Advance Clipping Algorithms

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Consider the parametric definition of a line:

```
-x = x_1 + u\Delta x
-y = y_1 + u\Delta y
-\Delta x = (x_2 - x_1), \, \Delta y = (y_2 - y_1), \, 0 \le (u) \le 1
```

 What if we could find the range for u in which both x and y are inside the viewport?

- Mathematically, this means
 - $-X_{min} \leq X_1 + U\Delta X \leq X_{max}$
 - $-y_{min} \le y_1 + u\Delta y \le y_{max}$
- Rearranging, we get
 - $--u\Delta x \leq (x_1 x_{min})$
 - $-u\Delta x \leq (x_{max} x_1)$
 - $--u\Delta y \leq (y_1 y_{min})$
 - $-u\Delta y \leq (y_{max} y_1)$
 - In general: $u * p_k \le q_k$

Cases:

$$1.p_k = 0$$

- Line is parallel to boundaries
 - If for the same k, $q_k < 0$, reject
 - Else, accept

$2.p_k < 0$

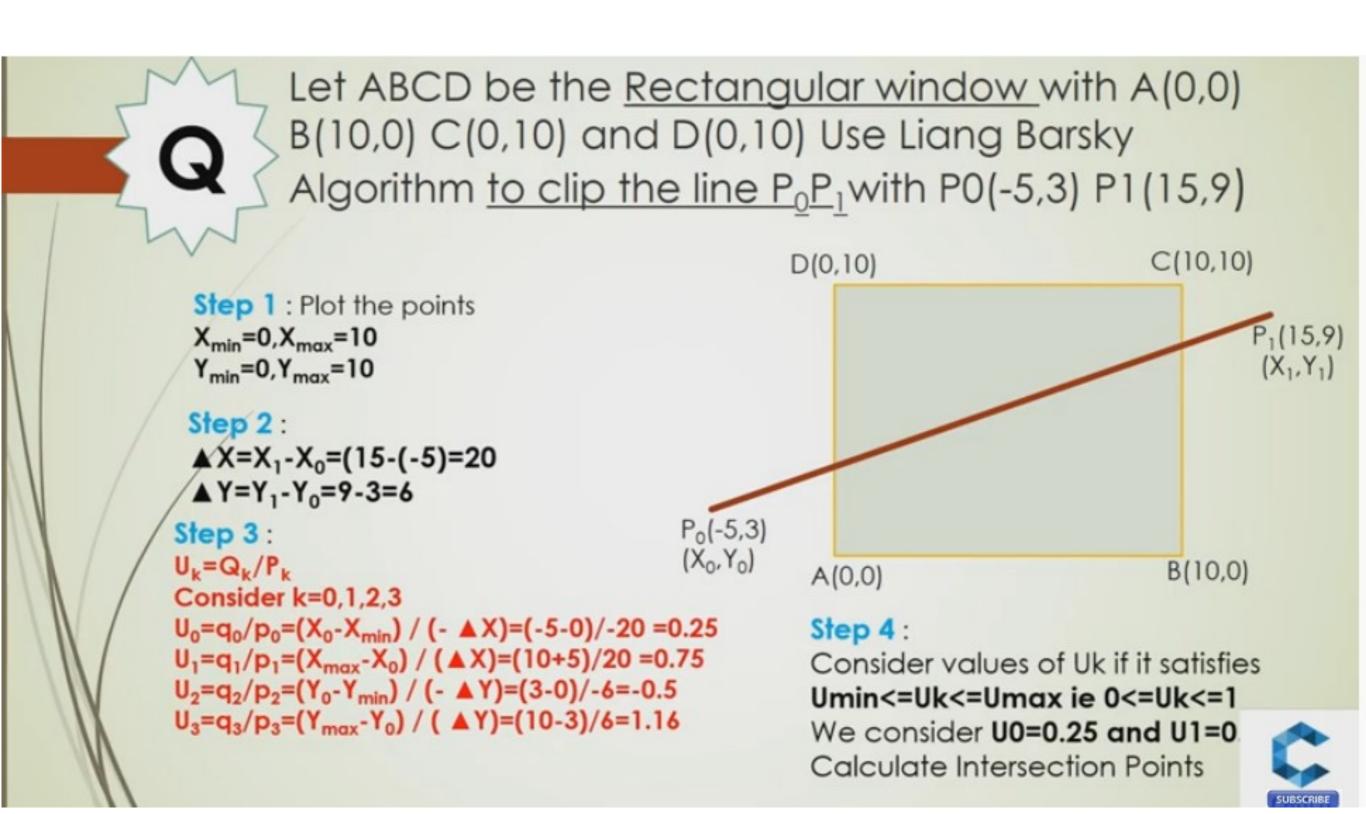
Line starts outside this boundary

$$-r_k = q_k / p_k$$

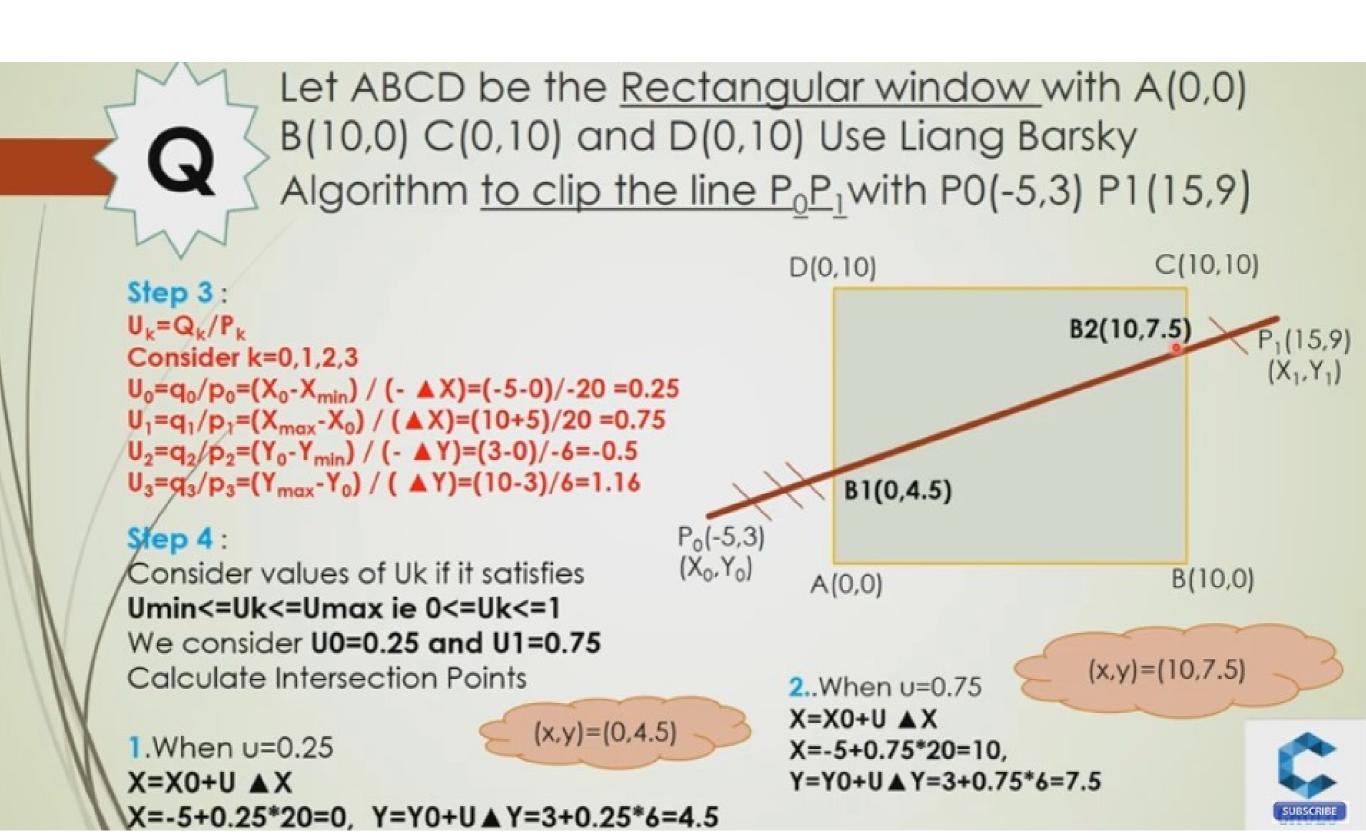
$$-u_1 = max(0, r_k, u_1)$$

- Cases: (cont'd)
 - $3.p_k > 0$
 - Line starts inside this boundary
 - $-r_k = q_k / p_k$ $-u_2 = min(1, r_k, u_2)$
 - 4.If u₁ > u₂, the line is completely outside

