

SVKM's  
D. J. Sanghvi College of Engineering

Program: B.Tech in Comp. Sci. and Eng.(Data Science)  
Academic Year: 2022  
Date: 12.01.2023  
Time: 10:30 am to 01:30 pm  
Subject: Probabilistic Graph Models (Semester V)

Duration: 3 hours

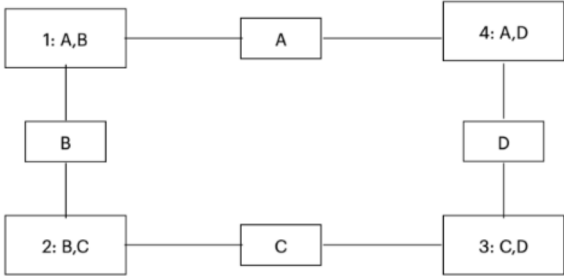
Marks: 75

**REGULAR EXAMINATION**

**Instructions:** Candidates should read carefully the instructions printed on the question paper and on the cover page of the Answer Book, which is provided for their use.

- (1) This question paper contains 03 pages.
- (2) **All Questions are Compulsory.**
- (3) All questions carry equal marks.
- (4) **Answer to each new question is to be started on a fresh page.**
- (5) **Figures in the brackets on the right indicate full marks.**
- (6) **Assume suitable data wherever required, but justify it.**
- (7) Draw the neat labelled diagrams, wherever necessary.
- (8) Mention **correct question number** in the answer sheet.

Question No.		Max. Marks
Q1 (a)	<ol style="list-style-type: none"><li>1. Difference between Bayesian and Markovian representations.</li><li>2. Assume that A and B are independent random variables. Which of the following options are always true? Give reason.<ol style="list-style-type: none"><li>a) <math>P(A,B) = P(A) * P(B)</math></li><li>b) <math>P(B/A) = P(B)</math></li><li>c) <math>P(A) + P(B) = 1</math></li><li>d) <math>P(A,B) = P(A) + P(B)</math></li></ol></li></ol>	[05] [02]
Q1 (b)	<pre>graph TD; Coherence --&gt; Difficult; Difficult --&gt; Grade; Intelligent --&gt; Grade; Intelligent --&gt; GRE; Grade --&gt; LOR; GRE --&gt; Job; LOR --&gt; Job; Grade --&gt; Happy; Job --&gt; Happy;</pre> <p style="text-align: center;">Graph 1</p>	[ 08]

	<p>What are the conditions of an Active Trail in Bayesian Network? Give reasons which of the following are active trail if Grade is observed in graph 1?</p> <ol style="list-style-type: none"> <li>1. Intelligent <math>\rightarrow</math> GRE <math>\rightarrow</math> Job <math>\rightarrow</math> Happy</li> <li>2. Coherence <math>\rightarrow</math> Difficult <math>\rightarrow</math> Grade <math>\leftarrow</math> Intelligent <math>\rightarrow</math> GRE <math>\rightarrow</math> Job <math>\leftarrow</math> Letter</li> <li>3. Intelligent <math>\rightarrow</math> Grade <math>\rightarrow</math> Letter <math>\rightarrow</math> Job <math>\rightarrow</math> Happy</li> <li>4. Coherence <math>\rightarrow</math> Difficult <math>\rightarrow</math> Grade <math>\leftarrow</math> Intelligent <math>\rightarrow</math> GRE</li> </ol>	
Q2 (a)	1. If P factorizes over G and d-sepG (XY  X) then P satisfies (X $\perp$ Y Z)	[07]
	OR	
Q2 (a)	2. What is the advantage of <b>Conditional Random Field</b> in representing high dimensional data? Take any two real world examples and explain.	[07]
Q2 (b)	1. What is a Markov assumption? Discuss a situation where this assumption is not true. So how to modify it in order to make the assumption true.	[08]
	OR	
Q 2 (b)	2. Discuss a speech recognition system using Hidden Markov Model (HMM).	[08]
Q3 (a)	Derive the complexity of variable elimination.	[05]
Q3 (b)	Can we guarantee regularity in Gibbs Sampling on XOR for all conditions? Justify your answer.	[05]
Q3 (c)	<p>In the shown message passing process (graph 2), what would be the right definition for messages: (1) <math>\delta_{1,2}</math>, (2) <math>\delta_{4,3}</math>, (3) <math>\delta_{2,3}</math>, (4) <math>\delta_{2,1}</math> and (5) <math>\delta_{4,1}</math></p>  <p style="text-align: center;">Graph 2</p>	[05]
Q4 (a)	<p>What is a Clique Tree? Define <b>Max-Sum in Clique Tree</b>. What are the <b>convergence criteria</b> of message passing in a clique tree? Shown below is a message passing for a given clique tree. Fill in the blanks (?) considering <b>max marginalization</b>.</p>	[10]

	<table><tr><td>A1</td><td>B1</td><td>3</td></tr><tr><td>A1</td><td>B2</td><td>0</td></tr><tr><td>A2</td><td>B1</td><td>-1</td></tr><tr><td>A2</td><td>B2</td><td>1</td></tr></table> <div><div>1: A,B</div><div>B</div><div>2: B,C</div></div> <div><table><tr><td>B1</td><td>?</td></tr><tr><td>B2</td><td>?</td></tr></table><p>M<sub>1</sub></p><table><tr><td>A1</td><td>B1</td><td>?</td></tr><tr><td>A1</td><td>B2</td><td>?</td></tr><tr><td>A2</td><td>B1</td><td>?</td></tr><tr><td>A2</td><td>B2</td><td>?</td></tr></table><div><table><tr><td>B1</td><td>?</td></tr><tr><td>B2</td><td>?</td></tr></table><p>M<sub>2</sub></p><table><tr><td>B1</td><td>C1</td><td>?</td></tr><tr><td>B1</td><td>C2</td><td>?</td></tr><tr><td>B2</td><td>C1</td><td>?</td></tr><tr><td>B2</td><td>C2</td><td>?</td></tr></table></div><p>Graph 3</p></div>	A1	B1	3	A1	B2	0	A2	B1	-1	A2	B2	1	B1	?	B2	?	A1	B1	?	A1	B2	?	A2	B1	?	A2	B2	?	B1	?	B2	?	B1	C1	?	B1	C2	?	B2	C1	?	B2	C2	?	
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Q4 (b)	1. Discuss the limitations of the bounds.	[05]																																												
	OR																																													
Q4 (b)	2. Discuss the Pros and Cons of Markov Chain Monte Carlo (MCMC) Method.	[05]																																												
Q5 (a)	1. How do we perform maximum likelihood function in case of Bayesian Network and Markov Network if there is missing data issue in the given dataset?	[10]																																												
	OR																																													
Q5 (a)	2. Explain Tree-Augmented Naïve Bayes (TAN) and its application in Chow-Liu algorithm.	[10]																																												
Q5 (b)	What are the various sufficient statistics used for maximum likelihood estimators?	[05]																																												