 = \int (t_n + h, y_n + h k_3)$
 $K \cdot E = \int m_1 v_1^2 + \int m v_2^2$
 $Spring PE = \int R (|v_2 - v_3| - L)^2$
 $PE = m_1 g g_1 + m_2 g g_2$
 $g_1 = \begin{cases} v_1 \\ v_2 \end{cases}$

$$\frac{3}{10} = \alpha_{1}$$

$$\frac{3}{10} = \alpha_{2}$$

$$\frac{3}{10} =$$

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% ME21BTECH11001 Abhishek Ghosh
% Define system parameters
             % Mass of ml in kg
m1 = 1.0;
m2 = 1.0;
               % Mass of m2 in kg
k = 1000.0;
               % Spring stiffness in N/m
               % Damping coefficient in Ns/m
c = 5.0;
             % Free length of the spring in m
1 = 0.5;
             % Acceleration due to gravity in m/s^2
g = 9.81;
% Positions in order x1, y1, x2, y2
init_position = [0.0; 0.0; 0.5; 0.0];
final position = [1.0; 1.0; 1.0; 1.5];
% Guess for initial velocities in order vx1, vy1, vx2, vy2
v = [0.5; -0.5; -0.\overline{5}; 0.5];
% Small change
dv = 1.0e-3;
% Convergence criteria
epsilon = 1e-3;
initial time = 0.0;
final_time = 2.0;
while(true)
    temp_final_position = rk4_solve(init_position, v, initial_time, final_time, m1,
m2, k, c, l, g);
    f = temp final position - final position;
    if (max(abs(f))) < epsilon
        temp_final_position
        break
    end
    % Jacobian
    J = zeros(4, 4);
    for i = 1:4
        temp v = v;
        temp v(i) = temp v(i) + dv;
        temp_final_position_dv = rk4_solve(init_position, temp_v, initial time,
final time, \overline{m1}, m2, k, c, l, g);
        J col = zeros(4, 1);
        for j = 1:4
            derivative = (temp final position dv(j) - temp final position(j)) / dv;
            J_{col}(j) = derivative;
        end
        J(:, i) = J_{col};
    end
    v = v - J \setminus f;
end
function final_position = rk4_solve(init_position, init_velocity, init_time,
final_time, m1, m2, k, c, l, g)
    % Initial conditions
    x1 i = init_position(1);
    y1_i = init_position(2);
  vx1_i = init_velocity(1);
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vy1_i = init_velocity(2);
    x2_i = init_position(3);
    y2_i = init_position(4);
    vx2_i = init_velocity(3);
vy2_i = init_velocity(4);
    % Time step
    dt = 1.0e-5;
    % Number of time steps
    num_steps = round((final_time - init_time) / dt + 1);
    \ensuremath{\mbox{\$}} Initialize arrays to store positions and velocities
    x1 = zeros(1, num_steps);
y1 = zeros(1, num_steps);
    vx1 = zeros(1, num_steps);
    vy1 = zeros(1, num steps);
    x2 = zeros(1, num_steps);
    y2 = zeros(1, num steps);
    vx2 = zeros(1, num_steps);
    vy2 = zeros(1, num_steps);
    % Set initial conditions
    x1(1) = x1 i;
    y1(1) = y1_i;
    vx1(1) = vx1_i;
    vy1(1) = vy1 i;
    x2(1) = x2 i;
    y2(1) = y2_i;
    vx2(1) = vx2 i;
    vy2(1) = vy2_i;
    arr = [x1(1); y1(1); vx1(1); vy1(1); x2(1); y2(1); vx2(1); vy2(1)];
    % Using RK4 method
    for i = 1:num steps-1
        k1 = dt * calculate_derivative(arr, m1, m2, k, c, l, g);
        k2 = dt * calculate_derivative(arr + 0.5 * k1, m1, m2, k, c, l, g);
k3 = dt * calculate_derivative(arr + 0.5 * k2, m1, m2, k, c, l, g);
        k4 = dt * calculate_derivative(arr + k3, m1, m2, k, c, 1, g);
        arr = arr + (k1 + 2.0 * k2 + 2.0 * k3 + k4) / 6.0;
        x1(i+1) = arr(1);
        y1(i+1) = arr(2);
        vx1(i+1) = arr(3);
        vy1(i+1) = arr(4);
        x2(i+1) = arr(5);
        y2(i+1) = arr(6);
        vx2(i+1) = arr(7);
        vy2(i+1) = arr(8);
    final_position = [arr(1); arr(2); arr(5); arr(6)];
function calculated der = calculate derivative(arr, m1, m2, k, c, l, g)
   x1 = arr(1);
    y1 = arr(2);
  vx1 = arr(3);
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vy1 = arr(4);
   x2 = arr(5);
   y2 = arr(6);
   vx2 = arr(7);
   vy2 = arr(8);
   distance = sqrt((x1 - x2)^2 + (y1 - y2)^2);
   spring_force = k * (distance - 1);
   damper_force_x = c * (vx2 - vx1);
   damper_force_y = c * (vy2 - vy1);
   ax1 = (spring_force * (x2 - x1)) / (m1 * distance) + damper_force_x / m1;
   ay1 = (spring_force * (y2 - y1)) / (m1 * distance) + damper_force_y / m1 - g;
   calculated_der = [vx1 ; vy1 ; ax1 ; ay1 ; vx2 ; vy2 ; ax2 ; ay2];
temp_final_position =
   1.0000
   1.0000
   1.0000
   1.5000
v =
  21.8235
  10.2166
 -15.9017
  10.8252
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The above values are for vx1,vy1,vx2,vy2