

Why?
Unbreakable?

Bit level shuffling

Page No.

Date

* AES (Advanced Encryption Standard)

→ NIST - 2001

→ scandisk

FD

HD

Secure Access Program } AES 128-bit

In our syllabus,

① AES - 128 bit

② AES - 192 bit

③ AES - 256 bit

Key Size

128 bit

192 bit

256 bit

No. of Rounds

10

12

14

→ Lightweight algo. Used in mobile phone.

→ If password lost, cannot be recovered.

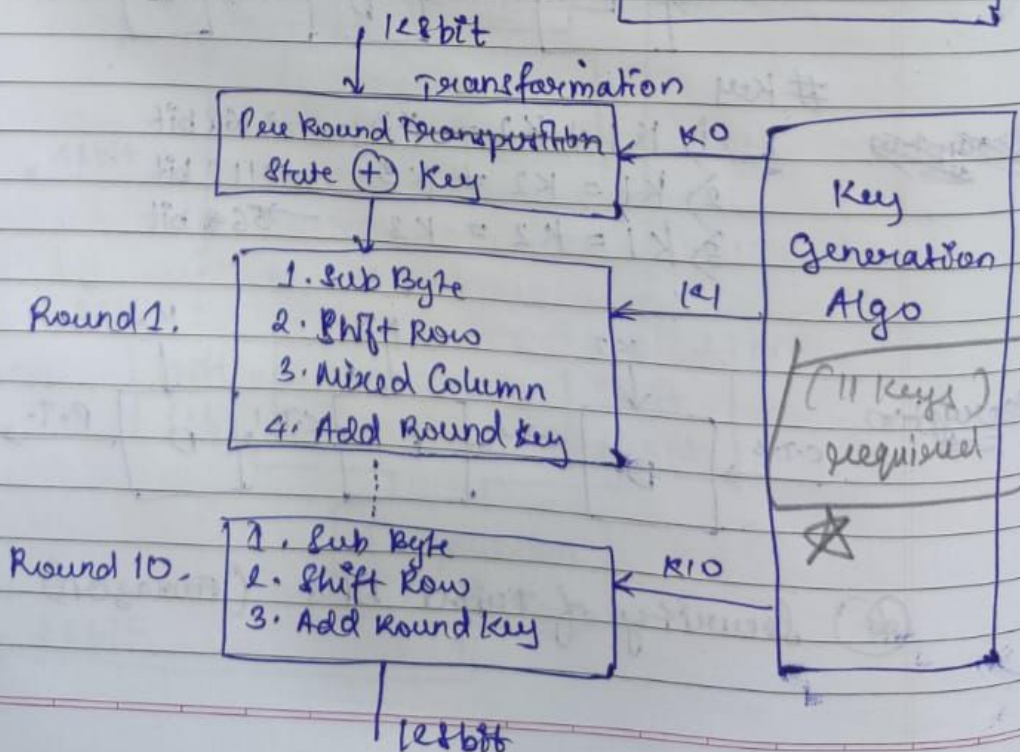
→ If you know, AES is unbreakable (due to bit level shuffling)

Mixed Column Operation

* AES - 128 bit.

Block Diagram of AES:

State: - 4x4 Matrix
16x8 = 128 bit





En Exam
For numerical 2x2

State: UPPER CASE ONLY

Ⓐ Per Round Transformation.

$$\begin{bmatrix} a_0 & a_4 & a_8 & a_{12} \\ a_1 & a_5 & & \\ a_2 & a_6 & & \\ a_3 & a_7 & & a_{15} \end{bmatrix} \text{ State.}$$

Input \Rightarrow ABCDEF OP

$$\begin{bmatrix} A & E & I & M \\ B & F & J & N \\ C & G & K & O \\ D & H & L & P \end{bmatrix}$$

Key \Rightarrow DJCANGHVICDECOMP.

$$\begin{bmatrix} D & N & I & C \\ J & G & C & O \\ S & H & O & M \\ A & V & E & P \end{bmatrix}$$

	Hex		Hex
A	00	N	0D
B	01	O	0E
C	02	P	0F
D	03	Q	10
E	04	R	11
F	05	S	12
G	06	T	13
H	07	U	14
I	08	V	15
J	09	W	16
K	0A	X	17
L	0B	Y	18
		Z	19

Key
Generation
Algo

(11 keys)
required

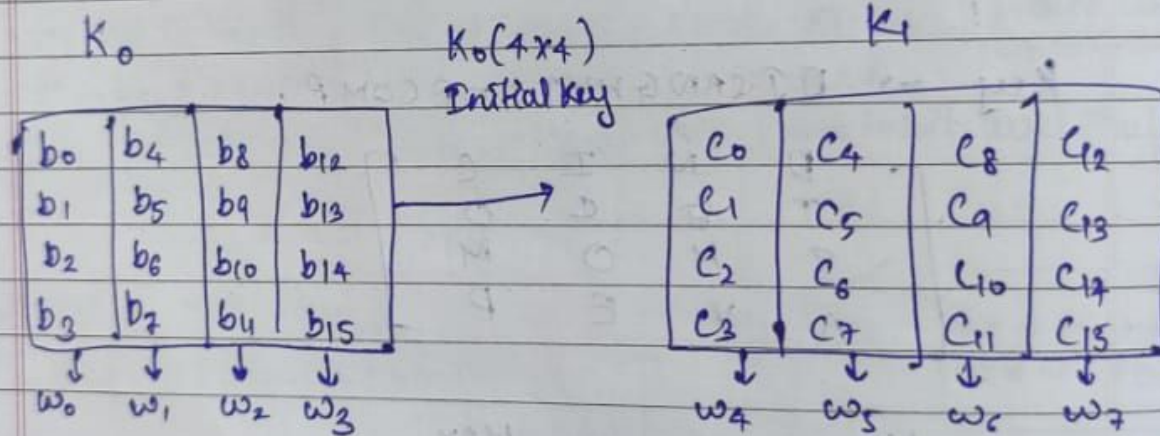


State \oplus Key
 A \oplus D
 Hexa $\left\{ \begin{array}{l} \text{00} \oplus \text{03} \end{array} \right.$
 8-bit $\left\{ \begin{array}{l} \text{00} \oplus \text{03} \end{array} \right.$
 Binary $\left\{ \begin{array}{l} \text{00} \oplus \text{03} \end{array} \right.$

$$\begin{aligned} &0000\ 0000 \oplus 0000\ 0011 \\ &= 0000\ 0011 \\ &= D \end{aligned}$$

* Key Expansion in AES 128 bit Algo.