Example



Example



- In most cases, Liang-Barsky is slightly more efficient
 - Avoids multiple shortenings of line segments
- However, Cohen-Sutherland is much easier to understand
 - An important issue if you're actually implementing

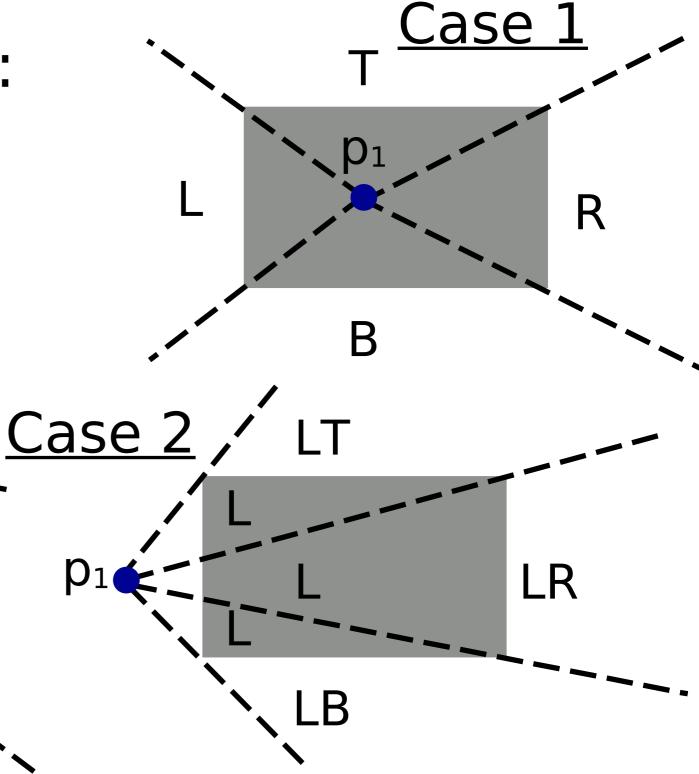
Nicholl-Lee-Nicholl Line Clipping • This is a theoretically optimal

- This is a theoretically optimal clipping algorithm (at least in 2D)
 - However, it only works well in 2D
- More complicated than the others
- Just do an overview here

Nicholl-Lee-Nicholl Line Clinning

- Partition the Clipping region based on the first point (p₁):
 - Case 1: p₁ inside region
 - Case 2: p₁ across edge
 - Case 3: p₁ across

Case 3



Nicholl-Lee-Nicholl Line Clipping

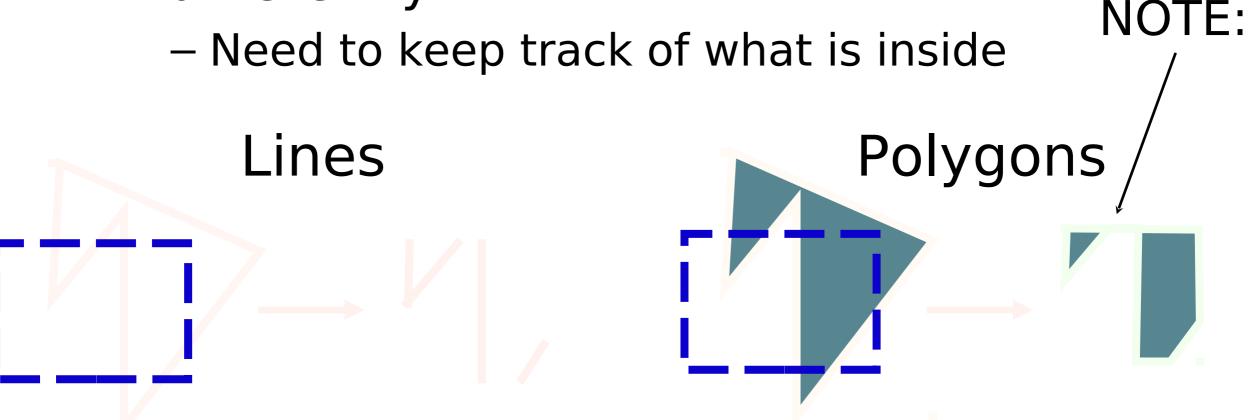
- Can use symmetry to handle all other cases
- "Algorithm" (really just a sketch):
 - Find slopes of the line and the 4 region bounding lines
 - Determine what region p₂ is in
 - If not in a labeled region, discard
 - If in a labeled region, clip against the indicated sides