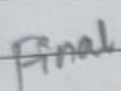
13/3/24



$$\begin{aligned} w_4 &= w_0 \oplus g(w_3) \\ w_5 &= w_1 \oplus w_4 \\ w_6 &= w_2 \oplus w_5 \\ w_7 &= w_3 \oplus w_6 \end{aligned}$$

What happens -

b_{12} b_{13} b_{14} b_{15}
 \downarrow \downarrow \downarrow \downarrow
 b''_{13} b''_{14} b''_{15} b''_{16}



Round 1 = 01

$$2 = 02$$

3 = 04

4 = 08

$$5 = 10$$

1

Round 10 = 36

$$R_{ij} = x^{i-1} \text{ mod prime.}$$

128-bit

Q) Using AES Key Expansion technique generate w_4 & w_5 .

$$w_0 = \{24, 75, A2, B3\}$$

$$w_3 = \{13, AA, 54, 87\}$$

$$w_1 = \{34, 75, 56, 88\}$$

S-Box

13	AA	54	87
AC	20	17	7D

→

7D
 ↙ ↘
 0111 1101

$$w_4 = ?$$

Formulae:

$$w_0 \oplus g(w_3)$$

$$w_5 = ?$$

$$w_1 \oplus w_4$$

Start:- $g(w_3)$

13	AA	54	87
----	----	----	----

Do 1 byte circular left shift

AA	54	87	13
----	----	----	----

S-Box

(Given in Question)

20	17	7D	AC
----	----	----	----

Convert into binary

+

01	00	00	00
----	----	----	----

2)

+

3) Convert back to hexadecimal.

x_1	x_2	x_3	x_4
-------	-------	-------	-------

00	0
11	0
01	1
10	1

$$\begin{array}{r} 01 \\ 01 \\ \oplus \\ \hline 00 \end{array}$$

Page No.	
Date	

$$\begin{aligned} x_1 &= 20 \oplus 01 \\ &= (\text{binary of } 20) \oplus (\text{binary of } 01) \quad (\text{Lazy to convert}) \\ &= 21 \quad \rightarrow \text{Hexa} \end{aligned}$$

$$\begin{aligned} x_2 &= 17 \oplus 00 \\ &= \text{binary} \oplus \text{binary} \\ &= 17 \quad \rightarrow \text{Hexa} \end{aligned}$$

$$\begin{aligned} x_3 &= 7D \oplus 00 \\ &= \text{binary} \oplus \text{binary} \\ &= 7D \quad \rightarrow \text{Hexa} \end{aligned}$$

$$\begin{aligned} x_4 &= AC \oplus 00 \\ &= \text{binary} \oplus \text{binary} \\ &= AC \quad \rightarrow \text{Hexa} \end{aligned}$$

$$\begin{aligned} \therefore w_4 &= w_0 + g(w_3) \\ &= \{24, 75, A2, B3\} \oplus \{21, 17, 7D, AC\} \\ &= \text{Binary} \oplus \text{Binary} \quad \rightarrow \text{Hexa} \\ &= \text{Hexa} \end{aligned}$$

- Round 1 :-
1. Sub Byte
 2. Shift Row
 3. Mixed Column
 4. Add Round Key

Sub Byte Operation

$$\begin{bmatrix} 2A & 3B \\ C1 & 12 \end{bmatrix}$$

State { 2A, C1, 3B, 12 }

S-Box

2A	C1	3B	12
D3	F1	14	15

⇒ Output:-

$$\begin{bmatrix} D3 & 14 \\ F1 & 15 \end{bmatrix}$$

{ D3, F1, 14, 15 }

Shift Row Operation

0th row	63	47	a2	F0
1st row	F2	9c	63	65
2nd row	7b	ab	7b	7c
3rd row	af	76	76	ca

After Shift Row

63	47	a2	F0
9c	63	65	F2
7b	7c	Fb	ab
ca	af	76	76

1 byte LS
 2 byte LS
 3 byte LS

Mixed Column Operation

★ Bit Level Shuffling / Transposition ★

State

x_0	x_2
x_1	x_3

↓
 col 1 col 2

$$\begin{bmatrix} b_0 \\ b_1 \end{bmatrix} = \begin{bmatrix} c_0 & c_2 \\ c_1 & c_3 \end{bmatrix} * \begin{bmatrix} x_0 \\ x_1 \end{bmatrix}$$

↓
 constant matrix

⇒

$$b_0 = (c_0 * x_0) + (c_2 * x_1)$$

$$b_1 = (c_1 * x_0) + (c_3 * x_1)$$

Modulo Matrix Multiplication

⊛ In exam constant matrix not given, dont worry It is PREDEFINED ⊛.

Constant Matrices (4x4)

Constant
Matrix
2x2

$$\begin{bmatrix} 02 & 03 & 01 & 01 \\ 01 & 02 & 03 & 01 \\ 01 & 01 & 02 & 03 \\ 03 & 01 & 01 & 02 \end{bmatrix} \begin{matrix} \text{1 byte RS (circular)} \\ \text{1 byte RL (circular)} \\ \text{1 byte RL (circular)} \end{matrix}$$

$S = \begin{bmatrix} 63 & 47 \\ f2 & 9c \end{bmatrix}$ $C = \begin{bmatrix} 02 & 03 \\ 01 & 02 \end{bmatrix}$

$b = \begin{bmatrix} b_0 & b_2 \\ b_1 & b_3 \end{bmatrix}$ ← Output of colⁿ transposition

→ $b_0 = \begin{bmatrix} 02 & 03 \\ 01 & 02 \end{bmatrix} * \begin{bmatrix} 63 \\ f2 \end{bmatrix}$

$b_0 = (02 * 63) \oplus (03 * f2) \oplus (01 * 63) \oplus (02 * f2)$

$b_1 = (01 * 63) \oplus (02 * f2)$

(*) Finite Field Arithmetic Operation

$GF(2^8) \rightarrow$ Galium Field.

→ Max shuffling of data/info
will be carried out by $GF(2^8)$

In ~~add~~ AES, multiplication is performed of 2
hexadecimal values is performed by using
FFAO i.e. $GF(2^8)$

This FFAO is supporting maximum scrambling
of data.

$$b_0 = \underline{(02 * 63)} \oplus \underline{(03 * f2)}$$

$$02 = 0000 \quad 0010$$

$$63 = 0110 \quad 0011$$

$$GF(2^8) = x^7 + x^6 + x^5 + x^4 + x^3 + x^2 + x + 1$$

$$GF(2^8) = \{0000 \ 0000 \ \dots \ 1111 \ 1111\}$$

$$\{02\} = x^7 + x^6 + x^5 + x^4 + x^3 + x^2 + x + 1$$

$$0 \ 0 \ 0 \ 0 \ 0 \ 0 \ 1 \ 0$$

$$= x$$

$$\{63\} = x^7 + x^6 + x^5 + x^4 + x^3 + x^2 + x + 1$$

$$= 0 \ 1 \ 1 \ 0 \ 0 \ 0 \ 1 \ 1$$

$$= x^6 + x^5 + x + 1$$

$$\therefore 02 * 63$$

$$= x * (x^6 + x^5 + x + 1)$$

$$= x^7 + x^6 + x^2 + x$$

Now,

$$\begin{array}{cccccccc} x^7 & x^6 & x^5 & x^4 & x^3 & x^2 & x & 1 \\ 1 & 1 & 0 & 0 & 0 & 1 & 1 & 0 \end{array}$$

$$= 1100 \ 0110$$

$$= C6$$

$$\begin{aligned} 03 &= 0000 & 0011 \\ f2 &= 1111 & 0010 \end{aligned}$$

$$\begin{aligned} \{03\} &= x^7 + x^6 + x^5 + x^4 + x^3 + x^2 + x + 1 \\ &= 0 \quad 0 \quad 0 \quad 0 \quad 0 \quad 0 \quad 1 \quad 1 \\ &= x + 1 \end{aligned}$$

$$\begin{aligned} \{f2\} &= x^7 + x^6 + x^5 + x^4 + x^3 + x^2 + x + 1 \\ &= 1 \quad 1 \quad 1 \quad 1 \quad 0 \quad 0 \quad 1 \quad 0 \\ &= x^7 + x^6 + x^5 + x^4 + x \end{aligned}$$

$$\therefore 03 * f2$$

$$\begin{aligned} &= (x+1) * (x^7 + x^6 + x^5 + x^4 + x) \\ &= x^8 + x^7 + x^6 + x^5 + x^2 + x^7 + x^6 + x^5 + x^4 + x \\ &= x^8 + 2x^7 + 2x^6 + 2x^5 + x^4 + x^2 + x \end{aligned}$$

$$\begin{aligned} &\text{EX-OR} \\ &= x^8 \oplus x^7 \oplus x^6 \oplus x^5 \oplus x^2 \oplus x^7 \oplus x^6 \oplus x^5 \oplus x^4 \oplus x \\ &= x^8 \oplus x^4 \oplus x^2 \oplus x \end{aligned}$$

The degree of above polynomial is 8 which is not part of $GF(2^8)$.

Maximum degree supported by $GF(2^8)$ is 7.

We need to convert above polynomial into reduced poly. For that purpose, \div above polynomial by irreducible poly.

Irreducible Polynomial:

$$\begin{aligned} p(x) &= x^8 + x^4 + x^3 + x + 1 \\ &= 100011011 \end{aligned}$$