A Note on Redundancy

- Why am I presenting multiple forms of clipping?
 - Why do you learn multiple sorts?
 - Fastest can be harder to understand / implement
 - Best for the general case may not be for the specific case
 - Bubble sort is really great on mostly sorted lists
 - "History repeats itself"
 - You may need to use a similar algorithm for something else; grab the closest match

Polygon Clipping

Polygons are just composed of lines.
 Why do we need to treat them differently?

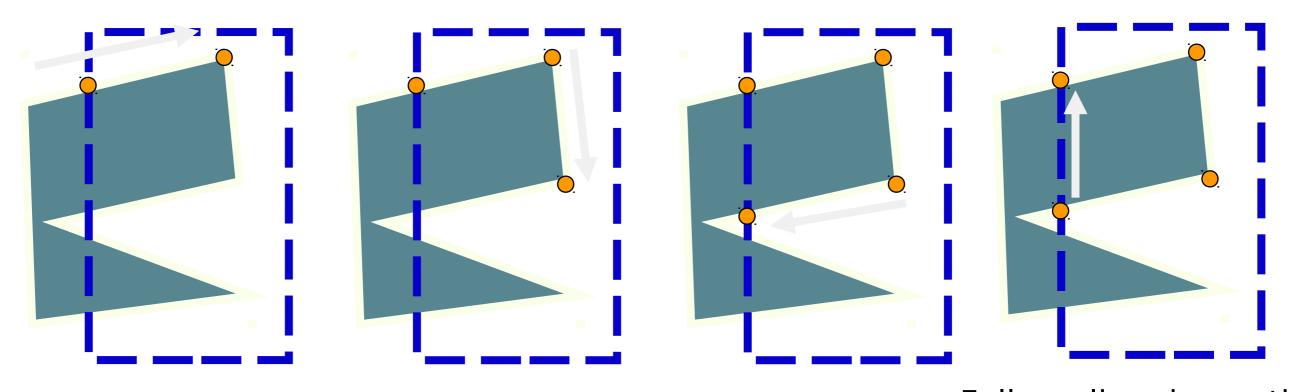


 When using Sutherland-Hodgeman, concavities can end up linked

Remember this?

 A different clipping algorithm, the Weiler-Atherton algorithm, creates separate polygons

• Example:



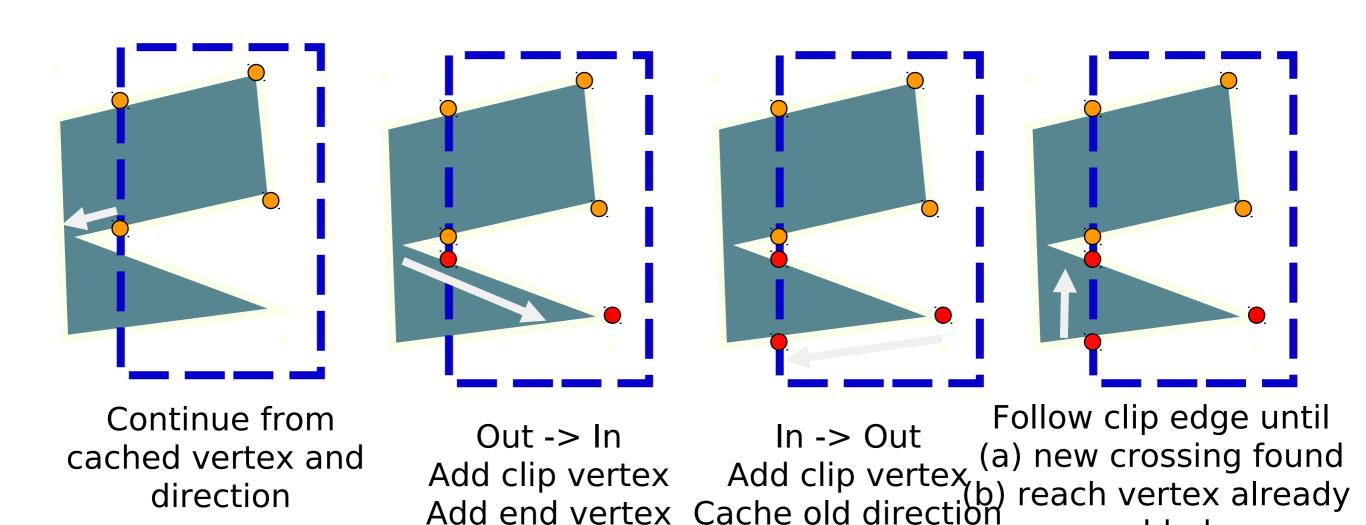
Out -> In
Add clip vertex
Add end vertex

In -> In Add end vertex

In -> Out
Add clip vertex
Cache old direction

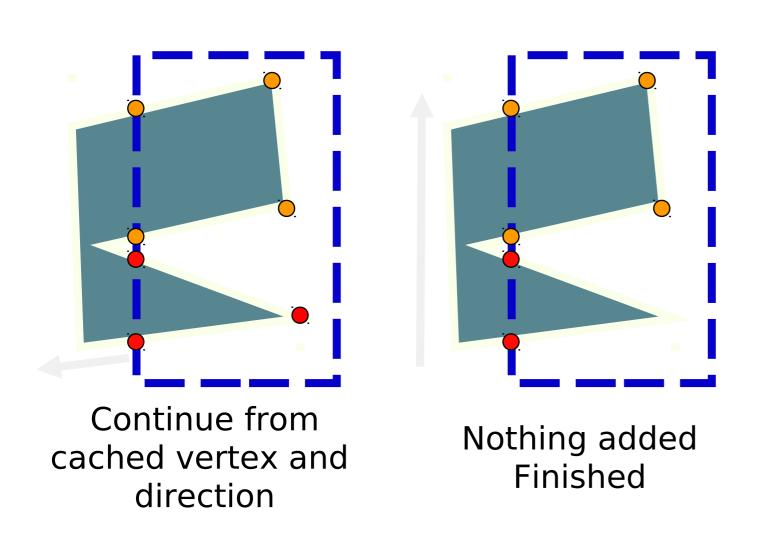
Follow clip edge until
(a) new crossing found
(b) reach vertex already
added

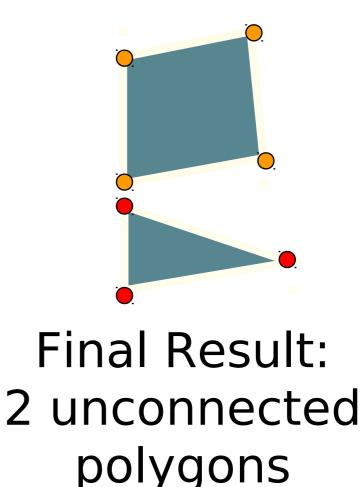
• Example (cont'd):



added

• Example (cont'd):





- Difficulties:
 - What if the polygon rec. ss. an edge?
 - How big should your cach
 - Geometry step must be able to create new polygons
 - Not 1 in, 1 out

Done with Clipping

- Point Clipping (really just culling)
 - Easy, just do inequalities
- Line Clipping
 - Cohen-Sutherland Any Questions?
 - Liang-Barsky
 - Nicholl-Lee-Nicholl
- Polygon Clipping
 - Sutherland-Hodgeman
 - Weiler-Atherton