$$G(x) = x^8 + x^4 + x^2 + x$$

~~$$P(x) = 10001$$~~

$$P(x) = x^8 + x^4 + x^3 + x + 1$$

$$\therefore t(x) = G(x) / P(x)$$

~~$$= 100010110$$~~

$$100011011$$

	1	0	0	0	1	0	1	1	0
(+)	1	0	0	0	1	1	0	1	1
	0	0	0	0	0	1	1	0	1

$$= 0D$$

$$\therefore (03 * F2) = 0D$$

$$b_0 = (02 * 63) (+) (03 * F2)$$

$$= C6 (+) 0D$$

$$=$$

1	1	0	0	0	1	1	0	
(+)	0	0	0	0	1	1	0	1

$$b_0 =$$

1	1	0	0	1	0	1	1
---	---	---	---	---	---	---	---

$$CB$$

$$\equiv$$

$$b_1 = (01 * 63) (+) (02 * f_2)$$

$$01 = 0000 \quad 0001$$

$$63 = 0110 \quad 0011$$

$$GF(2^8) = x^7 + x^6 + x^5 + x^4 + x^3 + x^2 + x + 1$$

$$\{01\} = x^7 + x^6 + x^5 + x^4 + x^3 + x^2 + x + 1$$

$$0 \quad 0 \quad 0 \quad 0 \quad 0 \quad 0 \quad 0 \quad 1$$

$$= 1$$

$$\{63\} = x^7 + x^6 + x^5 + x^4 + x^3 + x^2 + x + 1$$

$$= 0 \quad 1 \quad 1 \quad 0 \quad 0 \quad 0 \quad 1 \quad 1$$

$$= x^6 + x^5 + x + 1$$

$$01 * 63$$

$$= 1 * (x^6 + x^5 + x + 1)$$

$$= x^6 + x^5 + x + 1$$

Now,

$$x^7 + x^6 + x^5 + x^4 + x^3 + x^2 + x + 1$$

$$0 \quad 1 \quad 1 \quad 0 \quad 0 \quad 0 \quad 1 \quad 1$$

$$= \underline{0110} \quad \underline{0011}$$

$$= \quad 6 \quad 3$$

$$02 = 0000 \quad 0010$$

$$f2 = 1111 \quad 0010$$

$$\{02\} = x$$

$$\{f2\} = x^7 + x^6 + x^5 + x^4 + x$$

$$02 * f2$$

$$= x * (x^7 + x^6 + x^5 + x^4 + x)$$

$$= x^8 + x^7 + x^6 + x^5 + x^2$$

Now,

Pre defined

$$G(x) = x^8 + x^7 + x^6 + x^5 + x^2$$

$$P(x) = x^4 + x^3 + x^2 + x + 1$$

$$\begin{array}{cccccccc} x^8 + x^7 + x^6 + x^5 + x^4 + x^3 + x^2 + x + 1 \\ 1 & 1 & 1 & 1 & 0 & 0 & 1 & 0 & 0 \end{array}$$

$$\begin{array}{cccccccc} 1 & 0 & 0 & 0 & 1 & 1 & 0 & 1 & 1 \end{array}$$

$$t(x) = G(x) / P(x)$$

$$100011011$$

$$\begin{array}{r} 1 \\ 111100100 \\ \oplus 100011011 \\ \hline 011111111 \end{array}$$

$$\begin{array}{r} = 11111111 \\ = FF \end{array}$$

$$b_1 = (01 * 63) \oplus (02 * f2)$$

$$= 63 \oplus FF$$

$$= 0110 \quad 0011$$

$$\oplus 1111 \quad 1111$$

$$\underline{1001 \quad 1100}$$

binary to hexadecimal

$$b_1 = 9c$$

$$\begin{bmatrix} b_2 \\ b_3 \end{bmatrix} = \begin{bmatrix} 02 & 03 \\ 01 & 02 \end{bmatrix} * \begin{bmatrix} 47 \\ 9c \end{bmatrix}$$

$$b_2 = (02 * 47) \oplus (63 * 9c)$$

$$b_3 = (01 * 47) \oplus (02 * 9c)$$

$$b_2 = (02 * 47) \oplus (63 * 9c)$$

Threat \rightarrow Man in Middle \times

Page No. /

Date 5 / 4 / 24.

Objective

Key Exchange

Not Encryption/Decryption

* Diffie-Hellman Algo.

Process to find out primitive root of prime number.
 $P = 7$

$$2^1 \bmod 7 = 2$$

$$2^2 \bmod 7 = 4$$

$$2^3 \bmod 7 = 1$$

$$2^4 \bmod 7 = 2$$

$$\vdots$$

$$(1 \dots (P-1))$$

$$\text{Power} = (1 \dots 6)$$

Repeating.

$\therefore 2$ \times

$$3^1 \bmod 7 = 3$$

$$3^2 \bmod 7 = 2$$

$$3^3 \bmod 7 = 6$$

$$3^4 \bmod 7 = 4$$

$$3^5 \bmod 7 = 5$$

$$3^6 \bmod 7 = 1$$

$$\alpha = 3$$

Sender

Receiver.

① Select Prime no P .

$\alpha \rightarrow$ Primitive Root
of P

P, α

② Find out private

Key $= (x_A)$
Random number

② Find out Private

Key (x_B)
Random number.

③ Find out public key

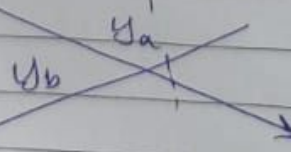
$$y_A = (\alpha)^{x_A} \bmod P$$

③ Find out public Key

$$y_B = (\alpha)^{x_B} \bmod P$$

④

④



⑤ Secret Key Calculation

$$y_1 = (y_B)^{x_A} \bmod P$$

\rightarrow Public Key of
Receiver.

⑤ Secret Key Calculation

$$y_2 = (y_A)^{x_B} \bmod P$$

\rightarrow Public Key of
Sender

$$y_1 = y_2$$

$P = 11$ Find α .

Find Private, Public, Secret Key.

⇒

$$P = 11$$

$$2^1 \bmod 11 = 2$$

$$2^6 \bmod 11 = 9$$

$$2^2 \bmod 11 = 4$$

$$2^7 \bmod 11 = 7$$

$$2^3 \bmod 11 = 8$$

$$2^8 \bmod 11 = 3$$

$$2^4 \bmod 11 = 5$$

$$2^9 \bmod 11 = 6$$

$$2^5 \bmod 11 = 10$$

$$2^{10} \bmod 11 = 1$$

$$\alpha = 2 \checkmark$$

$$\text{Now, } X_A = 3$$

$$X_B = 5$$

$$\therefore Y_A = (\alpha)^{X_A} \bmod P$$

$$Y_B = (\alpha)^{X_B} \bmod P$$

$$= (2)^3 \bmod 11$$

$$= (2)^5 \bmod 11$$

$$Y_A = 8$$

$$Y_B = 10$$

Now Exchange.

$$Y_1 = (10)^3 \bmod 11$$

$$Y_2 = (8)^5 \bmod 11$$

$$Y_1 = 10$$

$$Y_2 = 10$$

$$Y_1 = Y_2$$

$$\text{Private Key} = 3, 5$$

$$\text{Public Key} = 8, 10$$

$$\text{Secret Key} = 10$$

$$(2)^{13} \bmod 11$$

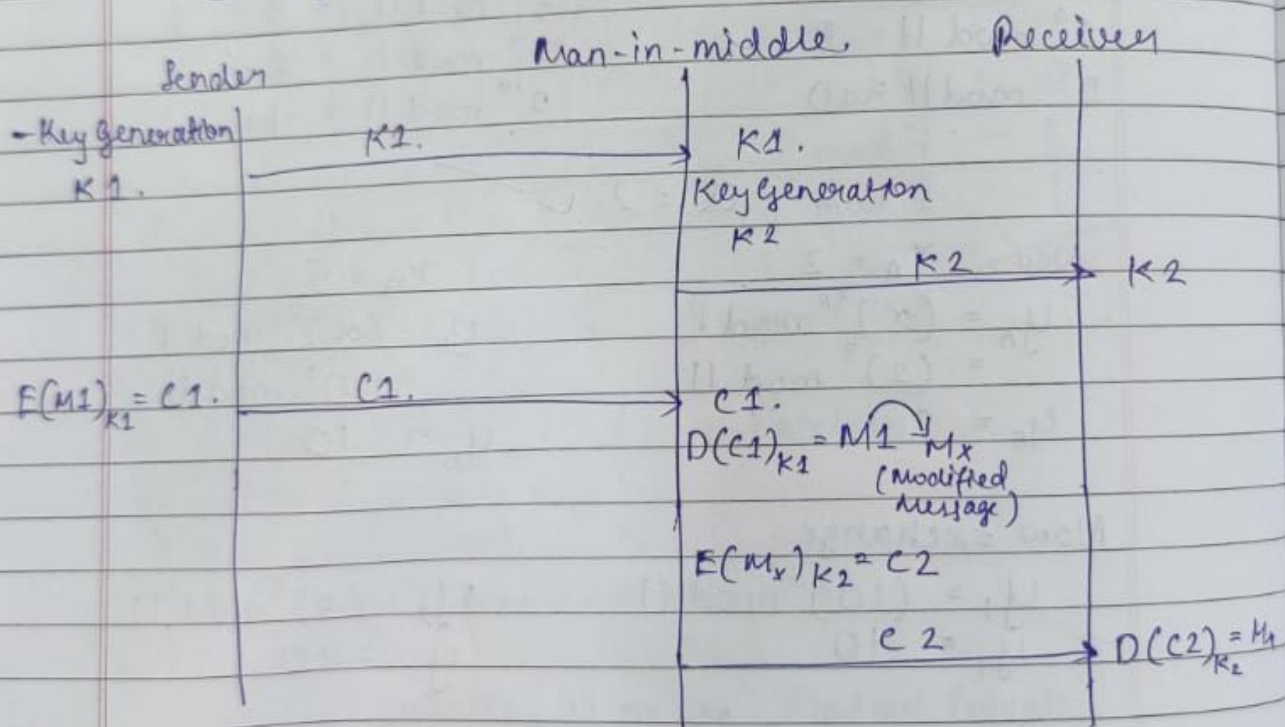
$$(2)^{15} \bmod 11$$

* Man-in-Middle Attack.

* During Key Exchange.

Man-in-middle attack on

(a) Symmetric Key Exchange Algo.



(b) Asymmetric Key Exchange Algo.

[Objective : Sender wants to transfer message of communication (Ms) to Receiver in secured manner.

Receiver will generate the public key & private key using RSA algorithm.

X_A

$y = ca_A$

Secret

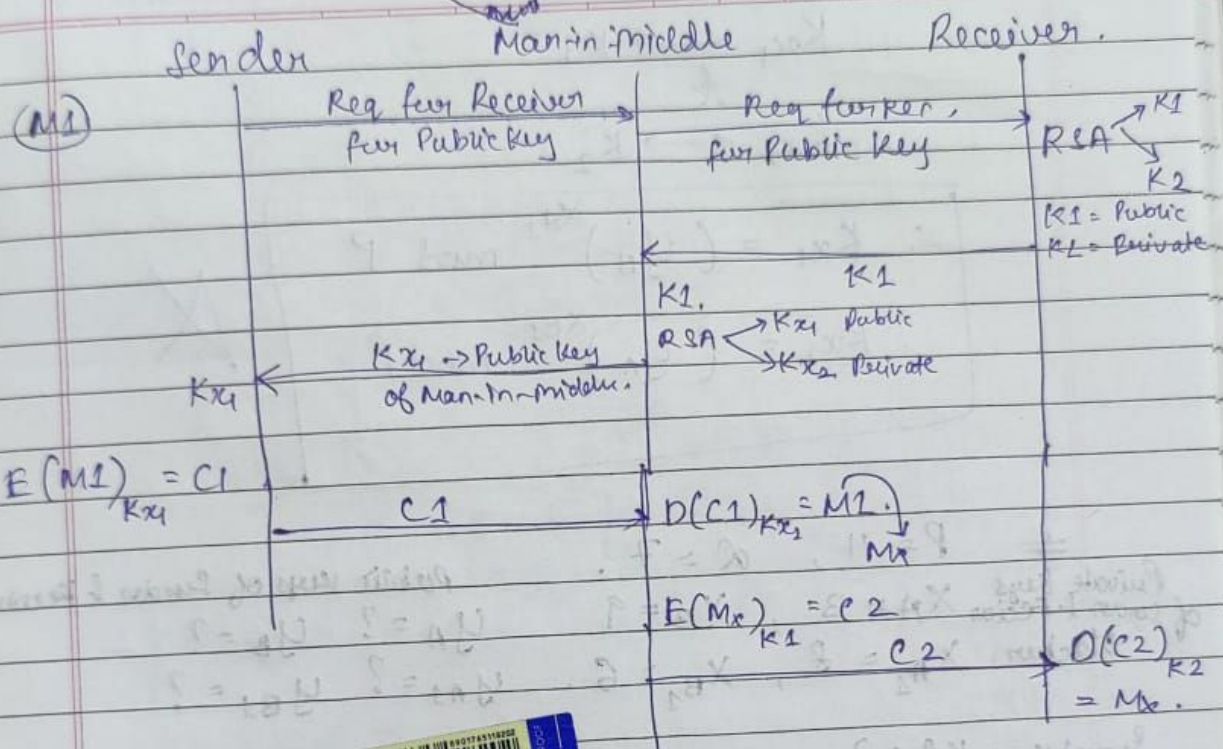
$K1 =$

$$K_{x1} = (y_B)^{x_{A1}} \bmod P$$

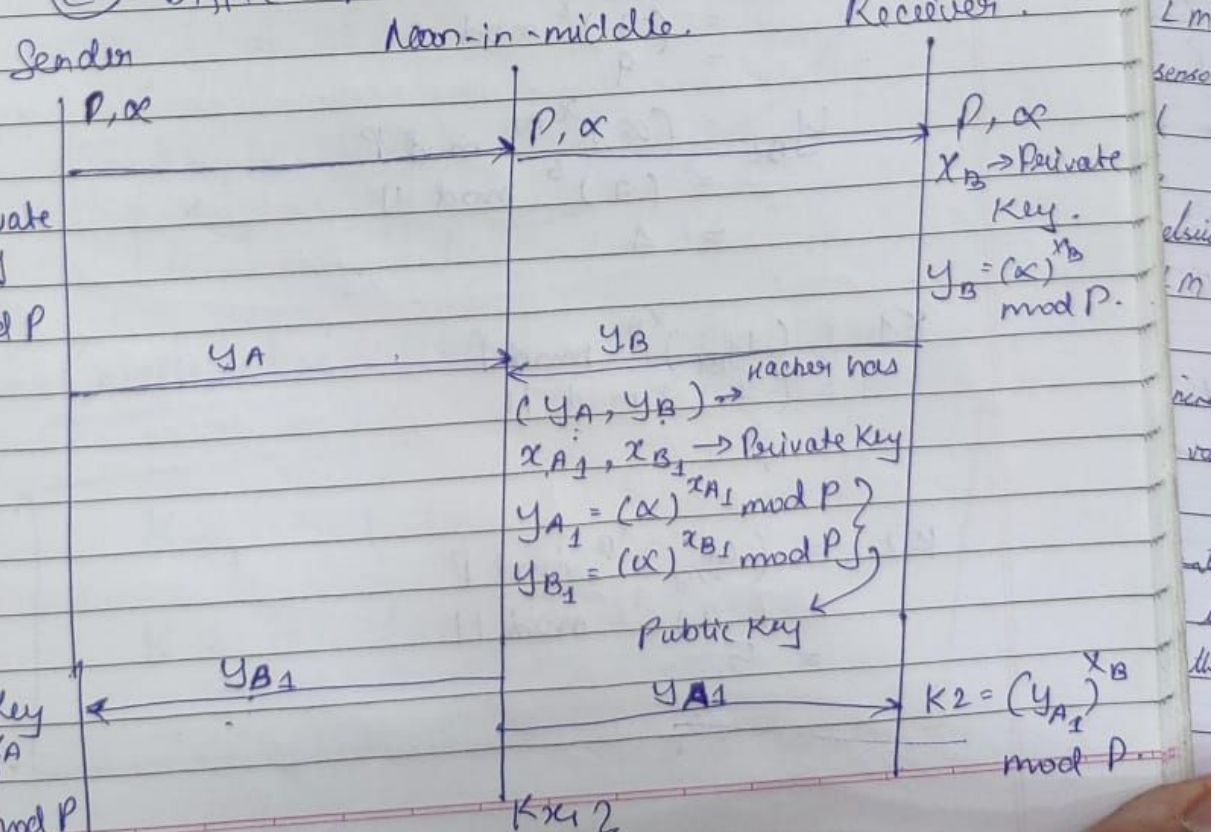


Page No. /

Date / /



(c) Diffie - Hellman Algo.



$$K_{x1} \longleftrightarrow K_1$$

$$K_{x2} \longleftrightarrow K_2$$

$$\begin{aligned} \therefore K_{x1} &= (Y_B)^{x_{A1}} \bmod P \\ K_{x2} &= (Y_A)^{x_{B1}} \bmod P \end{aligned}$$



$$\# \quad P = 11, \quad \alpha = 7.$$

Public Keys of Sender & Receiver.

Private Keys
of Sender & Receiver

$$x_A = 3, \quad x_B = 9$$

$$y_A = ?, \quad y_B = ?$$

$$\text{Hackers: } x_{A1} = 8, \quad x_{B1} = 6.$$

$$y_{A1} = ?, \quad y_{B1} = ?$$

$$\text{Secret Keys: } K1 = ?, \quad K2 = ?, \quad K_{x1} = ?, \quad K_{x2} = ?.$$

$$\begin{aligned} \Rightarrow y_{A1} &= (\alpha)^{x_{A1}} \bmod P \\ &= (7)^8 \bmod 11 \\ &= 9 \end{aligned}$$

$$\begin{aligned} y_{B1} &= (\alpha)^{x_{B1}} \bmod P \\ &= (7)^6 \bmod 11 \\ &= 4 \end{aligned}$$

$$\begin{aligned} K1 &= (y_{B1})^{x_A} \bmod P \\ &= (4)^3 \bmod 11 \\ &= 9 \end{aligned}$$

$$\begin{aligned} K2 &= (y_{A1})^{x_B} \bmod P \\ &= (9)^9 \bmod 11 \\ &= 5 \end{aligned}$$

$$Kx_1 = (y_B)^{x_{A1}} \bmod P$$

~~28~~

$$\begin{aligned} \therefore y_B &= (\alpha)^{x_B} \bmod 11 \\ &= (7)^9 \bmod 11 \\ &= 8 \end{aligned}$$

$$Kx_1 = (8)^8 \bmod 11$$

$$Kx_1 = 5$$

$$Kx_2 = (y_A)^{x_{B1}} \bmod P$$

~~28~~

Uta aa

$$\begin{aligned} \therefore y_A &= (\alpha)^{x_A} \bmod 11 \\ &= (7)^3 \bmod 11 \\ &= 13 \end{aligned}$$

Ans should gaya.

$$K1 = Kx_1$$

$$K2 = Kx_2$$

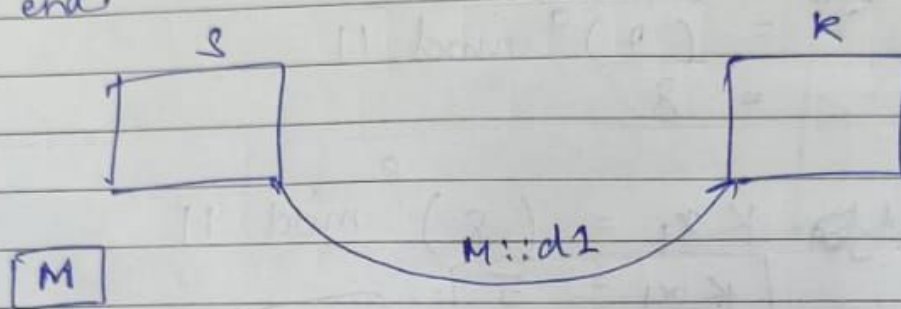
$$\begin{aligned} \therefore Kx_2 &= (13)^6 \bmod 11 \\ Kx_2 &= 9 \end{aligned}$$

Correct:

$$\begin{aligned} Kx_1 &= (y_A)^{x_{B1}} \bmod P \\ Kx_2 &= (y_B)^{x_{A1}} \bmod P \end{aligned}$$

④ Integrity

Various hashing algo is used to msg. Below diagram is representing how integrity of msg is verified at receiving end.



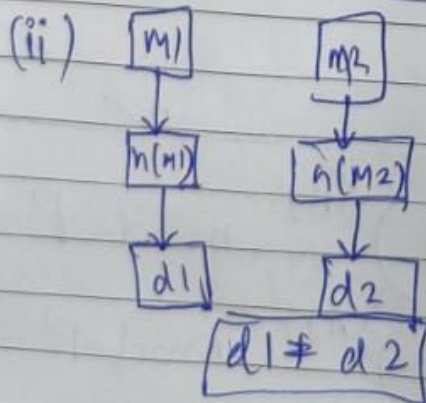
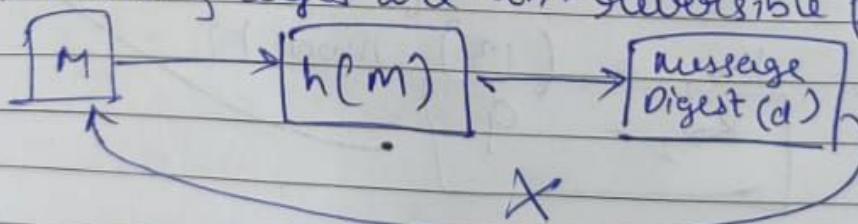
① $h(m) = d1$ (message Digest) $h(m) = d2$

② $M \rightarrow$ message. $d2 - d1 = 0$

Hashing Technique

Hashing Properties:

(i) Hashing algo are non-reversible function.

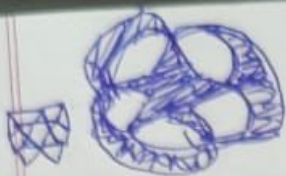


No collision should be there.

★ Hashing Algorithm Properties ★

Self-Study.

Security



Page No. _____

Date/____/____/____

⑤ Message Digest (MD)

- Ron Rivest

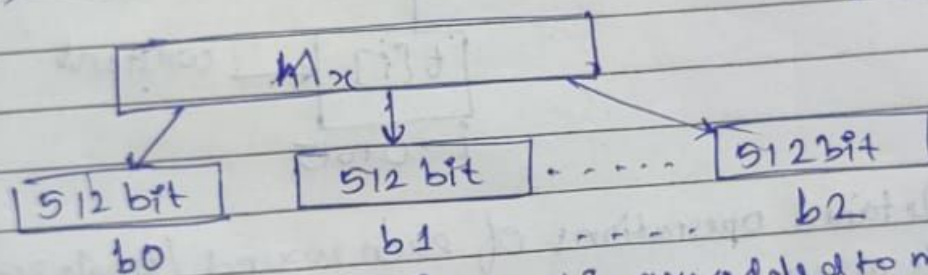
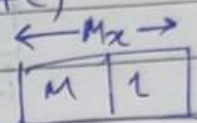
- MD, MD2, MD3, MD4, MD5.

MD5 - Algorithm:

(i) Calculate length of Message. (L)

(ii) Add length to the original message. (m+L)

(iii) Divide message into 512 bit blocks.



(iv) Padding. (Extra bits are added to make sure all blocks are 512 bits.)

(v) Divide 512 bit blocks into 16

(v) Initial chaining variable

a, b, c, d

Size of each chaining variable is 32-bit.

→ Inducing Randomness
Increases strength.

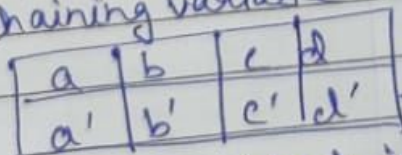
Eg:-

a=

01 23 45 67

hexadecimal value.

(vi) Copy chaining variable into another temp variables.

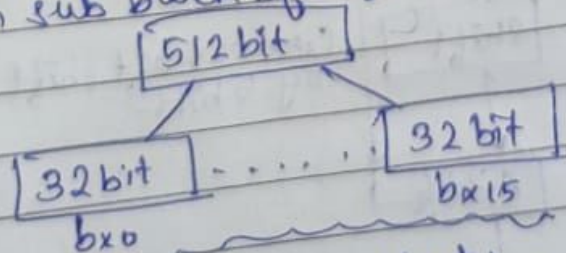


→ chaining variable

→ Temp. chaining variable.

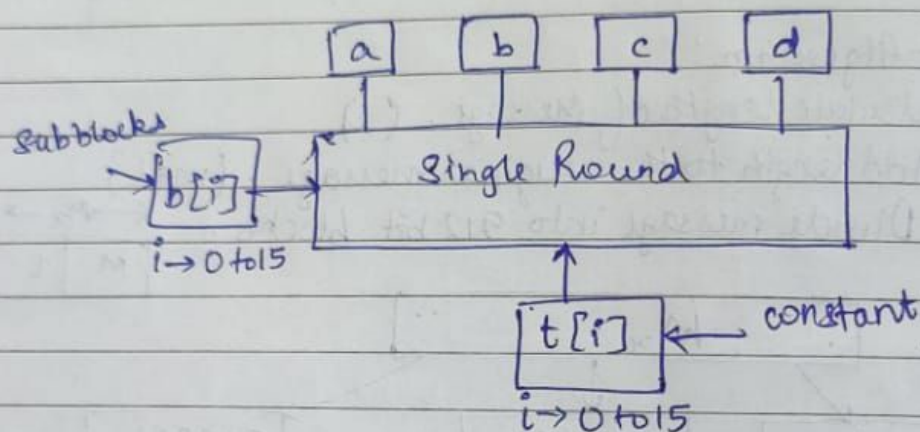
(vii) Divide 512 bit block into 16 sub block

& each sub block of size 32 bit.

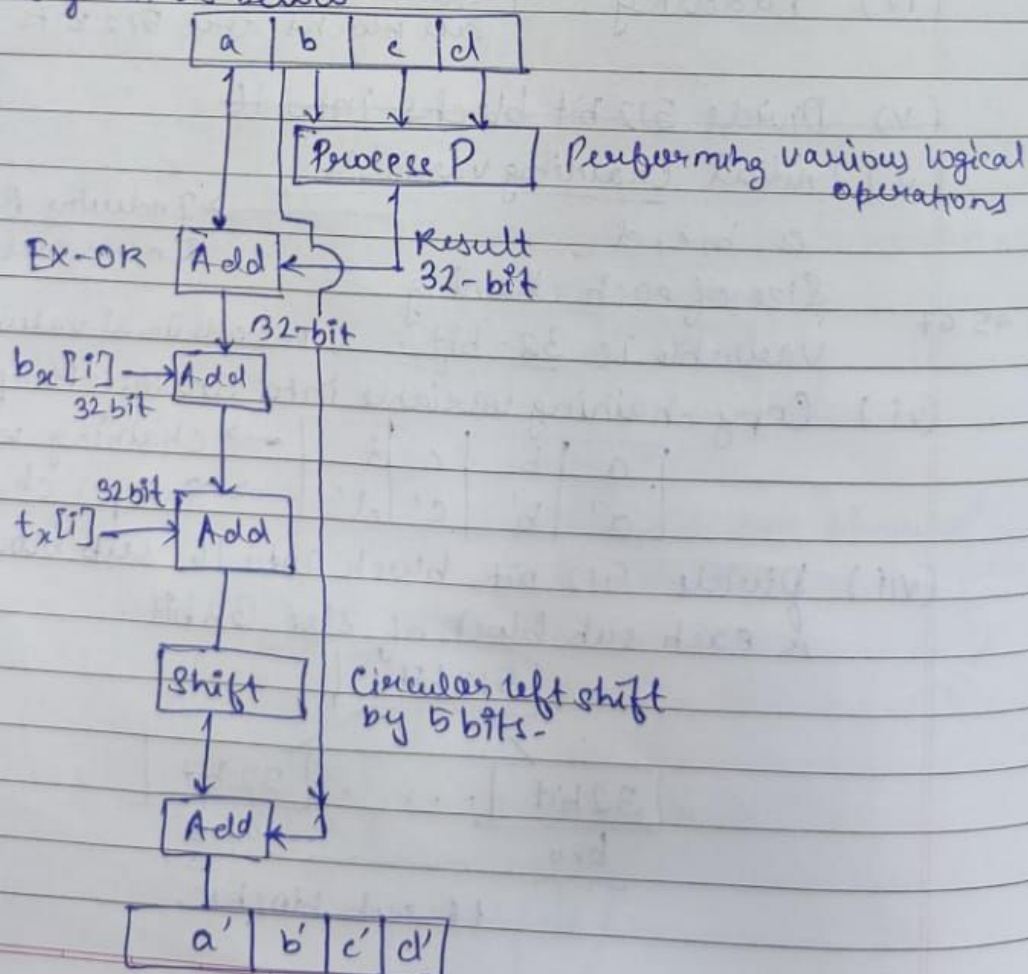


16 sub blocks.

(viii) MD5 Algo is performing 4 Round off operation.
Block dig of each Round is given as below
chaining variable



(ix) Detailed operations of each round / single round is given as below



The limitation / drawbacks of MD5 algorithm is only single chaining variable is being modified during each operation.